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See "Exam Registration" in the Exams \& Admissions section of the CAS website

## 2015 SYLLABUS UPDATES

In Fall 2015, the CAS will be administering Exams LC, ST, S, 5, 6 Canada, 6 United States, and 8. The CAS Syllabus Committee has approved changes for the Fall 2015 syllabus as outlined in the Changes for the Fall 2015 CAS Syllabus of Basic Education memorandum from the Vice President-Admissions.

The following are the changes made to the Syllabus of Basic Education after its initial publication.

## 2015 Spring Examinations

## Exam 7

Errata added for International Actuarial Association, "A Global Framework for Insurer Solvency Assessment," a research report of the Insurer Solvency Assessment Working Party, 2004, Chapters 1, 2, 5, 7, 8, and 9; Appendices $B, D, E, H$, and $I$.

## Exam 6-U.S.

Errata added for Odomirok, K. C.; McFarlane, L.M.; Kennedy, G.L; and Brenden, J., Financial Reporting Through the Lens of a Property/ Casualty Actuary, Casualty Actuarial Society, 2014, Edition 4.

## 2015 Fall Examinations

## Exam S

An initial syllabus for Exam S was published on the CAS website earlier this year. After careful review, the Syllabus Committee made some clarifying changes to the Exam S Syllabus. The final syllabus for the October 2015 administration of this exam can be found in the Exams \& Admissions section of the CAS website.

Note: This Syllabus is subject to change in the future. The CAS is not responsible for any errors or omissions in the Syllabus.

## ANOUNCEMENTS FOR FALL 2015

(Revised May 14, 2015)

## Exam Registration

Candidates may find online exam registration and related information on the Exam Registration page of the CAS website. Prior to completing an online application for Exams LC, ST, S, and 5-9, candidates must submit an Electronic Signature Authorization Form - details are available on the same page.

There is only one registration deadline for each exam. No late registrations will be accepted. The exam dates and registration deadlines are available in the " 2015 Examination Schedule" section. Please allow at least 10 working days for your mailed application to reach its destination. Whether payment is made by personal or company check, it is the candidate's responsibility to ensure that the application and fee are received by the stated deadline. Exceptions will not be made.

## Transition Rules for new Exam S

Candidates should review carefully the Transition Rules for Exam S approved by the CAS Board of Directors. These rules can be located in the Examination Rules, C. Grades and Accreditation, Transition Programs section of the Syllabus.

## Syllabus Update for Exam S

An initial syllabus for Exam $S$ was published on the CAS website earlier this year. After careful review, the Syllabus Committee made some clarifying changes to the Exam S Syllabus. The final syllabus for the October 2015 administration of this exam can be found in the Exams \& Admissions section of the CAS website.

The Examination Committee expects that Exam S will consist of approximately 40 to 50 multiple-choice questions.

Note: This Syllabus is subject to change in the future. The CAS is not responsible for any errors or omissions in the Syllabus.

## INTRODUCTION

## Principles of the Casualty Actuarial Society for Basic Education

The primary purpose of the Casualty Actuarial Society (CAS) basic education process is to ascertain whether candidates for the CAS designations have satisfied CAS learning objectives. The CAS Board of Directors adopted the following principles on May 6, 2001.

1. Basic education will remain a cornerstone of the CAS.
2. The CAS will assure that its members have the knowledge of those areas needed to practice effectively in the broad and expanding range of property, casualty, and similar business and financial risks (general insurance).
3. The CAS is committed to a depth of knowledge of techniques associated with the broad range of property, casualty, and similar business and financial risks.
4. The CAS will provide the basic education necessary to meet qualification standards to sign statements of actuarial opinion for general insurance and related specialties in at least the U.S. and Canada.
5. The education process will provide a balance among theoretical concepts, practical applications, and business acumen, to prepare our members to deliver high-quality service to meet current and projected future needs of employers and clients.
6. The CAS will approve the syllabus and examination standards used in determining eligibility for CAS membership.
7. Demonstration of mastery of the skill sets required of members is critical to basic education.
8. The CAS is committed to maintaining self-study as one route for attainment of designations.
9. The CAS will pursue strong working relationships with academia and professionals in related fields.
10. The CAS will attract a pool of strong candidates from a variety of backgrounds to the actuarial profession.
11. The CAS supports the goal of developing a global shared foundation of actuarial education, including joint sponsorship of examinations where consistent with other principles.
12. The CAS, as an educator of general insurance and related specialties, will remain a significant contributor to the worldwide actuarial profession.

## Syllabus Goals and Objectives

One of the primary objectives of the Casualty Actuarial Society (CAS) is the development of qualified professionals in the field of casualty actuarial science. The CAS conducts an educational and examination program for prospective members in order to achieve this objective.

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The syllabus goals and objectives are as follows:

1. To develop a general understanding of the social, political, regulatory, legal, economic, and financial environment of the business of property and casualty insurance and similar risk assessment as well as the historical development of that environment.
2. To develop a thorough understanding of the fundamental mathematical concepts applicable to solving insurance and similar risk assessment problems, and to develop a high degree of skill in their applications.
3. To develop a comprehensive understanding of the business of property and casualty insurance, including underwriting, claims, marketing, and finance, as well as how these functions are performed and interrelated.
4. To develop a working knowledge of property and casualty insurance policies and contracts.
5. To develop an expert knowledge of a broad range of techniques to solve problems and to develop the ability to discern the appropriateness of techniques for particular applications based on knowledge of the underlying assumptions, strengths, and weaknesses.
6. To develop an expert knowledge of a broad range of relevant and standard actuarial practices in order to present a framework for the use of problem-solving techniques.
7. To encourage a sense of inquisitiveness and creativity toward problem solving in order to foster an appreciation of the art in actuarial science.

Note: The items in this Syllabus were chosen for their educational value. They are intended to expose the candidate to a wide range of information and to a variety of methods, opinions, and practices in the casualty actuarial field. Inclusion of material in the Syllabus does not imply that the CAS endorses the views, methodologies, or techniques therein.

## Education and Examination System

The CAS vice president-admissions supervises the CAS education and examination system. The vice president-admissions is supported by the following four admissions committees:

## CAS Education Policy Committee

The Education Policy Committee recommends to the CAS Board of Directors the goals and objectives of the CAS education and examination system to ensure that the needs of the Society, its members, and its potential members are met. The committee reviews and recommends any changes to the CAS Executive Council on the CAS Basic Education Waiver Policy and similar issues. The committee also monitors the operations of the other educational and examination committees to ensure continued effectiveness.

## CAS Syllabus Committee

The Syllabus Committee determines the scope and content of the CAS Syllabus and course of readings for CAS Examinations.

A chairperson supervises the committee that is composed of Fellows who represent a broad spectrum of CAS

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members including insurers, consultants, regulators, and academicians. At least one representative of the Canadian Institute of Actuaries (CIA) also serves on the committee; usually at least one of the representatives is a member of the CIA Education and Examination Committee. One or more members specialize in the material for each examination part. These specialists recommend changes to the Syllabus; however, the entire committee must approve recommendations.

Members of the Syllabus Committee review the individual exam syllabi regularly. Both short- and long-term goals for improvement are developed. Textbooks and articles may be designated for inclusion. If the committee determines that new study material needs to be developed or that existing material needs to be revised, the committee may commission the creation of Study Notes for inclusion. Every effort is made to develop material that is appropriate, relevant, up-to-date, concise, and well written. Suggestions for improvement are always welcome and should be directed to the Syllabus Committee at the CAS Office address.

## CAS Examination Committee

The Examination Committee organizes, manages, administers, and grades the CAS Examinations. The committee also establishes the standards to be achieved by successful candidates.

The chairperson supervises the committee and is responsible for the overall administration of the CAS Examinations. Several senior committee officers with the title of general officer assist the chairperson. The committee is subdivided into Examination Part Committees, each headed by an examination part chairperson.

The following provides details about the CAS-specific examinations:

- The responsibility for each CAS Examination is assigned to a part committee that writes, grades, and maintains the standards for that examination. One or more examination consultants who are CAS members and are experts on the material covered by that examination assist each part committee. A proofreader who concentrates on uniformity and grammar also assists the part committees. In addition, academic consultants who are independent experts from the academic community assist some part committees.
- Each examination is drafted by the responsible Examination Part Committee to test candidates' knowledge of the items listed in the syllabus for the specific exam. The individual part committee, examination consultants, one of the Examination Committee general officers, the Examination Committee chairperson, and, in some cases, academic consultants review each examination to assure its quality.
- Every effort is made to ensure that the questions fall within the scope of the individual exam syllabus. Complete coverage of all material is not practical for every examination every year. The goal is to produce examinations that contain representative, high-quality questions that test candidates' knowledge of the material. Trick questions are deliberately avoided, and the wording of each question is considered carefully to eliminate possible ambiguities. Preliminary versions of each examination are thoroughly reviewed in relation to all of these factors before the final examination is approved.


## CAS Candidate Liaison Committee

The Candidate Liaison Committee strives to focus on issues of importance to candidates who are taking CAS

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Examinations. The committee serves as a direct point of contact for candidates to voice individual or group concerns regarding the education and examination process. It also provides a means for an exchange of information between candidates and the admissions committees via Future Fellows, a quarterly newsletter. Candidate representatives who are actively involved in the examination process serve as advisors to the committee.

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## 2015 EXAMINATION SCHEDULE

Exams for Online Courses 1 and 2 by Computer-Based Testing

|  | EXAM DATES | DURATION | START TIME | EXAM REFUND DEADLINE |
| :--- | :---: | :---: | :---: | :---: |
| January-March Test Window | Jan. 15-March 15, 2015 | 2 Hours | Various | Three business days prior to scheduled exam-fees <br> apply. |
| April-June Test Window | April 15-June 15, 2015 | 2 Hours | Various | Three business days prior to scheduled exam-fees <br> apply. |
| July-September Test Window | July 15 - Sept. 15, 2015 | 2 Hours | Various | Three business days prior to scheduled exam-fees <br> apply. |
| October-December Test Window | Oct. 15-Dec. 15,2015 | 2 Hours | Various | Three business days prior to scheduled exam -fees <br> apply. |

## April 2015 Exam Administration

| Exam | EXAM DATES | DURATION | START TIME | REGISTRATION DEADLINE | REFUND DEADLINE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Exam LC | April 30, 2015 | 1.5 Hours | 1:30 p.m. | March 5, 2015 | April 17, 2015 |
| Exam ST | April 30, 2015 | 2.5 Hours | 8:30 a.m. | March 5, 2015 | April 17, 2015 |
| Exam 5 | April 27, 2015 | 4 Hours | 8:30 a.m. | March 5, 2015 | April 17, 2015 |
| Exam 6-Canada and 6 U.S. | April 28, 2015 | 4 Hours | 8:30 a.m. | March 5, 2015 | April 17, 2015 |
| Exam 7 | April 24, 2015 | 4 Hours | 8:30 a.m. | March 5, 2015 | April 17, 2015 |
| Exam 9 | April 29, 2015 | 4 Hours | 8:30 a.m. | March 5, 2015 | April 17, 2015 |

Examination Schedule, 2015

October 2015 Exam Administration

| Exam | EXAM DATES | DURATION | START TIME | REGISTRATION DEADLINE | REFUND DEADLINE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Exam LC | October 29, 2015 | 1.5 Hours | 1:30 p.m. | September 3, 2015 | October 23, 2015 |
| Exam ST | October 29, 2015 | 2.5 Hours | 8:30 a.m. | September 3, 2015 | October 23, 2015 |
| Exam S | October 30, 2015 | 4 Hours | 8:30 a.m. | September 3, 2015 | October 23, 2015 |
| Exam 5 | October 26, 2015 | 4 Hours | 8:30 a.m. | September 3, 2015 | October 23, 2015 |
| Exams 6-Canada and 6-U.S. | October 27, 2015 | 4 Hours | 8:30 a.m. | September 3, 2015 | October 23, 2015 |
| Exam 8 | October 28, 2015 | 4 Hours | 8:30 a.m. | September 3, 2015 | October 23, 2015 |

## ST9 Exam Administration for CERA Designation

| Exam | EXAM DATES | DURATION | START TIME | REGISTRATION DEADLINE | REFUND DEADLINE |
| :--- | :---: | :---: | :---: | :---: | :---: |
| April Administration | April 30, 2015 | 3 Hours | Check Entry <br> Permit | February 12, 2015 | February 11, 2015 |
| October Administration | October 12,2015 | 3 Hours | Check Entry <br> Permit | July 23, 2015 | July 22,2015 |

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## Important Schedule Notes

- Starting times listed for examinations refer to the local time.
- Candidates should arrive at the examination center at least 30 minutes prior to the scheduled exam time for the check-in process.
- Examinations administered exclusively by the CAS will have a reading time prior to the commencement of the timed exams. For Exams LC and ST, there will be a 10 -minute reading period; for Exams $S, 5-9$, there will be a 15 -minute reading period.
- Currently, waivers for Exam 1, Exam 2, Exam 3F, and Exam 4 are accepted from the Actuarial Society of South Africa, the Actuaries Institute (Australia), the Canadian Institute of Actuaries (except for Exam 1), the Institute and Faculty of Actuaries, and the Society of Actuaries.
- Updated information for waivers for Exam 1, Exam 2, Exam 3F, and Exam 4 will be incorporated as necessary and will be noted in the syllabus section for the specific exam.
- To meet the CAS requirements for CERA, candidates should submit their registration to the CAS for Institute and Faculty of Actuaries (U.K.) Exam ST9.


## ASSOCIATESHIP REQUIREMENTS

## Validation by Educational Experience

VEE-Corporate Finance
VEE-Economics.

## Online Courses

Online Course 1 Risk Management and Insurance Operations (same as The Institutes Course CA1)
Online Course 2 Insurance Accounting, Coverage Analysis, Insurance Law, and Insurance Regulation (same as The Institutes Course CA2)

## Examinations

Exam 1 Probability (receive credit for SOA Exam P)
Exam $2 \quad$ Financial Mathematics (receive credit for SOA Exam FM)
Exam 3F Models for Financial Economics (receive credit for SOA Exam MFE)
Exam 4 Construction and Evaluation of Actuarial Models (receive credit for SOA Exam C)
Exam S Statistics and Probabilistic Models*
Exam $5 \quad$ Basic Techniques for Ratemaking and Estimating Claim Liabilities
Exam 6 Regulation and Financial Reporting (Nation-Specific)
*Newexam requiredbeginninginFall2015replacing Exam LC, ExamST, and VEE-AppliedStatistical Methods. However, transition rules allowcandidates with creditforeitherExam LCand/orExamSTto take the remainingexam/educationalrequirementstoobtaincreditforthe newExamSbyAugust31,2016.

## Course on Professionalism

## FELLOWSHIP REOUIREMENTS

Fellowship requires all Associateship requirements plus the following:
Exam 7 Estimation of Policy Liabilities, Insurance Company Valuation, and ERM
Exam $8 \quad$ Advanced Ratemaking
Exam 9 Financial Risk and Rate of Return

## EXAMINATION RULES

## A. Registration

## Administration of Examinations

The CAS basic education structure has Validation by Educational Experience (VEE) requirements, two online courses, several examinations (see Basic Education Summary), and the Course on Professionalism. Credit for Exams 1, 2, 3F, and 4 is granted based on exam options as defined in the individual exam syllabi. The two online courses are available through The Institutes. The CAS exclusively administers Exams LC, ST, S, and 5-9 and the Course on Professionalism. ${ }^{1}$ The Canadian Institute of Actuaries (CIA) cosponsors all the examinations except Exam 6-United States and Exam 6Actuarial Institute of Chinese Taipei.

## Filing of Applications and Deadlines

## Exams 1, 2, 3F, and 4

For Exams 1, 2, 3F, and 4, the candidate should follow the application process and deadlines of the sponsoring organizations.

## Exams LC, ST, S, and5-9

All candidates filing for an examination(s) must submit a signed application for each examination period. Both online registration and application forms are linked at each of the individual Examination pages under the "Exams and Admissions" section of the CAS website. Payment must accompany each application to be valid. Applications must be received by the registration deadlines stated in the Examination Schedule of this Syllabus. Please allow at least 10 working days for your mailed application to reach its destination. Whether payment is made by personal or company check, it is the candidate's responsibility to ensure that the application and fee are received by the stated deadline. Exceptions will not be made.

Send applications as follows: Candidates may submit examination registrations for Exams LC, ST, S, and 5-9 by mail or online. Applications must be received by the published deadlines. Candidates submitting a hard copy of their registration should mail them as follows:

| Mailapplication with checkormoneyorderin | Send application with credit card payment |
| :---: | :---: |
| U.S. fundsorCanadianequivalent(payableto | (Visa, MasterCard, or American Express) and all |
| "Casualty Actuarial Society") to: | overnight deliveries to: |
| Casualty Actuarial Society | Casualty Actuarial Society 4350 |
| P.O. Box 425 | N. Fairfax Drive, Suite 250 |
| Merrifield, VA 22116-0425 | Arlington, Virginia 22203 |
|  | Telephone: 703.276.3100 |

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Candidates submitting their registrations online for Exams LC, ST, S, and 5-9 must pay by credit card. All credit card payments will be processed in U.S. funds. Prior to completing an online application, candidates must submit an Electronic Signature Authorization Form (ESAF). By signing the ESAF, candidates agrees to be bound by the rules and regulations related to the examinations. It will also provide a signature of record for comparison to signatures on the individual examination envelopes. The ESAF is available in the Exam Registration page of the CAS website. Unless the candidate has a name change, the ESAF only needs to be submitted once. Candidates who intend to register online should submit their ESAFs at least one week prior to the exam registration deadline to allow for processing time.

Candidates will be sent an acknowledgment of receipt of their application within three weeks of the date that the application form was received at the CAS Office beginning in early February for April Examinations and early August for October Examinations. This acknowledgment is the candidate's receipt of exam fees paid. Please retain this acknowledgment for tax purposes if needed. Candidates that have not received an acknowledgment prior to the registration deadline should contact the CAS Office or their accounting department to ensure that their applications reached the CAS Office. The candidate can also verify their registration by logging into their CAS account and checking their profile.

## Online Courses 1 and 2

CAS Online Courses 1/CA1 and 2/CA2 are available through The Institutes. When candidates register for the individual online course, the fee includes one attempt at the exam. Before registering for the exam, candidates must obtain their Master ID number from the CAS-it will be required to register for the exam. After progressing through the online course, candidates arrange for their exam by contacting:

The Institutes, Customer Service<br>720 Providence Road, Suite 100<br>Malvern, PA 19355-3433<br>Telephone: (800) 644-2101 or (610) 644-2100 ext. 6000<br>E-mail: CustomerService@Thelnstitutes.org<br>CAS Online Courses page at The Institutes website: www.aicpcu.org/cas.htm

## Name

Candidates must use their legal name on all examination registration materials and when corresponding with the CAS. Any change in name must be accompanied by acceptable documentation.

## Fees

Examination fees must be paid each time a candidate registers for an exam. Payment options are described in a previous section, Filing of Applications and Deadlines. A $\$ 20$ surcharge will be assessed for all returned checks. The charts below show the examination fee schedules for 2015 at the time of publication. All fees are listed in U.S. dollars and are subject to change. Other fees that may apply include fees for change of center, refund, and/or a special exam center.

## Exams 1,2,3F, and 4

Contact the sponsoring organization.

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## Exams LC, ST, S, and 5-9 and Online Courses 1 and 2

| 2015 Examination Fees |  |  |
| :--- | :---: | :---: |
|  | Candidates | Full- <br> Time |
| Exams LC and ST | $\$ 200$ | $\$ 160$ |
| Exam S | $\$ 400$ | $\$ 320$ |
| Exams 5, 6, 7, 8, and 9 | $\$ 625$ | $\$ 500$ |
| Online Courses 1 \& 2 <br> Retest $^{\dagger}$ | $\$ 315$ | $\$ 315$ |
| Exam ST9 $^{l}$ | $\$ 625$ | $\$ 625$ |


| Other Fees |  |
| :--- | :---: |
| Refund (Exams LC, ST, S, 5-9, and <br> ST9) | $\$ 100$ |
| Change of Exam Center | $\$ 60$ |
| Special Exam Center | $\$ 60$ |
| Online Courses 1/CA1 and 2/CA2: Contact <br> The Institutes for fees that apply. |  |

${ }^{\dagger}$ The first exam attempt is included in the $\$ 575$ Online Course fee.

## Exams 1 and 2 Fee Reimbursement Program in the U.S.

The CAS/SOA Committee on Diversity Recruiting sponsors a program to reimburse qualified minority candidates for Exam 1 (SOA Exam P) and Exam 2 (SOA Exam FM) fees. Eligible candidates are members of specified groups that are underrepresented in the actuarial profession in the United States, including African-Americans, Hispanics, and Native North Americans who are sitting for actuarial exams. The reimbursement application is available in the Diversity Programs section of the actuarial career website at www.BeAnActuary.org.

## Fee Discount Program in Qualified Countries

The CAS sponsors a program to provide financial relief to candidates of qualified countries. Eligible candidates must be current full-time residents of a qualified country and verify that they are personally paying for exam fees and study materials without assistance from employers or other entities. Candidates must write their exams in a qualified country. Information, including a list of qualified countries and the application, is available on the Exams page of the CAS website.

## Computer-Based Testing-Online Courses 1 and 2

The exams for Online Courses 1/CA1 and 2/CA2 are offered by computer-based testing (CBT). Because there are distinctive processes and procedures for CBT, additional information is available on The Institutes website. The rules and procedures provided on The Institutes website related to Online Courses 1/CA1 and 2/CA2 are part of the CAS examination rules.

## Examination Centers

CAS examination centers are listed on the Exam Registration page of the CAS website. Centers are determined by the number of candidates near a center and the availability of proctors. Special examination centers may be arranged at the discretion of the CAS if the request is received by the registration deadline. The additional fee for a special center is $\$ 60$. Candidates will be sent the exact location of their examination center at least three weeks before the examination.

Examinations by computer-based testing are administered at established test centers. The Prometric website (http://www.prometric.com/SOA/default.htm) contains a list of the CBT centers.

The CAS will not host exams in any country that has trade sanctions held against it per the U.S. Department of the Treasury.

## Change of Center

For Exams LC, ST, S, and 5-9, any registered candidate who requests a change in examination center must pay a change-of-center fee. No requests will be accepted after the registration deadline. If a request for a change of center occurs, every effort will be made to have the candidate's records and supplies on hand at the appropriate center in time for the examination. If this effort fails, however, the CAS is not responsible. If either a candidate's registration and fees, or request for change of center are received so late that it is not feasible to arrange for the candidate to write the examination, the fees will be refunded in full. The CAS is not responsible for difficulties caused by postal service delays or inadequate postage.

Details for changing a CBT center for the exams for Online Courses 1/CA1 and 2/CA2 are available on The Institutes website (http://www.aicpcu.org/cas.htm).

## Languages other than English

## Exams LC, ST, S, and 5-9 and Online Courses 1 and 2

Exam questions and instructions will be printed, and exams administered, exclusively in English. Candidates must submit written responses in English; non-English responses will not be graded with the following exception: Should a candidate for an exam jointly sponsored by the Canadian Institute of Actuaries wish to respond to any or all of the constructed response (essay) questions in French, advanced notice must be provided to the CAS Office when applying to write the exam. Provided such advanced notice was received and a suitable translator is available from the Canadian Institute of Actuaries, responses submitted in French will be translated into English by qualified translators and graded exclusively in translation. All translations will be literal translations from French to English. If advanced notice has not been provided, non-English responses will not be graded. If a suitable translator cannot be engaged before the date of the exam, the candidate will be notified. The CAS cannot guarantee the accuracy of any translation. Appeals based upon errors in translation of candidates' responses will not be considered. Grade reports for exams requiring translation may be delayed.

## Special Arrangements for Candidates with a Disability

A candidate with a formally diagnosed disability who needs special testing arrangements must submit a written request for each examination that the candidate intends to write. For Exams 1, 2, 3F, and 4, contact the sponsoring organization. For Exams LC, ST, S, and 5-9, contact the CAS Office. For the two online courses, contact The Institutes. Documentation of the disability, e.g., physician's statement, diagnostic test results, as well as the need for special arrangements, is required of each candidate. Previous accommodations given to the candidate in an educational program or work setting may be considered. Requests for special arrangements and supporting documentation must be submitted at the applicant's expense at least two weeks prior to the registration deadline for Exams LC, ST, S, and 5-9; and prior to the first day of the testing window for exams for Online Courses 1/CA1 and 2/CA2.

## Refunds

## Exams 1, 2, 3F, and 4

Contact the sponsoring organization.

## Online Courses 1 and 2

The fee for Online Courses 1/CA1 and 2/CA2 includes one attempt at the exam by CBT. No refund for a course is provided once the candidate has accessed the online course. If the candidate decides not to access the online course after payment has been made, the candidate may submit a request for a refund. The request must be submitted to Customer Service at The Institutes.

Any candidate who registered for a course exam and subsequently decides not to take the exam may receive a refund for the exam portion of the course fee ( $\$ 190$ ) only by doing both of the following:

- Cancel the appointment prior to the third day preceding the exam at the test center as described the in the Canceling or Changing an Appointment section under Exam Rules on the Be An Actuary website (http://www.beanactuary.org/exams/rules/?fa=canceling-or-changing-an-appointment).
- Submit a refund request to Customer Service at The Institutes (CustomerService@TheInstitutes.org) that must arrive prior to the third day preceding the exam.


## Exams LC, ST, S, and5-9

Any candidate who submits an application for Exams LC, ST, S, or 5-9 and subsequently does not write the examination should submit a written request for an examination fee refund. This request must reach the CAS Office by the refund deadline stated in the Examination Schedule of this Syllabus. Refund requests may be sent via e-mail to refund@casact.org or by fax to (703) 276-3108. Late requests will not be considered. A $\$ 100$ administrative fee per examination will be assessed on all refunds. Change-of-center fees, special center fees, and other additional fees will not be refunded in any case. Refunds will be issued one month after the refund deadline. Refunds are issued in the manner that fees were paid (i.e., by credit to a bank card or by check to an individual or company). Fees cannot be transferred from one exam session to another.

## B. The Examination

## Introduction

The examinations for admission to the Casualty Actuarial Society are designed to establish the qualifications of candidates. The Examination Committee creates exams that follow guidelines developed by the Syllabus Committee. Complete coverage of all readings listed in the Syllabus is not practical for every exam every year. The goal is to produce exams that contain representative, high-quality questions that test candidates' knowledge of topics that are presented in the learning objectives. Thus, the candidate should expect that each exam will cover a large proportion of the learning objectives and associated knowledge statements and syllabus readings, and that all of these will be tested at least once over the course of a few years.

The exam questions will be based on the published learning objectives and supporting knowledge statements. It is intended that the readings, in conjunction with the material on the lower numbered examinations, will provide sufficient resources to allow the candidate to perform the learning objectives. The exams will test not only candidates' knowledge of the subject matter, but also candidates' ability to apply that knowledge.

The Institutes create exams for the online courses that follow the learning objectives contained in the individual courses.

## Order of Examinations and VEE Topics

In the development of the syllabus readings and exam questions, it is generally assumed that candidates for Associateship-level Exams S, 5, and 6 are familiar with material covered on Exams 1, 2, 3F, and 4; Fellowship-level Exams 7, 8, and 9 generally assume familiarity with material on the Associateship-level exams. There are, however, circumstances when another order might be more appropriate. For example, a candidate may wish to study an exam that is closely related to his or her current work.

VEE topics are not prerequisites to taking actuarial exams and may be fulfilled independently of the exam process (i.e., prior to or concurrent with taking actuarial exams). The following insights on VEE topics, however, may be helpful. VEEApplied Statistical Methods will help strengthen candidates' statistical skills and completing it prior to taking Exams ST and 4 will make these exams easier to understand. ${ }^{2}$ VEE-Economics and VEE-Corporate Finance will help strengthen candidates' understanding of managerial decision-making and completing these topics prior to taking Exam 9 will make this exam easier to understand.

To help candidates decide which exam to take, the following chart indicates which exams assume knowledge of material found on prior exams. Most candidates will find it easiest to study for an exam after studying for all of the exams listed in the "prior knowledge" column.

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| Exam or VEE Topic | Assumes Prior Knowledge from the Following Exam(s) |
| :--- | :--- |
| VEE-Applied Statistical Methods | None |
| VEE-Corporate Finance | None |
| VEE-Economics | None |
| Online Course 1/CA1 | None |
| Online Course 2/CA2 | None |
| Exam 1 | None |
| Exam 2 | None |
| Exam 3F | Exams 1 and 2 |
| Exams LC and ST | Exam 1 |
| Exam 4 | Exam 1 |
| Exam S | Exam 1 |
| Exam 5 | Exams 1 and 2 |
| Exam 6 | Exams 1 and 5 and Online Course 2 |
| Exam 7 | Exams 1, 2, 4, and 5 |
| Exam 8 | Exams 1, 2, 3F, 4, S, and 5 |
| Exam 9 | Exams 1, 2, 3F, 4, and 5 |

## Notes on Order of Examinations

- Candidates may find it helpful to take Online Course 1 and Online Course 2 immediately after they begin their first property-casualty employment.
- Candidates should generally take the exams in order noted in the table above, except that a candidate with a background in finance may wish to take Exam 2 before Exam 1.
- Many candidates find it easier to study for the more mathematical exams (i.e., Exams 1, 2, 3F, LC, ST, 4, and S) when they are not too far removed from college math.
- The statistical material on Exam S is closely related to the material on Exam 4, and so candidates may wish to take these exams close together, but it is reasonable to take Exam $S$ at any point after Exam $3 F$ and before Exam 7.
- Exams 3F, 4, S (or the prior Exams LC and ST), and 8 make extensive use of Exam 1 material. Exams 5 and 9 assume an understanding of Exam 1 material.
- Some candidates may find it helpful to take Exam 4 closer to Exam S (or the prior Exams LC and ST) as the statistical concepts in those exams are related. Similarly, candidates may find it helpful to take Exams 2 and 3 F close together.
- Exam 5 is approachable without detailed knowledge of the material on Exam 2. A candidate who has studied this material, however, may gain a deeper understanding of the material on Exam 5 and its foundations.
- Exam 4 covers the theory of credibility. Credibility theory is applied in Exam 5. Candidates who have mastered credibility theory in Exam 4 may find its application more intuitive on Exam 5. On the other hand, candidates who have experience applying credibility on Exam 5 may find the theory on Exam 4 easier to understand.
- Candidates may find their understanding of Exam 7, which has the advanced reserving techniques in the Estimation of Policy Liabilities section, and Exam 8, the Advanced Ratemaking exam, enhanced by material learned on Exam 5, Basic Techniques for Ratemaking and Estimating Claims Liabilities


## Requirements for Admission to Examination Center

To be admitted into an examination center, each candidate must present a positive identification with a signature and a photograph (e.g., driver's license, passport, etc.). If a photo ID is not available, the candidate must present two forms of identification with a signature, with at least one form containing a physical description (height, weight, hair color, eye color, etc.). Each candidate will be required to sign in at the examination center. A candidate who does not present positive identification or who refuses or is unable to provide a matching signature will not be permitted to write the examination.

For examinations offered by computer-based testing, each candidate must present a valid government-issued photo identification that includes the candidate's signature (details are available on The Institutes website for exams for the two online courses).

