AKUR8

Penalized regression - Between Credibility and GBMs



Guillaume Béraud-Sudreau Chief Actuary & Co-Founder of Akur8

Biography

Guillaume is the **Chief Actuary** and **Co-Founder** of Akur8.

He has both a data science and an actuarial background.
Guillaume started researching the potential of AI for insurance pricing as Head of Pricing R&D at Axa Global Direct, before being incubated at Kamet Ventures and founding Akur8.

Guillaume is a Fellow of the French Institute of Actuaries and holds Master degrees in Actuarial Science, Cognitive Science and Engineering from Institut des Actuaires - CNAM, Ecole normale supérieure, and Télécom Paris.





Mattia Casotto
Head of Product US

Biography

Mattia Casotto is the Head of Product for the United States division of the pricing software Akur8.

He has more than 7 years of experience on predictive modeling in insurance and is one of the founding members of Akur8.

He is one of the co-author of the white-paper 'Credibility and Penalized Regression'.



Low-Exposure Levels



Worker's Compensation example

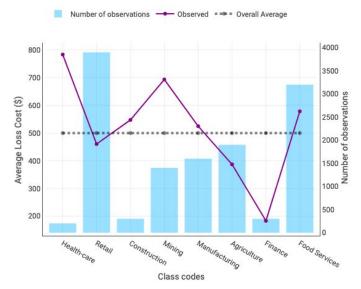
Loss Cost by class code example

Losses and exposures for companies are collected, and we want to compute an estimation of the average loss cost per class code.

The data can be represented visually:

- The blue bars represent the number of observations for a given class;
- The purple lines represent the Observed Experience as the average loss cost for each class;
- The **black line** represent the **overall average** (or grand average) of \$500 in this example.

Observed loss by class code



GLMs: Univariate estimate

A natural estimate is the average loss cost by class code.

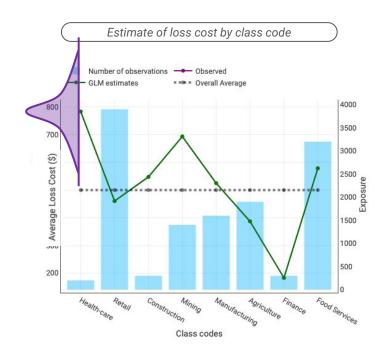
Such estimate may be inappropriate for class Health-Care which has low exposure.

The same argument applies for Finance and Construction.

This approach is followed in the GLM framework, that fully trusts the data:

$$\beta^* = Argmax \ Likelihood(Obs., \beta)$$

In many cases (for instance Posson-LogLink or Gaussian-IdentityLink) the maximum of likelihood matches the average.



Removing non-significant levels



Number of observations

Removing low-significance levels

A classic approach is to use the **statistical significance** of the different levels.

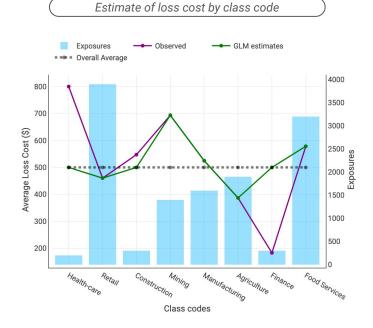
Levels that have low exposure (or small effects) are grouped together, or put at the average value.

The goal of this approach is to avoid trusting very noisy models with a few observations.

The result obtained will depend on the **significance threshold** above which levels will be kept into the final model or grouped:

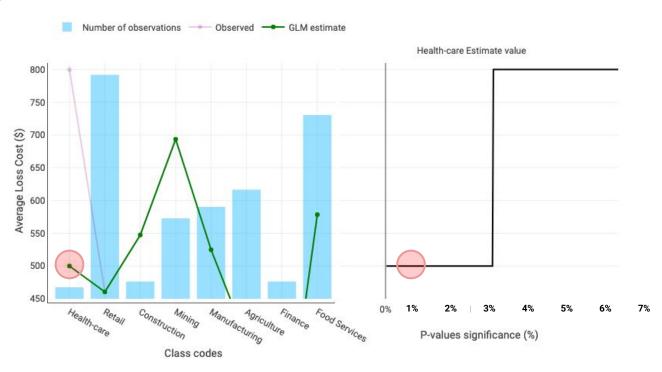
- If a level is **more significant** than the threshold, it is **kept**;
- If a level is **less significant** than the threshold, it is **removed**.

Modelers often use a "5% significance level" but any other value can be selected.



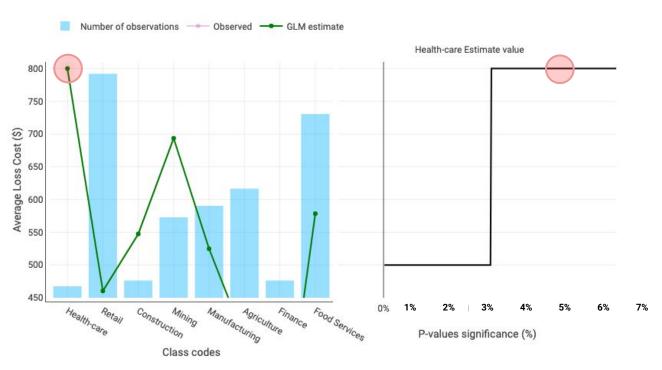
Fitted model depends on the threshold

Strong (low) significance thresholds are hard to validate and lead to a **robust** model.



Fitted model depends on the threshold

Weak (high) significance threshold are easy to validate and lead to a volatile model.

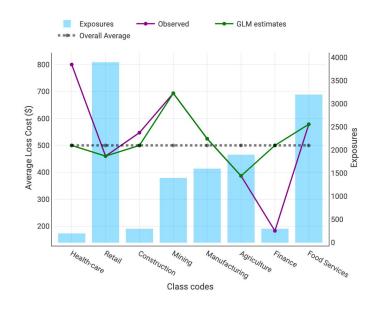


Strengths & limits of levels selection

This approach has well know strengths and limits:

- ✓ It is a binary method, leading to clear decisions;
- ✓ It is very frequently used and widely accepted;
- ✓ It relies on very classic statistics.
- X It is a binary method: it does not use efficiently the limited observations we have on "health-care";
- X Tests justification rely on hypothesis often not met in practice.

Estimate of loss cost by class code



Credibility



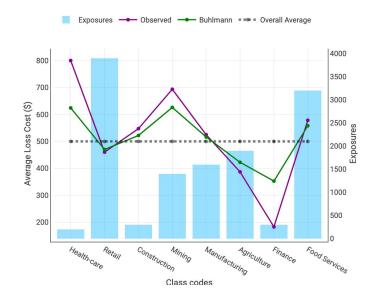
The Credibility solution

The idea of a credibility framework is to create predictions between these two extreme "yes" and "no" solutions.

Low-exposure levels are:

- Not fully trusted (like they would in a standard GLM framework);
- Not fully discarded (like they would if we applied a grouping of non-significant levels).

Estimate of loss cost by class code

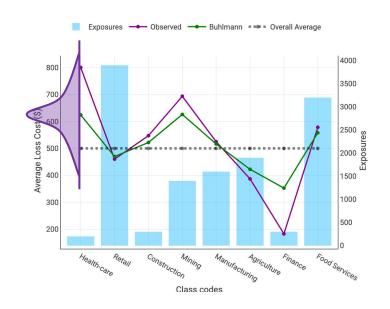


What is the idea motivating Credibility?

The Bühlmann credibility creates predictions by mixing two sources of informations:

- The "pure GLM" predictions, centered on the observed values;
- The "a-priori" distribution of the observations, centered on the grand-average.

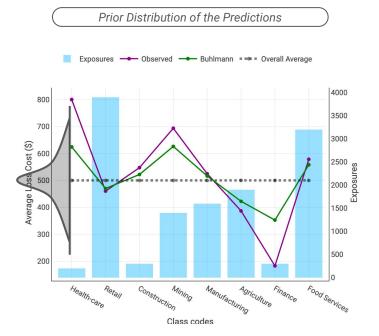
Distribution of the Observations



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What is the idea motivating Credibility?

