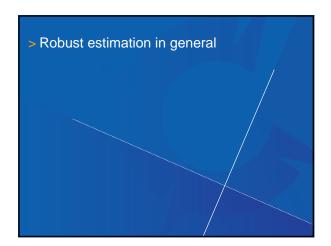
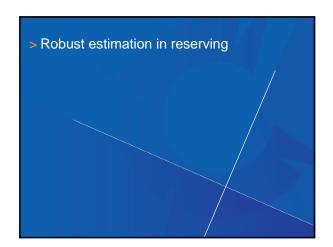


CHARTIS Look at sensitivity of reserves to each point in the triangle Measured by derivative of reserves wrt each incremental point Good model would not be overly sensitive to any point Sensitive to point means sensitive to random component of point Use as a test of models If test indicates problem points, try to find alternative model



Robust Methods ■Classical view —» Data is generated as a sample from model process being fitted Efficiency of methods like MLE come from this view Could be a more complex process that is generating the data and model is a convenient simplification Even a few points generated by a different process can throw off the estimated parameters ■Responses Identify and exclude outliers Try to understand when outliers arise and not use model in those circumstances Try to find models that are not so influenced by those points

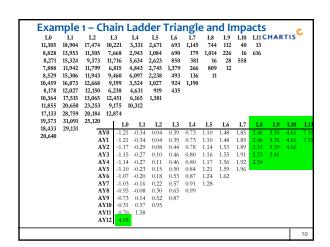
Influence ■Excluding points —» ■Look at change in parameters from leaving out observations ■Done for each point ●Called empirical influence function ●Sample size times change from excluding a point is called gross error sensitivity (GES) ●Look for estimators with low GES but close to efficiency of MLE ■Changing points —» ■Look at change in parameters or predictions from changing a point ●E.g., take the derivative of the prediction with respect to each point ④If the points have a lot of randomness, a point with strong effect will have strong effect from its random component

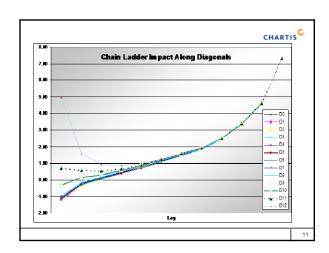


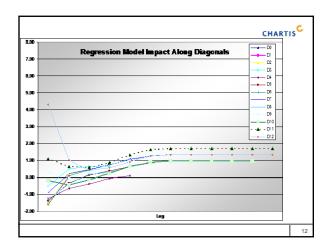
Reserving Application Leaving out cells can be awkward so look at derivative of reserve wrt each point in triangle Called impact of the cell on the reserve From Tampubolon PhD thesis Examples from previous CAS papers Derivatives usually done numerically Redo reserve estimate after small change in cell Also look at generalized degrees of freedom Change in fitted value for a cell wrt observed value A better measure of degrees of freedom than just counting parameters when model is non-linear GDFs may help understand impacts

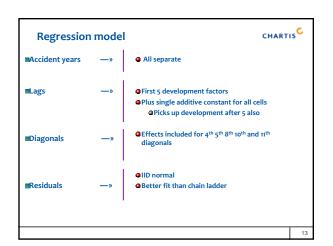
General Observations All 3 corners of triangle have fairly high impact Clower left All development factors apply to it Impact = cumulative factor Opper right Outper right Increasing it reduces all development factors Impact = cumulative factor I