Candidates should arrive at the examination center at least 30 minutes before the scheduled exam time. Candidates may not leave until two hours after the start of the examination. For Exams LC, ST, S, and 5-9, candidates may not leave during the last 15 minutes of the examination.

## Conduct of Examinations

The examinations are recorded exclusively in writing (except for exams that are administered by computer-based testing). Except as is noted in the following paragraphs, no books, papers, typewriters, slide rules, laptops, or electronic or mechanical aids for computation of any kind may be brought into the examination room by candidates, nor may any candidate communicate with, or obtain any assistance from, any other candidate during the examination. Candidates must respond to constructed response (essay) questions in English unless advance notice is given (see Languages Other than English under Examination Rules-Registration). Examination answer sheets are not returned to candidates.

For Exams LC, ST, S, and 5-9, a candidate wishing to obtain his or her own examination booklet and scrap paper subsequent to the examination must bring a self-addressed stamped envelope to the examination center. The recommended minimum postage is $\$ 2.87$ for domestic mail in the U.S. For Exams LC, ST, S, and 5-9, approximately one week after all exams have been completed, the exam will be posted on the Exams page of the CAS website.

## Calculators

Electronic calculators will be allowed in the examination room for all examinations. Only the calculators listed below may be brought into the examination room. Books, papers, computers, or other electronic devices may not be brought into the examination room. Candidates may use the battery- or solar-powered models of the following Texas Instruments calculators:

$$
\begin{array}{ll}
\text { BA-35 } & \text { TI-30Xa } \\
\text { BA II Plus } & \text { TI-30X II (IIS solar or IIB battery) } \\
\text { BA II Plus Professional } & \text { TI-30XS MultiView (or XB battery) }
\end{array}
$$

Candidates may use more than one of the approved calculators during the examination. For those using the BA II Plus, BA II Plus Professional, TI-30X II (IIS solar or IIB battery) or TI-30XS MultiView (or XB battery) models, candidates will be required to show examination proctors that the memory has been cleared prior to the start of the examination. For the BA II Plus and BA II Plus Professional, clearing will reset the calculator to the factory default settings.

Calculator instructions cannot be brought into the examination room. During the examination, the calculator must be removed from its carrying case so the proctor can confirm it is an approved model. Any unauthorized calculator brought to the examination center will be confiscated for the duration of the examination. Candidates using a calculator other than the approved models will be subject to examination disqualification and other disciplinary action.

Candidates may purchase calculators from stores or directly from Texas Instruments: telephone: (800) 842-2737; website: www.ti.com.

It is the candidate's responsibility to see that the calculator used during the examination is in good working order.

## Earplugs

Simple foam earplugs are allowed and must be checked in with the supervisor upon entrance to the exam. The ability to hear all verbal instructions, including exam start and stop times is the responsibility of the candidates, regardless of the use of earplugs.

## Examination Discipline

Candidates must not give or receive assistance of any kind during the examination. Any cheating, attempt to cheat, assisting others to cheat, participating therein, or engaging in such improper conduct as listed below is a serious violation and will result in the CAS disqualifying the candidate's paper and other disciplinary action as may be deemed appropriate. Candidates have agreed in their applications for examination to be bound by the rules and regulations governing the examinations.

Examples of improper conduct include but are not limited to:

1. Gaining access to examination questions before the examination or aiding someone else to do so.
2. Using an unauthorized calculator (as defined in the Syllabus) or other mechanical aid that is not permitted.
3. Looking in the examination book before the instruction to begin is given.

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4. Marking or otherwise writing on the examination book or answer sheet before the instruction to begin is given.
5. Making any changes, additions, deletions, or otherwise marking, erasing, or writing on the examination book or answer sheet after the time for the examination has expired.
6. Having access to or consulting notes or books during the examination.
7. Looking at or copying from another candidate's paper.
8. Enabling another candidate to copy from one's paper.
9. Talking or otherwise communicating with another candidate during the examination.
10. Disturbing other candidates during the examination.
11. Consulting other persons outside the examination room during the examination.
12. Copying questions, answers, or answer choices to take from the examination room.
13. Taking an examination book from the examination room.
14. Taking an examination for another candidate.
15. Arranging to have another person take an examination for the candidate.
16. Threatening or physically or verbally abusing a supervisor or proctor responsible for curbing or reporting improper conduct.
17. Disclosing the contents of an examination to any other person prior to the examination's release. (For CAS Exams LC, ST, S, and 5-9, this would generally apply to the day when the examination is administered.)
18. Presenting false information on an examination application.
19. Failing to remain in the examination room for a minimum of two hours during the examination [for examinations with this requirement].
20. Failing to follow other examination instructions.
21. Accessing or using a communication device (PDA, cell phone, etc.) during the exam or while at the exam site.

The CAS Examination Committee, or its designee, will investigate any irregularity or suspected violation of the rules involving the examination process, and a determination will be made regarding the matter. Where there is a determination to invoke a penalty, the candidate is advised by letter. In the case of a candidate who is a member of the CAS, the candidate's conduct will be reported to the Actuarial Board for Counseling and Discipline (ABCD) or to the Canadian Institute of Actuaries (CIA) if the final penalty invoked is more than disqualification of the examination.

Candidates for the CAS Examinations are expected to follow the rules and procedures included in this Syllabus, the Instructions to Candidates printed on their examination booklets, and announcements made by the supervisors at the examination locations. All candidates, on their applications for examinations, are required to read and sign the following statement: "I have read the rules and regulations concerning the examination(s) for which I am applying and agree to be bound by them. I also agree that the results of any examination(s) which I take, and any action taken as a result of my conduct may, at the sole discretion of the Casualty Actuarial Society, be disclosed to any other bona fide actuarial organization that has a legitimate interest in such results and/or actions."

The CAS may, at its sole discretion, disclose to any other bona fide actuarial organization having a legitimate interest, information on the identity of candidates determined to have committed a serious examination violation (those for which the penalty is greater than the simple disqualification/nullification of the examination), and the specific penalties imposed on those candidates.

If an actuarial organization with which the CAS has a working relationship (such as the Society of Actuaries) invokes a penalty against a candidate for improper conduct during an examination for which the CAS is not a joint sponsor, the CAS will invoke the same penalty for all CAS-sponsored examinations. If the CAS takes any disciplinary action, it will notify the other actuarial organizations of that action.

These standards may seem stricter than those which candidates are accustomed to in other examination environments. The CAS maintains these strict standards because the examinations are such a significant part of a candidate's career. Therefore, the equitable administration of the examinations and enforcement of the highest standards of conduct cannot be emphasized too strongly.

Candidates may obtain a copy of the full CAS Policy on Examination Discipline by sending a written request to the CAS Office.

## Discipline for Computer-Based Testing

The Policy on Examination Discipline is the same for those taking exams by computer-based testing or in the traditional paper-and-pencil format. The rules for the CBT administration for Online Courses 1/CA1 and 2/CA2 are available on The Institutes website (http://www.aicpcu.org/). If there is a discrepancy between specific rules for the traditional paper-andpencil exam administration and computer-based testing, the computer-based testing rules will govern.

## Multiple-Choice Questions

Exams LC, ST, and S consist entirely of multiple-choice questions; other CAS examinations may have a section of multiple-choice questions. Each multiple-choice problem includes five answer choices identified by the letters A, B, C, D, and $E$, only one of which is correct. For examinations administered by computer-based testing, candidates should click on the appropriate answer. For all other exams, a separate answer sheet provides a row of five ovals for each problem, identified with the letters A, B, C, D, and E, corresponding to the five answer choices. After deciding which answer is correct, candidates should blacken the oval that has the same letter as the appropriate answer. Since the answer sheets are scored by optical scanning equipment, a Number 2 pencil must be used to blacken the ovals. It is important that only one oval be blackened for each question.

Exams for the two online courses will consist entirely of multiple-choice questions. Each multiple-choice problem includes four answer choices identified by the letters A, B, C, and D, only one of which is correct. For exams administered by computer-based testing, candidates should click on the appropriate answer. For all other exams, a separate answer sheet provides a row of four ovals for each problem, identified with the letters A, B, C, and D, corresponding to the four answer choices. After deciding which answer is correct, candidates should blacken the oval that has the same letter as the appropriate answer. Since the answer sheets are scored by optical scanning equipment, a Number 2 pencil must be used to blacken the ovals. It is important that only one oval be blackened for each question.

## Guessing Adjustment

For the exams for Online Courses 1/CA1 and 2/CA2, no guessing adjustment are made to candidates' scores. Therefore, candidates will maximize their scores on these examinations by answering every question. On Exams LC, ST, S, and 59 , multiple-choice questions are scored in such a way that there is no advantage or disadvantage to be anticipated from
guessing answers in a purely random fashion as compared with omitting the answers entirely. No additional points will be given for multiple-choice questions left blank, but one-quarter of the point value for each question will be deducted for each incorrect answer.

## Constructed Response Test Items

The admissions process is intended to identify candidates that have demonstrated sufficient mastery of the learning objectives to be admitted as members of the CAS. Examinations that provide a means for better-prepared candidates to demonstrate that mastery are critical to meeting that objective.

Educators often refer to a tool called Bloom's Taxonomy to classify questions into six cognitive levels. Bloom's levels range from Level 1, broadly characterized as knowledge, to Level 6, characterized as evaluation. Lower levels of the taxonomy stress recall of facts and an understanding of main ideas; higher levels within the taxonomy stress synthesis, comparison, and subtlety of understanding.

Bloom's levels are as follows:
Level 1: Knowledge-tests the ability of the candidate to recall or remember knowledge or facts
Level 2: Comprehension-requires the candidate to demonstrate comprehension of central concepts through explanation of those concepts

Level 3: Application-measures the candidate's ability to apply ideas and concepts to new situations
Level 4: Analysis-requires the candidate to analyze information by separating material into component parts, including identification of facts and development of inferences with respect to a situation

Level 5: Synthesis-tests the ability of a candidate to synthesize, or combine, concepts or ideas and develop and defend the position resulting from that combination

Level 6: Evaluation-requires the candidate to support conclusions by evaluating the validity of ideas and concepts
The test specifications for each upper-level examination include the long-term target range of points for each Bloom's cognitive level. A thorough review of the learning objectives in the Bloom's context described above will help the candidate to assess the level of mastery that the CAS expects successful candidates to demonstrate.

Generally, questions at higher Bloom's levels will have higher associated point values. As a result, examinations with higher synthesis and evaluation targets will contain fewer questions that may result in less syllabus coverage on a particular exam.

## Lost Examinations

The CAS-or its designee-is not responsible for lost or destroyed examinations. In the case where an examination is lost or destroyed, the examination fee will be refunded. The CAS and its designees will assume no other obligation and candidates must take the examinations with this knowledge. For Online Courses 1/CA1 and 2/CA2 that are administered by The Institutes, the policy of The Institutes will apply.

## C. Grades and Accreditation

## Defective Questions

Occasionally, through error or because of varying interpretations, a question on an examination is found to be ambiguous or defective. If a candidate believes a question is ambiguous or defective, he or she should bring this to the attention of the Examination Committee in writing within two weeks after the examination date. The candidate must submit this correspondence to The Institutes for the two online courses; or to the CAS Office for Exams LC, ST, S, and 59. The correspondence should include detailed reasons why the question is believed to be ambiguous or defective. In addition, statistics are calculated on each test item to determine how well the candidates answered the question. The statistics can indicate that a question may be faulty and the question will be reviewed even without a candidate writing.

The CAS Examination Committee and/or The Institutes, as appropriate, will investigate all questions brought to their attention in this manner. Correspondence that does not reach these organizations within two weeks after the date of the examination will not be considered in the grading process.

Any multiple-choice question found to be defective is carefully examined to determine the most reasonable way to correct the situation. In some cases, the question is discarded, leaving scores and rankings as they would have been if the defective question had not been asked. In other cases, more than one answer for a multiple-choice question is given credit for being correct.

For Exams 1, 2, 3F, and 4, the candidate should follow the procedural rules of the sponsoring organizations.

## CAS Examination Processing

Computer-based tests are administered and scored according to computer-based testing methodologies. Although the multiple-choice exams that are administered exclusively by paper-and-pencil have a process that is similar to the description below, this section and the next, Grading of Examinations: A Timeline, provide details about CAS-specific Exams 5-9.

Examination papers are sent to the CAS Office upon completion of the examination. The CAS Office prepares the examinations for the grading process. Approximately one week after all examinations have been completed, the examination and a preliminary list of multiple-choice answers will be posted on the Exams page of the CAS website. This is intended to assist candidates and the Examination Committee in determining whether they believe a question is ambiguous or defective.

## Grading of Examinations: A Timeline

## Week 1

After the examinations are administered, proctors return the exam packages to the CAS Office. Staff members log in each exam. Signatures are verified and the candidate numbers are checked against the proctor's report. As each envelope is opened, the candidate's number must be checked against the number on the short answer card (both the written number and the coded number) and on all the essay sheets. The short answer cards are prepared for scanning and the essay sheets for all the candidates must be sorted so that individual questions can be copied for the graders.

## Week 2

Constructed response (essay) question responses are sent to a vendor to be reproduced. Short answer cards are scanned twice and output is compared to ensure accuracy. Random checks are made of each series of cards to ensure that the scanner is working properly. When the essay sheet copies are received, copies of candidate responses are sent
to the individual graders. Any comments on potentially ambiguous or defective questions are forwarded to the graders, exam part chair, and the general officer of the exam series for review.

## Weeks 3 and 4

Committee members review candidate comments about possibly defective questions and decide how they will be handled in the grading process. Discussions on the best course of action are often a very time-consuming part of the grading process.

Copies of responses to each constructed response question on the exam are sent to two graders. Some graders are given more than one question to grade. There can be 500 to more than 1,000 answer sheets for each grader to evaluate for a single question. A suggested answer key exists for each question, but alternative solutions may be correct, and the graders must be open to different approaches to a problem. About two-dozen responses are graded and then the results are compared. The grading partners will establish a consistent grading scale and then evaluate the solution key. Consistency and accuracy are the most important factors in grading the responses. After looking at hundreds of papers, it is possible that a grader could slightly shift focus (either harder or easier). To minimize the chance of this happening the graders will begin grading at different points on the candidate list, then when the two grades are compared any significant differences will be checked. Each grader prepares a computer file with each candidate's number and the score for each question.

## Week 5

The part chair holds the grading session with the graders. The first step is running the data through a standard grading program, verifying the data, and noting any significant discrepancies. For each candidate and each question the scores of each grading partner must be within a prescribed tolerance. If the scores do not fall within this tolerance, the partners must discuss the candidate's answer sheet and come to a decision on what the point value should be. When all the questions have been reconciled to the required tolerance, the scores are totaled and a tentative pass score is selected based on the pass mark panel's recommendation, various statistics, and guidelines.

This triggers the second round of reconciliation. Candidates who have scores within a certain number of points from the tentative pass score will have all of their answers reconciled completely. This gives an exact score for any candidate near the passing score. The scores for any candidates who are close to passing will be checked manually as well. The committee members will then look at the statistics one more time and make a final recommendation for the passing score.

## Weeks 6 and 7

After the grading session, the part chair will create and submit a report to the general officer of the exam series, the Examination Committee chairperson, and the vice president-admissions. In the report, the part chair recommends a passing score, gives a detailed analysis of the exam, and notes any unusual questions or situations that required special handling. The chairperson and general officer hold a teleconference with the vice president-admissions and a representative from the Canadian Institute of Actuaries to discuss all of the exams from the series and to finalize the passing scores.

## Week 8

After the vice president-admissions has approved the passing score the data is verified and released to the CAS Office to update each candidate's record. A link to the web page with passing candidate numbers, which will reside at a randomly generated web address, will be sent via e-mail to the candidates who sat for the exam for which results are available Lastly, grade reports will be sent to candidates.

## Determination of the Pass Mark

The goal of the examination system of the CAS is to pass all candidates who have demonstrated adequate knowledge of the syllabus and to fail those candidates who have not. The objective of the examinations is to evaluate candidate performance using criteria for demonstrating adequate knowledge that remain constant throughout the lifetime of the exam series. Pre-set pass marks (e.g., a candidate will pass if he or she answers $\times$ percent of the questions correctly) are counter to this philosophy. The examinations are meant to measure the candidate's level of achievement of the required learning objectives and their required level of capability of accomplishing specified learning outcomes.

## Multiple-Choice Test Items

As part of the input to the pass mark determination process for the multiple-choice exams that are not offered by computer-based testing, a modified Angoff passing score study is performed where a panel of experts in the subject material is convened to review the examination. This is a common testing and measurement technique. Each expert is asked to review each question in the examination, and assess the difficulty of that question. More specifically, they are asked to estimate the likelihood that a candidate with minimum adequate knowledge competency would answer the question correctly. The sum of these probabilities, averaged across the panel of experts, gives a preliminary estimate of the pass mark.

The estimated pass mark resulting from the modified Angoff passing score study is compared to and balanced with the actual performance statistics on the exam in finalizing the pass mark. The effects of any particularly difficult questions are also factored into the determination of the final pass mark.

Computer-based tests are administered and scored according to computer-based testing methodologies.

## Constructed Response Test Items

For CAS examinations consisting in whole or in part of constructed response items (written-answer or essay test items), the assessment process is somewhat different. Before the exam is administered, a pass mark panel reviews the exam and assesses it based on how the panelists think a minimally qualified candidate will perform based on a predetermined definition of the minimally qualified candidate. This process follows the same basic technique used for multiple-choice exams as described above. Based on this assessment, an expected pass mark is set.

Following the administration of each exam, responses to each constructed response item are graded simultaneously by two graders who must reconcile their grading rubrics and grades. When all responses have been scored, the part committee chooses a preliminary pass mark based on the results of the pass mark panel augmented by actual performance of the current candidates versus historical performance of previous candidate cohorts. Candidate papers with scores close to the preliminary pass mark are re-graded to ensure correct and consistent scoring.

The part committee then determines the tentative pass mark by again balancing actual performance statistics against minimum adequate knowledge while taking into account other factors such as time pressure situations that may have occurred on some questions. Because the level of difficulty for each examination may vary from year to year, each part committee collects extensive data to ascertain the level of difficulty of its examination. The part committee compares the performance of the present year's candidates to the performance of candidates from prior years. Appropriate recognition is given to any peculiarities that may appear in connection with the answers to any question on an examination despite all the care taken in setting the examination questions.

With the use of content-based pass marks, fluctuation in the pass rate from session to session is expected. Although the percentage of candidates passing will vary from year to year, those candidates demonstrating the required level of
competence with the material will pass.

## Final Pass Mark

A recommended pass mark is reached by consultation among the part chairperson, the general officer overseeing that examination, and the Examination Committee chairperson. Any significant deviations from the a priori pass mark set by the pass mark panel are explored at this time. The recommended pass mark and explanations for deviations from the a priori pass mark and any abnormal passing percentages are submitted to the vice president-admissions who approves the final pass mark. The final exam statistics are forwarded to the Executive Council and Board of Directors.

After the pass mark is finalized, each candidate is assigned a score. Scores of 0 to 5 are assigned to candidates who do not pass. On this scale, each interval is 10 percent of the pass mark. For example, a grade of 5 equates to a candidate's score of at least 90 percent, but less than 100 percent, of the pass mark. A grade of 0 means that the candidate's score is less than 50 percent of the pass mark. Candidates at or above the passing mark receive a grade of Pass.

The CAS releases the pass scores for Exams LC, ST, S, and 5-9 after the appeals deadline for the specific exam session. They are available from the Past Exams and Pass Marks page of the CAS website (http://www.casact.org/admissions/studytools/index.cfm?parentlD=163\&fa=PastExams). The purpose of releasing the pass scores is to help candidates prepare for future exam sittings. The 75th and 95th percentile scores are also released for each exam. These two key statistics indicate the performance level achieved by the better-prepared candidates on the exam. Raw scores are not provided to candidates.

## Examination Results

Examination results are available approximately eight weeks after the examination date. After exam results are received at the CAS Office, a list of passing candidate ID numbers will be e-mailed to candidates. Individual statements of examination results generally are sent to candidates on the day that they become available.

For Exams LC, ST, S, and 5-9, passing candidates are informed that they passed the exam, but they are not given a numeric score. Candidates with scores of 0 to 5 are informed of the score. Within a few days, a list of the names of all passing candidates is posted on the CAS website. Requests for reprints of individual grade reports will be accepted starting two weeks after the date that results were released.

To preserve candidate confidentiality, in the event of a lost or misplaced candidate ID number, the candidate ID number will be mailed to the candidate upon request. Under no circumstance will a candidate number be given over the telephone or by e-mail. Candidates can also verify their candidate number by logging into their profile on the CAS webpage.

## Online Courses 1 and 2

The exams for Online Courses 1 and 2 are offered by computer-based testing. An unofficial pass/fail result will be displayed on the computer screen at the conclusion of the exam. When the official grades have been processed, candidates will receive an e-mail from The Institutes stating that their grades are available. Candidates may then log into their account on The Institutes website (www.TheInstitutes.org) to access their grades. The grade report for each candidate will show the candidate's overall score on the exam in ten point increments (e.g., 60 to $69 \%, 70$ to $79 \%$, and so on). It will similarly show the candidate's performance by assignment using those same ten point increments. Numeric scores are not released. Once final grades have been released, The Institutes will send a copy of the grades directly to the CAS Office to be added to the candidates' admissions records. The Institutes sends this information to the CAS several weeks following the closing of the testing window. The CAS will post the list of passing names

## approximately two weeks later.

## Analyses for Exams LC, ST, S, and 5-9

Candidates for Exams LC, ST, S, and 5-9 who did not pass will automatically be sent an analysis of their examination with the grade notification. The analysis of an examination is computer-generated. Actual points received for multiplechoice questions will be displayed. For constructed response test items, ranges will be given for the actual score. This information is intended to provide the educational guidance that most candidates desire. Copies of the exam analyses will not be provided after the appeals deadline.

## Appeals for Exams LC, ST, S, and 5-9

## Multiple-Choice Questions

If a candidate believes that a multiple-choice question is ambiguous or defective, he or she should bring this to the attention of the Examination Committee in writing within two weeks after the examination date. In order to aid the candidate, preliminary answer keys for multiple-choice questions will be available the week following the examinations. The candidate may submit comments to the CAS Office by mail, fax, or e-mail. The correspondence should include detailed reasons why the question is believed to be ambiguous or defective. (In addition to candidate comments, statistics are calculated on each problem to see how well the candidates answered the question. The statistics can indicate that a question may be faulty and the question will be reviewed even without a candidate writing.) The CAS Examination Committee will investigate all questions brought to its attention in writing. To be considered in the grading process, correspondence must reach the CAS Office within two weeks of the date that the exam was administered. The decision of the Examination Committee chairperson is final.

No appeals based on ambiguous or defective questions will be considered after these deadlines. After grades are released, the only appeal permitted on multiple-choice questions will be to request an administrative check of the candidate's short answer card to verify that the card reader scanned the card correctly and that the output file reflected this data. This request must be made within three weeks after the release of grades.

## Constructed Response Test Items

Once candidates have received the analyses of their exams, they may appeal their grade. Only candidates with valid appeals will be considered.

Appeals must reach the CAS Office not later than 30 days for Exams 7-9, and 2 weeks for Exams 5, 6-Canada, and 6United States, from the publication of the Examiner's Report for the specific exam. The Examiner's Report is generally published 12 weeks after the exams are administered. (Should an Examiner's Report for a given exam be posted later than this, the appeal deadline for that specific exam will be extended to 30 days after the posting date of that report.)

If the candidate believes that the sample constructed response answer is incorrect or there is an alternative correct solution, the candidate must provide specific information on why his or her solution is correct. With specific information, the Examination Committee can research the answer properly and reply to the candidate. An example of an invalid appeal would be the following: "I am appealing my score of 5 on Exam 9, please recheck my examination." Another example of an invalid appeal would be: "On question number 2, I believe I should get full credit because I answered the following . . ."

When a valid appeal is received, the part chairperson reviews the appeal and makes a recommendation to the Examination Committee chairperson. The Examination Committee chairperson will respond based on the
recommendation of the part chairperson. The decision of the Examination Committee chairperson is final.

## Confidentiality of Examination Records

The fact that a candidate has passed a particular examination is considered public knowledge. Any further information as to examinations taken by candidates and scores received by candidates is available only to the candidates themselves, to Examination Committee officials if required for committee purposes, and to the CAS Office, unless the candidate requests in writing that such information be provided to someone else. However, if any action is taken against a candidate as a result of his or her conduct (as described in the section on Examination Discipline), the Casualty Actuarial Society, at its sole discretion, may disclose such information to any other bona fide actuarial organization that has a legitimate interest in such results and/or actions. The candidate authorizes and consents to the Society using and disclosing (including, but not limited to, disclosing to the third-party contractors and serviceproviders of the Society) personally identifiable information about the candidate as necessary and appropriate for the purposes of registering the candidate for the exam, conducting the exam, determining the results of the exam, and communicating with the candidate regarding the results of the exam.

## Transition Programs

The CAS generally reviews and makes revisions to the study material on an annual basis. Occasionally, a major topic will be added to or deleted from the syllabus. A major topic is defined as a series of learning objectives comprising a segment of an examination. When a major topic is added, the Syllabus Committee will determine if a transition program is appropriate. A transition program is generally appropriate when candidates are in a position to lose credit for a segment of an examination.

A transition program usually will provide candidates with at least two opportunities to complete the requirements for that examination. The completion of the requirements will result in the achievement of credit for that entire examination. The failure to fulfill the requirements for that complete examination could result in the expiration of credit for that deleted topic at the end of the transition period. The CAS Board of Directors must approve any transition program.

## Current Education Structure

The CAS Board of Directors approved the following transition rules for the Fall 2015 education structure.
To receive credit for the new Exam S on Statistics and Probabilistic Models during the transition, the candidate must have credit for Exams ST and LC ${ }^{\dagger}$ and the VEE-Applied Statistical Methods educational requirement. At the time of transition, if a candidate has credit for either Exam ST or Exam LC, but not both, the candidate will be allowed to take just the exam for which he or she is missing credit in order to obtain partial credit for the new exam. This option will be available for a transition period of two sittings, i.e., Fall 2015 and Spring 2016.

Credit for the VEE-Applied Statistical Methods educational requirement will also be accepted for those candidates who complete it by August 31, 2016. If the candidate has not completed Exam ST, Exam LC, and the VEE-Applied Statistical Methods educational requirement by this date, the candidate will need to pass the full version of Exam $S$ to receive credit.

Candidates with credit for neither Exam ST nor Exam LC on August 31, 2015 will not be permitted to sit for Exam ST or Exam LC during the transition period and will need to pass the full version of Exam $S$ to receive credit.

The following table summarizes the above:

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| Candidate Credit on August 31, 2015 |  |  | Action Required by August 31, 2016 to Earn Credit for new Exam S |
| :---: | :---: | :---: | :---: |
| Exam ST | Exam LC | VEE- <br> Applied Statistical |  |
| $\checkmark$ | $\checkmark$ | $\checkmark$ | Credit granted. No candidate action required. |
| $\checkmark$ | $\checkmark$ |  | Complete VEE-Applied Statistical Methods. |
| $\checkmark$ |  | $\checkmark$ | Pass Exam LC. |
| $\checkmark$ |  |  | Pass Exam LC and complete VEE-Applied Statistical Methods. |
|  | $\checkmark$ | $\checkmark$ | Pass Exam ST. |
|  | $\checkmark$ |  | Pass Exam ST and complete VEE-Applied Statistical Methods. |
|  |  | $\checkmark$ | Candidate must take full version of Exam S. |
|  |  |  | Candidate must take full version of Exam S. |

${ }^{\dagger}$ The CAS has also granted waivers for Exam LC to candidates who have:

- Passed SOA Exam MLC;
- Passed the Institute and Faculty of Actuaries (U.K.), Actuaries Institute (Australia), or Institute of Actuaries of India Subject CT5; or
- Passed the Actuarial Society of South Africa Course A203; or
- Received a waiver granted by the Canadian Institute of Actuaries University Accreditation Program.

For those candidates who have credit for Exam ST by August 31, 2015, the CAS will continue to grant Exam LC waivers through August 31, 2016.

## Older Transition Rules Applicable to the Current Education Structure

1. The CAS Board of Directors approved the following transition rules for the education structure that was implemented in January 2014:

## Creditin 2013* CreditinEducation Structure Implementedin 2014

Exam 3L Exams LC and ST
SOA Exam MLC Exams LC and ST
*Note: Credit for Exam 3L or SOA Exam MLC must have been achieved through an examination administered prior to January 2014.

In addition, the CAS Board of Directors approved the following waiver that will continue beyond January 2014:
Credit Creditin Current CAS Education Structure
SOA Exam MLC Exam LC
2. The CAS Board of Directors approved the following transition rules for the education structure that was implemented in January 2011:

| Credit in 2010 | Credit in Education Structure Implemented in 2011 |
| :---: | :---: |
| Exam 5 | Half of Exam 5 (section on Basic Techniques for Ratemaking)* and Online Course 1 |
| Exam 6 | Half of Exam 5 (section on Estimating Claim Liabilities)* and Exam 7 on Estimation of Policy Liabilities, Insurance Company Valuation, and Enterprise Risk Management |
| Exam 7 | Nation-specific Exam 6 on Regulation and Financial Reporting and Online Course 2 |
| Exam 8 | Exam 9 on Financial Risk and Rate of Return |
| Exam 9 | Exam 8 on Advanced Ratemaking |

[^2]100 Years of Expertise, Insight \& Solutions
3. The CAS Board of Directors approved the following transition rule for the revision to Exam 3 that was implemented in January 2008:

| Credit in 2007 | Credit in Education Structure Implemented in 2008 |
| :--- | :--- |
| Exam 3 | Exams 3F and 3L |

4. The CAS Board of Directors approved the following transition rules for the revised education structure that was implemented in January 2005:

| Creditin 2004 | Creditin Education Structure Implementedin 2005 |
| :--- | :--- |
| Exam 1 | Exam 1 |
| Exam 2 | Exam 2, VEE-Economics, VEE-Corporate Finance |
| Exam 3 | Exam 3 [Exams 3F and 3L] |
| Exam 4 | Exam 4, VEE-Applied Statistical Methods |

5. The following rules apply for candidates with unused credit from exams administered prior to 2000:

| Pre-2000 Credit | Credit in Education Structure Implementedin 2014 |
| :--- | :--- |
| Exam 2 (Probability \& |  |
| Statistics) and Exam |  |
| 4B (Credibility Theory |  |
| and Loss |  |
| Distributions) | Exam ST |
| Pre-2000 Credit | Credit in Education Structure Implementedin 2011 |
| Exam 3B | Online Course 1 |
| Pre-2000 Credit | Credit in Education Structure Implementedin 2005 |
| Exam 3A | VEE-Applied Statistical Methods |
| Exam 4A | Exam 2 |
| Exam 4B | Exam 4 |
| Exam 5A | VEE-Economics |
| Exam 5B | VEE-Corporate Finance |

## CAS Course on Professionalism

The CAS Course on Professionalism is designed to present candidates with real situations that contain ethical and professional issues for the actuary. Volunteer members of the CAS facilitate small group discussions of actual case studies. Although grades are not given for the course, candidates must actively participate in order to receive credit. Successful completion of this course is required before a candidate can become a member of the Casualty Actuarial Society.