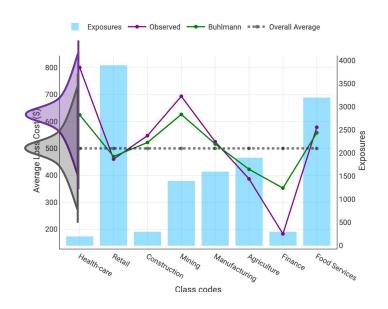
The Bühlmann credibility creates predictions by mixing two sources of informations:

- The "pure GLM" predictions, centered on the observed values;
- The "a-priori" distribution of the observations, centered on the grand-average.

More data means the observed values vary less around the predictions, meaning they can be trusted: a **strong weight** is given to **the observed values**.

Less data means the observed values vary a lot around the predictions, meaning they can't be trusted: a **strong weight** is given to the **a-priori (grand average)**.

Mixing the two distributions



Quick Reminder... What is Credibility

"Credibility, simply put, is the weighting together of different estimates to come up with a combined estimate."

Foundations of Casualty Actuarial Science

When the volume of data is not enough to accurately estimate the losses, Credibility methodologies provide ways to complement the observed experience with additional information.

The Credibility formula is:

Estimate = Z * Observed Experience + (1 - Z) * Complement of Credibility

where the Credibility factor **Z** is a number between 0 and 1.

This simple equation is reached only for couples of well-chosen losses and priors.

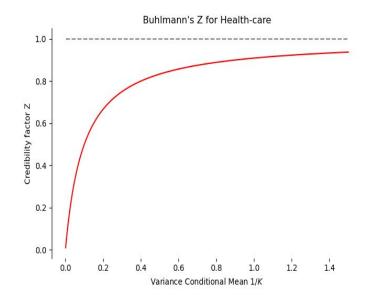
Bühlmann Credibility: Computing Z

The modeler decides to use Bühlmann Credibility.

The formula for credibility is:

$$Z = rac{n}{n+K}$$

Where K can be estimated from the data via standard formulas.

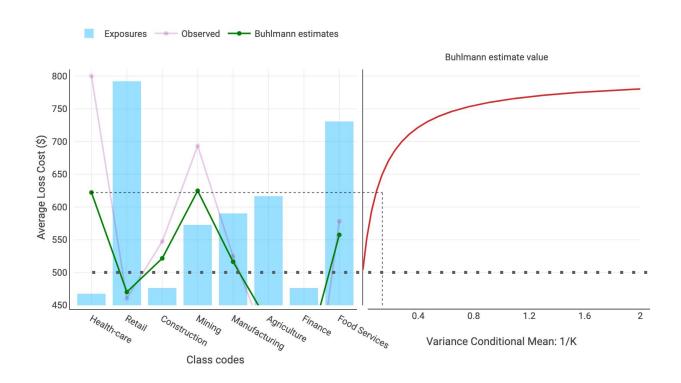


¹ K in R⁺ is the ratio between the variances of the two distributions presented earlier: mean of conditional variance (in purple, Expected Process Variance, EPV) / variance of conditional means (in grey, Variance of the Hypothetical Mean, VHM)

Large K (low credibility)

Weak information on the predictions can be derived from the observations (the distributions of the observations around the prediction has a large variance).

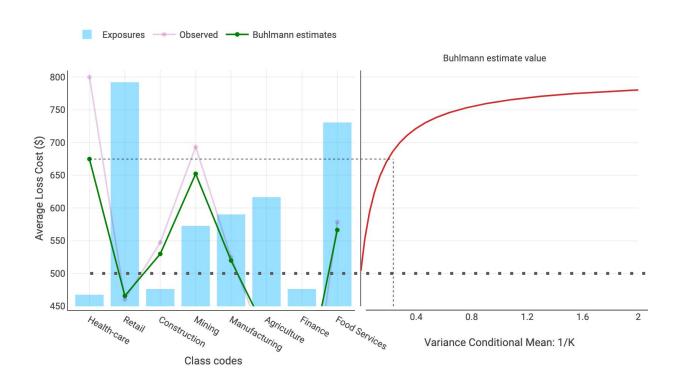
Predictions are close to the overall average.



Medium K (intermediate credibility)

Intermediate information on the predictions can be derived from the observation (the distributions of the observations around the prediction has a medium variance).

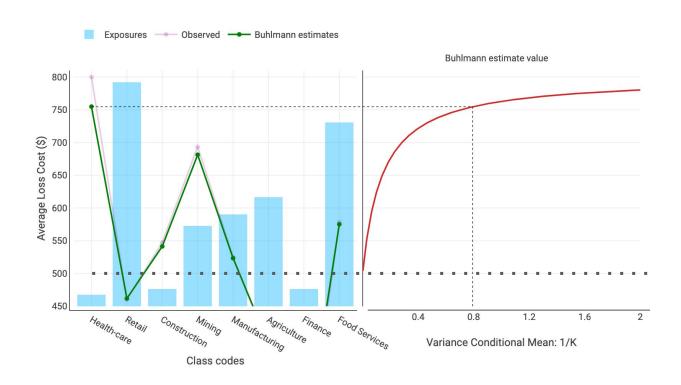
Predictions are between the overall average and the observations.



Small K (strong credibility)

Strong information on the predictions can be derived from the observation (the distributions of the observations around the prediction has a small variance).

Predictions are close to the observations.



Credibility works on a single dimension!

Credibility hypothesis are on the observed values and predictions, not the coefficients!

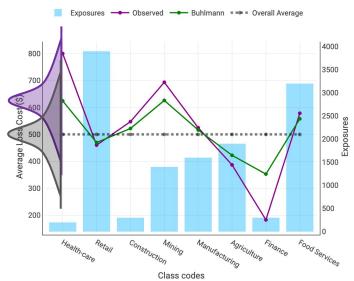
Integration of credibility is done as a post-processing, after the GLM has been built.

It can be applied to a single variable: it is not a multivariate analysis!

The statisticians who designed our GLMs were unaware we intended to subject GLM estimates to the violence of a subsequent round of ad hoc credibility adjustments. If they had known, they might have suggested a better starting point than GLM estimates.."

F. Klinker, Generalized Linear Mixed Models for Ratemaking 2010

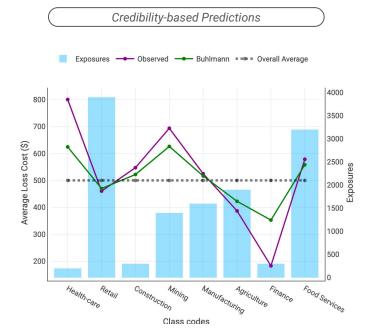
Mixing the two distributions ■ Exposures → Observed → Buhlmann • • • • Over



Strengths & limits of Bühlmann Credibility

This approach has also well-documented strengths & limits:

- ✓ It allows to leverage all the available data;
- ✓ It is very frequently used and widely accepted;
- ✓ It relies on very classic statistics;
- Results can be computed without a computer (which didn't exist in the 1960's when the method was proposed).
- X It is applied as a post-processing, only between two risk estimates.



Comparing different techniques

Control low-exposure segments to prevent overfitting

Set coefficients of low-exposure segments at zero

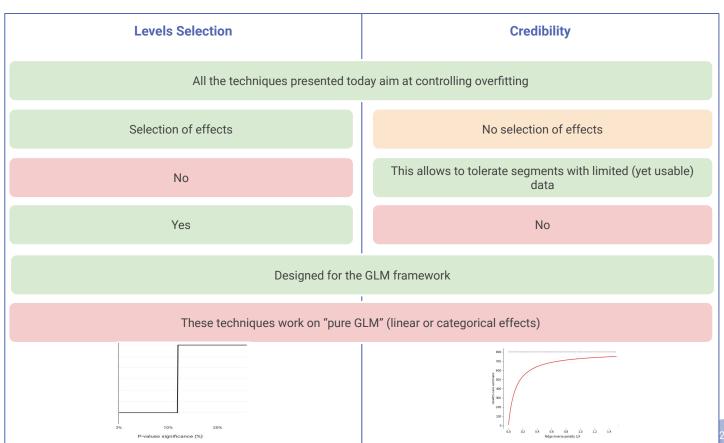
Shrink low-exposure segments

Work for multivariate models

Creates transparent models (GLM or additive models)

> Natively manage non-linear effects

Coefficient depending on the robustness parameter



Enriching the GLM framework

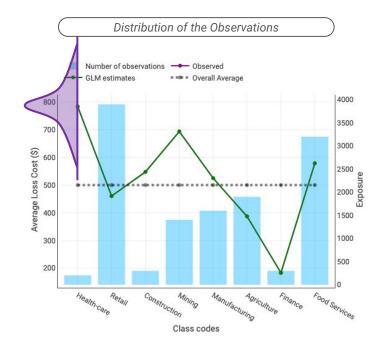


Why the GLM lacks credibility

GLM coefficients are the **maximum of likelihood** (probability of observing the data, given the model):

$$\beta^* = Argmax \ Likelihood(Obs., \beta)$$

The probability of observations is displayed in purple on the right.