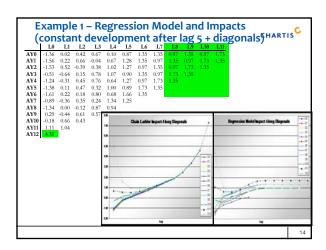












■In general	—»	Not supported by data Not likely anyway
■Alternatives tried	—»	■ Regression on square root of incremental values ■ Gamma residuals with variance ~ mean ^{e,71} . ■ Both had problems with high impacts
■What worked	—»	 Gamma with multiplicative diagonals Before they were additive Gave better fit without problem of high impacts Impacts similar to model with IID normal residuals but with more realistic distribution of residuals Robust analysis showed weakness of alternatives

		le 2 –					le an	d Im	pact	s		C
(I	mpac	ts san	າe for	· CL a	and C	DP)				СН	ARTI	5
Lag 0	L1	L2	L3	L4	L5	L6	L7	L8	L9			
357,848	766,940	610,542	482,940	527,326	574,398	146,342	139,950	227,229	67,948	-		
352,118	884,021	933,894	1,183,289	445,745	320,996	527,804	266,172	425,046				
290,507	1,001,799	926,219	1,016,654	750,816		495,992	280,405					
310,608	1,108,250	776,189	1,562,400	272,482	352,053	206,286						
443,160	693,190	991,983	769,488	504,851	470,639							
396,132	937,085	847,498	805,037	705,960								
440,832	847,631		1,063,269									
359,480	1,061,648	1,443,370										
376,686	986,608											
344,014				l	l	l		l	l			
			L0	L1	L2	L3	L4	L5	L6	L7	L8	L9
		AY0		-1.62	-1.01	-0.45	0.01	0.51	1.16	2.27	4.54	12.59
		AY1		-1.38	-0.77	-0.20	0.25	0.76	1.40	2.51	4.78	
		AY2		-0.93	-0.33	0.24	0.69	1.20	1.85	2.95		
		AY3		-0.72	-0.11	0.45	0.91	1.41	2.06			
		AY4 AY5		-0.46 -0.18	0.15	0.71	1.17 1.45	1.67				
l		AY5		0.18	0.45	1.42	1.45					
		AY7		1.35	1.96	1.42						
l		AY8		3.57	1.90							
		AY9		3.31								
												16

Regression	model	CHARTI	s ^C
■Accident years	—»	 Three levels: high, medium, low, plus average of high and medium 	
■ Lags	—»	 High and low levels of % of ultimate paid in cell Average of high and low, and 1 – sum of others also used 	
■Diagonals	—»	■Effects included for 4 th 6 th 7 th diagonals	
■Residuals	—»	● Gamma with variance ∝ mean ^{1/2} ● Better fit than chain ladder or ODP	
			17

IIII	pacts	OT K	egre	SSIOI	Mod	iei oi	n IA			CHARTIS
	L0	L1	L2	L3	L4	L5	L6	L7	L8	L9
AY0	0.65	-0.82	-1.08	-2.07	-0.87	0.97	-0.32	0.33	0.53	12.06
AY1	1.45	-0.02	0.68	0.60	-0.25	1.90	1.40	1.61	1.57	
AY2	1.64	0.75	-0.19	0.84	0.90	1.93	1.66	1.36		
.Y3	1.26	0.43	-0.21	0.97	-0.36	1.70	1.71			
Y4	1.62	0.08	0.67	0.37	0.63	1.35				
.¥5	1.19	-0.11	0.57	0.51	1.17					
Y6	2.56	1.19	0.91	1.13						
Y7	2.18	1.27	1.49							
Y8	1.72	0.92								
Y9	1.59									

TA Regression	CHART	ıs [©]
■Remaining problem —»	● Upper right	
■Alternate model —»	□ Lag 9 gets half the % paid as low level □ Consider as a trend to 0% for lag 10 □ Still force lag factors to sum to 1.0 □ Largest impact now 2.35, and only 2 above 2	
		19

Summary and Extensions CHART	ıs
■Robust analysis looks for observations with high impact on result	
■Problem in that random component would have high impact	
■Derivative of reserve wrt each cell used as impact measure	
■Add to list of model checks	
■Led to finding improved models in example cases	
■Possible extension: multiply impact by modeled standard deviation of cell estimate	
Would combine impact of a small change with degree of change likely	
	20