Candidates are urged to register for this course as soon as they are eligible. To be eligible for the CAS Course on Professionalism, in the current education structure, a candidate must:

- Have credit for any five actuarial exams in the current education structure-regardless of online courses or VEE status.

OR

- Have credit for any four actuarial exams and credit for any four of the following five requirements: Online Course 1/CA1, Online Course 2/CA2, VEE-Applied Statistical Methods, VEE-Corporate Finance, or VEEEconomics.

Note: For this eligibility prerequisite, the actuarial exams are: Exams 1, 2, 3F AND S (or prior Exams LC and ST together), 4,5 , and 6 . While VEE-Applied Statistical Methods is no longer part of the current education requirements, it will still be considered for eligibility to take the CAS Course on Professionalism.

Dates for the course will be posted in the CAS Course on Professionalism page of the CAS website
(http://www.casact.org/education/index.cfm?fa=prof). This page also has a link to the course readings that must be completed prior to attending the course. Each course is limited to 60 participants; early registration is recommended. Facility information and course times are provided when registration for specific courses is announced.

## CAS Membership Requirements

## Associateship

Candidates for Associateship in the Casualty Actuarial Society must fulfill the examination requirements by successful completion of, or credit for, Exams 1, 2, 3F, 4, S, 5, and 6; have credit for Online Courses 1/CA1 and 2/CA2; have credit by Validation by Educational Experience (VEE) for the required topics of corporate finance and economics; and successful completion of, or credit for, the CAS Course on Professionalism. Exam 6 is nation specific and passage of any one of the CAS-approved nation-specific exams fulfills the Associateship requirements.

After completing all the prescribed requirements, all prospective Associate members must submit a formal application to the Casualty Actuarial Society. The application form and list of application requirements are available on the CAS website in the Join/Renew section. Obtaining the two letters of reference is the prospective member's responsibility. If no member of the CAS is familiar with the prospective Associate and his or her work history, references from members of the American Academy of Actuaries, the Canadian Institute of Actuaries, the Society of Actuaries, other actuarial organizations that are part of the International Actuarial Association, or senior executives where the candidate is employed may be substituted. For further information on alternative acceptable references, please contact the CAS Office. An application for membership will not be processed without these references.

Candidates must have completed all educational requirements prior to submitting an application for CAS membership.
After all requirements are met and a completed application has been submitted to the CAS, each candidate is voted on by the CAS Executive Council. Upon approval of the CAS Executive Council, the candidate will be admitted as an Associate of the Casualty Actuarial Society (ACAS). Candidates approved by the Executive Council will be notified by
letter from the CAS president. Members may indicate their designation as an Associate of the Casualty Actuarial Society by using the initials "A.C.A.S." after their names only after they have received official notification of acceptance as an Associate from the CAS.

## Fellowship

In addition to fulfilling all the requirements of Associateship, successful completion of, or credit for, all Fellowship examinations is required to fulfill the requirements for Fellowship and to be designated as a Fellow of the Casualty Actuarial Society (FCAS). Candidates who are admitted to the CAS as Fellows rather than Associates may indicate their designation as a Fellow of the Casualty Actuarial Society by using the initials "F.C.A.S." after their names only after they have received official notification of acceptance as a Fellow from the CAS. Associates who complete their Fellowship requirements may use the "F.C.A.S." designation immediately following official notification of successful completion of all the Fellowship requirements as prescribed by the Board of Directors.

## CERA Requirements

Candidates for the CERA (Certified Enterprise Risk Analyst) designation must fulfill the educational requirements by successful completion of all CAS Associateship requirements, CAS Exams 7 and 9, the Enterprise Risk Management and Modeling Seminar (specifically designed for the CERA designation), and Exam ST9 of the Institute and Faculty of Actuaries (U.K.).

After completing all the prescribed requirements, all prospective CERA designees must submit a formal application to the Casualty Actuarial Society. The application form will be available in the CERA section of the CAS website (http://www.casact.org/cera/). Candidates must have completed all educational requirements prior to submitting an application for the CERA designation.

After all requirements are met and a completed application has been submitted to the CAS, each candidate is voted on by the CAS Executive Council and then submitted to the international Treaty Board for the CERA Global Credential for approval. Upon approval, the candidate will be granted the CERA designation. CERA designees may indicate their designation by using the initials "CERA" after their names only after they have received official notification from the CAS.

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## Waiver of Examinations

## Actuarial Examinations

The CAS's Basic Education Waiver Policy addresses the extent to which the CAS will grant waivers of its basic education requirements including Exams 1, 2, 3F, LC, ST, and 4; Online Courses 1 and 2; Course on Professionalism; and Validation by Educational Experience requirements, or their equivalents as defined by the Executive Council.

The Board of Directors agrees that an exam waiver should be considered for verified educational accomplishments, e.g., exams or university courses, required by another actuarial organization that substantially meet the learning objectives of a particular CAS exam with reasonably equivalent rigor and level of mastery of the material. The Board agrees that the alternative should not be required to cover every learning objective that is covered in the CAS syllabus for the particular exam in order to consider a waiver and that other learning objectives covered by the alternative may be considered as substitutes.

In addition to actuarial exam requirements, the CAS may grant waivers for other basic education requirements provided that the educational experience is deemed equivalent in subject matter coverage and depth. For example, the CAS may accept a professionalism course offered by another actuarial organization provided that it is deemed equivalent to the CAS Course on Professionalism or the Executive Council provides a supplement to address any significant CAS requirement that may be lacking. Other examples where CAS requirements may be waived include Online Courses or Validation by Educational Experience requirements. In general, the CAS will not grant waivers for its upper-level exams.

The CAS will not grant waiver of all or any portion of its examination requirements for work experience or contribution to actuarial literature.

Under this Policy, the granting of waivers by the Executive Council will be based on the recommendation of the vice president-admissions. The vice president-admissions' recommendation will be guided by policy discussions and recommendations of the CAS Education Policy Committee.

## Canadian Institute of Actuaries

The CAS recognizes the exam waivers granted by the Canadian Institute of Actuaries University Accreditation Program for Exams 2, 3F, LC, and 4. The CAS will only grant waivers for CIA UAP exam credits that were awarded based on work at universities in Canada

## Institute and Faculty of Actuaries (U.K.), Actuaries Institute (Australia), Actuarial Society of South Africa (ASSA), and Institute of Actuaries of India Examinations

The CAS recognizes some of the examinations sponsored by the Institute and Faculty of Actuaries (United Kingdom), Actuaries Institute (Australia), Actuarial Society of South Africa (ASSA), and the Institute of Actuaries of India. Credit will be granted for examinations passed or waived in accordance with examination equivalencies between the CAS Syllabus and the syllabi of each of the aforementioned actuarial organizations.

The CAS will not grant credit for examinations waived on account of academic records achieved in U.S. universities, nor for credit granted to candidates not qualifying directly in obtaining membership through the normal qualification/examination process.

Credit will not be given to Fellows of these actuarial organizations who have attained their designation through mutual recognition rather than through the organization's standard credentialing process. Fellows by mutual recognition

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should pursue examination waivers based on their original credentials.
The CAS has approved the following waiver policy:

| Subject ofthe Institute and <br> Faculty of Actuaries <br> (U.K.), Actuaries Institute <br> (Australia), and Institute <br> of Actuaries of India | Actuarial Society of <br> South Africa | Waiver Granted for CAS <br> Exam/Educational |
| :---: | :---: | :---: |
| CT1 | A201 | Exam 2 |
| CT2 | A103 | VEE-Corporate Finance |
| CT3 | A101 | Exam 1 |
| CT4 and CT6 | A202 and A204 | Exams ST \& 4 and VEE-Applied <br> Statistical Methods |
| CT5 | A203 | Exam LC |
| CT7 | A102 | VEE-Economics |
| CT8 | A205 | Exam 3F |

## Society of Actuaries

The CAS recognized the SOA exams listed in the chart below. Candidates who check the "Property and Casualty" field on their preliminary exam application will have the results of their exams automatically updated in the CAS candidate database. Candidates who did not check the Property and Casualty field can have their exam results verified and updated in the CAS candidate database by completing the online form.

The CAS recognizes the following exams:

| SOA Exam | Waiver Granted for CAS Exam |
| :---: | :---: |
| P | 1 |
| FM | 2 |
| MFE | 3 F |
| MLC | LC |
| C | 4 |

## CAS Exam Requirements of SOA Members

The CAS has seen an increase in the number of credentialed actuaries in the SOA asking what is needed to obtain their ACAS or FCAS designation from the CAS. The Education Policy Committee reviewed this issue and noted that until 2014 the CAS and the SOA administered jointly preliminary exams, and that prior to that, both societies gave conversion credit that was applicable to the current CAS exam requirements. Thus, any actuary who achieved Fellowship or

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Associateship of the SOA by completing the qualification requirements of the SOA, not solely in recognition of membership of another actuarial association, has CAS examination credit for:

Exam 1
Exam 2
Exam 3F
Exam LC
Exam ST if credit for MLC was obtained prior to 2014

## Exam 4

All 3 VEE Requirements
Therefore, the remaining exams/courses required of an ASA or FSA to achieve ACAS are:
Online Course 1
Online Course 2
Exam ST unless credit for MLC was obtained prior to 2014; only required for ASA
Exam 5
Exam 6
CAS Course on Professionalism
Important Note: The syllabus material covered on CAS Exam 7 is still required in addition to ACAS to sign a Statement of Actuarial Opinion, NAIC Property and Casualty Annual Statement, in the United States.

At this time, there is no waiver of any other CAS exams based on the SOA's General Insurance (GI) exam materials process.

## Other Actuarial Organizations

For individuals that have obtained the highest possible actuarial qualification in an actuarial organization that is a member of the International Association of Actuaries, the CAS will grant waivers of some of its examinations/educational requirements as defined by the Executive Council (Exams 1, 2, 3F, LC, ST, and 4; and Validation by Educational Experience requirements) provided that the individual has been practicing as a professional actuary for at least two years subsequent to obtaining the qualification.

## Online Courses and VEE

Online Courses: The CAS will grant a waiver of CAS Online Course 1, Risk Management and Insurance Operations, to those who have the Chartered Property Casualty Underwriter (CPCU) designation.

Validation by Educational Experience: Unlike other CAS admissions requirements, the Validation by Educational Experience (VEE) requirements are generally fulfilled outside an actuarial organization. Candidates requesting waiver of any VEE requirements based on actuarial exams should follow the procedure for requesting a waiver. Most candidates, however, will fulfill the VEE requirements through approved educational experiences and must submit the Application for Validation by Educational Experience Credit. Details are provided in the VEE section of this Syllabus.

## Waiver Request Process

For a waiver of a CAS admissions requirement that has an approved waiver policy stated above, candidates should present their request to the vice president-admissions with appropriate evidence that demonstrates the passing of (or score on) the educational equivalent for which a waiver is requested.

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Requests for waivers for CAS admissions requirements for which there currently is no approved waiver policy are considered on a case-by-case basis. Candidates must present their requests to the vice president-admissions and include with their applications documented evidence that demonstrates the asserted equivalence, as well as the appropriate educational policy material of their local actuarial organization or appropriate educational organization. If such material is not included, the vice president-admissions will request it from the candidates. The vice presidentadmissions will forward the request to the Education Policy Committee for a determination of whether sufficient equivalence exists to permit granting a waiver. The vice president-admissions will review all such requests and, when appropriate, recommend action to the CAS Board of Directors.

Please address all waiver requests to: Vice President-Admissions, Casualty Actuarial Society, 4350 N. Fairfax Drive, Suite 250, Arlington, VA 22203, U.S.A.

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## D. CAS Code of Professional Ethics for Candidates

The purpose of the Casualty Actuarial Society (CAS) Code of Professional Ethics for Candidates (Candidate Code) is to require actuarial candidates to adhere to the high standards of conduct, practice, and qualifications of the actuarial profession, thereby supporting the actuarial profession in fulfilling its responsibility to the public. An actuarial candidate shall comply with the Candidate Code. An actuarial candidate who commits a material violation of the provisions of the Candidate Code shall be subject to the counseling and discipline procedures of the CAS.
"Actuarial candidates" are those persons who have registered for a CAS specific exam but have yet to fulfill all of the requirements for admission into the CAS. In situations where actuarial candidates perform actuarial work, their "principal" is defined as their client or employer. "Actuarial services" are professional services provided to a principal by an individual acting in the capacity of an actuary. Such services include the rendering of advice, recommendations, findings, or opinions based upon actuarial considerations.

Rule 1: An actuarial candidate shall act honestly, with integrity and competence, to uphold the reputation of the actuarial profession.

Rule 2: An actuarial candidate shall not engage in any professional conduct involving dishonesty, fraud, deceit, or misrepresentation or commit any act that reflects adversely on the actuarial profession.

Rule 3: An actuarial candidate shall perform actuarial services with courtesy and professional respect and shall cooperate with others in the principal's interest.

Rule 4: An actuarial candidate shall adhere to the CAS Policy on Examination Discipline.
Rule 5: Actuarial candidates are not authorized to use membership designations of the CAS until they are admitted to membership by the CAS Executive Council.

Rule 6: An actuarial candidate shall not disclose to another party any confidential information unless authorized to do so by the principal or required to do so by law, statute, or regulation. Confidential information includes information of a proprietary nature and information that is legally restricted from circulation.

Rule 7: An actuarial candidate shall respond promptly, truthfully, and fully to any request for information by, and cooperate fully with, appropriate counseling and disciplinary body of the CAS in connection with any disciplinary, counseling or other proceeding of such body relating to the Candidate Code. The actuarial candidate's responsibility to respond shall be subject to applicable restrictions listed in Rule 6 and those imposed by law, statute, or regulation.
(The CAS Board of Directors approved the code above on November 12, 2006.)
A copy of the Casualty Actuarial Society Rules of Procedure for Disciplinary Actions Involving Candidates is available in the Exams \& Admissions section of the CAS website under "Candidates' Code of Ethics."

SYLLABUS OF BASIC EDUCATION
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Examination Rules

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normal qualification/examination process.
Credit will not be given to Fellows of these actuarial organizations who have attained their designation through mutual recognition rather than through the organization's standard credentialing process. Fellows by mutual recognition should pursue examination waivers based on their original credentials.

The CAS has approved the following waiver policy:

| Subject of the Institute and <br> Faculty of Actuaries <br> (U.K.), Actuaries Institute <br> (Australia), and Institute <br> of Actuaries of India | Actuarial Society of <br> South Africa | Waiver Granted for CAS <br> Exam/Educational |
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The CAS has seen an increase in the number of credentialed actuaries in the SOA asking what is needed to obtain their ACAS or FCAS designation from the CAS. The Education Policy Committee reviewed this issue and noted that until 2014 the CAS and the SOA administered jointly preliminary exams, and that prior to that, both societies gave conversion credit that was applicable to the current CAS exam requirements. Thus, any actuary who achieved Fellowship or Associateship of the SOA by completing the qualification requirements of the SOA, not solely in recognition of membership of another actuarial association, has CAS examination credit for:

Exam 1
Exam 2
Exam 3F
Exam LC
Exam ST if credit for MLC was obtained prior to 2014
Exam 4
All 3 VEE Requirements
Therefore, the remaining exams/courses required of an ASA or FSA to achieve ACAS are:
Online Course 1
Online Course 2
Exam ST unless credit for MLC was obtained prior to 2014; only required for ASA
Exam 5
Exam 6
CAS Course on Professionalism
Important Note: The syllabus material covered on CAS Exam 7 is still required in addition to ACAS to sign a Statement of Actuarial Opinion, NAIC Property and Casualty Annual Statement, in the United States.

At this time, there is no waiver of any other CAS exams based on the SOA's General Insurance (GI) exam materials process.

## Other Actuarial Organizations

For individuals that have obtained the highest possible actuarial qualification in an actuarial organization that is a member of the International Association of Actuaries, the CAS will grant waivers of some of its examinations/educational requirements as defined by the Executive Council (Exams 1, 2, 3F, LC, ST, and 4; and Validation by Educational Experience requirements) provided that the individual has been practicing as a professional actuary for at least two years subsequent to obtaining the qualification.

## Online Courses and VEE

Online Courses: The CAS will grant a waiver of CAS Online Course 1, Risk Management and Insurance Operations, to those who have the Chartered Property Casualty Underwriter (CPCU) designation.

Validation by Educational Experience: Unlike other CAS admissions requirements, the Validation by Educational Experience (VEE) requirements are generally fulfilled outside an actuarial organization. Candidates requesting waiver of any VEE requirements based on actuarial exams should follow the procedure for requesting a waiver. Most candidates, however, will fulfill the VEE requirements through approved educational experiences and must submit the Application for Validation by Educational Experience Credit. Details are provided in the VEE section of this Syllabus.

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## Waiver Request Process

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Requests for waivers for CAS admissions requirements for which there currently is no approved waiver policy are considered on a case-by-case basis. Candidates must present their requests to the vice presidentadmissions and include with their applications documented evidence that demonstrates the asserted equivalence, as well as the appropriate educational policy material of their local actuarial organization or appropriate educational organization. If such material is not included, the vice president-admissions will request it from the candidates. The vice president-admissions will forward the request to the Education Policy Committee for a determination of whether sufficient equivalence exists to permit granting a waiver. The vice president-admissions will review all such requests and, when appropriate, recommend action to the CAS Board of Directors.

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## D. CAS Code of Professional Ethics for Candidates

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"Actuarial candidates" are those persons who have registered for a CAS specific exam but have yet to fulfill all of the requirements for admission into the CAS. In situations where actuarial candidates perform actuarial work, their "principal" is defined as their client or employer. "Actuarial services" are professional services provided to a principal by an individual acting in the capacity of an actuary. Such services include the rendering of advice, recommendations, findings, or opinions based upon actuarial considerations.

Rule 1: An actuarial candidate shall act honestly, with integrity and competence, to uphold the reputation of the actuarial profession.

Rule 2: An actuarial candidate shall not engage in any professional conduct involving dishonesty, fraud, deceit, or misrepresentation or commit any act that reflects adversely on the actuarial profession.

Rule 3: An actuarial candidate shall perform actuarial services with courtesy and professional respect and shall cooperate with others in the principal's interest.

Rule 4: An actuarial candidate shall adhere to the CAS Policy on Examination Discipline.
Rule 5: Actuarial candidates are not authorized to use membership designations of the CAS until they are admitted to membership by the CAS Executive Council.

Rule 6: An actuarial candidate shall not disclose to another party any confidential information unless authorized to do so by the principal or required to do so by law, statute, or regulation. Confidential information includes information of a proprietary nature and information that is legally restricted from circulation.

Rule 7: An actuarial candidate shall respond promptly, truthfully, and fully to any request for information by, and cooperate fully with, appropriate counseling and disciplinary body of the CAS in connection with any disciplinary, counseling or other proceeding of such body relating to the Candidate Code. The actuarial candidate's responsibility to respond shall be subject to applicable restrictions listed in Rule 6 and those imposed by law, statute, or regulation.
(The CAS Board of Directors approved the code above on November 12, 2006.)
A copy of the Casualty Actuarial Society Rules of Procedure for Disciplinary Actions Involving Candidates is available in the Exams \& Admissions section of the CAS website under "Candidates' Code of Ethics."

## HINTS ON STUDY AND EXAM TECHNIQUES

Editor's Note: These hints do not include any material on which candidates will be examined, but are provided by members of the CAS Syllabus and Examination Committees to encourage candidates to do their best when sitting for CAS Examinations. This section has been updated many times over the years, most recently in 2014. It is based on the experience and advice of many people. James L. Clare for the Society of Actuariespreparedanearly versionandthen G.D. Morisonadapted itforthe Casualty ActuarialSociety.

## Motivation

Motivation is the single most important ingredient in learning-and in passing exams. Motivation suffers when candidates worry about or are preoccupied with personal matters or other problems. This suggests that candidates should keep the studying for the exam at the very top of their lists of priorities, and should always have a constructive attitude about their studying. In particular, candidates should approach the exam as an opportunity to enhance their knowledge and understanding of actuarial science, rather than as an obstacle in their paths to membership in the CAS.

Motivation is increased by incentives, such as the following:

- Passing actuarial exams requires many hours of study-more for some people and less for others-but often more than many candidates realize. Putting in enough hours can actually save a candidate time. Suppose, for example, that mastering the syllabus for one exam will take a candidate 400 study hours, and that a candidate only puts in 300 hours and fails the exam the first time. He or she then puts in an additional 300 hours and passes the exam the second time. That candidate will have spent 600 hours, when by studying 400 hours the first time around, he or she would have saved 200 hours, not to mention passing sooner. It is recommended that candidates decide for themselves how many hours they really need to study, and then do that much studying-the first time around.
- Candidates can increase their motivation level by regarding the exams as a stepping stone to greater responsibility at their places of employment, to opportunities for getting more done on their own, and to greater results and rewards from their work.
- Candidates can also increase their motivation through sufficiently intensive and sustained study so that they come to appreciate more fully the fascination of the various subjects, and the interrelationships between them. A number of doctors, educators, executives, and human resources professionals agree that motivation can be greatly increased by having a goal in mind. Candidates must determine their goals and keep them in mind.


## Techniques

It has been proven many times in various countries, both by individuals and by controlled groups, that improved study and exam techniques can strengthen a candidate's mastery of a subject and increase his or her exam scores significantly. Provided that the candidate is motivated and spends enough time studying, techniques such as those given here often make the difference between failing or passing an exam.

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Each person has his or her own strengths and weaknesses, so candidates are advised to work out their own personal sets of techniques which will work best for them. What follows are merely suggestions to help candidates in getting started in building up their own techniques.

## The Challenge

It is easy to underestimate the effort that is required because substantial changes may be needed to switch from college or university life to successful study of actuarial exams.

University courses often do much to smooth the path for students with lectures, personal contacts, organized places of study, and a focus on learning.

By contrast, actuarial candidates must work a great deal on their own to reach their goals. Much actuarial studying is normally fit in after a full day's work, or is done on a weekend when one's friends are free to do as they please. Making adequate time available for studying requires sustained self-discipline and is a purely individual and personal responsibility.

## Schedule of Study

There is only one substitute for hours of study time omitted one week-at least as many additional hours of study in another week. An unavoidably "necessary condition" for success in studying (though not necessarily "sufficient condition") is simply spending enough total hours studying.

Candidates must decide how many hours in total they need to study. Then they need to set out their schedules in writing, specifically stating the weekday evening and weekend periods allocated to studying. They then should total the number of hours made available. If the total hours scheduled are less than the total hours necessary, candidates should expand their schedules until they at least have equaled the required total time plus an additional cushion for absorbing time that will inevitably be lost along the way on account of illness, work pressures, etc.

Then candidates should fit all the segments of the syllabus into their schedules so that they will thoroughly cover all the learning objectives, knowledge statements, and readings in good time before the exam, with time left over for a thorough final review. It is important for candidates to spread their time over the entire syllabus in some deliberate way, for example, in proportion to the pages of reading material on the syllabus or to the range of weight given to the material.

It is not appropriate to assume that certain parts of the syllabus will not appear on the exam either because of historical precedent or because of the range of weight given to the material.

Candidates may find it helpful to study several subjects within an exam, or all of them, in parallel. This gives them more variety each week, and may give them a combination of both study that is more appealing and study that requires greater effort and concentration. Particularly demanding study may be best left for weekends when candidates are less fatigued from regular work.

It is a good idea for candidates to keep a record of the hours they spend studying. Even if candidates are completely confident that they know the syllabus before putting in their required total hours, there is much to be said for carrying out the full schedule and completing the total time quotas.

## Retention

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As part of human nature, our memories forget facts and ideas most rapidly during the time immediately following our study of them. For a given number of study hours, therefore, candidates will remember more if they review promptly and frequently. It is recommended that candidates review what they have learned as part of ending their study for the day.

Before reading a paper or section of text, candidates should scan the section for titles, headings, subheadings, and topic sentences to get the general idea, paying attention to graphs, charts, and diagrams. They should read the summary at the end of the paper or chapter and look for leading questions and exercises at the beginning and at the end.

After the initial skim, candidates should read through the entire material one section at a time for the main ideas, and not worry if the reading is relatively slow. Technical reading is challenging and requires more careful processing. Although it is tempting, candidates may want to avoid taking detailed notes at this time, but rather focus on understanding the material. Taking notes at this point may not be an efficient techniquecandidates may take down too much information or simply copy information without understanding. If a section is difficult to understand, candidates should mark it to review in a later pass.

As each section or paper is completed, candidates should paraphrase and write down just the main ideas in their own words without looking at the source material. Putting the information in one's own words forces one to become actively involved with the material. It helps improve retention, and forces attention to those items that are not really understood and require further study. While the extent of a candidate's notes will be a matter of his or her own personal tastes, taking thorough notes will be a good investment of time for most people. Upon reviewing their notes, if candidates find gaps in their knowledge or in their understanding, they should bear down on those areas and master them.

As they begin their next study session, candidates should review what they learned the last time and what they learned during other recent sessions. Then they can recall points they have learned during odd spare moments in between study sessions.

In their study for the mathematical sections of the exams, candidates are advised to work out as many examples as possible in order to acquire facility in the application of the mathematical principles and methods to specific problems.

Candidates should note the considerable emphasis in actuarial exams on knowledge. They should remember, however, that the best way to learn facts by heart is to understand the whole subject, and to tie together ideas that are related. They should look at any single subject from several different angles, relating what they learn to what they know already. Candidates should look for as many connections as they can between their actuarial work and their actuarial studies.

Another study technique candidates might want to try is to test themselves as they go along. They can review previous exams when they start to study to get an idea of the mastery of the syllabus expected. Candidates can also take these as "trial exams" to help them in testing their knowledge and understanding of the course of reading, and in improving their exam speed and confidence.

Some candidates deliberately test themselves; others prefer not to do so. Candidates should expect a gradual gathering of momentum as they begin their study for a particular exam. By keeping at it, according to their plans, candidates will find their rate of progress speeding up after the first few weeks.

When a candidate finds himself or herself getting very "stale," one possibility is to stop studying altogether for, perhaps, three days. Then the candidate should continue on with his or her study plan, no matter how he

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or she feels, for at least the next month or six weeks. A candidate's study plan should have enough spare time available in it to allow for such occasional "down time." Following a mixed schedule, with a weekly combination of subjects that the candidate likes and subjects that he or she finds difficult, will help to minimize staleness.

Discussing the syllabus with friends taking the same exam, or with others who have passed the exam, will help candidates remember the material firmly and understand it. It also helps candidates to realize their own gaps and difficulties. If effective study circles, online forums, and review courses can be found, they will give candidates a different slant on the subject, give them a chance to review and to practice, keep them moving through the syllabus, and help to combat lethargy and self-satisfaction.

It is important for candidates to leave time for a thorough final review before the exam. In the last three or four weeks before the exam, candidates should use practice exams to simulate the exam experience as closely as possible, while keeping in mind that they need to be able to pass any set of exam questions which has been drawn from the syllabus.

When taking the practice exams, candidates should set up a clean, distraction-free space and allow plenty of uninterrupted time. Candidates should develop a plan for how to answer the questions. One strategy is to determine a time limit for each point and stick to it. If there are 80 points on the four-hour exam, allow about two and a half minutes for each point, leaving time for review at the end. When the time is up for one question, move on to the next question. Incomplete answers may be completed during the review time.

Candidates are responsible for mastery of the learning objectives and knowledge statements in the syllabus and the associated readings that pertain to these learning objectives and knowledge statements. Simply relying on seminar notes, past exams, or on material from review courses or online forums may leave a candidate missing salient and important knowledge necessary to obtain maximum points on the exam.

## Formulating Answers

## Multiple-Choice Questions

Candidates can definitely improve their speed and mastery by seriously practicing sample exam type questions before the exam. It helps to have a good understanding of the subject material. Candidates can also develop valuable shortcuts, such as eliminating impossible answers by checking out boundary conditions, by inspecting other aspects of certain suggested solutions, or by substituting numerical values and cutting out some answers. Since questions are varied, candidates will need a variety of techniques to cope with them.

In a multiple-choice exam, candidates increase their chances of passing if they are able to seriously attempt each question on the entire exam at least once. It may help them to determine the proportionate number of questions to answer in the first half-hour of the exam, to check how much ground they cover in that time, and then accordingly either speed up, or slow down and dig more deeply.

When pressed for time, it may pay for candidates to omit a few multiple-choice questions that they expect to take more time than average; so as to have time for a larger number of more quickly answered questions. For example, a cluster of questions may have a common introduction that a candidate does not readily grasp, in which case he or she might skip the entire cluster at a first attempt.

Candidates may find it helpful to keep a list of the number of the questions not answered so that they quickly can get an idea of how many they are omitting. This will allow the candidate to quickly return to these

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questions.
Candidates should change their answers only if they are sure that their first solution was wrong.

## Constructed Response Questions

The model response to the typical constructed response (e.g., essay style) question depends on the level of knowledge that the question is asking the candidate to demonstrate.

For non-calculation questions, there are typically six levels of information that may be tested corresponding with Bloom's taxonomy:

Level 1: Knowledge-tests the ability of the candidate to recall or remember knowledge or facts
Level 2: Comprehension-requires the candidate to demonstrate comprehension of central concepts through explanation of those concepts

Level 3: Application-measures the candidate's ability to apply ideas and concepts to new situations
Level 4: Analysis-requires the candidate to analyze information by separating material into component parts, including identification of facts and development of inferences with respect to a situation

Level 5: Synthesis-tests the ability of a candidate to synthesize, or combine, concepts or ideas and develop and defend the position resulting from that combination

Level 6: Evaluation-requires the candidate to support conclusions by evaluating the validity of ideas and concepts

The "action" verbs of each question (e.g., explain, identify, describe, determine, etc.) are chosen very deliberately by question writers to instruct the candidates how to answer the question in order to demonstrate the required mastery of the learning objective(s) that the question is testing.

Very often, the question writer will add an adverb before the action verb, most notably the adverb "briefly." This one simple word means a great deal to both the question writer and the grader. Just as importantly, the absence of this word means a great deal to the writer and the grader. The verbs and adverbs used, or not used, and the point values assigned to each question and subpart provide cues to how the candidates are expected to answer each item. A typical key for any exam follows this rubric:

- "Brief" descriptions, discussions, etc., are worth generally $1 / 4$ point, so candidates should respond concisely, but with clarity regarding what is being communicated.
- (Unmodified) discussions or descriptions are worth generally $1 / 2$ point, so candidates should provide a more in-depth response with more detail compared to a question that asks for a brief response, but typically not more than one-half of a written page.

As upper level exam questions gravitate towards higher levels in the Bloom's taxonomy (in particular, levels $3-6)$, candidates should pay closer attention to the wording of the item. Prompts such as "recommend," "justify," "propose," "assess," "fully discuss," and "compare and contrast" will require the candidate to write a more substantive and coherent answer rather than simply list knowledge gained from syllabus readings. For such items, point totals can vary considerably. Nevertheless, candidates can continue to use point totals as a guide to gauge how much content is required to appropriately answer the item.

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For questions that require candidates to work a numerical solution, candidates should take the time to set up the problem so that they document their understanding. They should set forth relevant equations or formulae, and then enter appropriate values. They should lay out complicated calculations in tables that demonstrate their understanding of the correct solution. If the candidate needs to set forth further assumptions to answer the question, these assumptions should be provided and explained. If a candidate is pressed for time, then setting up the response and walking through how it would be calculated will earn the candidate partial credit on the question despite not having punched the numbers on the calculator to get the final answer.