Number of observations

The Penalized GLM Formula

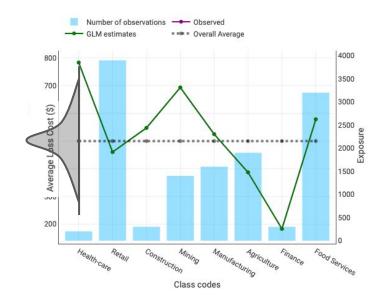
Like for Credibility, Penalized Regressions integrate another prior hypothesis.

But this time, **the prior hypothesis is directly on the coefficient** values: we integrate a probability for different values of the coefficients.

For instance, in the Ridge-regression framework, we assume coefficients follow a normal distribution:

$$\beta \sim N(0, 1/\lambda)$$

Prior Distribution of the Coefficients



The Penalized GLM Formula

The idea of Penalized Regression is to include a second hypothesis in the GLM framework: the coefficients have a a-priori distribution.

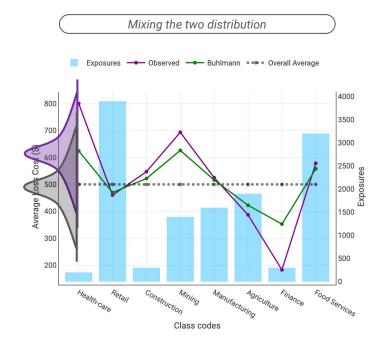
This prior is visible in the maximum of likelihood definition:

$$\beta^* = Argmax \ Likelihood(Obs., \beta) \times \alpha \ e^{\frac{-\beta^2}{1/\lambda^2}}$$

Which means:

$$\beta^* = Argmax \ LogLikelihood(Obs., \beta) - \lambda \beta^2$$

This hypothesis looks **similar to the Bühlmann credibility** but applies on the coefficients instead of the observations; they are equivalent for a one-dimensional model.

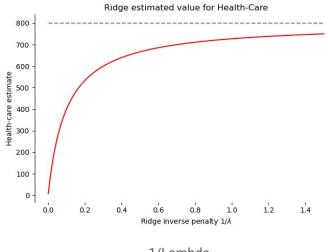


The Ridge

The coefficients computed depend on the λ parameter.

- For small lambda, the coefficients will be close to a simple GLM;
- For large lambda, the coefficients will be close to zero (and the predictions will be close to the base-level).

$$\beta^* = Argmax \ LogLikelihood(Obs., \beta) - \lambda \beta^2$$

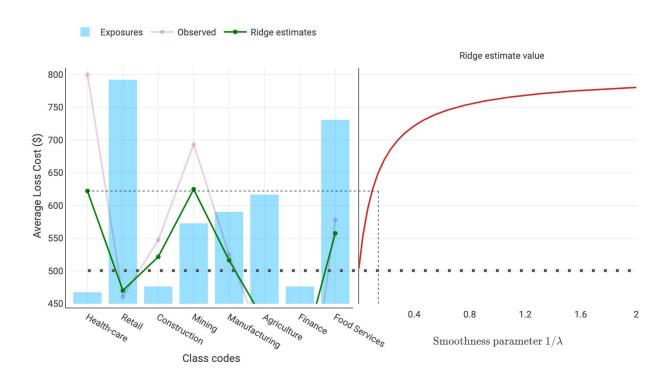


1/Lambda

Large λ (large penalty)

Strong prior on the coefficient (the prior distribution has a small variance).

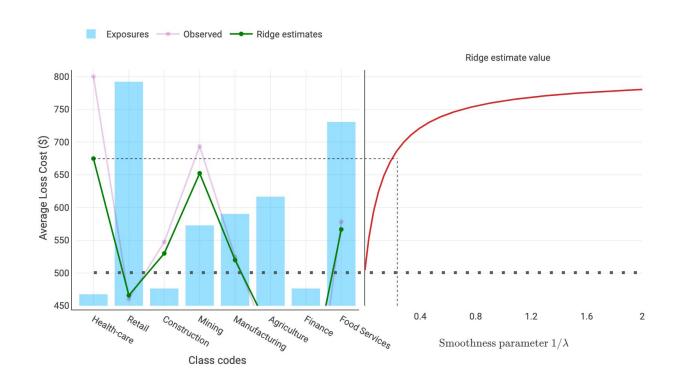
Coefficients and predictions are close to the overall average.



Medium λ (medium penalty)

Intermediate prior on the coefficient (the prior distribution has a small variance).

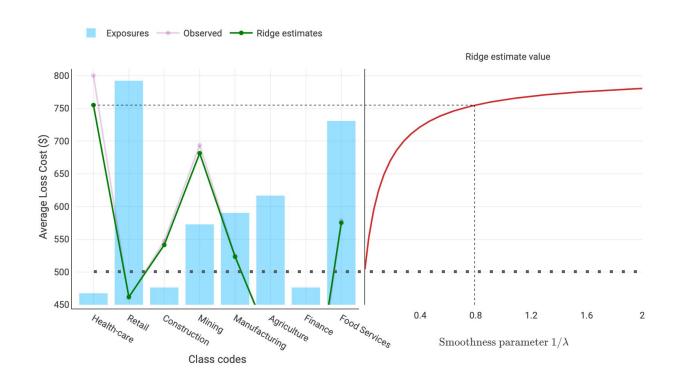
Coefficients and predictions are **further to the overall average**.



Small λ (small penalty)

Weak prior on the coefficient (the prior distribution has a large variance).

Coefficients and predictions are close to the observed value.



Blending GLM with Credibility

Penalized GLMs share the same properties as **Credibility** in the following ways:

- Both shrink GLM estimates toward the complement of Credibility (grand average);
- Both apply more shrinkage to segments with low volume of data / credibility
- 3. Both based on a **Bayesian model**, as in Bühlmann Credibility

The theoretical connection between Credibility and Penalized GLM can be found in:

- Fry, Taylor. "A discussion on credibility and penalised regression, with implications for actuarial work" (2015)
- M.Casotto et al. "Credibility and Penalized Regression" (2022); this topic was also presented last year during the CAS seminar.
- 4. However, while the Credibility approach can be applied to predictions (or one variable) after the GLM fit, the ridge regression can be applied to all variables simultaneously.



A discussion on credibility and penalised regression, with implications for actuarial work

author(s) and include

Preparation of the Addition of

ABSTRACT: In recent years a number of extensions to Generalized Linear Models (GLIA6) have been developed to address some limitations, such as their inability to incorporate Credibility-like assumptions. Among these adaptations, Penalized regression techniques, which bleed GLIA6 with Credibility are widely adopted in the Machine Learning community but are not very popular within the actuarial world. While Credibility methods and GLIA6 are part of the standard actuarial toolkid of predictive modeling, the actuarial iterature describing how Penalized regression blends Credibility with GLIAs is not equally developed. The aim of this whitepaper is to ported penalized regression, the world and the content of the production of t

Comparing different techniques

Control low-exposure segments to prevent overfitting

Set coefficients of low-exposure segments at zero

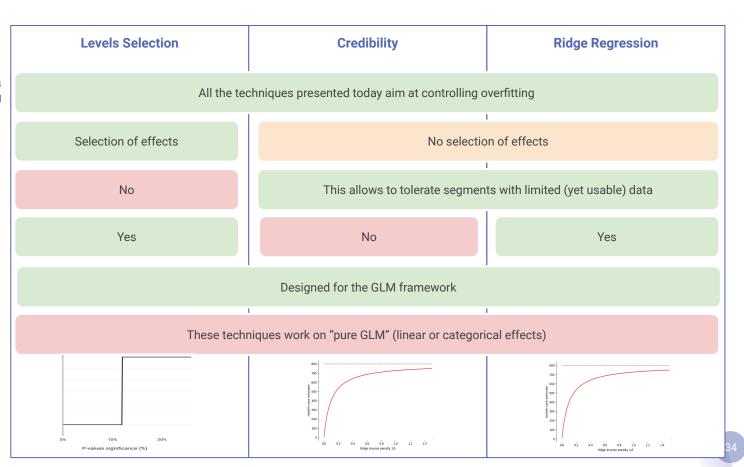
Shrink low-exposure segments

Work for multivariate models

Creates transparent models (GLM or additive models)

Natively manage non-linear effects

Coefficient depending on the robustness parameter



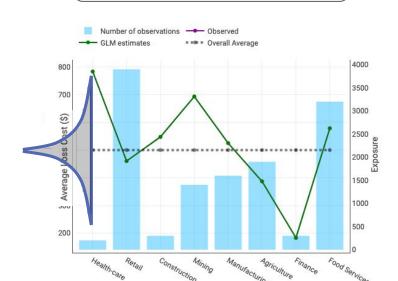
Number of observations

The Penalized GLM Formula: the Lasso

Like the Ridge, Lasso-regression framework, assumes coefficients follow a given distribution.

But this time the distribution used is the Laplace distribution:

$$\beta \sim Laplace(0, \frac{1}{\lambda})$$



Class codes

Prior Distribution of the Coefficients

The Penalized GLM Formula

Ridge-regression also includes a second hypothesis in the GLM framework: the coefficients a-priori follow the Laplace distribution.

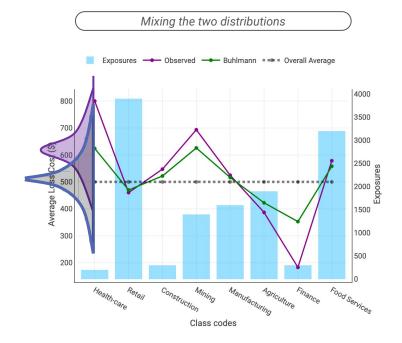
This prior is included in the maximum of likelihood definition:

$$\beta^* = Argmax \ Likelihood(Obs., \beta) \times \alpha \ e^{\frac{-|\beta|}{1/\lambda}}$$

Which means:

$$\beta^* = Argmax \ LogLikelihood(Obs., \beta) - \lambda |\beta|$$

This is very similar to the Ridge regression (and the credibility), but the distribution used is different. Here it is very "pointy" (coefficients have a high probability of being exactly zero).



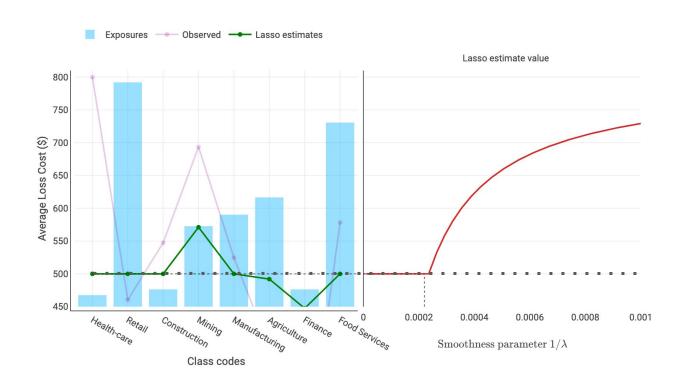
Impact of smoothness to Lasso estimates

Workers Compensation example

Large λ (large penalty)

Strong prior on the coefficient (the prior distribution has a small variance).

Coefficients and predictions are close to the overall average.



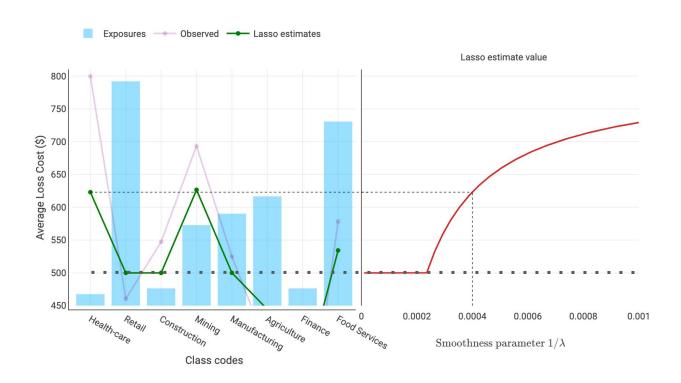
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Medium λ (medium penalty)

Intermediate prior on the coefficient (the prior distribution has a small variance)

Coefficients and predictions are **further to the overall average**.



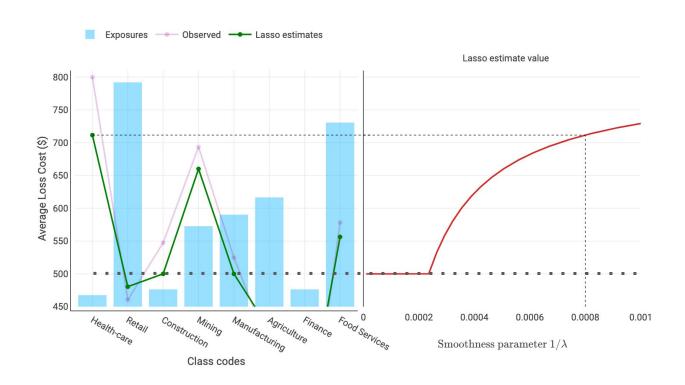
Impact of smoothness to Lasso estimates

Workers Compensation example

Small λ (small penalty)

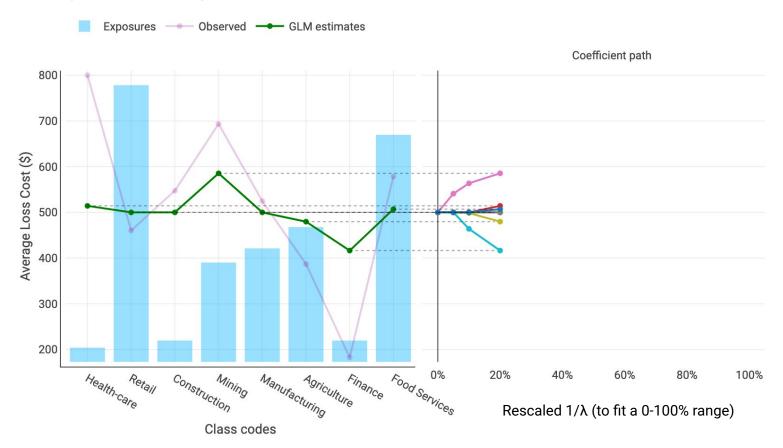
Weak prior on the coefficient (the prior distribution has a large variance)

Coefficients and predictions are close to the observed value.