Candidates should keep each answer relevant to the precise question being asked. They should make sure they first understand exactly what is wanted before they begin to answer a question. When they have written part or all of their answer, they should take another look at the question and make sure they have answerednot their own question-but the question as set on the exam page.

If a candidate believes that a question is ambiguous, or that it does not provide all the information necessary to answer the question, the candidate should state how he or she interprets the question and/or what assumptions are made to answer it.

Candidates should take time to write legibly, since examiners can only give credit for what they can read. They should try to "organize" their answer. Then, their aim should be to get down sufficient relevant detail given the question's scope and available time.

There is no advantage to answering the questions in any particular order. Candidates may answer the questions in the order given if they wish. Candidates are given a 15 -minute reading period prior to the exam at which point the candidate can quickly read over the whole paper and determine their ideal test taking approach. For example, candidates may wish to start on questions that come easily to them, then gradually work into the questions they find more challenging, and end on a question that they think can be answered readily even though, by that time, their energy and concentration may be falling off.

Note that since each question is graded separately, each answer must be self-contained. Candidates should not write, "Part of my answer to question 3 is found in my answer to question 1."

It is important that candidates remember that they have limited time. Candidates will find that it is worth checking their progress to assure that they have an opportunity to respond to every question. If they know that a question will take too much time, they can pass it and return to it later, if time permits.

Candidates should never give up in the examination room. They should use every minute and every second of the available time. They should not "grade their own papers," and decide not to hand in an answer to a question or two because they feel it is all-wrong. They should hand in all of their answers, and let the examiners do the grading. More than one candidate has not handed in some answer pages which he or she had condemned in his or her own mind, only to find out later that the work was correct, and to find out still later that he or she had narrowly failed to pass.

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Study Resources

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## STUDY RESOURCES

## Study Notes

Official Study Notes are published to help candidates prepare for the examinations. In some instances, Study Notes are the principal materials for study; in others, they are designed to coordinate the subject for the candidate or to complement other readings. Occasionally, the course of reading for an examination may be changed after publication of the Syllabus. Such a change will be announced on the specific exam syllabus Web page.

Study Notes may be downloaded at no charge from the specific exam syllabus Web page.

## Study Kits for Exams 5-9

The Study Kit contains required readings not owned by the CAS but for which the CAS has been granted permission to include in the Study Kit. Study Kits will be available the first Monday in December, for April 2015 exams and on the first Monday in April 2015, for October 2015 exams. Study Kits may be purchased from the CAS Online Store; there are NO RETURNS and NO REFUNDS.

## Online Publications for Exams LC, ST, S, and 5-9

All readings listed as "Online Publications" will be available on a web page titled Complete Text References at no charge.

## Online Courses 1/CA1 and 2/CA2

All required educational content for Online Courses 1/CA1 and 2/CA2 is provided in the online courses themselves.

## Sample Examination Questions

## Preliminary Exams

Sample examination questions for Exams 1, 2, 3F, and 4 may be available from the sponsoring organizations.

## Exams LC, ST, S, and 5-9

Copies of recent past exams including answer key for Exams LC and ST are available at no charge in the "Past Exams and Pass Marks" section of the CAS website.

Copies of recent past exams for Exams 5-9 with sample answers are available at no charge in the "Past Exams and Pass Marks" section of the CAS website. Sample essay answers are actual responses that received credit and are illustrative of successful answers, although they may not be considered perfect answers.

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Sample questions/answers for new topics for Exam ST are available on the website, but candidates can look to previously administered Exam 3L for sample questions/answers for Learning Objectives that overlap with Exams LC and ST. For Exam S, the candidate can look to previously administered Exams 3L, LC, and ST for sample questions/answers for Learning Objectives that overlap with Exam S. Sample questions/answers for new topics for Exam $S$ are available on the website.

Exams LC, ST, S, and 5-9 will be posted in the "Exams" section of the CAS website approximately one week after these examinations have been administered. They will include a preliminary list of multiple-choice answers. Sample essay answers and final multiple-choice answers will be posted at the end of July for April Examinations and at the end of January for October Examinations.

In referring to a published prior examination, candidates should keep in mind that the questions were based on the learning objectives in effect for that particular examination and may not reflect the current learning objectives. Candidates may also expect future examinations to vary somewhat as to the proportions of question styles and subjects. New forms of questions may appear from time to time, and the total number of questions may vary from one exam sitting to the next.

## E-Mail Study Groups

The CAS has available e-mail study groups for those preparing for CAS examinations. Information about joining a study group is available in the "E-Mail Study Groups" section of the CAS website. Please direct any questions to the CAS Webmaster at webmaster@casact.org.

## CAS Library

The CAS Library has available for loan a limited number of the books marked with a bold B in this Syllabus. Candidates registered for CAS Examinations and all members of the CAS have access to the library. The CAS Library is located at the CAS Office in Arlington, Virginia. For those who reside in East Asia, the Actuaries Office in Hong Kong has CAS Library books available for lending and candidates residing in that area should contact the office in Hong Kong.

Books and manuals may be withdrawn from the library for a period of one month without charge. In general, not more than two references may be in the hands of one borrower at a time. Requests must be in writing and must include the borrower's complete name, address, and telephone number as well as the complete title(s) and author(s) of the requested book(s). Address requests for library books to:

## For Candidates Outside East Asia:

Casualty Actuarial Society
Attention: Library Service
4350 N. Fairfax Drive, Suite 250
Arlington, Virginia 22203
Fax: (703) 276-3108
E-mail: library@casact.org

## For candidates in East Asia:

Actuaries Office in Hong Kong
Attention: Patricia Kum
2202 Tower Two, Lippo Centre
89 Queensway
Hong Kong
E-mail: hongkonglibrary@casact.org

Candidates are responsible for the cost of returning library books. Books must be returned to the office from which they were borrowed. The CAS ships the requested book(s) in the U.S. via United Parcel Service (UPS) and internationally via Air Mail. Due to delays in the mail system, the CAS requires all shipments of books returned to the CAS Office to be shipped via UPS, FedEx, or an equivalent carrier with tracking capabilities.

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Please do not use the postal service. Overdue books will be charged at a cost of $25 \phi$ per day.
Books that are not available through the CAS Library may be obtained by contacting the organizations listed in the "Publishers and Distributors" section at the end of each examination syllabus section.

## 2015 Exam 1 Syllabus Probability

The syllabus for this exam is defined in the form of learning objectives that set forth, usually in broad terms, what the candidate should be able to do in actual practice.

Please check the "Syllabus Update" for this exam for any changes to this syllabus or options for obtaining credit for this exam.
The purpose of the syllabus for this examination is to develop knowledge of the fundamental probability tools for quantitatively assessing risk. The application of these tools to problems encountered in actuarial science is emphasized. A thorough command of the supporting calculus is assumed. Additionally, a very basic knowledge of insurance and risk management is assumed.

## A. General Probability

## LEARNING OBJECTIVES

1. Use and apply the following concepts in a risk management context:

- Set functions including set notation and basic elements of probability
- Mutually exclusive events
- Addition and multiplication rules
- Independence of events
- Combinatorial probability
- Conditional probability
- Bayes Theorem / Law of total probability


## B. Univariate Probability Distributions

This section includes binomial, negative binomial, geometric, hypergeometric, Poisson, uniform, exponential, gamma, and normal distributions.

[^3]
## C. Multivariate Probability Distributions

This section includes the bivariate normal distribution.
LEARNING OBJECTIVES

1. Use and apply the following concepts in a risk management context:

- Joint probability functions and joint probability density functions
- Joint cumulative distribution functions
- Central Limit Theorem
- Conditional and marginal probability distributions
- Moments for joint, conditional, and marginal probability distributions
- Joint moment generating functions
- Variance and measures of dispersion for conditional and marginal probability distributions
- Covariance and correlation coefficients
- Transformations and order statistics
- Probabilities and moments for linear combinations of independent random variables


## Options for Obtaining Exam 1 Credit

The CAS will grant credit for Exam 1 to those who have successfully completed one of the following examinations:

| Organization | Exam |
| :--- | :--- |
| Actuarial Society of South Africa | A101, Probability and Mathematical Statistics |
| Actuaries Institute (Australia) | CT3, Probability and Mathematical Statistics |
| Institute of Actuaries of India | CT3, Probability and Mathematical Statistics |
| Institute and Faculty of Actuaries (U.K.) | CT3, Probability and Mathematical Statistics |
| Society of Actuaries | P, Probability |

To obtain credit, the candidate should contact the Actuaries’ Resource Center (arc@casact.org). Provide the name of the actuarial organization that administered the exam, the exam name and number, the date that you passed, as well as your full name, date of birth, and contact information.

[^4]
## 2015 Exam 2 Syllabus Financial Mathematics Exam

The syllabus for this exam is defined in the form of learning objectives that set forth, usually in broad terms, what the candidate should be able to do in actual practice.

Please check the "Syllabus Update" for this exam for any changes to this syllabus or options for obtaining credit for this exam.

The purpose of the syllabus for this examination is to develop knowledge of the fundamental concepts of financial mathematics, and how those concepts are applied in calculating present and accumulated values for various streams of cash flows as a basis for future use in: reserving, valuation, pricing, asset/liability management, investment income, capital budgeting, and valuing contingent cash flows. The candidate will also be given an introduction to financial instruments, including derivatives, and the concept of noarbitrage as it relates to financial mathematics.

The Financial Mathematics Exam assumes a basic knowledge of calculus and an introductory knowledge of probability.

## A. Interest Theory

## LEARNING OBJECTIVES

1. For time value of money, define and recognize the definitions of the following terms:
a. Interest rate (rate of interest)
b. Simple interest
c. Compound interest
d. Accumulation function
e. Future value
f. Present value/net present value
g. Discount factor
h. Discount rate (rate of discount)
i. Convertible m-thly
j. Nominal rate
k. Effective rate
2. Inflation and real rate of interest
m . Force of interest
n. Equation of value
3. For time value of money, the candidate will be able to do the following:
a. Given any two of interest rate, present value, or future value, calculate the third based on simple or compound interest.
b. Given any one of the effective interest rate, the nominal interest rate convertible $m$-thly, the effective discount rate, the nominal discount rate convertible m-thly, or the force of interest, calculate all of the other items.
c. Write the equation of value given a set of cash flows and an interest rate.
4. For annuities with payments that are not contingent, define and recognize the definitions of the following terms:
a. Annuity-immediate
b. Annuity-due
c. Perpetuity
d. Payable m-thly, or Payable continuously
e. Level payment annuity
f. Arithmetic increasing/decreasing payment annuity
g. Geometric increasing/decreasing payment annuity
h. Term of annuity
5. For annuities with payments that are not contingent, the candidate will be able to do the following:
a. Given an annuity with level payments, immediate (or due), payable m-thly, (or payable continuously), and any three of present value, future value, interest rate, payment, and term calculate the remaining two items.
b. Given an annuity with non-level payments, immediate (or due), payable m-thly, (or payable continuously), the pattern of payment amounts, and any three of present value, future value, interest rate, payment amounts, and term of annuity calculate the remaining two items.
6. For loans, define and recognize the definitions of the following terms:
a. Principal
b. Interest
c. Term of loan
d. Outstanding balance
e. Final payment (drop payment, balloon payment)
f. Amortization
g. Sinking fund
7. For loans, the candidate will be able to do the following:
a. Given any four of term of loan, interest rate, payment amount, payment period, principal, calculate the remaining items.
b. Calculate the outstanding balance at any point in time.
c. Calculate the amount of interest and principal repayment in a given payment.
d. Given the quantities, except one, in a sinking fund arrangement calculate the missing quantity.
8. For bonds, define and recognize the definitions of the following terms:
a. Price
b. Redemption value
c. Par Value/Face value
d. Coupon, Coupon rate
e. Term of bond
f. Yield rate g. Callable/non-callable
g. Book value
h. Accumulation of discount/Amortization of premium
9. For bonds, the candidate will be able to do the following:
a. Given any four of price, redemption value, yield rate, coupon rate, and term of bond, calculate the remaining item.
10. For general cash flows and portfolios, define and recognize the definitions of the following terms:
a. Yield rate/rate of return
b. Dollar-weighted rate of return/Time-weighted rate of return
c. Current value
d. Duration (Macaulay, modified and effective)
e. Convexity
f. Portfolio and investment year allocation methods
g. Spot rate
h. Forward rate
i. Yield curve
j. Stock price, stock dividend
11. For general cash flows and portfolios, the candidate will be able to do the following:
a. Calculate the current value of a set of cash flows.
b. Calculate the portfolio yield rate.
c. Calculate the dollar-weighted and time-weighted rate of return.
d. Calculate the duration and convexity of a set of cash flows.
e. Calculate either Macaulay or modified duration given the other.
f. Use duration and convexity to approximate the change in present value due to a change in interest rate.
g. Calculate the price of a stock using the dividend discount model.
12. For immunization, define and recognize the definitions of the following terms:
a. Cash-flow matching;
b. Immunization (including full immunization);
c. Redington immunization.
13. For immunization, the candidate will be able to do the following:
a. Construct an investment portfolio to fully immunize a set of liability cash flows.
b. Construct an investment portfolio to match present value and duration of a set of liability cash flows.
c. Construct an investment portfolio to exactly match a set of liability cash flows.

## B. Financial Economics

## LEARNING OBJECTIVES

1. For general derivatives, define and recognize the definitions of the following terms:
a. Derivative, Underlying asset, Over-the-counter market
b. Ask price, Bid price, Bid-ask spread
c. Short selling, Short position, Long position
d. Stock index
e. Spot price
f. Net profit/payoff
g. Credit risk
h. Marking-to-market
i. Margin, Maintenance margin, Margin call
2. For general derivatives, evaluate an investor's margin position based on changes in asset values.
3. For options, define and recognize the definitions of the following terms:
a. Call option, Put option
b. Expiration, Expiration date
c. Strike price/Exercise price
d. European option, American option, Bermudan option
e. In-the-money, At-the-money, Out-of-the-money
f. Covered call, Naked writing
g. Dividends
h. Put-call parity
4. For options, evaluate the payoff and profit of basic derivative contracts.
5. For hedging and investment strategies, define and recognize the definitions of the following terms:
a. Hedging, Arbitrage
b. Diversifiable risk, Nondiversifiable risk
c. Synthetic forwards
d. Spreads (including bull, bear, box, and ratio spreads)
e. Collars (including zero-cost collars), Paylater strategy
f. Straddles (including strangles, written straddles and butterfly spreads)
g. Convertible bond, Mandatorily convertible bond
6. For hedging and investment strategies, the candidate will be able to:
a. Explain how derivative securities can be used as tools to manage financial risk.
b. Explain the reasons to hedge and not to hedge.
c. Evaluate the payoff and profit of hedging strategies.
7. For forwards and futures, define and recognize the definitions of the following terms:
a. Forward contract, Prepaid forward contract
b. Outright purchase, Fully leveraged purchase
c. Implied repo rate
d. Cost of carry
e. Lease rate
f. Futures contract
8. For forwards and futures, the candidate will be able to:
a. Determine forward price from prepaid forward price.
b. Explain the relationship between forward price and futures price.
c. Explain the relationship between forward price and future stock price.
d. Use the concept of no-arbitrage to determine the theoretical value of futures and forwards.
e. Given any four of call premium, put premium, forward price, strike price and interest rate, calculate the remaining item using the put-call parity formula.
9. For swaps, define and recognize the definitions of the following terms:
a. Swap, Prepaid swap
b. Swap term, Swap spread, Notional Amount
c. Simple commodity swap, Interest rate swap
d. Deferred swap
10. Use the concept of no-arbitrage to determine the theoretical values of swaps.

## Options for Obtaining Exam 2 Credit

The CAS will grant credit for Exam 2 to those who have successfully completed one of the following examinations:

| Organization | Exam |
| :--- | :--- |
| Actuarial Society of South Africa | A201, Financial Mathematics |
| Actuaries Institute (Australia) | CT1, Financial Mathematics |
| Canadian Institute of Actuaries | University Accreditation Program credit for <br> Financial Mathematics |
| Institute of Actuaries of India | CT1, Financial Mathematics |
| Institute and Faculty of Actuaries (U.K.) | CT1, Financial Mathematics |
| Society of Actuaries | Exam FM, Financial Mathematics |

To obtain credit, the candidate should contact the Actuaries' Resource Center (arc@casact.org). Provide the name of the actuarial organization that administered the exam, the exam name and number, the date that you passed, as well as your full name, date of birth, and contact information.
*Note: The Exam 2 credit chart includes a new waiver for the Actuarial Society of South Africa.

## 2015 Exam 3F Syllabus Models for Financial Economics

The syllabus for this exam is defined in the form of learning objectives that set forth, usually in broad terms, what the candidate should be able to do in actual practice.

Please check the "Syllabus Update" for this exam for any changes to this syllabus or options for obtaining credit for this exam.

The purpose of the syllabus is to develop the candidate's knowledge of the theoretical basis of certain actuarial models and the application of those models to insurance and other financial risks. A thorough knowledge of calculus, probability, and interest theory is assumed.

## A. Interest Rate Models

## LEARNING OBJECTIVES

1. Evaluate features of the Vasicek and Cox-Ingersoll-Ross bond price models.
2. Explain why the time-zero yield curve in the Vasicek and Cox-Ingersoll-Ross bond price models cannot be exogenously prescribed.
3. Construct a Black-Derman-Toy binomial model matching a given time-zero yield curve and a set of volatilities.

## B. Rational valuation of derivative securities

## LEARNING OBJECTIVES

1. Use put-call parity to determine the relationship between prices of European put and call options and to identify arbitrage opportunities.
2. Calculate the value of European and American options using the binomial model.
3. Calculate the value of European options using the Black-Scholes option-pricing model.
4. Identify the situations where the values of European and American options are the same.
5. Interpret the option Greeks.
6. Explain the cash flow characteristics of the following exotic options: Asian, barrier, compound, gap, and exchange.
7. Explain the properties of a lognormal distribution and explain the Black-Scholes formula as an expected value for a lognormal distribution.
8. Explain what it means to say that stock prices follow a diffusion process.
9. Apply Itô's lemma in the one-dimensional case.

## C. Simulation

## LEARNING OBJECTIVES

1. Simulate lognormal stock prices.
2. Use variance reduction techniques to accelerate convergence.

## D. Risk Management Techniques

## LEARNING OBJECTIVES

1. Explain and demonstrate how to control risk using the method of delta-hedging.

## Options for Obtaining Exam 3F Credit

The CAS will grant credit for Exam 3F to those who have successfully completed one of the following examinations:

| Organization | Exam |
| :--- | :--- |
| Actuarial Society of South Africa | A205, Financial Economics |
| Actuaries Institute (Australia) | CT8, Financial Economics |
| Canadian Institute of Actuaries | University Accreditation Program credit for <br> Models for Financial Economics |
| Institute of Actuaries of India | CT8, Financial Economics |
| Institute and Faculty of Actuaries (U.K.) | CT8, Financial Economics |
| Society of Actuaries | MFE, Models for Financial Economics |

To obtain credit, the candidate should contact the Actuaries’ Resource Center (arc@casact.org). Provide the name of the actuarial organization that administered the exam, the exam name and number, the date that you passed, as well as your full name, date of birth, and contact information.
*Note: The Exam 3F credit chart includes a new waiver for the Actuarial Society of South Africa.

## 2015 Exam 4 Syllabus Construction and Evaluation of Actuarial Models Exam

The syllabus for this exam is defined in the form of learning objectives that set forth, usually in broad terms, what the candidate should be able to do in actual practice.
Please check the "Syllabus Update" for this exam for any changes to this syllabus or options for obtaining credit for this exam.

The syllabus for this examination provides an introduction to modeling and covers important actuarial methods that are useful in modeling. A thorough knowledge of calculus, probability, and mathematical statistics is assumed.

The candidate will be introduced to useful frequency and severity models beyond those covered in Exams 3F and 3 L . The candidate will be required to understand the steps involved in the modeling process and how to carry out these steps in solving business problems. The candidate should be able to: (1) analyze data from an application in a business context; (2) determine a suitable model including parameter values; and (3) provide measures of confidence for decisions based upon the model. The candidate will be introduced to a variety of tools for the calibration and evaluation of the models.

The candidate is expected to be familiar with survival, severity, frequency and aggregate models, and use statistical methods to estimate parameters of such models given sample data. The candidate is further expected to identify steps in the modeling process, understand the underlying assumptions implicit in each family of models, recognize which assumptions are applicable in a given business application, and appropriately adjust the models for impact of insurance coverage modifications.

Specifically, the candidate is expected to be able to perform the tasks listed below.

## A. Severity Models

## LEARNING OBJECTIVES

1. Calculate the basic distributional quantities:
a. Moments
b. Percentiles
c. Generating functions
2. Describe how changes in parameters affect the distribution.
3. Recognize classes of distributions and their relationships.
4. Apply the following techniques for creating new families of distributions:
a. Multiplication by a constant
b. Raising to a power
c. Exponentiation,
d. Mixing
5. Identify the applications in which each distribution is used and reasons why.
6. Apply the distribution to an application, given the parameters.
7. Calculate various measures of tail weight and interpret the results to compare the tail weights.

## B. Frequency Models

## LEARNING OBJECTIVES

For the Poisson, Mixed Poisson, Binomial, Negative Binomial, Geometric distribution and mixtures thereof:

1. Describe how changes in parameters affect the distribution.
2. Calculate moments.
3. Identify the applications for which each distribution is used and reasons why.
4. Apply the distribution to an application given the parameters.
5. Apply the zero-truncated or zero-modified distribution to an application given the parameters.

## C. Aggregate Models

## LEARNING OBJECTIVES

1. Compute relevant parameters and statistics for collective risk models.
2. Evaluate compound models for aggregate claims.
3. Compute aggregate claims distributions.

## D. For Severity, Frequency and Aggregate Models

## LEARNING OBJECTIVES

1. Evaluate the impacts of coverage modifications:
a. Deductibles
b. Limits
c. Coinsurance
2. Calculate Loss Elimination Ratios.
3. Evaluate effects of inflation on losses.

## E. Risk Measures

## LEARNING OBJECTIVES

1. Calculate VaR, and TVaR and explain their use and limitations.

## F. Construction of Empirical Models

## LEARNING OBJECTIVES

1. Estimate failure time and loss distributions using:
a. Kaplan-Meier estimator, including approximations for large data sets
b. Nelson-Åalen estimator
c. Kernel density estimators
2. Estimate the variance of estimators and confidence intervals for failure time and loss distributions.
3. Apply the following concepts in estimating failure time and loss distribution:
a. Unbiasedness
b. Consistency
c. Mean squared error

## G. Construction and Selection of Parametric Models

## LEARNING OBJECTIVES

1. Estimate the parameters of failure time and loss distributions using:
a. Maximum likelihood
b. Method of moments
c. Percentile matching
d. Bayesian procedures
2. Estimate the parameters of failure time and loss distributions with censored and/or truncated data using maximum likelihood.
3. Estimate the variance of estimators and the confidence intervals for the parameters and functions of parameters of failure time and loss distributions.
4. Apply the following concepts in estimating failure time and loss distributions:
a. Unbiasedness
b. Asymptotic unbiasedness
c. Consistency
d. Mean squared error
e. Uniform minimum variance estimator
5. Determine the acceptability of a fitted model and/or compare models using:
a. Graphical procedures
b. Kolmogorov-Smirnov test
c. Anderson-Darling test
d. Chi-square goodness-of-fit test
e. Likelihood ratio test
f. Schwarz Bayesian Criterion

## H. Credibility

## LEARNING OBJECTIVES

1. Apply limited fluctuation (classical) credibility including criteria for both full and partial credibility.
2. Perform Bayesian analysis using both discrete and continuous models.
3. Apply Bühlmann and Bühlmann-Straub models and understand the relationship of these to the Bayesian model.
4. Apply conjugate priors in Bayesian analysis and in particular the Poisson-gamma model.
5. Apply empirical Bayesian methods in the nonparametric and semiparametric cases.

## I. Simulation

## LEARNING OBJECTIVES

1. Simulate both discrete and continuous random variables using the inversion method.
2. Estimate the number of simulations needed to obtain an estimate with a given error and a given degree of confidence.
3. Use simulation to determine the p -value for a hypothesis test.
4. Use the bootstrap method to estimate the mean squared error of an estimator.
5. Apply simulation methods within the context of actuarial models.

## Options for Obtaining Exam 4 Credit

The CAS will grant credit for Exam 4 to those who have successfully completed one of the following examinations:

| Organization | Exam |
| :--- | :--- |
| Actuarial Society of South Africa | A202, Models, and A204, Statistical Methods** |
| Actuaries Institute (Australia) | CT4, Models, and CT6, Statistical Methods* |
| Canadian Institute of Actuaries | University Accreditation Program credit for <br> Construction and Evaluation of Actuarial Models |
| Institute of Actuaries of India | CT4, Models, and CT6, Statistical Methods* |
| Institute and Faculty of Actuaries (U.K.) | CT4, Models, and CT6, Statistical Methods* |
| Society of Actuaries | C, Construction and Evaluation of Actuarial <br> Models Exam |

*CT4 \& CT6, together, will provide credit for CAS Exams ST and 4 \& Validation by Education Experience for Applied Statistical Methods.
**A202 \& A204, together, will provide credit for CAS Exams ST and $4 \&$ Validation by Education Experience for Applied Statistical Methods.

To obtain credit, the candidate should contact the Actuaries’ Resource Center (arc@casact.org). Provide the name of the actuarial organization that administered the exam, the exam name and number, the date that you passed, as well as your full name, date of birth, and contact information.
*Note: The Exam 4 credit chart includes a new waiver for the Actuarial Society of South Africa.

## Spring and Fall 2015 Exam LC Syllabus Models for Life Contingencies

The syllabus for this one-and-a-half-hour exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain conceptually in the context of an examination.

KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.
Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.

Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from links in the Complete Text References section below. Books and other publications marked with a bold B may be purchased from the publisher or a bookstore (with limited copies available to be borrowed from the CAS Library). Items marked with a bold BO are optional books that may be purchased from the publisher or bookstore.

Please check the "Syllabus Update" for this exam for any changes to this syllabus.
The CAS will grant credit for CAS Exam LC to those who successfully complete SOA Exam MLC (Models for Life Contingencies) in the current education structure.

A thorough knowledge of calculus, probability, and interest theory is assumed. Knowledge of risk management at the level of Exam 1 is also assumed.

This examination develops the candidate's knowledge of the theoretical basis of contingent payment models and the application of those models to insurance risks.

The candidate will be required to develop an understanding of contingent payment models. The candidate will be expected to understand what important results can be obtained from these models for the purpose of making business decisions, and what approaches can be used to determine these results.
A variety of tables will be provided to the candidate with the exam. The tables include values for the standard normal distribution and illustrative life tables. Since they will be included with the examination, candidates will not be allowed to bring copies of the tables into the examination room.

The CAS will test the candidate's knowledge of topics that are presented in the learning objectives. Thus, the candidate should expect that each exam will cover a large proportion of the learning objectives and associated knowledge statements and syllabus readings, and that all of these will be tested at least once over the course of a few years-but each one may not be covered on each exam.

A guessing adjustment will be used in grading Exam LC. Details are provided under "Guessing Adjustment" in the "Rules-The Examination" section of the CAS Syllabus of Basic Education.

## A. Survival Models

## Range of weight for Section A: 65-70 percent

Candidates should be able to work with discrete and continuous univariate probability distributions for failure time random variables. They will be expected to set up and solve equations in terms of life table functions, cumulative distribution functions, survival functions, probability density functions, and hazard functions (e.g., force of mortality), as appropriate. They should have similar facility with models of the joint distribution of two failure times (multiple lives) and the joint distribution of competing risks (multiple decrement).
Candidates should be able to use Markov Chains in order to determine state probabilities and transition probabilities.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. For discrete and continuous univariate probability distributions for failure time random variables, develop expressions in terms of the life table functions, $\mathrm{l}_{\mathrm{x}}, \mathrm{q}_{\mathrm{x}}, \mathrm{p}_{\mathrm{x}}$, ${ }_{n} q_{x},{ }_{n} p_{x}$, and ${ }_{m \mid n} q_{x}$, for the cumulative distribution function, the survival function, the probability density function and the hazard function (force of mortality), and be able to: <br> - Establish relations between the different functions <br> - Develop expressions, including recursion relations, in terms of the functions for probabilities and moments associated with functions of failure time random variables, and calculate such quantities using simple failure time distributions <br> The distributions may be left-truncated, right-censored, both, or neither. <br> Range of weight: 10-20 percent | a. Failure time random variables <br> b. Life table functions <br> c. Cumulative distribution functions <br> d. Survival functions <br> e. Probability density functions <br> f. Hazard functions <br> g. Relationships between failure time random variables in the functions above |
| READINGS |  |
| Cunningham et al., Chapters 5.1-5.3 and 6.1-6.4 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 2. Assuming a uniform distribution of deaths, define the continuous survival time random variable that arises from the discrete survival time random variable. <br> Range of weight: 5-10 percent | a. Life table function forms under uniform distribution of deaths assumption |
| READINGS |  |
| Cunningham et al., Chapter 6.6 |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 3. Given the joint distribution of two failure times: <br> - Calculate probabilities and moments associated with functions of these random variables' variances. <br> - Characterize the distribution of the smaller failure time (the joint life status) and the larger failure time (the last survivor status) in terms of functions analogous to those in the Learning Objective 1 above, as appropriate. <br> - Develop expressions, including recursion relations, for probabilities and moments of functions of the joint life status and the last survivor status, and express these in terms of the univariate functions in Learning Objective A1 above (assuming independence of the two failure times). <br> Range of weight: 10-20 percent | a. Joint distribution of failure times <br> b. Probabilities and moments |
| READINGS |  |
| Cunningham et al., Chapters 12.1-12.2 and 12.6 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 4. Based on the joint distribution (pdf and cdf) of the time until failure and the cause of failure in the competing risk (multiple decrement) model and in terms of the functions $1_{x}{ }^{(t)},{ }_{t} q_{x}{ }^{(t)},{ }_{t} p_{x}^{(t)},{ }_{t} d_{x}{ }^{(t)}$ : <br> - Establish relations between the functions. <br> - Calculate probabilities and moments associated with functions of these random variables, given the joint distribution of the time of failure and the cause of failure. <br> Note: Candidates will not be tested on the absolute rate of death ( $\mathrm{q}_{\mathrm{x}}{ }^{\prime(1)}$ ) <br> Range of weight: 10-20 percent | a. Time until failure <br> b. Competing risk (multiple decrement) models |
| READINGS |  |
| Cunningham et al., Chapters 13.1-13.3 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 5. For homogenous and non-homogenous | a. Markov chains |
| discrete-time Markov chain models: | b. Transition probability matrix |
| • Define each model. | c. Discrete-time Markov chains |
| - Calculate probabilities of being in a |  |
| $\quad$ particular state at a particular time. |  |
| - Calculate probabilities of transitioning |  |
| $\quad$between states. |  |
| Range of weight: 10-20 percent |  |
| READINGS |  |
| Daniel Markov, Chapters 1 and 3 |  |

## B. Life Contingency Models

Range of weight for Section B: 30-35 percent
$\left.\left.\begin{array}{|l|l|}\hline \text { LEARNING OBJECTIVES } & \text { KNOWLEDGE STATEMENTS } \\ \hline \begin{array}{ll}\text { 1. Apply a principle to a present value model } \\ \text { to associate a cost or pattern of costs } \\ \text { (possibly contingent) with a set of future } \\ \text { contingent cash flows. } \\ \text { Range of weight: 20-25 percent }\end{array} & \begin{array}{l}\text { a. Principles include: equivalence, exponential, } \\ \text { standard deviation, variance, and percentile }\end{array} \\ \text { b. Models including those listed in Learning } \\ \text { Objective A: Survival Models. }\end{array}\right\} \begin{array}{l}\text { c. Principle applications include: life insurance, } \\ \text { annuities, health care, credit risk, environmental } \\ \text { risk, consumer behavior (e.g., subscriptions), and } \\ \text { warranties }\end{array}\right]$

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 2. Using present-value-of-benefit random variables extended to discrete time Markov chains, calculate: <br> - Actuarial present values of cash flows at transitions between states <br> - Actuarial present values of cash flows while in a state <br> - Considerations (premiums) using the Equivalence Principle <br> Range of weight: 5-15 percent | a. Cash flows at transition <br> b. Triple product summation <br> c. Transition probabilities |
| READINGS |  |
| Daniel Markov, Chapters 2 and 3 |  |

## Complete Text References for Exam LC

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning <br> Objectives | Source |
| :--- | :--- | ---: | ---: |
| Cunningham, R.; Herzog, T.; and London, R., Models for <br> Quantifying Risk (Fifth Edition), 2012, ACTEX Publications, <br> Chapters 5.1-5.3, 6.1-6.4, 6.6, 7.1-7.3, 8.1-8.3, 9.1.1-9.1.3, 9.2, | Cunningham <br> et al. | A1-A4, | B1 |
| 9.4, 12.1-12.2, 12.6, and 13.1-13.3. Candidates are not <br> responsible for formulae 6.51 through 6.55 nor are they <br> responsible for the "Hyperbolic (Balducci)" column of Table <br> 6.3. |  |  |  |
| Note: Note: Candidates may use the Fourth Edition in place of <br> the Fifth Edition. Text references for the Fourth Edition are <br> identical to those listed for the Fifth Edition. |  |  |  |
| Daniel, J.W., "Multi-state Transition Models with Actuarial <br> Applications," Study Note, 2004 (second printing with minor <br> corrections, October 2007). | Daniel <br> Markov | A5, B2 | OP |

## Source Key

B Book-may be purchased from the publisher or bookstore or borrowed from the CAS Library.