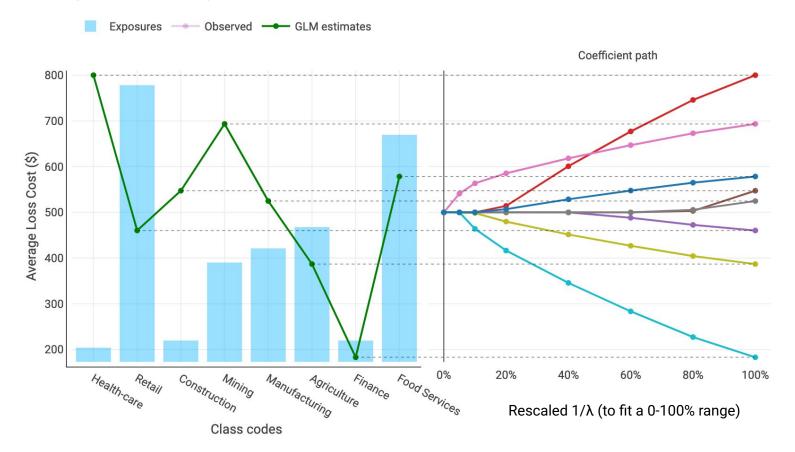
Coefficient path graph of the Lasso

Workers Compensation example



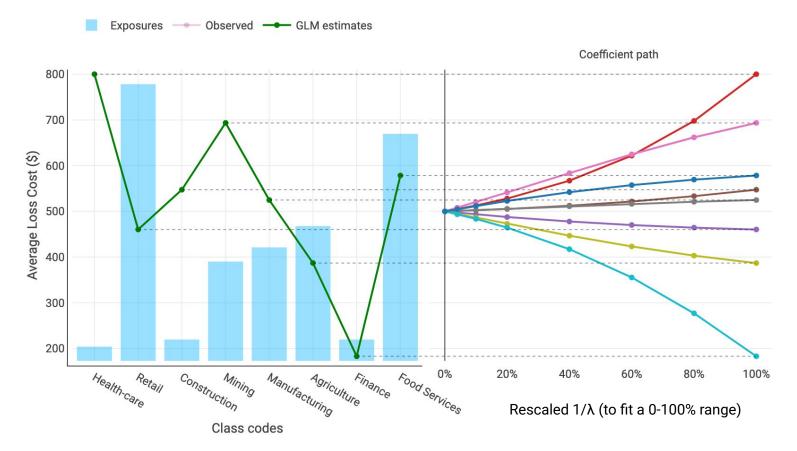
Coefficient path graph of the Lasso

Workers Compensation example



Coefficient path graph of the Ridge

The same graph can be computed for a Ridge regression



Comparing different techniques

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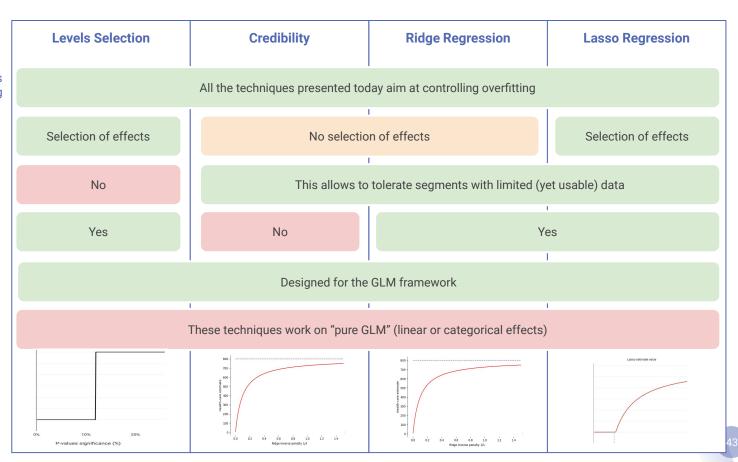
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GBMs and Penalized Regression



Connection between GBMs and Penalized Regression

There is a strong relationship between Credibility and Penalized Regression methods.

There is an equal connection, between Gradient Boosting Machines (GBMs) and Penalized Regression.

Such additional connection highlights the flexibility of the Penalized framework, which can be used to enhance components of the current methodologies of insurance pricing.

Introduction to GBM

What is a Boosted Tree?

GBMs are also referred as **Boosted Trees**.

- Boosted as in Boosting a learning technique that "learns from the mistakes" by iterating models on residuals.
- Trees as in <u>Decision Tree</u> simple model that predicts a target based on decision rules learnt from the data.

What is a tree

Trees estimate losses via recursive if/else decision rules.

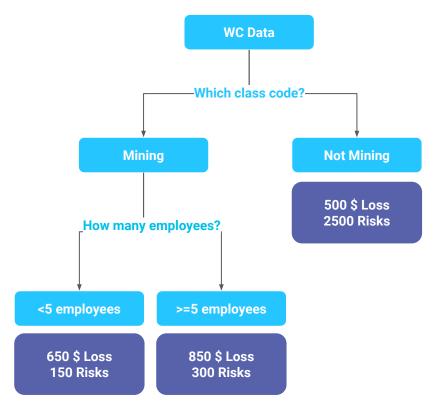
Rules are inferred from the data in a **greedy fashion**.

Each possible two way split of the data is evaluated by comparing the averages of the two complementary partitions.

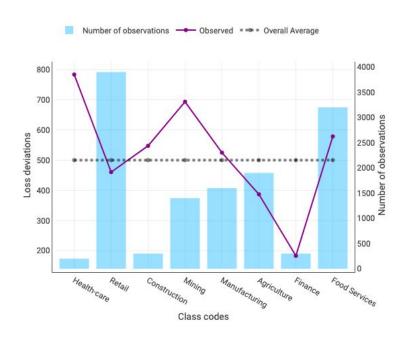
The split leading to the biggest likelihood increase will be selected.

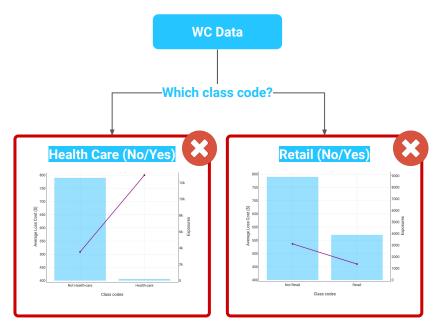
The search is then iterated on each subpopulation until one stopping criteria is met, such as:

- Maximum tree depth;
- Minimum amount observation per leaf;
- Min deviance gain...

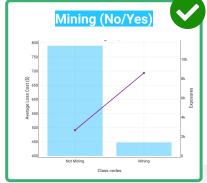


Application: Worker Compensation









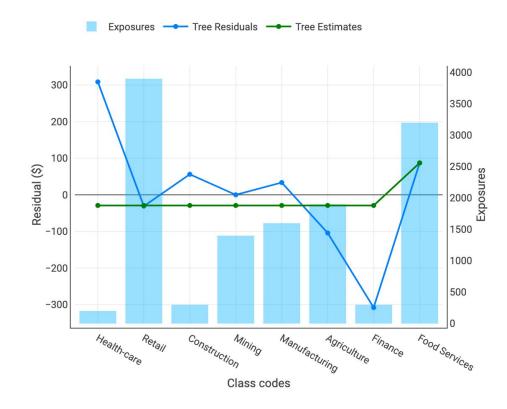
Application: Worker Compensation

The tree split the dataset between Mining and Not Mining, leading to two different predictions.

In a GBM, the **first** tree is the first step of the learning procedure: the **boosting**.

The boosting procedure consist of three steps:

- 1. Compute the **residuals**
- 2. Fit a new tree



Application: Worker Compensation

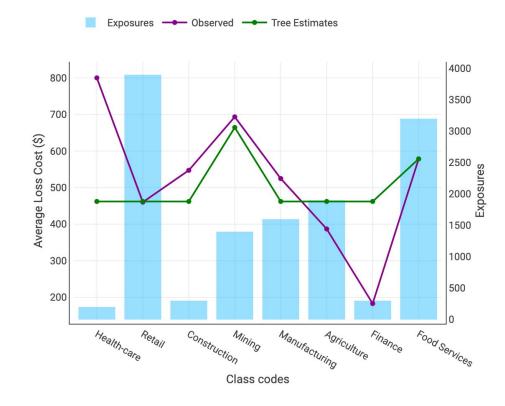
The tree split the dataset between Mining and Not Mining, leading to two different predictions.

In a GBM, the **first** tree is the first step of the learning procedure: the **boosting.**

The boosting procedure consist of three steps:

- 1. Compute the **residuals**
- 2. Fit a new tree
- 3. Compute the estimates by summing the previous trees

Estimate = Tree 1 + Tree 2 + ...



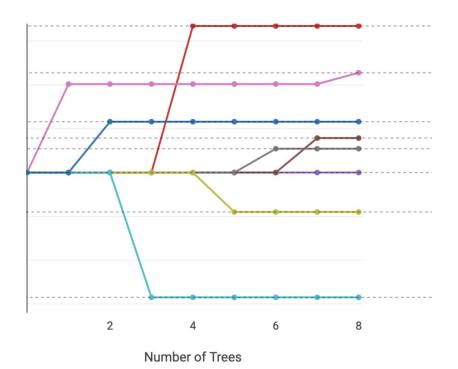
Boosting and stepwise learning

In the simple Worker Compensation example, the GBM learns as in a **forward stepwise procedure**, by iteratively:

- 1. Selecting the most important feature.
- 2. Including (fitting) the effects.

Forward stepwise procedures work well in a very simple case like here, but they are known to **not handle correctly correlated variables.**

For a similar reason, boosting procedures are always combined with a learning rate to improve the model's ability to generalize.



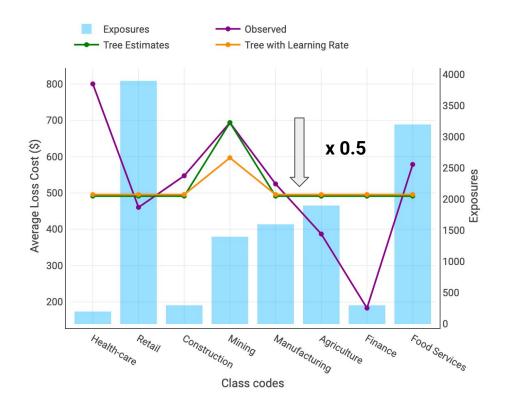
The learning rate

The learning rate is a constant between 0 and 1 that **mitigates** the contribution of an individual tree to the overall prediction.

For each step, the predictions of the tree will be multiplied by the **learning rate**.

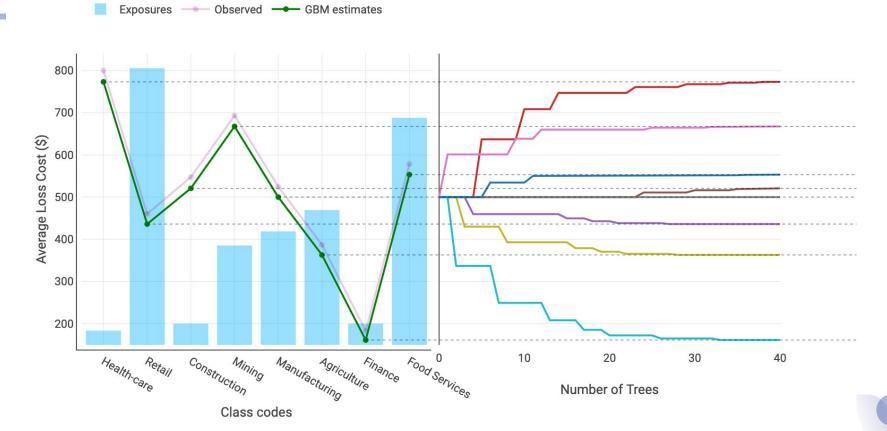
When the learning rate is **0.5** the GBM formula becomes

GBM estimate = **0.5** * Tree_1 + **0.5** * Tree_2 + **0.5** * ...



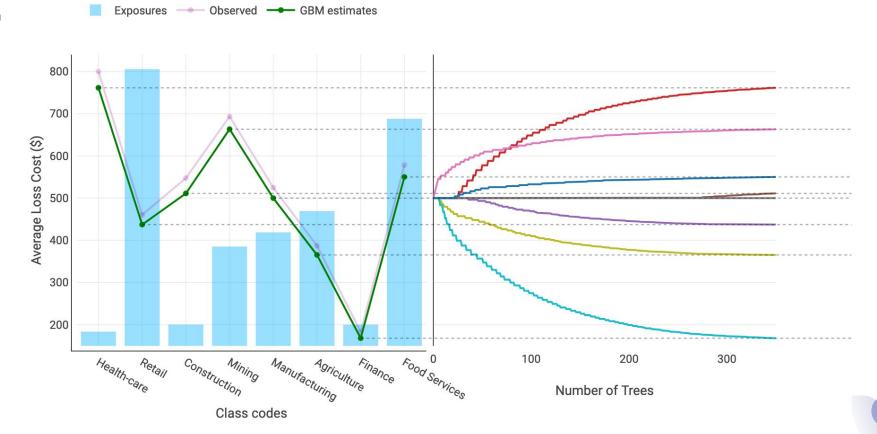
Learning rate = 0.5

Estimate evolution until 40 trees



Learning rate = 0.05

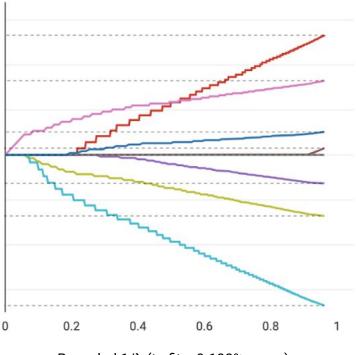
Estimate evolution until 350 trees



Toward the coefficient path graph

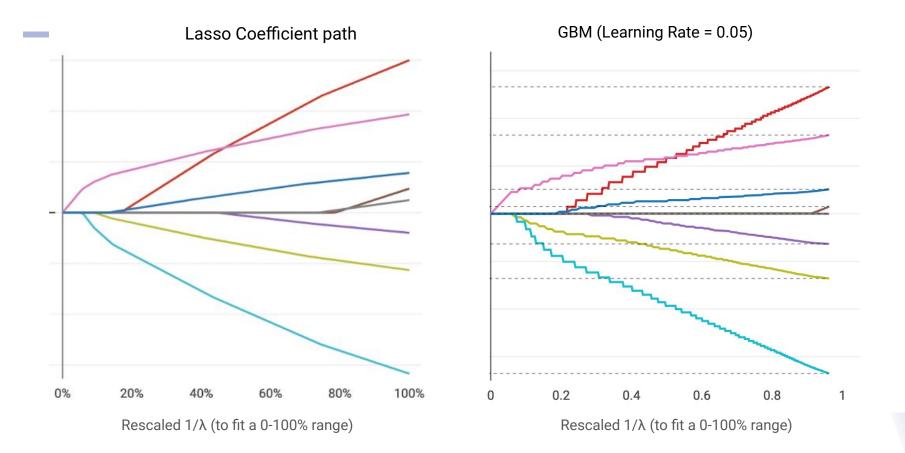
The graph on the right represents the evolution of the estimates **by the number of trees.**

The same graph can be represented by rescaling the x-axis in the same scale as in penalized regression (to fit a 0-100% range).



Rescaled $1/\lambda$ (to fit a 0-100% range)

Comparing Lasso and GBM



Boosting converges to the Lasso

The convergence of boosting toward Lasso solution is a proven mathematical result.

- 1. GBMs provide a good approximation of a Lasso regression;
- Both GBMs and Lasso allow to tune a parameter in order to control the training error and ability to generalise,
 - a. GBMs via the combination of number of trees learning rate (and many other tree-related parameter);
 - b. Lasso via the smoothness parameter.



A discussion on credibility and penalised regression, with implications for actuarial work

The Annals of Stationer 2004, Vol. 32, No. 2, 467-499 Preport © Institute of Mathematical Statistics, 20

Presented to ASTIN, AFIR/E

The institute will ensure that all re-

LEAST ANGLE REGRESSION

By Bradley Efron, ¹ Trevor Hastie, ² Iain Johnstone ³ and Robert Tibshirani ⁴

Stanford University

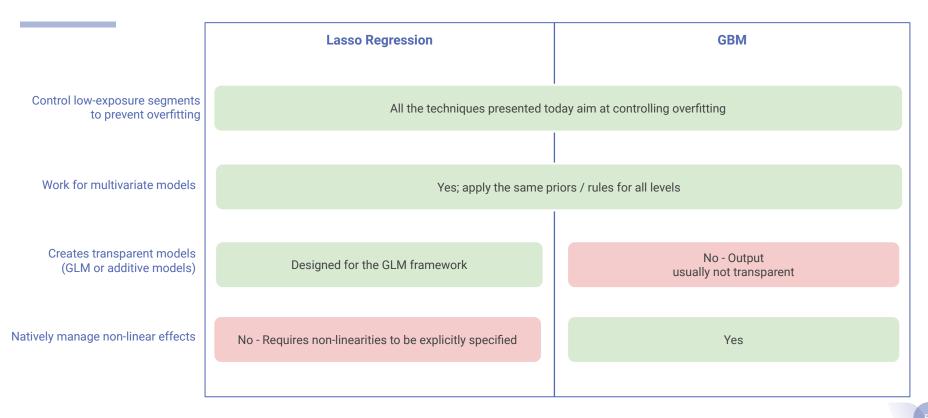
The purpose of model selection algorithms such as All Subsets, Forward Selection and Backward Elimination is to choose a linear model on the basis of the same set of data to which the model will be applied. Typically we have available a large collection of possible covariates from which we hope to select a parsimonious set for the efficient prediction of a response variable. Least Angle Regression (LARS), a new model selection algorithm, is a useful and less greedy version of traditional forward selection methods. Three main properties are derived: (1) A simple modification of the LARS algorithm implements the Lasso, an attractive version of ordinary least squares that constrains the sum of the absolute regression coefficients; the LARS modification calculates all possible Lasso estimates for a given problem, using an order of magnitude less computer time than previous methods. (2) A different LARS modification efficiently implements Forward Stagewise linear regression, another promising new model selection method; this connection explains the similar numerical results previously observed for the Lasso and Stagewise, and helps us understand the properties of both methods, which are seen as constrained versions of the simpler LARS algorithm. (3) A simple approximation for the degrees of freedom of a LARS estimate is available, from which we derive a C_p estimate of prediction error; this allows a principled choice among the range of possible LARS estimates. LARS and its variants are computationally efficient: the paper describes a publicly available algorithm that requires only the same order of magnitude of computational effort as ordinary least squares applied to the full set of

1. Introduction. Automatic model-building algorithms are familiar, and sometimes notorious, in the linear model literature: Forward Selection, Backward Elimination, All Subsets regression and various combinations are used to automatically produce "good" linear models for predicting a response y on the basis of some measured covariates x₁, x₂, ..., x_m, cohomes is often defined in terms of prediction accuracy, but parsimony is another important criterion: simpler models are preferred for the sake of scientific insight into the x - y relationship. Two promising recent model-building algorithms, the Lasso and Forward Stagewise limited.