OP All text references marked as Online Publications will be available on a web page titled Complete Text References.

## Publishers and Distributors for Exam LC

Contact information is furnished for those who wish to purchase the text references cited for Exam LC. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

ACTEX Publications, 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com; Website: www.actexmadriver.com.

Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Website: www.actuarialbookstore.com.

Cunningham, R.; Herzog, T.; and London, R, Models for Quantifying Risk (Fifth Edition), 2012, ACTEX Publications, Inc., 140 Willow Street, Suite One, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; Website: www.actexmadriver.com; e-mail: retail@actexmadriver.com.

Mad River Books (A division of ACTEX Publications), 140 Willow Street, Suite One, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com.

SlideRule Books, P.O. Box 69, Greenland, NH 03840; telephone: (877) 407-5433 or (603) 373-6140; fax: (877) 417-5433 or (603) 430-1258; Website: www.sliderulebooks.com.

# Tables for CAS Exam LC 

## Updated 2013

The following tables will be provided to the candidate with the exam. The tables are reprinted with the permission of the Society of Actuaries.

## Tables of the Normal Distribution



Values of $\mathbf{z}$ for selected values of $\operatorname{Pr}(\mathbf{Z}<\mathbf{z})$

| z | 0.842 | 1.036 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{Pr}(\mathrm{Z}<\mathrm{z})$ | 0.800 | 0.850 | 0.900 | 0.950 | 0.975 | 0.990 | 0.995 |

Illustrative Life Table: Basic Functions and Single Benefit Premiums at $\boldsymbol{i}=0.06$

| $\boldsymbol{x}$ | $I_{x}$ | $1000 q_{x}$ | $\ddot{z}_{\boldsymbol{x}}$ | 1000 $A_{x}$ | $1000\left(2 A_{x}\right)$ | $1000{ }_{5} E_{x}$ | $1000{ }_{10} E_{x}$ | $1000{ }_{20} E_{x}$ | $\boldsymbol{x}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 10,000,000 | 20.42 | 16.8010 | 49.00 | 25.92 | 728.54 | 541.95 | 299.89 | 0 |
| 5 | 9,749,503 | 0.98 | 17.0379 | 35.59 | 8.45 | 743.89 | 553.48 | 305.90 | 5 |
| 10 | 9,705,588 | 0.85 | 16.9119 | 42.72 | 9.37 | 744.04 | 553.34 | 305.24 | 10 |
| 15 | 9,663,731 | 0.91 | 16.7384 | 52.55 | 11.33 | 743.71 | 552.69 | 303.96 | 15 |
| 20 | 9,617,802 | 1.03 | 16.5133 | 65.28 | 14.30 | 743.16 | 551.64 | 301.93 | 20 |
| 21 | 9,607,896 | 1.06 | 16.4611 | 68.24 | 15.06 | 743.01 | 551.36 | 301.40 | 21 |
| 22 | 9,597,695 | 1.10 | 16.4061 | 71.35 | 15.87 | 742.86 | 551.06 | 300.82 | 22 |
| 23 | 9,587,169 | 1.13 | 16.3484 | 74.62 | 16.76 | 742.68 | 550.73 | 300.19 | 23 |
| 24 | 9,576,288 | 1.18 | 16.2878 | 78.05 | 17.71 | 742.49 | 550.36 | 299.49 | 24 |
| 25 | 9,565,017 | 1.22 | 16.2242 | 81.65 | 18.75 | 742.29 | 549.97 | 298.73 | 25 |
| 26 | 9,553,319 | 1.27 | 16.1574 | 85.43 | 19.87 | 742.06 | 549.53 | 297.90 | 26 |
| 27 | 9,541,153 | 1.33 | 16.0873 | 89.40 | 21.07 | 741.81 | 549.05 | 297.00 | 27 |
| 28 | 9,528,475 | 1.39 | 16.0139 | 93.56 | 22.38 | 741.54 | 548.53 | 296.01 | 28 |
| 29 | 9,515,235 | 1.46 | 15.9368 | 97.92 | 23.79 | 741.24 | 547.96 | 294.92 | 29 |
| 30 | 9,501,381 | 1.53 | 15.8561 | 102.48 | 25.31 | 740.91 | 547.33 | 293.74 | 30 |
| 31 | 9,486,854 | 1.61 | 15.7716 | 107.27 | 26.95 | 740.55 | 546.65 | 292.45 | 31 |
| 32 | 9,471,591 | 1.70 | 15.6831 | 112.28 | 28.72 | 740.16 | 545.90 | 291.04 | 32 |
| 33 | 9,455,522 | 1.79 | 15.5906 | 117.51 | 30.63 | 739.72 | 545.07 | 289.50 | 33 |
| 34 | 9,438,571 | 1.90 | 15.4938 | 122.99 | 32.68 | 739.25 | 544.17 | 287.82 | 34 |
| 35 | 9,420,657 | 2.01 | 15.3926 | 128.72 | 34.88 | 738.73 | 543.18 | 286.00 | 35 |
| 36 | 9,401,688 | 2.14 | 15.2870 | 134.70 | 37.26 | 738.16 | 542.11 | 284.00 | 36 |
| 37 | 9,381,566 | 2.28 | 15.1767 | 140.94 | 39.81 | 737.54 | 540.92 | 281.84 | 37 |
| 38 | 9,360,184 | 2.43 | 15.0616 | 147.46 | 42.55 | 736.86 | 539.63 | 279.48 | 38 |
| 39 | 9,337,427 | 2.60 | 14.9416 | 154.25 | 45.48 | 736.11 | 538.22 | 276.92 | 39 |
| 40 | 9,313,166 | 2.78 | 14.8166 | 161.32 | 48.63 | 735.29 | 536.67 | 274.14 | 40 |
| 41 | 9,287,264 | 2.98 | 14.6864 | 168.69 | 52.01 | 734.40 | 534.99 | 271.12 | 41 |
| 42 | 9,259,571 | 3.20 | 14.5510 | 176.36 | 55.62 | 733.42 | 533.14 | 267.85 | 42 |
| 43 | 9,229,925 | 3.44 | 14.4102 | 184.33 | 59.48 | 732.34 | 531.12 | 264.31 | 43 |
| 44 | 9,198,149 | 3.71 | 14.2639 | 192.61 | 63.61 | 731.17 | 528.92 | 260.48 | 44 |
| 45 | 9,164,051 | 4.00 | 14.1121 | 201.20 | 68.02 | 729.88 | 526.52 | 256.34 | 45 |
| 46 | 9,127,426 | 4.31 | 13.9546 | 210.12 | 72.72 | 728.47 | 523.89 | 251.88 | 46 |
| 47 | 9,088,049 | 4.66 | 13.7914 | 219.36 | 77.73 | 726.93 | 521.03 | 247.08 | 47 |
| 48 | 9,045,679 | 5.04 | 13.6224 | 228.92 | 83.06 | 725.24 | 517.91 | 241.93 | 48 |
| 49 | 9,000,057 | 5.46 | 13.4475 | 238.82 | 88.73 | 723.39 | 514.51 | 236.39 | 49 |
| 50 | 8,950,901 | 5.92 | 13.2668 | 249.05 | 94.76 | 721.37 | 510.81 | 230.47 | 50 |
| 51 | 8,897,913 | 6.42 | 13.0803 | 259.61 | 101.15 | 719.17 | 506.78 | 224.15 | 51 |
| 52 | 8,840,770 | 6.97 | 12.8879 | 270.50 | 107.92 | 716.76 | 502.40 | 217.42 | 52 |
| 53 | 8,779,128 | 7.58 | 12.6896 | 281.72 | 115.09 | 714.12 | 497.64 | 210.27 | 53 |
| 54 | 8,712,621 | 8.24 | 12.4856 | 293.27 | 122.67 | 711.24 | 492.47 | 202.70 | 54 |
| 55 | 8,640,861 | 8.96 | 12.2758 | 305.14 | 130.67 | 708.10 | 486.86 | 194.72 | 55 |
| 56 | 8,563,435 | 9.75 | 12.0604 | 317.33 | 139.11 | 704.67 | 480.79 | 186.32 | 56 |
| 57 | 8,479,908 | 10.62 | 11.8395 | 329.84 | 147.99 | 700.93 | 474.22 | 177.53 | 57 |
| 58 | 8,389,826 | 11.58 | 11.6133 | 342.65 | 157.33 | 696.85 | 467.12 | 168.37 | 58 |
| 59 | 8,292,713 | 12.62 | 11.3818 | 355.75 | 167.13 | 692.41 | 459.46 | 158.87 | 59 |
| 60 | 8,188,074 | 13.76 | 11.1454 | 369.13 | 177.41 | 687.56 | 451.20 | 149.06 | 60 |
| 61 | 8,075,403 | 15.01 | 10.9041 | 382.79 | 188.17 | 682.29 | 442.31 | 139.00 | 61 |
| 62 | 7,954,179 | 16.38 | 10.6584 | 396.70 | 199.41 | 676.56 | 432.77 | 128.75 | 62 |
| 63 | 7,823,879 | 17.88 | 10.4084 | 410.85 | 211.13 | 670.33 | 422.54 | 118.38 | 63 |
| 64 | 7,683,979 | 19.52 | 10.1544 | 425.22 | 223.34 | 663.56 | 411.61 | 107.97 | 64 |
| 65 | 7,533,964 | 21.32 | 9.8969 | 439.80 | 236.03 | 656.23 | 399.94 | 97.60 | 65 |

Illustrative Life Table: Basic Functions and Single Benefit Premiums at $\boldsymbol{i}=0.06$

| $\boldsymbol{X}$ | $I_{x}$ | $1000{ }^{1} x$ | $\ddot{a}_{x}$ | 1000 $A_{x}$ | $1000\left({ }^{2} A_{x}\right)$ | $1000{ }_{5} E_{x}$ | $1000{ }_{10} E_{x}$ | $1000{ }_{20} E_{x}$ | $x$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 66 | 7,373,338 | 23.29 | 9.6362 | 454.56 | 249.20 | 648.27 | 387.53 | 87.37 | 66 |
| 67 | 7,201,635 | 25.44 | 9.3726 | 469.47 | 262.83 | 639.66 | 374.36 | 77.38 | 67 |
| 68 | 7,018,432 | 27.79 | 9.1066 | 484.53 | 276.92 | 630.35 | 360.44 | 67.74 | 68 |
| 69 | 6,823,367 | 30.37 | 8.8387 | 499.70 | 291.46 | 620.30 | 345.77 | 58.54 | 69 |
| 70 | 6,616,155 | 33.18 | 8.5693 | 514.95 | 306.42 | 609.46 | 330.37 | 49.88 | 70 |
| 71 | 6,396,609 | 36.26 | 8.2988 | 530.26 | 321.78 | 597.79 | 314.27 | 41.86 | 71 |
| 72 | 6,164,663 | 39.62 | 8.0278 | 545.60 | 337.54 | 585.25 | 297.51 | 34.53 | 72 |
| 73 | 5,920,394 | 43.30 | 7.7568 | 560.93 | 353.64 | 571.81 | 280.17 | 27.96 | 73 |
| 74 | 5,664,051 | 47.31 | 7.4864 | 576.24 | 370.08 | 557.43 | 262.31 | 22.19 | 74 |
| 75 | 5,396,081 | 51.69 | 7.2170 | 591.49 | 386.81 | 542.07 | 244.03 | 17.22 | 75 |
| 76 | 5,117,152 | 56.47 | 6.9493 | 606.65 | 403.80 | 525.71 | 225.46 | 13.04 | 76 |
| 77 | 4,828,182 | 61.68 | 6.6836 | 621.68 | 421.02 | 508.35 | 206.71 | 9.61 | 77 |
| 78 | 4,530,360 | 67.37 | 6.4207 | 636.56 | 438.42 | 489.97 | 187.94 | 6.88 | 78 |
| 79 | 4,225,163 | 73.56 | 6.1610 | 651.26 | 455.95 | 470.57 | 169.31 | 4.77 | 79 |
| 80 | 3,914,365 | 80.30 | 5.9050 | 665.75 | 473.59 | 450.19 | 151.00 | 3.19 | 80 |
| 81 | 3,600,038 | 87.64 | 5.6533 | 680.00 | 491.27 | 428.86 | 133.19 | 2.05 | 81 |
| 82 | 3,284,542 | 95.61 | 5.4063 | 693.98 | 508.96 | 406.62 | 116.06 | 1.27 | 82 |
| 83 | 2,970,496 | 104.28 | 5.1645 | 707.67 | 526.60 | 383.57 | 99.81 | 0.75 | 83 |
| 84 | 2,660,734 | 113.69 | 4.9282 | 721.04 | 544.15 | 359.79 | 84.59 | 0.42 | 84 |
| 85 | 2,358,246 | 123.89 | 4.6980 | 734.07 | 561.57 | 335.40 | 70.56 | 0.22 | 85 |
| 86 | 2,066,090 | 134.94 | 4.4742 | 746.74 | 578.80 | 310.56 | 57.83 | 0.11 | 86 |
| 87 | 1,787,299 | 146.89 | 4.2571 | 759.03 | 595.79 | 285.44 | 46.50 | 0.05 | 87 |
| 88 | 1,524,758 | 159.81 | 4.0470 | 770.92 | 612.51 | 260.21 | 36.61 | 0.02 | 88 |
| 89 | 1,281,083 | 173.75 | 3.8442 | 782.41 | 628.92 | 235.11 | 28.17 | 0.01 | 89 |
| 90 | 1,058,491 | 188.77 | 3.6488 | 793.46 | 644.96 | 210.36 | 21.13 | 0.00 | 90 |
| 91 | 858,676 | 204.93 | 3.4611 | 804.09 | 660.61 | 186.21 | 15.41 | 0.00 | 91 |
| 92 | 682,707 | 222.27 | 3.2812 | 814.27 | 675.83 | 162.90 | 10.91 | 0.00 | 92 |
| 93 | 530,959 | 240.86 | 3.1091 | 824.01 | 690.59 | 140.69 | 7.47 | 0.00 | 93 |
| 94 | 403,072 | 260.73 | 2.9450 | 833.30 | 704.86 | 119.79 | 4.93 | 0.00 | 94 |
| 95 | 297,981 | 281.91 | 2.7888 | 842.14 | 718.61 | 100.43 | 3.13 | 0.00 | 95 |
| 96 | 213,977 | 304.45 | 2.6406 | 850.53 | 731.83 | 82.78 | 1.90 | 0.00 | 96 |
| 97 | 148,832 | 328.34 | 2.5002 | 858.48 | 744.50 | 66.97 | 1.10 | 0.00 | 97 |
| 98 | 99,965 | 353.60 | 2.3676 | 865.99 | 756.60 | 53.09 | 0.60 | 0.00 | 98 |
| 99 | 64,617 | 380.20 | 2.2426 | 873.06 | 768.13 | 41.14 | 0.31 | 0.00 | 99 |
| 100 | 40,049 | 408.12 | 2.1252 | 879.70 | 779.08 | 31.12 | 0.15 | 0.00 | 100 |
| 101 | 23,705 | 437.28 | 2.0152 | 885.93 | 789.44 | 22.91 | 0.07 | 0.00 | 101 |
| 102 | 13,339 | 467.61 | 1.9123 | 891.76 | 799.21 | 16.37 | 0.03 | 0.00 | 102 |
| 103 | 7,101 | 498.99 | 1.8164 | 897.19 | 808.41 | 11.33 | 0.01 | 0.00 | 103 |
| 104 | 3,558 | 531.28 | 1.7273 | 902.23 | 817.02 | 7.56 | 0.00 | 0.00 | 104 |
| 105 | 1,668 | 564.29 | 1.6447 | 906.90 | 825.06 | 4.86 | 0.00 | 0.00 | 105 |
| 106 | 727 | 597.83 | 1.5685 | 911.22 | 832.53 | 2.99 | 0.00 | 0.00 | 106 |
| 107 | 292 | 631.64 | 1.4984 | 915.19 | 839.46 | 1.76 | 0.00 | 0.00 | 107 |
| 108 | 108 | 665.45 | 1.4341 | 918.82 | 845.84 | 0.98 | 0.00 | 0.00 | 108 |
| 109 | 36 | 698.97 | 1.3755 | 922.14 | 851.69 | 0.52 | 0.00 | 0.00 | 109 |
| 110 | 11 | 731.87 | 1.3223 | 925.15 | 857.04 | 0.26 | 0.00 | 0.00 | 110 |

Interest Functions

| Interest Functions at i=0.06 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $m$ | $i^{(m)}$ | $d^{(m)}$ | $i / i^{(m)}$ | $d / d^{(m)}$ | $\alpha(m)$ | $\beta(m)$ |
| 1 | 0.06000 | 0.05660 | 1.00000 | 1.00000 | 1.00000 | 0.00000 |
| 2 | 0.05913 | 0.05743 | 1.01478 | 0.98564 | 1.00021 | 0.25739 |
| 4 | 0.05870 | 0.05785 | 1.02223 | 0.97852 | 1.00027 | 0.38424 |
| 12 | 0.05841 | 0.05813 | 1.02721 | 0.97378 | 1.00028 | 0.46812 |
| $\infty$ | 0.05827 | 0.05827 | 1.02971 | 0.97142 | 1.00028 | 0.50985 |

Special Note: Unless specified, the force of interest is constant in each question .

## Spring and Fall 2015 Exam ST Syllabus Models for Stochastic Processes and Statistics

The syllabus for this two-and-a-half-hour exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as calculating the likelihood ratio test when there is no closed from solution, but that the candidate would still be expected to explain conceptually in the context of an examination.
KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.
Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.

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A thorough knowledge of calculus and probability is assumed, as is familiarity with discounting cash flows. While some problems may have an insurance or risk management theme, no prior knowledge of insurance terminology is expected.
In general, the material covered under the Statistics section covers topics that would be commonly found in a second semester course of a two-semester Probability \& Statistics sequence at the undergraduate level. Coverage of the topics listed under the Statistics section will vary by college and the candidate may need to supplement that course work with additional reading and problem solving work from the suggested textbooks listed at the end of section B.

A variety of tables will be provided to the candidate with the exam. The tables include values for the standard normal distribution, abridged inventories of discrete and continuous probability distributions, Chi-square Distribution, $t$-Distribution, $F$-Distribution as well as the tables required to perform the Signed-Rank test and Mann Whitney tests from the non-parametric section. Since they will be included with the examination, candidates will not be allowed to bring copies of the tables into the examination room.
The CAS will test the candidate's knowledge of topics that are presented in the learning objectives. Thus, the candidate should expect that each exam will cover a large proportion of the learning objectives and associated knowledge statements and syllabus readings, and that all of these will be tested at least once over the course of a few years-but each one may not be covered on each exam

A guessing adjustment will be used in grading Exam ST. Details are provided under "Guessing Adjustment" in the "Rules-The Examination" section.

## A. Stochastic Processes

## Range of weight for Section A: 5-15 percent

Candidates should be able to solve problems using stochastic processes. They should be able to determine the probabilities and distributions associated with these processes. Specifically, candidates should be able to use a Poisson process in these applications.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1. Describe the properties of Poisson | a. Poisson process |
| processes: |  |
| - For increments in the homogeneous case | b. Non-homogeneous Poisson process |
| - For interval times in the homogeneous |  |
| case |  |
| - For increments in the non-homogeneous |  |
| case |  |
| - Resulting from special types of events in |  |
| the Poisson process |  |
| - Resulting from sums of independent |  |
| $\quad$Poisson processes |  |
| Range of weight: 0-5 percent |  |


| 2. For any Poisson process and the inter arrival and waiting distributions associated with the Poisson process, calculate: <br> - Expected values <br> - Variances <br> - Probabilities <br> Range of weight: 0-5 percent | a. Probability calculations for Poisson process |
| :---: | :---: |
| 3. For a compound Poisson process, calculate moments associated with the value of the process at a given time. <br> Range of weight: 0-5 percent | - Compound Poisson process |
| READINGS |  |
| Daniel Poisson |  |

## B. Statistics

## Range of weight for Section B: 85-95 percent

Candidates should have a thorough understanding of the concepts typically covered in the $2^{\text {nd }}$ semester of a two semester undergraduate sequence in Probability and Statistics. The specific topics to be tested are described below.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Perform point estimation of statistical parameters using Maximum likelihood estimation ("MLE"). <br> Apply criteria to the estimates such as: <br> - Consistency <br> - Unbiasedness <br> - Sufficiency <br> - Efficiency <br> - Minimum variance <br> - Mean square error <br> Range of weight: 15-25 percent | a. Equations for MLE of mean, variance from a sample <br> b. Estimation of mean and variance based on sample <br> c. General equations for MLE of parameters <br> d. Recognition of consistency property of estimators and alternative measures of consistency <br> e. Application of criteria for measurement when estimating parameters through minimization of variance, mean square error <br> f. Definition of statistical bias and recognition of estimators that are unbiased or biased <br> g. Application of Rao-Cramer Lower Bound and Efficiency <br> h. Relationship between Sufficiency and Minimum Variance <br> i. Develop and estimate a sufficient statistic for a distribution <br> j. Factorization Criterion for sufficiency <br> k. Application of Rao-Cramer Lower Bound and Fisher Information <br> 1. Application of MVUE for the exponential class of distributions |


| 2. Test statistical hypotheses including Type I and Type II errors using: <br> - Neyman-Pearson lemma <br> - Likelihood ratio tests <br> - First principles <br> Apply Neyman-Pearson lemma to construct likelihood ratio equation. <br> Use critical values from a sampling distribution to test means and variances <br> Range of weight: 15-25 percent | a. Presentation of fundamental inequalities based on general assumptions and normal assumptions <br> b. Definition of Type I and Type II errors <br> c. Significance levels <br> d. One-sided versus two-sided tests <br> e. Estimation of sample sizes under normality to control for Type I and Type II errors <br> f. Determination of critical regions <br> g. Definition and measurement of likelihood ratio tests <br> h. Determining parameters and testing using tabular values <br> i. Recognizing when to apply likelihood ratio tests versus chi-square or other goodness of fit tests <br> j. Apply paired t -test to two samples <br> k. Test for difference in variance under Normal distribution between two samples through application of F-test <br> 1. Test of significance of means from two samples under Normal distribution assumption in both large and small sample cases <br> m . Test for significance of difference in proportions between two samples under Binomial distribution assumption in both large and small sample case <br> n. Application of contingency tables to test independence between effects <br> o. Asymptotic relationship between likelihood ratio tests and the Chi-Square distribution <br> p. Application of Neyman-Pearson lemma to Uniformly Most Powerful hypothesis tests <br> q. Equivalence between critical regions and confidence intervals |
| :---: | :---: |
| 3. Calculate order statistics of a sample for a given distribution and use non parametric statistics to describe a data set. <br> Range of weight $5-15$ percent | a. General form for distribution of $\mathrm{n}^{\text {th }}$ largest element of a set <br> b. Application to a given distributional form <br> c. Calculate Spearman's Rho and Kendall's Tau and understand how those correlation measures differ from the Pearson correlation coefficent <br> d. Apply rank order statistics using Sign-Rank Wilcoxon <br> e. Apply rank order statistics using Sign Test <br> f. Apply rank order statistics using Mann-WhitneyWilcoxon Procedure |
| 4. Test parameters from Normal Models Range of weight $5-15$ percent | a. Calculate student's $t$ test for regression parameter results <br> b. Calculate F test to compare two models (either Regression or ANOVA) <br> c. Calculate student's $t$ test to compare means in ANOVA |

5. Bayesian Statistics parameter estimation for conjugate prior and posterior distributions :

Beta-Binomial
Normal-Normal
Gamma-Poisson
Range of weight 10-20 percent
a. Calculate Bayesian Point Estimates for the three conjugate prior distributions listed on the Learning Objective
b. Calculate Bayesian Interval estimates for the three conjugate prior distributions listed on the Learning Objective

## READINGS

There is no single required text for Section B The texts listed below may be considered as representative of the many texts available to cover the material on which the candidate may be examined based on the learning objectives and knowledge statements. One should note that the Schaum's Outline Series referenced below are not textbooks, but they do provide a fair number of practice problems and examples with worked solutions which may be useful to candidates as a review of past course work.

In the Hints on Study and Exam Techniques for Exam ST we have included a table showing which sections of the texts listed below are good starting points to learn more about topics described in the Knowledge Statements, but any single section in one of the texts cited should not be viewed as the definitive source for problems on Exam ST.

Asimow and Maxwell
Hogg and Tanis
Hogg et al.
Larsen and Marx
Wackerly, Mendenhall, and Scheaffer.
Hsu
Salvatore and Reagle
Spiegel and Stevens
Schiller, Srinivasan, Spiegel

## Complete Text References for Exam ST

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning <br> Objectives | Source |
| :--- | :--- | ---: | ---: |
| Asimow, L.A.; and Maxwell, M.A., Probability and <br> Statistics with Applications: A Problem Solving Text, 2010, <br> ACTEX Publications, Inc. | Asimow and <br> Maxwell | B1-B5 | BO |
| Daniel, J.W., "Poisson processes (and mixture <br> distributions)," Study Note, June 2008. | Daniel <br> Poisson | A1-A3 | OP |
| Hogg, R.V.; McKean, J.W.; and Craig, A.T., Introduction to <br> Mathematical Statistics (Seventh Edition), 2013, Prentice <br> Hall. | Hogg et al. | B1-B5 | BO |
| Hogg, R.V.; and Tanis, E., Probability and Statistical <br> Inference (Eighth Edition), 2010, Prentice Hall. | Hogg and <br> Tanis | B1-B5 | BO |
| Larsen, R.J.; and Marx, M.L., An Introduction to <br> Mathematical Statistics and Its Applications (Fifth Edition), <br> 2012, Pearson Education, Inc. | Larsen and <br> Marx | B1-B5 | BO |


| Wackerly, D.; Mendenhall, W.; and Scheaffer, R., <br> Mathematical Statistics with Applications (7th edition), <br> 2008, Cengage Learning | Wackerly, <br> Mendenhall, <br> and Scheaffer | B1-B5 | BO |
| :--- | :--- | ---: | ---: |
| Hsu, Hewi P., Schaum's Outline of Probability, Random <br> Variables, and Random Processes, Second Edition <br> (Schaum's Outline Series), 2010, McGraw Hill | Hsu | B1 | BO |
| Salvatore, Dominick, and Reagele, Derrick, Schaum's <br> Outline of Statistics and Econometrics, (Second Edition <br> Schaum's Outline Series), 2010, McGraw Hill | Salvatore and <br> Reagle | B2-B4 | BO |
| Spiegel, Murray and Stephens, Larry, Schaum's Outline of <br> Statistics, (Fourth Edition Schaum's Outline Series), 2011, <br> McGraw Hill | Spiegel and <br> Stevens | B1-B4 | BO |
| Schiller, John, Srinivasan, R.,Spiegel, Murray, Schaum's <br> Outline of Probability and Statistics, (Fourth Edition <br> Schaum's Outline Series), 2013, McGraw Hill | Schiller, <br> Srinivasan, <br> Spiegel | B1-B5 | BO |

## Source Key

B Book-may be purchased from the publisher or bookstore or borrowed from the CAS Library.
BO Book (Optional)—may be purchased from the publisher or bookstore.
OP All text references marked as Online Publications will be available on a web page titled Complete Text References.

## Publishers and Distributors for Exam ST

Contact information is furnished for those who wish to purchase the text references cited for Exam ST. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

ACTEX Publications, 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com; Website: www.actexmadriver.com.
Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Website: www.actuarialbookstore.com.

Asimow, L.A.; and Maxwell, M.A., Probability and Statistics with Applications: A Problem Solving Text, 2010, ACTEX Publications, Inc., 140 Willow Street, Suite One, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; website: www.actexmadriver.com;
e-mail: retail@actexmadriver.com.
Hogg, R.V.; Craig, A.T.; and McKean, J.W., Introduction to Mathematical Statistics (Seventh Edition), 2013, Prentice Hall, Inc., 200 Old Tappan Road, Old Tappan, NJ 07675; telephone: (800) 282-0693; Website: www.pearsonhighered.com.
Hogg, R.V.; and Tanis, E., Probability and Statistical Inference (Eighth Edition), 2010, Prentice Hall, Inc., 200 Old Tappan Road, Old Tappan, NJ 07675; telephone: (800) 2820693; Website: www.pearsonhighered.com.
Larsen, R.J.; and Marx, M.L., An Introduction to Mathematical Statistics and Its Applications (Fifth Edition), 2012, Pearson Education, Inc., 200 Old Tappan Road, Old Tappan, NJ 07675; telephone: (800) 282-0693; Website: www.pearsonhighered.com.

Mad River Books (A division of ACTEX Publications), 140 Willow Street, Suite One, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com.