What about Ordinal variables?



Comparing GBM and Penalized Regression



What about Ordinal variables?

The Worker Compensation example highlights the connection between GBMs and Lasso for categorical variables.

The main benefit of a GBM is its ability to natively fit non-linear effect on ordinal variables.

At a first glance, Penalized Regressions seem unable to natively fit non-linear effects.

We will show that, by analyzing how GBMs incorporate non-linearities, it is possible to incorporate the same learning procedures to Penalized regression.

GBMs natively handles non-linear effects by combining

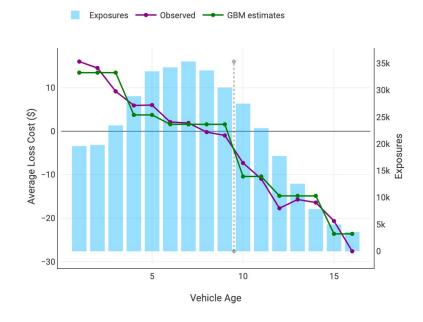
1. Trees

Detects the location on where to split the ordinal variables in two region

2. **Boosting**

Adaptively learns structure from the residuals / errors

GBM Estimate = Tree 1 + Tree 2 + ... + Tree 7



The impact of the Learning Rate

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1. Trees

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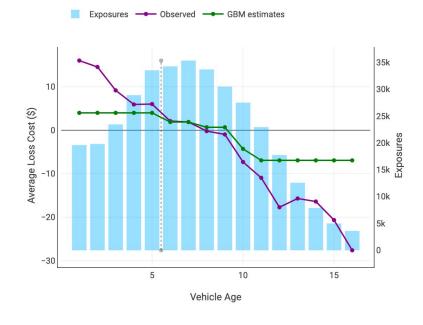
2. Boosting

Adaptively learns structure from the residuals / errors

3. Learning Rate

Allows to incrementally adapt the trees to the signal, making the model 'smoother' and more robust to correlations

GBM Estimate = **0.5** * Tree 1 +... + **0.5** * Tree 7



How GBMs 'learn' ordinal variables

These visual examples highlight **how** GBM effectively learn non-linearities:

- 1. The most significant split (the 'derivative') is computed;
- 2. The learning rate defines the amount of signal to be learnt (hence controlling for **smoothing**);
- 3. The number of trees defines the stopping point to prevent overfitting.

Penalized regression can replicate this structure by using an appropriate **prior distribution** (or **penalty**): the **derivative Lasso**.

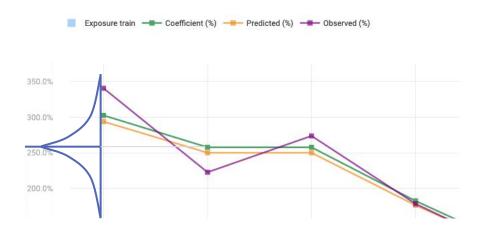
The derivative Lasso



Creating new Priors and Penalties

Grouping is statistically equivalent to the assumption that the coefficients of two consecutive levels:

- Are more likely to be close than far apart if they are significantly different;
- Or have the same coefficients if they are not significantly different...



Creating new Priors and Penalties

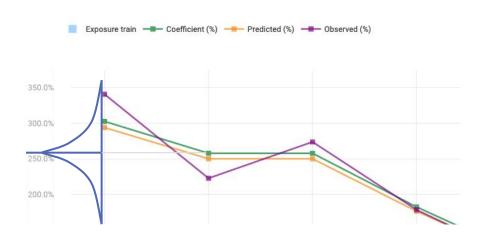
As the values of the coefficients are discrete, the derivative can be written as:

This distribution of probability is used as a prior when maximizing the likelihood to fit a model:

$$p(\beta) \alpha e^{-\lambda |\beta_i - \beta_{i+1}|}$$

This means that the derivative of the (ordinal) variable follows a Laplace distribution:

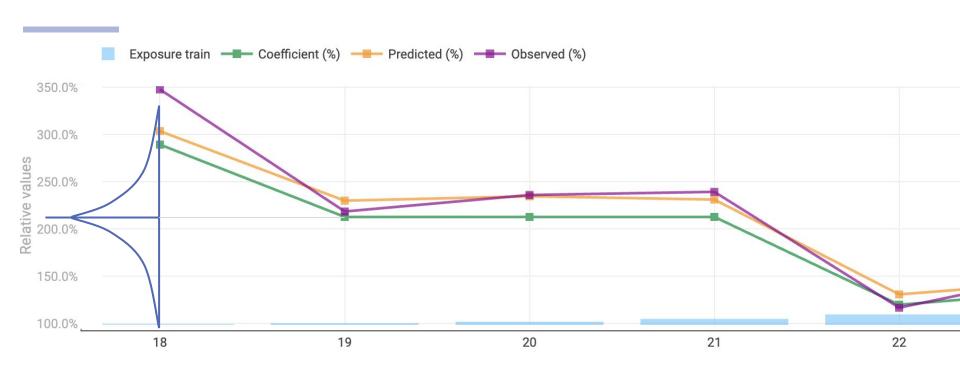
$$\beta^* = Argmax_{\beta} \ LL(x, y, \beta) - \lambda |\beta_i - \beta_{i+1}|$$





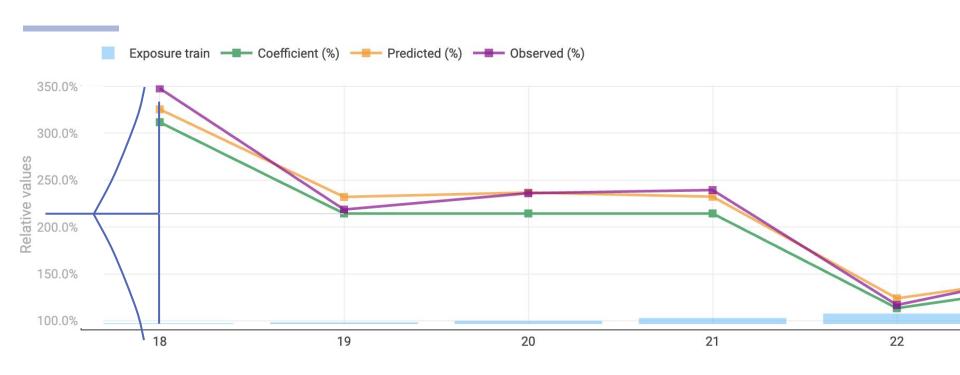
Average Smoothness Weaker reliance on the observation

The final model is an average between the most likely coefficients according to the prior and the observations



Weak Smoothness ⇔ Strong reliance on the observation

The prior has a very limited impact on the final model

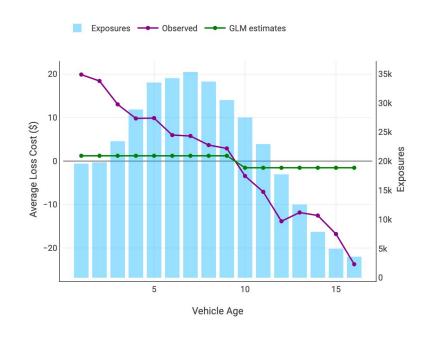


Under these "Lasso" assumption on the derivative, penalized regression can natively incorporate non-linear effects.

Furthermore, the convergence result between GBMs and Lasso is still valid.