Schaum's Outline Series (A division of McGraw Hill Education), 860 Taylor Station Road. Blacklick, Ohio 43004, telephone: (877) 833-5324,
Website: http://www.mhprofessional.com, Email: pbg.ecommerce_custserv@mcgrawhill.com.

|  |  | Hogg, <br> McKean <br> \& Craig (7th) | Schiller, Srinivasan \& Spiegel | Spiegel \& Stevens | Salvatore \& Reagle |  |  <br> Tannis <br> (8th) | Asimov \& Maxwell | Larsen \& Marx 5th Edition | Wackerly Mendenhal \& Scheafe |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Section | Knowledge Statement | Section | Chapter | Chapter | Chapter | Chapter | Section | Section | Section | Section |
| A. 1 | a. Equations for MLE of mean, variance from a sample | 6.1 | \#N/A | \#N/A | \#N/A | \#N/A | 6.1 | 11.2.2 | 5.1-5.2 | 9.7 |
| A. 1 | b. Estimation of mean and variance based on sample | 2.8 |  | 5, 3,8 | \#N/A | \#N/A | 2.3 | Various | 5.1-5.2 | 8.6-8 |
| A. 1 | c. General equations for MLE of parameters | 4.1, 6.1 | \#N/A | \#N/A | \#N/A |  | 6.1 | 11.2.2 (skip 11.1.1 - method of mo | 5.1-5.2 | 9.7 |
| A. 1 | d. Recognition of consistency property of estimators and alternative measures of consistency | 5.1 | \#N/A | \#N/A |  | 7 | \#N/A | 11.3 | 5.7 | 9.3 |
| A. 1 | e. Application of criteria for measurement when estimating parameters through minimization of variance, mean square error | 7.1 | \#N/A | \#N/A | 6 |  | \#N/A | \#N/A | 5.5 | 8.2 |
| A. 1 | f. Definition of statistical bias and recognition of estimators that are unbiased or biased | 4.1 |  | - 9 | - 6 | - 7 | 6.1 | 11.1 | 5.4 | 8.2 |
| A. 1 | g. Application of Rao-Cramer Lower Bound and Efficiency | 6.2 | -6 | - 9 | \#N/A | \#N/A | 10.7 | 11.3 | 5.5 | 9.5 |
| A. 1 | h. Relationship between Sufficiency and Minimum Variance | 7.3, 7.4 | \#N/A | \#N/A | \#N/A | \#N/A | 10.1 | \#N/A | 5.6 | 9.5 |
| A. 1 | i. Develop and estimate a sufficient statistic for a distribution | 7.2 | \#N/A | \#N/A | \#N/A | \#N/A | 10.1 | \#N/A | 5.6 | 9.4 |
| A. 1 | i. Factorization Criterion for sufficiency | 7.2 | \#N/A | \#N/A | \#N/A | \#N/A | 10.1 | \#N/A | 5.6 | 9.4 |
| A. 1 | k. Application of Rao-Cramer Lower Bound and Fisher Information | 6.2, 6.4 | \#N/A | \#N/A | \#N/A | \#N/A | \#N/A | 11.3 | 5.5 | 9.5 |
| A. 1 | 1. Application of MVUE for the exponential class of distributions |  | \#N/A | \#N/A | \#N/A | \#N/A | 6.1 | 11.3 | 5.2 | 9.8 |
| A. 2 | Presentation of fundamental inequalities based on general assumptions and normal assumptions | 4.5 | ${ }^{7}$ | 10 | 5 |  |  | 10.1 | 6.2 | 10.2 |
| A. 2 | b. Definition of Type I and Type II errors | 4.5, 8.1 |  | 10 | 5 |  | 7.1 | 10.1 | 6.4 | 10.2 |
| A. 2 | c. Significance levels | 4.5, 8.1 |  | 10 | 5 |  | 7.1 | 10.1 | 6.2 | 10.2 |
| A. 2 | d. One-sided versus two-sided tests | 4.6, 6.2 |  | 10 | 5 |  | 7.1 | 10.1 | 6.2 | 10.2 |
| A. 2 | e. Estimation of sample sizes under normality to control for Type I and Type II errors | 4.5 |  | 10 |  |  | 7.2 | 11.4 | 6.4 | 10.2 |
| A. 2 | f. Determination of critical regions | 4.5 |  | 10, 11 | 5 |  | 7.1 | 11.4, 11.5 | 6.2 | 10.2 |
| A. 2 | g. Definition and measurement of likelihood ratio tests | 6.3, 8.1, 8.2, 8.3 |  |  |  |  | 10.4 | 11.4, 11.5 | 6.5 | 10.11 |
| A. 2 | h. Determining parameters and testing using tabular values | 4.5, 4.6 |  | 10 | 5 |  | 7.1-7.4, 10.3-10.4 | 10 - various | Normal 6.2, t 7.4, F 7.3, Af |  |
| A. 2 | i. Recognizing when to apply likelihood ratio tests versus chi-square or other goodness of fit tests | 4.7 |  | 12 | 5 |  | 7.1-7.4. 10.3-10.4 | 10.6 | 10.1, 10.3-10.4 |  |
| A. 2 | i. Apply paired t-test to two samples |  | ? |  | ? | ? | 7.2 | 10.3 | 8.2, 13.3 | 12.3 |
| A. 2 | k. Test for difference in variance under Normal distribution between two samples through application of F -test | 8.3 | 5, 6, 7 | 9,11 |  |  | 7.4 | 10.55 ( skip the rest of 10.5 becaus | 7.1-7.4 | 10.9 |
| A. 2 | 1. Test of significance of means from two samples under Normal distribution assumption in both large and small sample cases | 4.5, 4.6, 5.3 | 5,6,7 | 9, 10, 11 | 5 |  | 7.3 | 10.2 | 7.2 | 10.8 |
| A. 2 | m. Test for significance of difference in proportions between two samples under Binomial distribution assumption in both large and small sample case | 4.5, 4.6, 5.3 | 5,6,7 | 9, 10, 11 | 5 |  | 7.1 | 10.4 | 8.1-8.2, 9.4 | 10.8 |
| A. 2 | n. Application of contingency tables to test independence between effects | 4.7 | 7 | 12 | 5 |  | 8.2 | 10.6 | 10.5 | 14.4 |
| A. 2 | 0. Asymptotic relationship between likelihood ratio tests and the Chi-Square distribution | 6.3,6.5 | \#N/A | \#N/A | \#N/A | \#N/A | 10.4 | \#N/A | 7.3 | \#N/A |
| A. 2 | p. Application of Neyman-Pearson lemma to Uniformly Most Powerful hypothesis tests | 6.4, 8.1 | \#N/A | \#N/A | \#N/A | \#N/A | 10.3 | 11.4 | N/A | 10.1 |
| A. 2 | q. Equivalence between critical regions and confidence intervals | 4.6 | \#N/A | \#N/A | \#N/A | \#N/A | 6.2-6.5, 7.1 | 9.1, 9.2, 9.3, 9.4, 9.5, 9.6, 9.7 | 9.5 | 10.5 |
| A. 3 | a. General form for distribution of ${ }^{\text {th }}$ largest element of a set | 4.4 | \#N/A | \#N/A | \#N/A | \#N/A | 8.3 | 8.1 .5 | 3.10 | 6.7 |
| A. 3 | b. Application to a given distributional form | 4.4 | \#N/A | \#N/A | \#N/A | \#N/A | 8.3 | 8.1.5 | 3.10 | 6.7 |
| A. 3 | c. Calculate Spearman's Rho and Kendall's Tau and understand how those correlation measures differ from the Pearson correlation coefficent | 10.8 | 8, 10 | 17 | \#N/A | \#N/A | NA | \#N/A | N/A | 15.10- |
| A. 3 | d. Apply rank order statistics using Sign-Rank Wilcoxon | 10.3 | 10 | \#N/A |  | \#N/A | 8.5 | \#N/A | 14.3 | 15.3 |
| A. 3 | e. Apply rank order stataistics using Sign Test | 10.2 | \#N/A | 17 | \#N/A | \#N/A | 8.5 | \#N/A | 14.2 | 15.4 |
| A. 3 | f. Apply rank order statistics using Mann-Whitney-Wilcoxon Procedure | 10.4 | 10 | \#N/A | \#N/A | \#N/A | 8.5 | \#N/A | N/A | 15.3 |
| A. 4 | a. Calculate student's test for regression parameter results | \#N/A | \#N/A | \#N/A | \#N/A | \#N/A |  | 11.7, 11.8 | 12.2 | 11.5 |
| A. 4 | b. Calculate F test to compare two models (either Regression or ANOVA) | 9.6 |  | 16 | 5 | \#N/A | 7.5 | 11.7, 11.8 | 12.2 | 13.3 |
| A. 4 | c. Calculate student's test to compare means in ANOVA | \#N/A | $\bigcirc$ | 16 | 5 | \#N/A | 7.3 | \#N/A | 12.2 | 13.3 |
| A. 5 | Calculat Bayesian Point Estimates for the three coniugate prior distributions listed on the Learning Objective | 11.1. 11.2.11.3 | 11 | \#N/A | \#N/A | \#N/A | 9.2 | \#N/A | 5.8 | 16.2 |
| A. 5 | b. Calculate Bayesian Interval estimates for the three conjugate prior distributions listed on the Learning Objective | 111.1, 11.2, 11.3 | 11 | \#N/A | \#N/A | \#N/A | 9.21 | \#N/A | 5.8 | 16.3 |

# Tables for CAS Exam ST 

## Updated 2014

The following tables will be provided to the candidate with the exam. The tables on pages 2 through 14 are reprinted with the permission of the Society of Actuaries; the tables on pages 15 through 19 are copyright material of the Casualty Actuarial Society.

We are furnishing a set of tables for statistical tests as well as a set of distribution functions for Exam ST. We do not have a single authoritative textbook for Statistics. The format of the tables may vary from one textbook to the next. The nomenclature used to describe distribution functions may vary from one textbook to the next. To avoid confusion on the part of the candidates we will use the tables and distribution functions definitions that follow when writing exam questions for Exam ST.

# Tables of the Normal Distribution 

| Probability Content from $-\infty$ to Z |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| 0.0 | 0.5000 | 0.5040 | 0.5080 | 0.5120 | 0.5160 | 0.5199 | 0.5239 | 0.5279 | 0.5319 | 0.5359 |
| 0.1 | 0.5398 | 0.5438 | 0.5478 | 0.5517 | 0.5557 | 0.5596 | 0.5636 | 0.5675 | 0.5714 | 0.5753 |
| 0.2 | 0.5793 | 0.5832 | 0.5871 | 0.5910 | 0.5948 | 0.5987 | 0.6026 | 0.6064 | 0.6103 | 0.6141 |
| 0.3 | 0.6179 | 0.6217 | 0.6255 | 0.6293 | 0.6331 | 0.6368 | 0.6406 | 0.6443 | 0.6480 | 5517 |
| 0.4 | 0.6554 | 0.6591 | 0.6628 | 0.6664 | 0.6700 | 0.6736 | 0.6772 | 0.6808 | 0.6844 | 79 |
| 0.5 | 0.6915 | 0.6950 | 0.6985 | 0.7019 | 0.7054 | 0.7088 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |
| 0.6 | 0.7257 | 0.7291 | 0.7324 | 0.7357 | 0.7389 | 0.7422 | 0.7454 | 0.7486 | 0.7517 | 0.7549 |
| 0.7 | 0.7580 | 0.7611 | 0.7642 | 0.7673 | 0.7704 | 0.7734 | 0.7764 | 0.7794 | 0.7823 | 0.7852 |
| 0.8 | 0.7881 | 0.7910 | 0.7939 | 0.7967 | 0.7995 | 0.8023 | 0.8051 | 0.8078 | 0.8106 | 0.8133 |
| 0.9 | 0.8159 | 0.8186 | 0.8212 | 0.8238 | 0.8264 | 0.8289 | 0.8315 | 0.8340 | 0.8365 | 0.8389 |
| 1.0 | 0.8413 | 0.8438 | 0.8461 | 0.8485 | 0.8508 | 0.8531 | 0.8554 | 0.8577 | 0.8599 | 0.8621 |
| 1.1 | 0.8643 | 0.8665 | 0.8686 | 0.8708 | 0.8729 | 0.8749 | 0.8770 | 0.8790 | 0.8810 | 0.8830 |
| 1.2 | 0.8849 | 0.8869 | 0.8888 | 0.8907 | 0.8925 | 0.8944 | 0.8962 | 0.8980 | 0.8997 | 0.9015 |
| 1.3 | 0.9032 | 0.9049 | 0.9066 | 0.9082 | 0.9099 | 0.9115 | 0.9131 | 0.9147 | 0.9162 | 0.9177 |
| 1.4 | 0.9192 | 0.9207 | 0.9222 | 0.9236 | 0.9251 | 0.9265 | 0.9279 | 0.9292 | 0.9306 | 0.9319 |
| 1.5 | 0.9332 | 0.9345 | 0.9357 | 0.9370 | 0.9382 | 0.9394 | 0.9406 | 0.9418 | 0.9429 | 0.9441 |
| 1.6 | 0.9452 | 0.9463 | 0.9474 | 0.9484 | 0.9495 | 0.9505 | 0.9515 | 0.9525 | 0.9535 | 0.9545 |
| 1.7 | 0.9554 | 0.9564 | 0.9573 | 0.9582 | 0.9591 | 0.9599 | 0.9608 | 0.9616 | 0.9625 | 0.9633 |
| 1.8 | 0.9641 | 0.9649 | 0.9656 | 0.9664 | 0.9671 | 0.9678 | 0.9686 | 0.9693 | 0.9699 | 0.9706 |
| 1.9 | 0.9713 | 0.9719 | 0.9726 | 0.9732 | 0.9738 | 0.9744 | 0.9750 | 0.9756 | 0.9761 | 0.9767 |
| 2.0 | 0.9772 | 0.9778 | 0.9783 | 0.9788 | 0.9793 | 0.9798 | 0.9803 | 0.9808 | 0.9812 | 0.9817 |
| 2.1 | 0.9821 | 0.9826 | 0.9830 | 0.9834 | 0.9838 | 0.9842 | 0.9846 | 0.9850 | 0.9854 | 0.9857 |
| 2.2 | 0.9861 | 0.9864 | 0.9868 | 0.9871 | 0.9875 | 0.9878 | 0.9881 | 0.9884 | 0.9887 | 0.9890 |
| 2.3 | 0.9893 | 0.9896 | 0.9898 | 0.9901 | 0.9904 | 0.9906 | 0.9909 | 0.9911 | 0.9913 | 0.9916 |
| 2. | 0.9918 | 0.9920 | 0.9922 | 0.9925 | 0.9927 | 0.9929 | 0.9931 | 0.9932 | 0.9934 | 0.9936 |
| 2.5 | 0.9938 | 0.9940 | 0.9941 | 0.9943 | 0.9945 | 0.9946 | 0.9948 | 0.9949 | 0.9951 | 0.9952 |
| 2.6 | 0.9953 | 0.9955 | 0.9956 | 0.9957 | 0.9959 | 0.9960 | 0.9961 | 0.9962 | 0.9963 | 0.9964 |
| 2.7 | 0.9965 | 0.9966 | 0.9967 | 0.9968 | 0.9969 | 0.9970 | 0.9971 | 0.9972 | 0.9973 | 0.9974 |
| 2.8 | 0.9974 | 0.9975 | 0.9976 | 0.9977 | 0.9977 | 0.9978 | 0.9979 | 0.9979 | 0.9980 | 0.9981 |
| 2.9 | 0.9981 | 0.9982 | 0.9982 | 0.9983 | 0.9984 | 0.9984 | 0.9985 | 0.9985 | 0.9986 | 0.9986 |
| 3.0 | 0.9987 | 0.9987 | 0.9987 | 0.9988 | 0.998 | 0.9989 | 0.998 | 0.99 | 0.9 | 0.9 |

Values of $\mathbf{z}$ for selected values of $\operatorname{Pr}(\mathrm{Z}<\mathbf{z})$

| Z | 0.842 | 1.036 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{Pr}(\mathrm{Z}<\mathrm{z})$ | 0.800 | 0.850 | 0.900 | 0.950 | 0.975 | 0.990 | 0.995 |

Excerpts from the Appendices to Loss Models: From Data to Decisions, 2nd edition

April 21, 2005

## Appendix A

## An Inventory of Continuous Distributions

## A. 1 Introduction

The incomplete gamma function is given by

$$
\begin{gathered}
\Gamma(\alpha ; x)=\frac{1}{\Gamma(\alpha)} \int_{0}^{x} t^{\alpha-1} e^{-t} d t, \quad \alpha>0, x>0 \\
\text { with } \Gamma(\alpha)=\int_{0}^{\infty} t^{\alpha-1} e^{-t} d t, \quad \alpha>0
\end{gathered}
$$

Also, define

$$
G(\alpha ; x)=\int_{x}^{\infty} t^{\alpha-1} e^{-t} d t, \quad x>0
$$

Integration by parts produces the relationship

$$
G(\alpha ; x)=-\frac{x^{\alpha} e^{-x}}{\alpha}+\frac{1}{\alpha} G(\alpha+1 ; x)
$$

For negative $\alpha$, this can repeated until the first argument is postive, say at $\alpha+k$. Then the incomplete gamma function can be evaluated from

$$
G(\alpha+k ; x)=\Gamma(\alpha+k)[1-\Gamma(\alpha+k ; x)] .
$$

The incomplete beta function is given by

$$
\beta(a, b ; x)=\frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} \int_{0}^{x} t^{a-1}(1-t)^{b-1} d t, \quad a>0, b>0,0<x<1
$$

## A. 2 Transformed beta family

## A.2.3 Three-parameter distributions

A.2.3.1 Generalized Pareto (beta of the second kind) - $\alpha, \theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\Gamma(\alpha+\tau)}{\Gamma(\alpha) \Gamma(\tau)} \frac{\theta^{\alpha} x^{\tau-1}}{(x+\theta)^{\alpha+\tau}} \quad \quad F(x)=\beta(\tau, \alpha ; u), \quad u=\frac{x}{x+\theta} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k) \Gamma(\alpha-k)}{\Gamma(\alpha) \Gamma(\tau)}, \quad-\tau<k<\alpha \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \tau(\tau+1) \cdots(\tau+k-1)}{(\alpha-1) \cdots(\alpha-k)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k) \Gamma(\alpha-k)}{\Gamma(\alpha) \Gamma(\tau)} \beta(\tau+k, \alpha-k ; u)+x^{k}[1-F(x)], \quad k>-\tau \\
\text { mode } & =\theta \frac{\tau-1}{\alpha+1}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

A.2.3.2 Burr (Burr Type XII, Singh-Maddala) - $\alpha, \theta, \gamma$

$$
\begin{aligned}
f(x) & =\frac{\alpha \gamma(x / \theta)^{\gamma}}{x\left[1+(x / \theta)^{\gamma} \alpha^{\alpha+1}\right.} \quad F(x)=1-u^{\alpha}, \quad u=\frac{1}{1+(x / \theta)^{\gamma}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \gamma) \Gamma(\alpha-k / \gamma)}{\Gamma(\alpha)}, \quad-\gamma<k<\alpha \gamma \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \gamma) \Gamma(\alpha-k / \gamma)}{\Gamma(\alpha)} \beta(1+k / \gamma, \alpha-k / \gamma ; 1-u)+x^{k} u^{\alpha}, \quad k>-\gamma \\
\text { mode } & =\theta\left(\frac{\gamma-1}{\alpha \gamma+1}\right)^{1 / \gamma}, \quad \gamma>1, \text { else } 0
\end{aligned}
$$

A.2.3.3 Inverse Burr (Dagum) - $\tau, \theta, \gamma$

$$
\begin{aligned}
f(x) & =\frac{\tau \gamma(x / \theta)^{\gamma \tau}}{x\left[1+(x / \theta)^{\gamma}\right]^{\tau+1}} \quad F(x)=u^{\tau}, \quad u=\frac{(x / \theta)^{\gamma}}{1+(x / \theta)^{\gamma}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \gamma) \Gamma(1-k / \gamma)}{\Gamma(\tau)}, \quad-\tau \gamma<k<\gamma \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \gamma) \Gamma(1-k / \gamma)}{\Gamma(\tau)} \beta(\tau+k / \gamma, 1-k / \gamma ; u)+x^{k}\left[1-u^{\tau}\right], \quad k>-\tau \gamma \\
\text { mode } & =\theta\left(\frac{\tau \gamma-1}{\gamma+1}\right)^{1 / \gamma}, \quad \tau \gamma>1, \text { else } 0
\end{aligned}
$$

## A.2.4 Two-parameter distributions

## A.2.4.1 Pareto- $\alpha, \theta$

$$
\begin{aligned}
f(x) & =\frac{\alpha \theta^{\alpha}}{(x+\theta)^{\alpha+1}} \quad F(x)=1-\left(\frac{\theta}{x+\theta}\right)^{\alpha} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(k+1) \Gamma(\alpha-k)}{\Gamma(\alpha)}, \quad-1<k<\alpha \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} k!}{(\alpha-1) \cdots(\alpha-k)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}[X \wedge x] & =\frac{\theta}{\alpha-1}\left[1-\left(\frac{\theta}{x+\theta}\right)^{\alpha-1}\right], \quad \alpha \neq 1 \\
\mathrm{E}[X \wedge x] & =-\theta \ln \left(\frac{\theta}{x+\theta}\right), \quad \alpha=1 \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(k+1) \Gamma(\alpha-k)}{\Gamma(\alpha)} \beta[k+1, \alpha-k ; x /(x+\theta)]+x^{k}\left(\frac{\theta}{x+\theta}\right)^{\alpha}, \quad \text { all } k \\
\text { mode } & =0
\end{aligned}
$$

## A.2.4.2 Inverse Pareto- $\tau, \theta$

$$
\begin{aligned}
f(x) & =\frac{\tau \theta x^{\tau-1}}{(x+\theta)^{\tau+1}} \quad F(x)=\left(\frac{x}{x+\theta}\right)^{\tau} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k) \Gamma(1-k)}{\Gamma(\tau)}, \quad-\tau<k<1 \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k}(-k)!}{(\tau-1) \cdots(\tau+k)}, \quad \text { if } k \text { is a negative integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \tau \int_{0}^{x /(x+\theta)} y^{\tau+k-1}(1-y)^{-k} d y+x^{k}\left[1-\left(\frac{x}{x+\theta}\right)^{\tau}\right], \quad k>-\tau \\
\text { mode } & =\theta \frac{\tau-1}{2}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

## A.2.4.3 Loglogistic (Fisk)- $\gamma, \theta$

$$
\begin{aligned}
f(x) & =\frac{\gamma(x / \theta)^{\gamma}}{x\left[1+(x / \theta)^{\gamma}\right]^{2}} \quad F(x)=u, \quad u=\frac{(x / \theta)^{\gamma}}{1+(x / \theta)^{\gamma}} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1+k / \gamma) \Gamma(1-k / \gamma), \quad-\gamma<k<\gamma \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(1+k / \gamma) \Gamma(1-k / \gamma) \beta(1+k / \gamma, 1-k / \gamma ; u)+x^{k}(1-u), \quad k>-\gamma \\
\text { mode } & =\theta\left(\frac{\gamma-1}{\gamma+1}\right)^{1 / \gamma}, \quad \gamma>1, \text { else } 0
\end{aligned}
$$

## A.2.4.4 Paralogistic- $\alpha, \theta$

This is a Burr distribution with $\gamma=\alpha$.

$$
\begin{aligned}
f(x) & =\frac{\alpha^{2}(x / \theta)^{\alpha}}{x\left[1+(x / \theta)^{\alpha}\right]^{\alpha+1}} \quad F(x)=1-u^{\alpha}, \quad u=\frac{1}{1+(x / \theta)^{\alpha}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \alpha) \Gamma(\alpha-k / \alpha)}{\Gamma(\alpha)}, \quad-\alpha<k<\alpha^{2} \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \alpha) \Gamma(\alpha-k / \alpha)}{\Gamma(\alpha)} \beta(1+k / \alpha, \alpha-k / \alpha ; 1-u)+x^{k} u^{\alpha}, \quad k>-\alpha \\
\text { mode } & =\theta\left(\frac{\alpha-1}{\alpha^{2}+1}\right)^{1 / \alpha}, \quad \alpha>1, \text { else } 0
\end{aligned}
$$

## A.2.4.5 Inverse paralogistic- $\tau, \theta$

This is an inverse Burr distribution with $\gamma=\tau$.

$$
\begin{aligned}
f(x) & =\frac{\tau^{2}(x / \theta)^{\tau^{2}}}{x\left[1+(x / \theta)^{\tau}\right]^{\tau+1}} \quad F(x)=u^{\tau}, \quad u=\frac{(x / \theta)^{\tau}}{1+(x / \theta)^{\tau}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \tau) \Gamma(1-k / \tau)}{\Gamma(\tau)}, \quad-\tau^{2}<k<\tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \tau) \Gamma(1-k / \tau)}{\Gamma(\tau)} \beta(\tau+k / \tau, 1-k / \tau ; u)+x^{k}\left[1-u^{\tau}\right], \quad k>-\tau^{2} \\
\text { mode } & =\theta(\tau-1)^{1 / \tau}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

## A. 3 Transformed gamma family

## A.3.2 Two-parameter distributions

A.3.2.1 Gamma- $\alpha, \theta$

$$
\begin{aligned}
f(x) & =\frac{(x / \theta)^{\alpha} e^{-x / \theta}}{x \Gamma(\alpha)} \quad F(x)=\Gamma(\alpha ; x / \theta) \\
M(t) & =(1-\theta t)^{-\alpha}, \quad t<1 / \theta \quad \mathrm{E}\left[X^{k}\right]=\frac{\theta^{k} \Gamma(\alpha+k)}{\Gamma(\alpha)}, \quad k>-\alpha \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k}(\alpha+k-1) \cdots \alpha, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\alpha+k)}{\Gamma(\alpha)} \Gamma(\alpha+k ; x / \theta)+x^{k}[1-\Gamma(\alpha ; x / \theta)], \quad k>-\alpha \\
& =\alpha(\alpha+1) \cdots(\alpha+k-1) \theta^{k} \Gamma(\alpha+k ; x / \theta)+x^{k}[1-\Gamma(\alpha ; x / \theta)], \quad k \text { an integer } \\
\text { mode } & =\theta(\alpha-1), \quad \alpha>1, \text { else } 0
\end{aligned}
$$

## A.3.2.2 Inverse gamma (Vinci) - $\alpha, \theta$

$$
\begin{aligned}
f(x) & =\frac{(\theta / x)^{\alpha} e^{-\theta / x}}{x \Gamma(\alpha)} \quad F(x)=1-\Gamma(\alpha ; \theta / x) \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\alpha-k)}{\Gamma(\alpha)}, \quad k<\alpha \quad \mathrm{E}\left[X^{k}\right]=\frac{\theta^{k}}{(\alpha-1) \cdots(\alpha-k)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\alpha-k)}{\Gamma(\alpha)}[1-\Gamma(\alpha-k ; \theta / x)]+x^{k} \Gamma(\alpha ; \theta / x) \\
& =\frac{\theta^{k} \Gamma(\alpha-k)}{\Gamma(\alpha)} G(\alpha-k ; \theta / x)+x^{k} \Gamma(\alpha ; \theta / x), \text { all } k \\
\text { mode } & =\theta /(\alpha+1)
\end{aligned}
$$

## A.3.2.3 Weibull- $\theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\tau(x / \theta)^{\tau} e^{-(x / \theta)^{\tau}}}{x} \quad F(x)=1-e^{-(x / \theta)^{\tau}} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1+k / \tau), \quad k>-\tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(1+k / \tau) \Gamma\left[1+k / \tau ;(x / \theta)^{\tau}\right]+x^{k} e^{-(x / \theta)^{\tau}}, \quad k>-\tau \\
\text { mode } & =\theta\left(\frac{\tau-1}{\tau}\right)^{1 / \tau}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

## A.3.2.4 Inverse Weibull (log Gompertz) - $\theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\tau(\theta / x)^{\tau} e^{-(\theta / x)^{\tau}}}{x} \quad F(x)=e^{-(\theta / x)^{\tau}} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1-k / \tau), \quad k<\tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(1-k / \tau)\left\{1-\Gamma\left[1-k / \tau ;(\theta / x)^{\tau}\right]\right\}+x^{k}\left[1-e^{-(\theta / x)^{\tau}}\right], \quad \text { all } k \\
& =\theta^{k} \Gamma(1-k / \tau) G\left[1-k / \tau ;(\theta / x)^{\tau}\right]+x^{k}\left[1-e^{-(\theta / x)^{\tau}}\right] \\
\text { mode } & =\theta\left(\frac{\tau}{\tau+1}\right)^{1 / \tau}
\end{aligned}
$$

## A.3.3 One-parameter distributions

## A.3.3.1 Exponential- $\theta$

$$
\begin{aligned}
f(x) & =\frac{e^{-x / \theta}}{\theta} \quad F(x)=1-e^{-x / \theta} \\
M(t) & =(1-\theta t)^{-1} \quad \mathrm{E}\left[X^{k}\right]=\theta^{k} \Gamma(k+1), \quad k>-1 \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} k!, \quad \text { if } k \text { is an integer } \\
\mathrm{E}[X \wedge x] & =\theta\left(1-e^{-x / \theta}\right) \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(k+1) \Gamma(k+1 ; x / \theta)+x^{k} e^{-x / \theta}, \quad k>-1 \\
& =\theta^{k} k!\Gamma(k+1 ; x / \theta)+x^{k} e^{-x / \theta}, \quad k \text { an integer } \\
\text { mode } & =0
\end{aligned}
$$

## A.3.3.2 Inverse exponential- $\theta$

$$
\begin{aligned}
f(x) & =\frac{\theta e^{-\theta / x}}{x^{2}} \quad F(x)=e^{-\theta / x} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1-k), \quad k<1 \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} G(1-k ; \theta / x)+x^{k}\left(1-e^{-\theta / x}\right), \quad \text { all } k \\
\text { mode } & =\theta / 2
\end{aligned}
$$

## A. 4 Other distributions

## A.4.1.1 Lognormal- $\mu, \sigma$ ( $\mu$ can be negative)

$$
\begin{aligned}
f(x) & =\frac{1}{x \sigma \sqrt{2 \pi}} \exp \left(-z^{2} / 2\right)=\phi(z) /(\sigma x), \quad z=\frac{\ln x-\mu}{\sigma} \quad F(x)=\Phi(z) \\
\mathrm{E}\left[X^{k}\right] & =\exp \left(k \mu+k^{2} \sigma^{2} / 2\right) \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\exp \left(k \mu+k^{2} \sigma^{2} / 2\right) \Phi\left(\frac{\ln x-\mu-k \sigma^{2}}{\sigma}\right)+x^{k}[1-F(x)] \\
\text { mode } & =\exp \left(\mu-\sigma^{2}\right)
\end{aligned}
$$

## A.4.1.2 Inverse Gaussian- $\mu, \theta$

$$
\begin{aligned}
f(x) & =\left(\frac{\theta}{2 \pi x^{3}}\right)^{1 / 2} \exp \left(-\frac{\theta z^{2}}{2 x}\right), \quad z=\frac{x-\mu}{\mu} \\
F(x) & =\Phi\left[z\left(\frac{\theta}{x}\right)^{1 / 2}\right]+\exp \left(\frac{2 \theta}{\mu}\right) \Phi\left[-y\left(\frac{\theta}{x}\right)^{1 / 2}\right], \quad y=\frac{x+\mu}{\mu} \\
M(t) & =\exp \left[\frac{\theta}{\mu}\left(1-\sqrt{1-\frac{2 t \mu^{2}}{\theta}}\right)\right], \quad t<\frac{\theta}{2 \mu^{2}}, \quad \mathrm{E}[X]=\mu, \quad \operatorname{Var}[X]=\mu^{3} / \theta \\
\mathrm{E}[X \wedge x] & =x-\mu z \Phi\left[z\left(\frac{\theta}{x}\right)^{1 / 2}\right]-\mu y \exp \left(\frac{2 \theta}{\mu}\right) \Phi\left[-y\left(\frac{\theta}{x}\right)^{1 / 2}\right]
\end{aligned}
$$

## A.4.1.3 log-t-r, $\mu, \sigma$ ( $\mu$ can be negative)

Let $Y$ have a $t$ distribution with $r$ degrees of freedom. Then $X=\exp (\sigma Y+\mu)$ has the log- $t$ distribution. Positive moments do not exist for this distribution. Just as the $t$ distribution has a heavier tail than the normal distribution, this distribution has a heavier tail than the lognormal distribution.

$$
\begin{aligned}
& f(x)=\frac{\Gamma\left(\frac{r+1}{2}\right)}{x \sigma \sqrt{\pi r} \Gamma\left(\frac{r}{2}\right)\left[1+\frac{1}{r}\left(\frac{\ln x-\mu}{\sigma}\right)^{2}\right]^{(r+1) / 2}} \\
& F(x)=F_{r}\left(\frac{\ln x-\mu}{\sigma}\right) \text { with } F_{r}(t) \text { the cdf of a } t \text { distribution with } r \text { d.f., }
\end{aligned}
$$

## APPENDIX A. AN INVENTORY OF CONTINUOUS DISTRIBUTIONS

$$
F(x)= \begin{cases}\frac{1}{2} \beta\left[\frac{r}{2}, \frac{1}{2} ; \frac{r}{r+\left(\frac{\ln x-\mu}{\sigma}\right)^{2}}\right], & 0<x \leq e^{\mu}, \\ 1-\frac{1}{2} \beta\left[\frac{r}{2}, \frac{1}{2} ; \frac{r}{r+\left(\frac{\ln x-\mu}{\sigma}\right)^{2}}\right], & x \geq e^{\mu} .\end{cases}
$$

## A.4.1.4 Single-parameter Pareto- $\alpha, \theta$

$$
\begin{array}{rlrl}
f(x) & =\frac{\alpha \theta^{\alpha}}{x^{\alpha+1}}, \quad x>\theta & F(x)=1-(\theta / x)^{\alpha}, \quad x>\theta \\
\mathrm{E}\left[X^{k}\right] & =\frac{\alpha \theta^{k}}{\alpha-k}, \quad k<\alpha & & \mathrm{E}\left[(X \wedge x)^{k}\right]=\frac{\alpha \theta^{k}}{\alpha-k}-\frac{k \theta^{\alpha}}{(\alpha-k) x^{\alpha-k}} \\
\text { mode } & =\theta & &
\end{array}
$$

Note: Although there appears to be two parameters, only $\alpha$ is a true parameter. The value of $\theta$ must be set in advance.