To control the training error and ability to generalise:

- Penalized Regression require the definition of a single parameter: the smoothness
- GBMs require to determine the combination of **several parameters**:
 - number of trees
 - learning rate
 - and other tree-related parameters

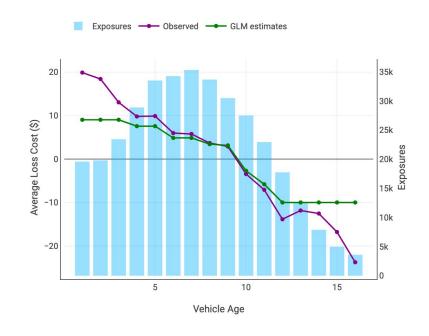


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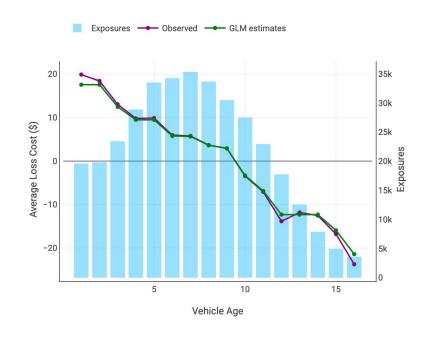


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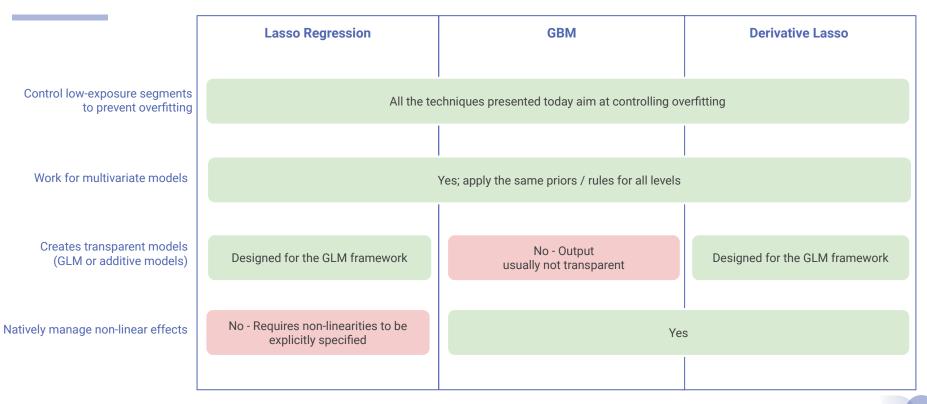
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Conclusion



Comparing GBM and Penalized Regression



Conclusion

Penalized regression offers a flexible and theoretically sound framework to tackle and address the GLM's drawbacks.

It does so in an accessible way:

- Penalized regression require the choice of **only one parameter: the smoothness**
 - Smoothness relates to known credibility techniques
- Penalized regression require **little to no** investment cost
 - Inputs and outputs are equal to GLMs adding penalizations to GLM is straightforward via software
- Potentially unlock use-cases not previously considered for modeling
 - Via complement of credibility, it is possible to gradually update current models to new ones
 - GLMs can be used as a data analysis alternative as modeling effort is reduced since non-linearities are natively handled.

The big picture

Control low-exposure segments to prevent overfitting

Set coefficients of low-exposure segments at zero

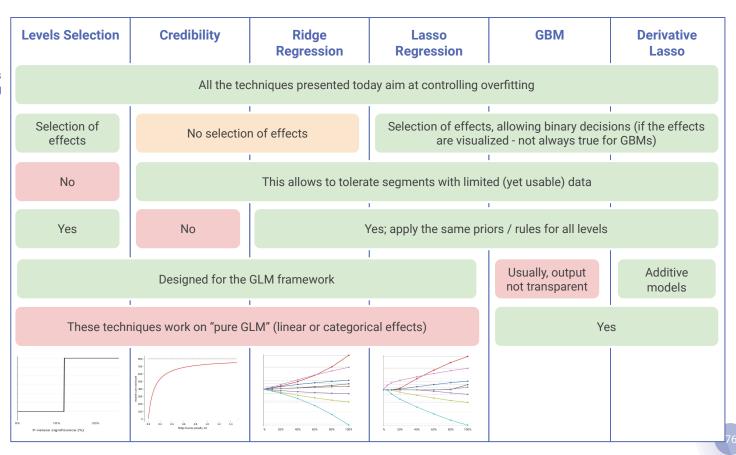
Shrink low-exposure segments

Work for multivariate models

Creates transparent models (GLM or additive models)

Natively manage non-linear effects

Coefficient depending on the robustness parameter



THANKS



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Is the convergence result a desirable property?

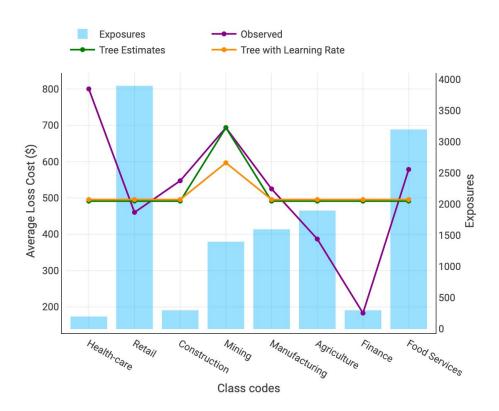
Smaller learning rate corresponds to better models, but at a cost

In GBMs the smaller the learning rate the better

- Smaller learning rates lead to more performant and robust models - as they handle better correlations
- Smaller learning rates require to build many more trees

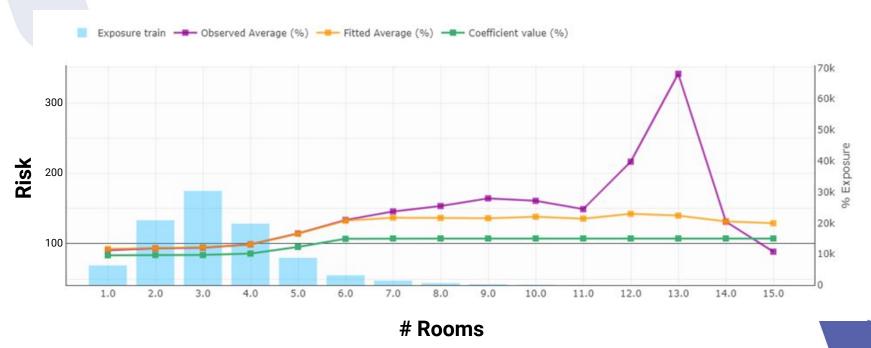
The only limit of choosing a smaller learning rate in a GBM is the time required to build the models.

Lasso being equivalent to a very little learning rate is a desirable property.



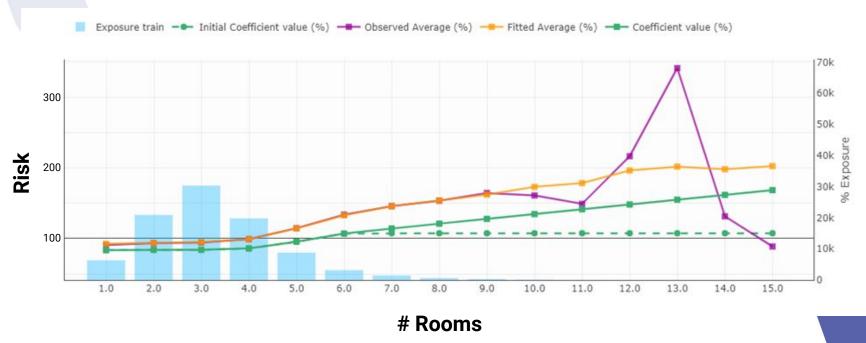
Interpretability and anti-selection

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The Models Life-cycle

The first layer of modeling is created by a machine-learning algorithm, leveraging the credibility principles described above.

The model created by this algorithm is additive (table-based model). It can be visualized, fully understood and modified if needed.

The output of the modeling process is a table-based model. It is fully transparent and can be analyzed and validated with no difficulties.

GLOBAL PARAMETERS

- Smoothness level
- Parsimony level

DATA

- Explanatory Variables
- Target Variable



MODEL PARAMETERS

Effect functions values
 Fitted from a purely data-driven process



FINAL MODEL PARAMETERS

 Effect functions values, based on expertise, to ensure safe extrapolation on low-data segments