## A. 5 Distributions with finite support

For these two distributions, the scale parameter $\theta$ is assumed known.

## A.5.1.1 Generalized beta- $a, b, \theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} u^{a}(1-u)^{b-1} \frac{\tau}{x}, \quad 0<x<\theta, \quad u=(x / \theta)^{\tau} \\
F(x) & =\beta(a, b ; u) \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(a+b) \Gamma(a+k / \tau)}{\Gamma(a) \Gamma(a+b+k / \tau)}, \quad k>-a \tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(a+b) \Gamma(a+k / \tau)}{\Gamma(a) \Gamma(a+b+k / \tau)} \beta(a+k / \tau, b ; u)+x^{k}[1-\beta(a, b ; u)]
\end{aligned}
$$

A.5.1.2 beta- $a, b, \theta$

$$
\begin{aligned}
f(x)= & \frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} u^{a}(1-u)^{b-1} \frac{1}{x}, \quad 0<x<\theta, \quad u=x / \theta \\
F(x)= & \beta(a, b ; u) \\
\mathrm{E}\left[X^{k}\right]= & \frac{\theta^{k} \Gamma(a+b) \Gamma(a+k)}{\Gamma(a) \Gamma(a+b+k)}, \quad k>-a \\
\mathrm{E}\left[X^{k}\right]= & \frac{\theta^{k} a(a+1) \cdots(a+k-1)}{(a+b)(a+b+1) \cdots(a+b+k-1)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right]= & \frac{\theta^{k} a(a+1) \cdots(a+k-1)}{(a+b)(a+b+1) \cdots(a+b+k-1)} \beta(a+k, b ; u) \\
& +x^{k}[1-\beta(a, b ; u)]
\end{aligned}
$$

## Appendix B

## An Inventory of Discrete Distributions

## B. 2 The ( $a, b, 0$ ) class

B.2.1.1 Poisson- $\lambda$

$$
\begin{array}{rlrlr}
p_{0} & =e^{-\lambda}, \quad a=0, \quad b=\lambda & p_{k}=\frac{e^{-\lambda} \lambda^{k}}{k!} \\
\mathrm{E}[N] & =\lambda, \quad \operatorname{Var}[N]=\lambda & P(z)=e^{\lambda(z-1)}
\end{array}
$$

B.2.1.2 Geometric- $\beta$

$$
\begin{array}{rlrc}
p_{0} & =\frac{1}{1+\beta}, \quad a=\frac{\beta}{1+\beta}, \quad b=0 & p_{k}=\frac{\beta^{k}}{(1+\beta)^{k+1}} \\
\mathrm{E}[N] & =\beta, \quad \operatorname{Var}[N]=\beta(1+\beta) & P(z)=[1-\beta(z-1)]^{-1} .
\end{array}
$$

This is a special case of the negative binomial with $r=1$.
B.2.1.3 Binomial- $q, m,(0<q<1, m$ an integer $)$

$$
\begin{aligned}
p_{0} & =(1-q)^{m}, \quad a=-\frac{q}{1-q}, \quad b=\frac{(m+1) q}{1-q} \\
p_{k} & =\binom{m}{k} q^{k}(1-q)^{m-k}, \quad k=0,1, \ldots, m \\
\mathrm{E}[N] & =m q, \quad \operatorname{Var}[N]=m q(1-q) \quad P(z)=[1+q(z-1)]^{m} .
\end{aligned}
$$

B.2.1.4 Negative binomial- $\beta, r$

$$
\begin{aligned}
p_{0} & =(1+\beta)^{-r}, \quad a=\frac{\beta}{1+\beta}, \quad b=\frac{(r-1) \beta}{1+\beta} \\
p_{k} & =\frac{r(r+1) \cdots(r+k-1) \beta^{k}}{k!(1+\beta)^{r+k}} \\
\mathrm{E}[N] & =r \beta, \quad \operatorname{Var}[N]=r \beta(1+\beta) \quad P(z)=[1-\beta(z-1)]^{-r}
\end{aligned}
$$

Approximate critical values of T in the Wilcoxon Matched-Pairs, Signed-Rank Test

| One-sided | Two-sided | $\mathrm{n}=5$ | $\mathrm{n}=6$ | $\mathrm{n}=7$ | $\mathrm{n}=8$ | $\mathrm{n}=9$ | $\mathrm{n}=10$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 0 | 2 | 3 | 5 | 8 | 10 |
| $P=.025$ | $\mathrm{P}=.05$ |  | 0 | 2 | 3 | 5 | 8 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ |  |  | 0 | 1 | 3 | 5 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ |  |  |  | 0 | 1 | 3 |
| One-sided | Two-sided | $\mathrm{n}=11$ | $\mathrm{n}=12$ | $\mathrm{n}=13$ | $\mathrm{n}=14$ | $\mathrm{n}=15$ | $\mathrm{n}=16$ |
| $\mathrm{P}=.05$ | P = . 10 | 13 | 17 | 21 | 25 | 30 | 35 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 10 | 13 | 17 | 21 | 25 | 29 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 7 | 9 | 12 | 15 | 19 | 23 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 5 | 7 | 9 | 12 | 15 | 19 |
| One-sided | Two-sided | $\mathrm{n}=17$ | $\mathrm{n}=18$ | $\mathrm{n}=19$ | $\mathrm{n}=20$ | $\mathrm{n}=21$ | $\mathrm{n}=22$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 41 | 47 | 53 | 60 | 67 | 75 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 34 | 40 | 46 | 52 | 58 | 65 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 27 | 32 | 37 | 43 | 49 | 55 |
| $P=.005$ | $\mathrm{P}=.01$ | 23 | 27 | 32 | 37 | 42 | 48 |
| One-sided | Two-sided | $\mathrm{n}=23$ | $\mathrm{n}=24$ | $\mathrm{n}=25$ | $\mathrm{n}=26$ | $\mathrm{n}=27$ | $\mathrm{n}=28$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 83 | 91 | 100 | 110 | 119 | 130 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 73 | 81 | 89 | 98 | 107 | 116 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 62 | 69 | 76 | 84 | 92 | 101 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 54 | 61 | 68 | 75 | 83 | 91 |
| One-sided | Two-sided | $\mathrm{n}=29$ | $\mathrm{n}=30$ | $\mathrm{n}=31$ | $\mathrm{n}=32$ | $\mathrm{n}=33$ | $\mathrm{n}=34$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 140 | 151 | 163 | 175 | 187 | 200 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 126 | 137 | 147 | 159 | 170 | 182 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 110 | 120 | 130 | 140 | 151 | 162 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 100 | 109 | 118 | 128 | 138 | 148 |
| One-sided | Two-sided | $\mathrm{n}=35$ | $\mathrm{n}=36$ | $\mathrm{n}=37$ | $\mathrm{n}=38$ | $\mathrm{n}=39$ | $\mathrm{n}=40$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 213 | 227 | 241 | 256 | 271 | 286 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 195 | 208 | 221 | 235 | 249 | 264 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 173 | 185 | 198 | 211 | 224 | 237 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 159 | 171 | 182 | 194 | 207 | 220 |
| One-sided | Two-sided | $\mathrm{n}=41$ | $\mathrm{n}=42$ | $\mathrm{n}=43$ | $\mathrm{n}=44$ | $\mathrm{n}=45$ | $\mathrm{n}=46$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 302 | 319 | 336 | 353 | 371 | 389 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 279 | 294 | 310 | 327 | 343 | 361 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 252 | 266 | 281 | 296 | 312 | 328 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 233 | 247 | 261 | 276 | 291 | 306 |
| One-sided | Two-sided | $\mathrm{n}=47$ | $\mathrm{n}=48$ | $\mathrm{n}=49$ | $\mathrm{n}=50$ |  |  |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 407 | 426 | 446 | 466 |  |  |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 378 | 396 | 415 | 434 |  |  |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 345 | 362 | 379 | 397 |  |  |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 322 | 339 | 355 | 373 |  |  |

For use on the CAS actuarial examinations

Tail areas (two-sided) for t-distributions

|  | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| df |  |  |  |  |  |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 |
| 35 | 1.306 | 1.690 | 2.030 | 2.438 | 2.724 |
| 40 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 |
| 45 | 1.301 | 1.679 | 2.014 | 2.412 | 2.690 |
| 50 | 1.299 | 1.676 | 2.009 | 2.403 | 2.678 |
| 55 | 1.297 | 1.673 | 2.004 | 2.396 | 2.668 |
| 60 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 |
| 70 | 1.294 | 1.667 | 1.994 | 2.381 | 2.648 |
| 80 | 1.292 | 1.664 | 1.990 | 2.374 | 2.639 |
| 90 | 1.291 | 1.662 | 1.987 | 2.368 | 2.632 |
| 100 | 1.290 | 1.660 | 1.984 | 2.364 | 2.626 |
| 120 | 1.289 | 1.658 | 1.980 | 2.358 | 2.617 |
| 400 | 1.284 | 1.649 | 1.966 | 2.336 | 2.588 |
| Inf | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |

[^5]Selected Upper-tail areas for F-distributions

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Numerator df | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 14 | 16 | 20 | 24 | 30 | 40 | 50 | 75 | 100 | 200 | 500 |

df Upper-ta



 | 20.62 | 18.86 | 18.11 | 17.69 | 17.43 | 17.25 | 17.11 | 17.01 | 16.93 | 16.86 | 16.81 | 16.76 | 16.69 | 16.63 | 16.55 | 16.5 | 16.45 | 16.39 | 16.36 | 16.32 | 16.3 | 16.26 | 16.24 | 16.23 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 0.02 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |



```
|2.351
```





| 14.04 | 12.142 | 11.344 | 10.899 | 10.616 | 10.419 | 10.274 | 10.162 | 10.074 | 10.003 | 9.944 | 9.894 | 9.815 | 9.755 | 9.67 | 9.612 | 9.554 | 9.495 | 9.46 | 9.412 | 9.388 | 9.352 | 9.33 | 9.315 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 120 | 0.02 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




| 4.06 | 3.78 | 3.619 | 3.52 | 3.453 | 3.405 | 3.368 | 3.339 | 3.316 | 3.297 | 3.282 | 3.268 | 3.247 | 3.23 | 3.207 | 3.191 | 3.174 | 3.157 | 3.147 | 3.133 | 3.126 | 3.116 | 3.109 | 3.105 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 6.608 | 5.786 | 5.409 | 5.192 | 5.05 | 4.95 | 4.876 | 4.818 | 4.772 | 4.735 | 4.704 | 4.678 | 4.636 | 4.604 | 4.558 | 4.527 | 4.496 | 4.464 | 4.444 | 4.418 | 4.405 | 4.385 | 4.373 | 4.365 |



| 11.323 | 9.454 | 8.67 | 8.233 | 7.953 | 7.758 | 7.614 | 7.503 | 7.415 | 7.344 | 7.285 | 7.235 | 7.156 | 7.095 | 7.009 | 6.951 | 6.893 | 6.833 | 6.797 | 6.749 | 6.724 | 6.687 | 6.665 | 6.65 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 16.258 | 13.274 | 12.06 | 11.392 | 10.967 | 10.672 | 10.456 | 10.289 | 10.158 | 10.051 | 9.963 | 9.888 | 9.77 | 9.68 | 9.553 | 9.466 | 9.379 | 9.291 | 9.238 | 9.166 | 9.13 | 9.075 | 9.042 | 9.02 |


| 2.077 | 2.13 | 2.113 | 2.092 | 2.076 | 2.062 | 2.051 | 2.042 | 2.034 | 2.028 | 2.022 | 2.018 | 2.01 | 2.004 | 1.995 | 1.989 | 1.982 | 1.976 | 1.972 | 1.966 | 1.963 | 1.959 | 1.956 | 1.954 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 3.776 | 3.463 | 3.289 | 3.181 | 3.108 | 3.055 | 3.014 | 2.983 | 2.958 | 2.937 | 2.92 | 2.905 | 2.881 | 2.863 | 2.836 | 2.818 | 2.8 | 2.781 | 2.77 | 2.754 | 2.746 | 2.734 | 2.727 | 2.722 |



| 5.987 | 5.143 | 4.757 | 4.534 | 4.387 | 4.284 | 4.207 | 4.147 | 4.099 | 4.06 | 4.027 | 4 | 3.956 | 3.922 | 3.874 | 3.841 | 3.808 | 3.774 | 3.754 | 3.726 | 3.712 | 3.69 | 3.678 | 3.669 | 0.05 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 9.876 | 8.052 | 7.287 | 6.859 | 6.585 | 6.393 | 6.251 | 6.141 | 6.055 | 5.984 | 5.925 | 5.876 | 5.797 | 5.737 | 5.651 | 5.593 | 5.534 | 5.474 | 5.438 | 5.389 | 5.364 | 5.327 | 5.304 | 5.289 | 0.02 |
| 1.5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




| 3.589 | 3.257 | 3.074 | 2.961 | 2.883 | 2.827 | 2.785 | 2.752 | 2.725 | 2.703 | 2.684 | 2.668 | 2.643 | 2.623 | 2.595 | 2.575 | 2.555 | 2.535 | 2.523 | 2.506 | 2.497 | 2.484 | 2.476 | 2.471 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.591 | 4.737 | 4.347 | 4.12 | 3.972 | 3.866 | 3.787 | 3.726 | 3.677 | 3.637 | 3.603 | 3.575 | 3.529 | 3.494 | 3.445 | 3.41 | 3.376 | 3.34 | 3.319 | 3.29 | 3.275 | 3.252 | 3.239 | 3.23 | 0.05 |






| 3.458 | 3.113 | 2.924 | 2.806 | 2.726 | 2.668 | 2.624 | 2.589 | 2.561 | 2.538 | 2.519 | 2.502 | 2.475 | 2.455 | 2.425 | 2.404 | 2.383 | 2.361 | 2.348 | 2.33 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.318 | 4.459 | 4.066 | 3.338 | 3.687 | 3.581 | 3.5 | 3.438 | 3.388 | 3.347 | 3.313 | 3.284 | 3.237 | 3.202 | 3.15 | 3.115 | 307 | 2.298 | 2.293 |  |
|  | 0.10 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 5.318 | 4.459 | 4.066 | 3.838 | 3.687 | 3.581 | 3.5 | 3.438 | 3.388 | 3.347 | 3.313 | 3.284 | 3.237 | 3.202 | 3.15 | 3.115 | 3.079 | 3.043 | 3.02 | 2.99 | 2.975 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 8.489 | 6.637 | 5.901 | 5.489 | 5.223 | 5.036 | 4.97 | 479 | 4.705 | 4635 | 4.577 | 4.528 | 4.449 | 4.389 | 4.304 | 4.937 | 2.928 | 0.05 |  |  |  |




| 3.36 | 3.006 | 2.813 | 2.693 | 2.611 | 2.551 | 2.505 | 2.469 | 2.44 | 2.416 | 2.396 | 2.379 | 2.351 | 2.329 | 2.298 | 2.277 | 2.255 | 2.232 | 2.218 | 2.199 | 2.189 | 2.174 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.117 | 4.256 | 3.863 | 3.633 | 3.482 | 3.374 | 3.293 | 3.23 | 3.179 | 3.137 | 3.102 | 3.073 | 3.025 | 2.989 | 2.936 | 2.159 | 2.864 | 2.826 | 2.803 | 2.771 | 2.756 | 2.731 |
| . | 2.717 | 2.707 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0.0 .05 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

$\left.\begin{array}{|l|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|}\hline 5.11\end{array}\right)$


| 1.883 | 1.899 | 1.861 | 1.829 | 1.803 | 1.782 | 1.766 | 1.752 | 1.741 | 1.732 | 1.723 | 1.716 | 1.705 | 1.696 | 1.682 | 1.673 | 1.663 | 1.653 | 1.646 | 1.637 | 1.633 | 1.626 | 1.621 | 1.618 | 0.20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.285 | 2.924 | 2.728 | 2.605 | 2.522 | 2.461 | 2.414 | 2.377 | 2.347 | 2.323 | 2.302 | 2.284 | 2.255 | 2.233 | 2.201 | 2.178 | 2.155 | 2.132 | 2.117 | 2.097 | 2.087 | 2.071 | 2.062 | 2.055 | 0.10 |
| 4.965 | 4.103 | 3.708 | 3.478 | 3.326 | 3.217 | 3.135 | 3.072 | 3.02 | 2.978 | 2.943 | 2.913 | 2.865 | 2.828 | 2.774 | 2.737 | 2.7 | 2.661 | 2.637 | 2.605 | 2.588 | 2.563 | 2.548 | 2.538 | 0.05 |
| 7.638 | 5.934 | 5.218 | 4.816 | 4.555 | 4.371 | 4.235 | 4.129 | 4.044 | 3.975 | 3.917 | 3.868 | 3.79 | 3.73 | 3.644 | 3.585 | 3.525 | 3.463 | 3.425 | 3.374 | 3.348 | 3.309 | 3.285 | 3.269 | 0.02 |
| 10.044 | 7.559 | 6.552 | 5.994 | 5.636 | 5.386 | 5.2 | 5.057 | 4.942 | 4.849 | 4.772 | 4.706 | 4.601 | 4.52 | 4.405 | 4.327 | 4.247 | 4.165 | 4.115 | 4.048 | 4.014 | 3.962 | 3.93 | 3.909 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 859 | 1.87 | 1.83 | 796 | 768 | 747 | . 73 | 1.716 | 1.704 | 1.694 | 68 | 1.678 | 1.666 | 1.65 | 1.642 | 1.632 | 62 | 1.61 | 1.60 | 1.594 | 1.58 | 1.58 | 1.57 | 1.57 | 0.20 |
| 3.225 | 2.86 | 2.66 | 2.536 | 2.451 | 2.389 | 2.342 | 2.304 | 2.274 | 2.248 | 2.227 | 2.209 | 2.179 | 2.156 | 2.123 | 2.1 | 2.0 | 2.052 | 2.036 | 2.016 | 2.005 | 1.989 | 1.979 | 1.97 | 0.10 |
| 4.844 | 3.982 | 3.587 | 3.357 | 3.204 | 3.095 | 3.012 | 2.948 | 2.896 | 2.854 | 2.818 | 2.788 | 2.739 | 2.70 | 2.6 | 2.609 | 2.5 | 2.53 | 2.507 | 2.473 | 2.457 | 2.43 | 2.41 | 2.404 | . 05 |
| 7.388 | 5.70 | 4.99 | 4.594 | 336 | 153 | 017 | 912 | 828 | 3.758 | 3.70 | 3.652 | 3.573 | 3.513 | 3.42 | 3.36 | 3.307 | 3.245 | 3.20 | 3.155 | 3.12 | 3.089 | 3.06 | 3.048 | 0.02 |
| 9.646 | 7.206 | 6.21 | 5.66 | 5.316 | 5.06 | 4.886 | 4.744 | 4.632 | 4.539 | 4.462 | 4.397 | 4.293 | 4.213 | 4.09 | 4.021 | 3.941 | 3.8 | 3.8 | 3.742 | 3.70 | 3.65 | 3.62 | 3.60 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.839 | 1.846 | 1.804 | 1.768 | 1.74 | 1.718 | 1.7 | 1.686 | 1.673 | 1.663 | 1.654 | 1.646 | 1.634 | 1.624 | 1.609 | 1.598 | 1.587 | 1.576 | 1.568 | 1.558 | 1.553 | 1.545 | 1.54 | 1.53 | 0.20 |
| 3.177 | 2.807 | 2.606 | 2.48 | 2.394 | 2.331 | 2.283 | 2.245 | 2.214 | 2.188 | 2.166 | 2.147 | 2.117 | 2.094 | 2.06 | 2.036 | 2.011 | 1.986 | 1.97 | 1.949 | 1.938 | 1.921 | 1.911 | 1.904 | 0.10 |
| 4.747 | 3.885 | 3.49 | 3.259 | 3.106 | 2.996 | 2.913 | 2.849 | 2.796 | 2.753 | 2.717 | 2.687 | 2.637 | 2.599 | 2.544 | 2.505 | 2.466 | 2.426 | 2.401 | 2.367 | 2.35 | 2.323 | 2.30 | 2.296 | 0.05 |
| 7.188 | 5.516 | 4.814 | 4.419 | 4.162 | 3.98 | 3.845 | 3.74 | 3.656 | 3.587 | 3.529 | 3.48 | 3.402 | 3.341 | 3.254 | 3.195 | 3.134 | 3.071 | 3.033 | 2.981 | 2.954 | 2.913 | 2.88 | 2.872 | 0.02 |
| 9.33 | 6.927 | 5.953 | 5.412 | 5.064 | 4.821 | 4.64 | 4.499 | 4.388 | 4.296 | 4.22 | 4.155 | 4.052 | 3.972 | 3.858 | 3.78 | 3.701 | 3.61 | 3.56 | 3.501 | 3.46 | 3.414 | 3.38 | 3.36 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.823 | 1.826 | 1.783 | 1.746 | 1.717 | 1.694 | 1.676 | 1.661 | 1.648 | 1.637 | 1.628 | 1.62 | 1.607 | 1.596 | 1.581 | 1.57 | 1.558 | 1.546 | 1.539 | 1.528 | 1.523 | 1.514 | 1.50 | 1.506 | 0.20 |
| 源 | 763 | 2.56 | 434 | 347 | 283 | 234 | 195 | 164 | 138 | 2.116 | 2.097 | 066 | 2.042 | 2.007 | 1.983 | 1.958 | 1.931 | 1.915 | 1.893 | 1.882 | 1.864 | 1.85 | 1.846 | 0.10 |
| , 67 | 806 | 3.411 | 179 | 3.025 | 2.915 | 2.832 | 2.767 | 714 | 2.671 | 2.635 | 2.604 | 2.554 | 2.515 | 2.459 | 2.42 | 2.38 | 2.339 | 2.314 | 2.27 | 2.261 | 2.234 | 2.218 | 2.206 | 0.05 |
| 7.024 | 366 | 669 | 276 | 4.02 | 3.84 | 705 | 3.6 | . 16 | 3.447 | 3.39 | 3.341 | 3.262 | 3.201 | 3.114 | 3.054 | 2.993 | 2.9 | 2.891 | 2.83 | 2.811 | 2.7 | 2.74 | 2.72 | 0.02 |
| 9.074 | 6.701 | 5.73 | 5.205 | 4.862 | 4.6 | 441 | 302 | 191 | 4.1 | 4.02 | 3.96 | 3.857 | 3.778 | 3.6 | 3.5 | 3.50 | 3.42 | 3.37 | 3.30 | 3.27 | 3.21 | 3.18 | 3.16 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.809 | 809 | 1.765 | 1.727 | 1.697 | 674 | 555 | 639 | 626 | 615 | 606 | 1.598 | 1.584 | 1.573 | 1.55 | 1.546 | 1.534 | 1.521 | 1.513 | 1.502 | 1.497 | 1.488 | 1.482 | 1.479 | 0.20 |
| 3.102 | 2.726 | 2.522 | 395 | 2.307 | 2.243 | 193 | 2.154 | 2.122 | 2.095 | . 073 | 2.054 | 2.022 | 1.998 | 1.962 | 1.938 | 1.912 | 1.88 | 1.86 | 1.846 | 1.834 | 1.81 | 1.805 | 1.797 | 0.10 |
| 4.6 | 3.739 | 3.344 | 112 | 2.958 | 2.848 | 2.764 | 2.699 | 2.646 | 2.602 | 2.565 | 2.534 | 2.484 | 2.445 | 2.38 | 2.349 | 2.308 | 2.26 | 2.241 | 2.205 | 2.187 | 2.15 | 2.14 | 2.131 | 0.05 |
| 6.888 | 5.241 | 4.549 | 4.158 | 3.904 | 3.724 | 3.589 | 3.485 | 3.401 | 3.332 | 3.274 | 3.225 | 3.146 | 3.086 | 2.998 | 2.938 | 2.876 | 2.812 | 2.773 | 2.72 | 2.692 | 2.651 | 2.62 | 2.608 | 0.02 |
| 8.862 | 6.515 | 5.564 | 5.035 | 4.695 | 4.456 | 4.278 | 4.14 | 4.03 | 939 | 86 | 3.8 | . 698 | 3.619 | 3.505 | 3.427 | 3.3 | 3.266 | 3.21 | 3.14 | 3.112 | 3.05 | 3.02 | 3.00 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.797 | 1.795 | 1.749 | 1.71 | 1.68 | 1.656 | 1.637 | 1.621 | 1.608 | 1.596 | 1.587 | 1.578 | 1.564 | 1.553 | 1.537 | 1.525 | 1.513 | 1.5 | 1.491 | 1.48 | 1.474 | 1.465 | 1.45 | 1.45 | 0.20 |
| . 73 | , 695 | 2.49 | 2.361 | 2.273 | 2.208 | 2.158 | 119 | 2.086 | 2.059 | 2.037 | . 17 | 1.985 | 961 | 1.924 | 1.899 | 873 | 1.845 | 1.828 | 1.805 | 1.793 | 1.77 | 1.76 | 1.755 | . 10 |
| 4.543 | 3.682 | 3.287 | 3.056 | 2.901 | 2.79 | 2.707 | 2.641 | 2.588 | 2.544 | 2.507 | 2.475 | 2.424 | 2.385 | 2.328 | 288 | 2.247 | 2.204 | 2.178 | 2.14 | 2.123 | 2.09 | 2.078 | 2.06 | 0.0 |
| 6.773 | 5.135 | 4.447 | 4.058 | 3.805 | 3.626 | 3.492 | 3.387 | 3.303 | 3.235 | 3.177 | 3.128 | 3.049 | 2.988 | 2.9 | 2.8 | 2.777 | 2.713 | 2.674 | 2.6 | 2.592 | 2.55 | 2.524 | 2.506 | 0.02 |
| 8.683 | 6.3 | 5.417 | 4.893 | 4.556 | 4.318 | 4.142 | 4.004 | 3.895 | 3.805 | 3.73 | 3.666 | 3.564 | 3.485 | 3.372 | 3.294 | 3.214 | 3.132 | 3.081 | 3.012 | 2.977 | 2.923 | 2.891 | 2.8 | 0.0 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.787 | 1.78 | 1.73 | 1.69 | 1.665 | 1.641 | 1.621 | 1.605 | 1.591 | 1.58 | 1.57 | 1.561 | 1.547 | 1.536 | 1.519 | 1.50 | 1.494 | 1.481 | 1.472 | 1.46 | 1.454 | 1.445 | 1.43 | 1.435 | . 20 |
| 3.048 | 2.66 | 2.4 | 2.333 | 2.244 | 2.178 | 2.128 | 2.088 | 2.055 | 2.028 | 2.005 | 1.985 | 1.953 | 1.928 | 1.891 | 1.866 | 1.839 | 1.811 | 1.793 | 1.769 | 1.757 | 1.7 | 1.726 | 1.718 | 0.10 |
| 4.4 | 3.63 | 3.23 | 3.007 | 852 | 2.741 | 2.657 | 2.591 | 2.538 | 2.494 | 2.456 | 2.425 | 2.373 | 2.333 | 2.2 | 2.235 | 2.194 | 2.151 | 2.12 | 2.08 | 2.06 | 2.03 | 2.02 | 2.01 | 0.05 |
| 6.674 | 5.04 | 4.361 | 3.974 | 3.721 | 543 | 3.409 | 3.304 | 3.221 | 3.152 | 3.094 | 3.045 | 2.966 | 2.905 | 2.817 | 2.756 | 2.693 | 2.628 | 2.589 | 2.534 | 2.506 | 2.463 | 2.43 | 2.419 | 0.02 |
| 8.531 | 6.22 | 5.29 | 4.7 | 4.437 | 4.2 | 4.0 | 3.89 | 3.78 | 3.691 | 3.616 | 3.553 | 3.451 | 3.372 | 3.259 | 3.181 | 3.101 | 3.018 | 2.96 | 2.898 | 2.86 | 2.80 | 2.77 | 2.75 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.778 | 1.772 | 1.724 | 1.684 | 1.652 | 1.628 | 1.608 | 1.591 | 1.577 | 1.566 | 1.555 | 1.547 | 1.532 | 1.52 | 1.503 | 1.491 | 1.478 | 1.464 | 1.455 | 1.443 | 1.437 | 1.427 | 1.421 | 1.416 | 0.20 |
| 3.026 | 2.645 | 2.437 | 2.308 | 2.218 | 2.152 | 2.102 | 2.061 | 2.028 | 2.001 | 1.978 | 1.958 | 1.925 | 1.9 | 1.862 | 1.836 | 1.809 | 1.781 | 1.763 | 1.738 | 1.726 | 1.706 | 1.694 | 1.686 | 0.10 |
| 4.451 | 3.592 | 3.197 | 2.965 | 2.81 | 2.699 | 2.614 | 2.548 | 2.494 | 2.45 | 2.413 | 2.381 | 2.329 | 2.289 | 2.23 | 2.19 | 2.148 | 2.104 | 2.077 | 2.04 | 2.02 | 1.991 | 1.973 | 1.96 | 0.05 |
| 6.589 | 4.968 | 4.28 | 3.901 | 3.649 | 47 | 3.337 | 233 | 149 | 3.0 | 02 | 2.973 | 2.894 | 2.833 | 2.745 | 2.683 | 2.62 | 2.55 | 2.515 | 2.46 | 2.431 | 2.38 | 2.36 | 2.343 | 0.02 |
| 8.4 | 6.11 | 5.185 | 4.669 | 4.336 | 4.102 | 3.927 | 3.791 | 3.682 | 3.593 | 3.519 | 3.455 | 3.353 | 3.275 | 3.162 | 3.084 | 3.003 | 2.92 | 2.869 | 2.8 | . 76 | 2.709 | 2.676 | 2.653 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.77 | 1.762 | 1.713 | 1.673 | 1.641 | 1.616 | 1.596 | 1.579 | 1.565 | 1.553 | 1.543 | 1.534 | 1.519 | 1.507 | 1.489 | 1.477 | 1.463 | 1.449 | 1.44 | 1.428 | 1.421 | 1.411 | 1.404 | 1.4 | 0.20 |
| 3.007 | 2.624 | 2.416 | 2.286 | 2.196 | 2.13 | 2.079 | 2.038 | 2.005 | 1.977 | 1.954 | 1.933 | 1.9 | 1.875 | 1.837 | 1.81 | 1.783 | 1.754 | 1.73 | 1.711 | 1.698 | 1.67 | 1.66 | 1.657 | 0.10 |
| 4.414 | 3.555 | 3.16 | 2.928 | 2.773 | 2.661 | 2.577 | 2.51 | 2.456 | 2.412 | 2.374 | 2.342 | 2.29 | 2.25 | 2.191 | 2.15 | 2.107 | 2.063 | 2.035 | 1.998 | 1.978 | 1.948 | 1.92 | 1.917 | 0.05 |
| 6.515 | 4.9 | 4.221 | 3.837 | 3.586 | 3.408 | 3.275 | 3.171 | 3.087 | 3.018 | 2.96 | 2.911 | 2.832 | 2.77 | 2.682 | 2.62 | 2.557 | 2.491 | 2.45 | 2.395 | 2.366 | 2.322 | 2.29 | 2.277 | 0.02 |
| 8.285 | 6.0 | 5.092 | 4.579 | 4.248 | 4.015 | 3.841 | 3.705 | 3.597 | 3.508 | 3.434 | 3.371 | 3.269 | 3.19 | 3.077 | 2.999 | 2.919 | 2.835 | 2.78 | 2.714 | 2.678 | 2.623 | . 5 | 2.56 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.763 | 1.754 | 1.704 | 1.663 | 1.631 | 1.605 | 1.585 | 1.568 | 1.554 | 1.542 | 1.531 | 1.522 | 1.507 | 1.495 | 1.477 | 1.464 | 1.45 | 1.436 | 1.427 | 1.414 | 1.407 | 1.396 | 1.3 | 1.385 | 0.20 |
| 2.99 | 2.606 | 2.397 | 2.266 | 2.176 | 2.109 | 2.058 | 2.017 | 1.984 | 1.956 | 1.932 | 1.912 | 1.878 | 1.852 | 1.814 | 1.787 | 1.759 | 1.73 | 1.711 | 1.686 | 1.673 | 1.652 | 1.639 | 1.631 | 0.10 |
| 4.381 | 3.522 | 3.127 | 2.895 | 2.74 | 2.628 | 2.544 | 2.477 | 2.423 | 2.378 | 2.34 | 2.308 | 2.256 | 2.215 | 2.155 | 2.114 | 2.071 | 2.026 | 1.999 | 1.96 | 1.94 | 1.91 | 1.89 | 1.878 | 0.05 |
| 6.449 | 4.84 | 4.164 | 3.781 | 3.531 | 3.353 | 3.22 | 3.116 | 3.032 | 2.963 | 2.906 | 2.856 | 2.777 | 2.715 | 2.626 | 2.564 | 2.501 | 2.434 | 2.394 | 2.337 | 2.308 | 2.264 | 2.23 | 2.218 | 0.02 |
| 8.185 | 5.926 | 5.0 | 4.5 | 4.17 | 3.939 | 3.76 | 3.63 | 3.52 | 3.4 | 3.36 | 3.29 | 3.195 | 3.116 | 3.003 | 2.925 | 2.844 | 2.761 | 2.709 | 2.639 | 2.602 | 2.54 | 2.512 | 2.48 | 0.01 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1.757 <br> 2.975 | 1.746 | 1.696 | 1.654 | 1.622 | 1.596 | 1.575 2.04 | 1.558 | 1.544 | 1.531 | 1.521 | 1.512 | 1.496 | 1.484 | 1.466 | 1.452 | 1.439 | 1.424 | 1.414 | 1.401 | 1.394 | 1.383 | 1.377 | 1.372 | 0.20 0.10 |
| 2.975 4.351 | 3.5893 | 2.088 3 | 2.849 | 2.711 | 2.091 | $\begin{array}{r}2.514 \\ \hline\end{array}$ | 1.9497 | 1.965 | 1.9378 | 1.9131 | 1.892 | 1.859 | 1.833 | 1.194 | 1.082 | 1.738 | 1.994 | 1.969 | 1.6927 | 1.907 | 1.829 | 1.8186 | 1.8073 | 0.05 |
| 6.391 | 4.788 | 4.113 | 3.731 | 3.482 | 3.304 | 3.171 | 3.067 | 2.984 | 2.915 | 2.857 | 2.808 | 2.728 | 2.666 | 2.577 | 2.515 | 2.451 | 2.384 | 2.343 | 2.286 | 2.257 | 2.212 | 2.184 | 2.165 | 0.02 |
| 8.096 | 5.849 | 4.938 | 4.431 | 4.103 | 3.871 | 3.699 | 3.564 | 3.457 | 3.368 | 3.294 | 3.231 | 3.13 | 3.051 | 2.938 | 2.859 | 2.778 | 2.695 | 2.643 | 2.572 | 2.535 | 2.479 | 2.445 | 2.421 | 0.0 |0.05

0.020.010.200.05
0.020.100.020.200.100.020.01
0.100.05
0.020.010.020.100.050.02
0.010.20

| 21 | 0.20 | 1.751 | 1.739 | 1.688 | 1.646 | 1.614 | 1.588 | 1.567 | 1.549 | 1.535 | 1.522 | 1.511 | 1.502 | 1.487 | 1.474 | 1.455 | 1.442 | 1.428 | 1.413 | 1.403 | 1.39 | 1.383 | 1.371 | 1.364 | 1.36 | 0.20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 21 | 0.10 | 2.961 | 2.575 | 2.365 | 2.233 | 2.142 | 2.075 | 2.023 | 1.982 | 1.948 | 1.92 | 1.896 | 1.875 | 1.841 | 1.815 | 1.776 | 1.748 | 1.719 | 1.689 | 1.67 | 1.644 | 1.63 | 1.608 | 1.595 | 1.586 |  |
| 21 | 0.05 | 4.325 | 3.467 | 3.072 | 2.84 | 2.685 | 2.573 | 2.488 | 2.42 | 2.366 | 2.321 | 2.283 | 2.25 | 2.197 | 2.156 | 2.096 | 2.054 | 2.01 | 1.965 | 1.936 | 1.897 | 1.876 | 1.845 | 1.825 | 1.812 | . 0 |
| 21 | 0.02 | 6.339 | 4.74 | 4.068 | 3.687 | 3.438 | 3.261 | 3.128 | 3.024 | 2.94 | 2.872 | 2.814 | 2.764 | 2.685 | 2.623 | 2.533 | 2.471 | 2.406 | 2.339 | 2.298 | 2.24 | 2.211 | 2.165 | 2.137 | 2.118 |  |
| 21 | 0.01 | 8.017 | 5.78 | 4.874 | 4.369 | 4.042 | 3.812 | 3.64 | 3.506 | 3.398 | 31 | 3.236 | 3.173 | 3.072 | 2.993 | 2.88 | 2.801 | 2.72 | 2.63 | 2.584 | 2.512 | 2.475 | 2.419 | 2.384 | 2.36 |  |
| 22 | 0.20 | 1.746 | 1.733 | 1.68 | 1.639 | 1.60 | 1.58 | 1.559 | 1.541 | 1.52 | 1.51 | 1.503 | 1.49 | 1.478 | 1.465 | 1.446 | 1.43 | 1.418 | 1.403 | 1.393 | 1.379 | 1.372 | 1.361 | 1.353 | 1.349 |  |
| 22 | 0.10 | 2.94 | 2.56 | 2.35 | . 21 | . 12 | 2.06 | . 00 | 1.967 | 1.933 | 1.904 | 1.88 | 1.859 | 1.825 | 1.798 | .759 | 1.731 | 1.70 | 1.67 | 1.6 | 1.62 | 1.61 | 1.5 | 1.57 | 1.56 | . 10 |
| 22 | 0.05 | 4.301 | 3.44 | 3.049 | 2.81 | 2.661 | .54 | . 46 | . 39 | 34 | 2.297 | . 25 | 2.226 | 2.173 | . 13 | . 07 | 2.02 | 1.98 | 1.93 | 1.90 | 1.86 | 1.84 | 1.81 | 1.79 | 1.783 |  |
| 22 | 0.02 | 6.29 | 4.69 | 4.028 | 3.64 | 3.399 | 3.222 | 3.089 | 2.985 | 2.902 | 2.833 | 2.775 | 2.725 | .64 | . 58 | 2.494 | 2.43 | 2.36 | 2.29 | 2.25 | 2.19 | 2.16 | 2.12 | 2.09 | 2.075 |  |
| 22 | 0.01 | 7.945 | 5.71 | 4.8 | 4.3 | 3.988 | 3.758 | 3.587 | 3.453 | 3.346 | 3.258 | 3.184 | 3.121 | 3.019 | 2.941 | 2.827 | 2.749 | 2.667 | 2.583 | 2.53 | 2.45 | 42 | 2.36 | 2.32 | 2.305 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 23 | 0.20 | 1.741 | 1.728 | 1.676 | 1.633 | 1.599 | 1.573 | 1.552 | 1.534 | 1.519 | 1.506 | 1.495 | 1.486 | 1.47 | 1.457 | 1.438 | 1.424 | 1.41 | 1.394 | 1.384 | 1.3 | 1.36 | 1.351 | 1.343 | 1.338 |  |
| 23 | 0.1 | 2.937 | 2.549 | 2.339 | 2.207 | 2.11 | 2.047 | 1.995 | 1.953 | 1.919 | 1.89 | 1.866 | 1.845 | 1.811 | 1.784 | 1.744 | 1.716 | 1.686 | 1.655 | 1.636 | 1.60 | 1.59 | 1.572 | 1.55 | 1.549 |  |
| 23 | 0.0 | 4.279 | 3.422 | 3.02 | 2.7 | 2.64 | 2.5 | 2.442 | 2.375 | 2.32 | 2.2 | 2.236 | 2.204 | 2.15 | 2.10 | 2.04 | 2.00 | 1.96 | 1.91 | 1.88 | 1.8 | 1.82 | 1.79 | 1.77 | 1.757 | . 0 |
| 23 | 0.0 | 6.2 | 4.6 | 3.9 | 3.6 | 3.3 | 3.18 | 3.05 | 2.95 | 2.867 | 2.7 | 2.74 | 2.69 | 2.61 | 2.54 | 2.45 | 2.39 | 2.3 | 2.26 | 2.2 | 2.16 | 2.13 | 2.08 | 2.05 | 2.037 |  |
| 23 | 0.01 | 7.881 | 5.66 | 4.76 | 4.26 | 3.93 | 3.71 | 3.5 | 3.406 | 3.2 | 3.211 | 3.137 | 3.07 | 2.973 | 2.89 | 2.78 | 2.70 | 2.6 | 2.53 | 2.48 | 2.41 | 2.37 | 2.31 | 2.2 | 2.256 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 24 | 0.20 | 1.737 | 1.722 | 1.67 | 1.627 | 1.593 | 1.567 | 1.545 | 1.527 | 1.512 | 1.499 | 1.488 | 1.479 | 1.463 | 1.45 | 1.43 | 1.416 | 1.401 | 1.385 | 1.375 | 1.361 | 1.353 | 1.341 | 1.334 | 1.329 |  |
| 24 | 0.10 | 2.927 | 2.538 | 2.327 | 2.195 | 2.103 | 2.035 | 1.983 | 1.941 | 1.906 | 1.877 | 1.853 | 1.832 | 1.797 | 1.77 | 1.73 | 1.702 | 1.672 | 1.641 | 1.621 | 1.593 | 1.579 | 1.556 | 1.542 | 1.533 |  |
| 24 | 0.05 | 4.26 | 3.403 | 3.009 | 2.776 | 2.621 | 2.508 | 2.423 | 2.355 | 2.3 | 2.255 | 2.216 | 2.183 | 2.13 | 2.088 | 2.027 | 1.984 | 1.939 | 1.892 | 1.863 | 1.822 | 1.8 | 1.768 | 1.747 | 1.733 |  |
| 24 | 0.02 | 6.211 | 4.625 | 3.958 | 3.579 | 3.331 | 3.155 | 3.022 | 2.919 | 2.835 | 2.766 | 2.708 | 2.658 | 2.578 | 2.516 | 2.426 | 2.363 | 2.297 | 2.229 | 2.187 | 2.128 | 2.097 | 2.05 | 2.021 | 2.001 |  |
| 24 | 0.01 | 7.823 | 5.614 | 4.718 | 4.218 | 3.895 | 3.66 | 3.496 | 3.363 | 3.256 | 3.168 | 3.094 | 3.032 | 2.93 | 2.85 | 2.73 | 2.65 | 2.57 | 2.49 | 2.44 | 2.36 | 2.32 | 2.27 | 2.23 | 2.211 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 25 | 0.20 | 1.733 | 1.718 | 1.665 | 1.622 | 1.588 | 1.561 | 1.539 | 1.521 | 1.506 | 1.493 | 1.482 | 1.472 | 1.456 | 1.443 | 1.423 | 1.409 | 1.394 | 1.378 | 1.367 | 1.35 | 1.345 | 1.333 | 1.325 | 1.32 |  |
| 25 | 0.10 | 2.918 | 2.528 | 2.317 | 2.184 | 2.092 | 2.024 | 1.971 | 1.929 | 1.895 | 1.866 | 1.841 | 1.82 | 1.785 | 1.758 | 1.718 | 1.689 | 1.65 | 1.62 | 1.607 | 1.579 | 1.56 | 1.542 | 1.52 | 1.518 |  |
| 25 | 0.05 | 4.242 | 3.385 | 2.991 | 2.759 | 2.603 | 2.49 | 2.405 | 2.337 | 2.282 | 2.23 | 2.198 | 2.165 | 2.111 | 2.06 | 2.00 | 1.96 | 1.919 | 1.872 | 1.842 | 1.80 | 1.779 | 1.74 | 1.72 | 1.711 |  |
| 25 | 0.02 | 6.176 | 4.593 | 3.928 | 3.549 | 3.302 | 3.126 | 2.993 | 2.89 | 2.806 | 2.737 | 2.67 | 2.629 | 2.549 | 2.48 | 2.39 | 2.33 | 2.26 | 2.19 | 2.156 | 2.09 | 2.06 | 2.01 | 1.98 | 1.96 |  |
| 25 | 0.01 | 7.77 | 5.568 | 4.67 | 4.177 | 3.85 | 3.627 | 3.45 | 3.324 | 3.217 | 3.12 | 3.05 | 2.993 | 2.892 | 2.81 | 2.69 | 2.62 | 2.538 | 2.45 | 2.4 | 2.32 | 2.289 | 2.2 | 2.19 | 2.16 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 26 | 0.20 | 1.729 | 1.713 | 1.66 | 1.617 | 1.583 | 1.556 | 1.534 | 1.516 | 1.5 | 1.487 | 1.476 | 1.466 | 1.45 | 1.437 | 1.417 | 1.402 | 1.387 | 1.371 | 1.36 | 1.345 | 1.337 | 1.325 | 1.317 | 1.312 |  |
| 26 | 0.10 | 2.909 | 2.519 | 2.307 | 2.174 | 2.082 | 2.014 | 1.961 | 1.919 | 1.884 | 1.855 | 1.83 | 1.809 | 1.774 | 1.747 | 1.706 | 1.677 | 1.647 | 1.615 | 1.594 | 1.566 | 1.551 | 1.528 | 1.514 | 1.504 |  |
| 26 | 0.05 | 4.225 | 3.369 | 2.975 | 2.743 | 2.587 | 2.474 | 2.388 | 2.321 | 2.265 | 2.22 | 2.181 | 2.148 | 2.094 | 2.052 | 1.99 | 1.946 | 1.901 | 1.853 | 1.823 | 1.782 | 1.76 | 1.726 | 1.705 | 1.691 |  |
| 26 | 0.02 | 6.144 | 4.564 | 3.9 | 3.522 | 3.275 | 3.099 | 2.967 | 2.863 | 2.78 | 2.711 | 2.652 | 2.603 | 2.523 | 2.46 | 2.369 | 2.306 | 2.24 | 2.171 | 2.128 | 2.068 | 2.037 | 1.989 | 1.959 | 1.939 |  |
|  | 0.01 | 7.721 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

0.02
0.01
0.01

Lower-tail areas for Chi-square distributions

|  | 0.005 | 0.010 | 0.025 | 0.050 | 0.950 | 0.975 | 0.990 | 0.995 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| df |  |  |  |  |  |  |  |  |
| 1 | 0.00 | 0.00 | 0.00 | 0.00 | 3.84 | 5.02 | 6.63 | 7.88 |
| 2 | 0.01 | 0.02 | 0.05 | 0.10 | 5.99 | 7.38 | 9.21 | 10.60 |
| 3 | 0.07 | 0.11 | 0.22 | 0.35 | 7.81 | 9.35 | 11.34 | 12.84 |
| 4 | 0.21 | 0.30 | 0.48 | 0.71 | 9.49 | 11.14 | 13.28 | 14.86 |
| 5 | 0.41 | 0.55 | 0.83 | 1.15 | 11.07 | 12.83 | 15.09 | 16.75 |
| 6 | 0.68 | 0.87 | 1.24 | 1.64 | 12.59 | 14.45 | 16.81 | 18.55 |
| 7 | 0.99 | 1.24 | 1.69 | 2.17 | 14.07 | 16.01 | 18.48 | 20.28 |
| 8 | 1.34 | 1.65 | 2.18 | 2.73 | 15.51 | 17.53 | 20.09 | 21.95 |
| 9 | 1.73 | 2.09 | 2.70 | 3.33 | 16.92 | 19.02 | 21.67 | 23.59 |
| 10 | 2.16 | 2.56 | 3.25 | 3.94 | 18.31 | 20.48 | 23.21 | 25.19 |
| 11 | 2.60 | 3.05 | 3.82 | 4.57 | 19.68 | 21.92 | 24.72 | 26.76 |
| 12 | 3.07 | 3.57 | 4.40 | 5.23 | 21.03 | 23.34 | 26.22 | 28.30 |
| 13 | 3.57 | 4.11 | 5.01 | 5.89 | 22.36 | 24.74 | 27.69 | 29.82 |
| 14 | 4.07 | 4.66 | 5.63 | 6.57 | 23.68 | 26.12 | 29.14 | 31.32 |
| 15 | 4.60 | 5.23 | 6.26 | 7.26 | 25.00 | 27.49 | 30.58 | 32.80 |
| 16 | 5.14 | 5.81 | 6.91 | 7.96 | 26.30 | 28.85 | 32.00 | 34.27 |
| 17 | 5.70 | 6.41 | 7.56 | 8.67 | 27.59 | 30.19 | 33.41 | 35.72 |
| 18 | 6.26 | 7.01 | 8.23 | 9.39 | 28.87 | 31.53 | 34.81 | 37.16 |
| 19 | 6.84 | 7.63 | 8.91 | 10.12 | 30.14 | 32.85 | 36.19 | 38.58 |
| 20 | 7.43 | 8.26 | 9.59 | 10.85 | 31.41 | 34.17 | 37.57 | 40.00 |
| 21 | 8.03 | 8.90 | 10.28 | 11.59 | 32.67 | 35.48 | 38.93 | 41.40 |
| 22 | 8.64 | 9.54 | 10.98 | 12.34 | 33.92 | 36.78 | 40.29 | 42.80 |
| 23 | 9.26 | 10.20 | 11.69 | 13.09 | 35.17 | 38.08 | 41.64 | 44.18 |
| 24 | 9.89 | 10.86 | 12.40 | 13.85 | 36.42 | 39.36 | 42.98 | 45.56 |
| 25 | 10.52 | 11.52 | 13.12 | 14.61 | 37.65 | 40.65 | 44.31 | 46.93 |
| 26 | 11.16 | 12.20 | 13.84 | 15.38 | 38.89 | 41.92 | 45.64 | 48.29 |
| 27 | 11.81 | 12.88 | 14.57 | 16.15 | 40.11 | 43.19 | 46.96 | 49.64 |
| 28 | 12.46 | 13.56 | 15.31 | 16.93 | 41.34 | 44.46 | 48.28 | 50.99 |
| 29 | 13.12 | 14.26 | 16.05 | 17.71 | 42.56 | 45.72 | 49.59 | 52.34 |
| 30 | 13.79 | 14.95 | 16.79 | 18.49 | 43.77 | 46.98 | 50.89 | 53.67 |
| 31 | 14.46 | 15.66 | 17.54 | 19.28 | 44.99 | 48.23 | 52.19 | 55.00 |
| 32 | 15.13 | 16.36 | 18.29 | 20.07 | 46.19 | 49.48 | 53.49 | 56.33 |
| 33 | 15.82 | 17.07 | 19.05 | 20.87 | 47.40 | 50.73 | 54.78 | 57.65 |
| 34 | 16.50 | 17.79 | 19.81 | 21.66 | 48.60 | 51.97 | 56.06 | 58.96 |
| 35 | 17.19 | 18.51 | 20.57 | 22.47 | 49.80 | 53.20 | 57.34 | 60.27 |
| 36 | 17.89 | 19.23 | 21.34 | 23.27 | 51.00 | 54.44 | 58.62 | 61.58 |
| 37 | 18.59 | 19.96 | 22.11 | 24.07 | 52.19 | 55.67 | 59.89 | 62.88 |
| 38 | 19.29 | 20.69 | 22.88 | 24.88 | 53.38 | 56.90 | 61.16 | 64.18 |
| 39 | 20.00 | 21.43 | 23.65 | 25.70 | 54.57 | 58.12 | 62.43 | 65.48 |
| 40 | 20.71 | 22.16 | 24.43 | 26.51 | 55.76 | 59.34 | 63.69 | 66.77 |
| 41 | 21.42 | 22.91 | 25.21 | 27.33 | 56.94 | 60.56 | 64.95 | 68.05 |
| 42 | 22.14 | 23.65 | 26.00 | 28.14 | 58.12 | 61.78 | 66.21 | 69.34 |
| 43 | 22.86 | 24.40 | 26.79 | 28.96 | 59.30 | 62.99 | 67.46 | 70.62 |
| 44 | 23.58 | 25.15 | 27.57 | 29.79 | 60.48 | 64.20 | 68.71 | 71.89 |
| 45 | 24.31 | 25.90 | 28.37 | 30.61 | 61.66 | 65.41 | 69.96 | 73.17 |
| 46 | 25.04 | 26.66 | 29.16 | 31.44 | 62.83 | 66.62 | 71.20 | 74.44 |
| 47 | 25.77 | 27.42 | 29.96 | 32.27 | 64.00 | 67.82 | 72.44 | 75.70 |
| 48 | 26.51 | 28.18 | 30.75 | 33.10 | 65.17 | 69.02 | 73.68 | 76.97 |
| 49 | 27.25 | 28.94 | 31.55 | 33.93 | 66.34 | 70.22 | 74.92 | 78.23 |
| 50 | 27.99 | 29.71 | 32.36 | 34.76 | 67.50 | 71.42 | 76.15 | 79.49 |

For use on the CAS exams

| $\mathrm{n} 2=3$ |  |  |  |  |
| ---: | :---: | ---: | ---: | ---: |
|  |  |  |  |  |
| U0 |  | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ |
|  | 0 | 0.250 | 0.100 | 0.050 |
| 1 | 0.500 | 0.200 | 0.100 |  |
| 2 |  | 0.400 | 0.200 |  |
| 3 |  | 0.600 | 0.350 |  |
|  |  |  |  | 0.500 |

$n 2=4$

U0 |  | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ |
| ---: | :---: | ---: | ---: | ---: |
| 0 | 0.200 | 0.067 | 0.029 | 0.014 |
| 1 | 0.400 | 0.134 | 0.057 | 0.029 |
| 2 | 0.600 | 0.267 | 0.114 | 0.057 |
| 3 |  | 0.400 | 0.200 | 0.100 |
| 4 |  | 0.600 | 0.314 | 0.172 |
| 5 |  |  | 0.428 | 0.243 |
| 6 |  |  | 0.572 | 0.343 |
| 7 |  |  |  | 0.443 |
| 8 |  |  |  | 0.557 |

| $n 2=5$ |  |  |  |  |  | $2=6$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ |
| 0 | 0.167 | 0.048 | 0.018 | 0.008 | 0.004 | 0 | 0.143 | 0.036 | 0.012 | 0.005 | 0.002 | 0.001 |
| 1 | 0.334 | 0.095 | 0.036 | 0.016 | 0.008 | 1 | 0.286 | 0.071 | 0.024 | 0.009 | 0.004 | 0.002 |
| 2 | 0.500 | 0.191 | 0.071 | 0.032 | 0.016 | 2 | 0.429 | 0.143 | 0.048 | 0.019 | 0.009 | 0.004 |
| 3 |  | 0.286 | 0.125 | 0.056 | 0.028 | 3 | 0.571 | 0.214 | 0.083 | 0.033 | 0.015 | 0.008 |
| 4 |  | 0.429 | 0.197 | 0.095 | 0.048 | 4 |  | 0.321 | 0.131 | 0.057 | 0.026 | 0.013 |
| 5 |  | 0.571 | 0.286 | 0.143 | 0.075 | 5 |  | 0.428 | 0.191 | 0.086 | 0.041 | 0.021 |
| 6 |  |  | 0.393 | 0.206 | 0.111 | 6 |  | 0.572 | 0.274 | 0.129 | 0.063 | 0.033 |
| 7 |  |  | 0.500 | 0.278 | 0.155 | 7 |  |  | 0.357 | 0.176 | 0.089 | 0.047 |
| 8 |  |  |  | 0.365 | 0.210 | 8 |  |  | 0.452 | 0.238 | 0.123 | 0.066 |
| 9 |  |  |  | 0.452 | 0.274 | 9 |  |  | 0.548 | 0.305 | 0.164 | 0.090 |
| 10 |  |  |  | 0.548 | 0.345 | 10 |  |  |  | 0.381 | 0.214 | 0.120 |
| 11 |  |  |  |  | 0.421 | 11 |  |  |  | 0.457 | 0.268 | 0.155 |
| 12 |  |  |  |  | 0.500 | 12 |  |  |  | 0.543 | 0.331 | 0.197 |
|  |  |  |  |  |  | 13 |  |  |  |  | 0.396 | 0.242 |
|  |  |  |  |  |  | 14 |  |  |  |  | 0.465 | 0.294 |
|  |  |  |  |  |  | 15 |  |  |  |  | 0.535 | 0.349 |
|  |  |  |  |  |  | 16 |  |  |  |  |  | 0.409 |
|  |  |  |  |  |  | 17 |  |  |  |  |  | 0.469 |
|  |  |  |  |  |  | 18 |  |  |  |  |  | 0.531 |

$\mathrm{n} 2=7$

U0 |  | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ |
| ---: | :--- | ---: | :--- | ---: | ---: | ---: | ---: |
| 0 | 0.125 | 0.028 | 0.008 | 0.003 | 0.001 | 0.001 | 0.000 |
| 1 | 0.250 | 0.056 | 0.017 | 0.006 | 0.003 | 0.001 | 0.001 |
| 2 | 0.375 | 0.111 | 0.033 | 0.012 | 0.005 | 0.002 | 0.001 |
| 3 | 0.500 | 0.167 | 0.058 | 0.021 | 0.009 | 0.004 | 0.002 |
| 4 |  | 0.250 | 0.092 | 0.036 | 0.015 | 0.007 | 0.004 |
| 5 |  | 0.333 | 0.133 | 0.054 | 0.024 | 0.011 | 0.005 |
| 6 |  | 0.444 | 0.192 | 0.082 | 0.037 | 0.018 | 0.009 |
| 7 |  | 0.556 | 0.258 | 0.115 | 0.053 | 0.026 | 0.013 |
| 8 |  |  | 0.333 | 0.158 | 0.074 | 0.037 | 0.019 |
| 9 |  |  | 0.417 | 0.206 | 0.101 | 0.051 | 0.027 |
| 10 |  |  | 0.500 | 0.264 | 0.134 | 0.069 | 0.036 |
| 11 |  |  |  | 0.324 | 0.172 | 0.090 | 0.049 |
| 12 |  |  |  | 0.394 | 0.216 | 0.117 | 0.064 |
| 13 |  |  |  | 0.464 | 0.265 | 0.148 | 0.083 |
| 14 |  |  |  |  | 0.536 | 0.319 | 0.183 |
| 15 |  |  |  |  | 0.378 | 0.223 | 0.133 |
| 16 |  |  |  |  | 0.500 | 0.367 | 0.159 |
| 17 |  |  |  |  |  | 0.365 | 0.191 |
| 18 |  |  |  |  |  | 0.228 |  |
| 19 |  |  |  |  |  | 0.418 | 0.268 |
| 20 |  |  |  |  |  | 0.310 |  |
| 21 |  |  |  |  |  |  | 0.355 |
| 22 |  |  |  |  |  |  | 0.403 |
| 23 |  |  |  |  |  |  |  |
| 24 |  |  |  |  |  |  |  |

| $\mathrm{n} 2=8$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ | $\mathrm{n} 1=8$ |
| 0 | 0.111 | 0.022 | 0.006 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 1 | 0.223 | 0.044 | 0.012 | 0.004 | 0.002 | 0.001 | 0.000 | 0.000 |
| 2 | 0.334 | 0.089 | 0.024 | 0.008 | 0.003 | 0.001 | 0.001 | 0.000 |
| 3 | 0.445 | 0.133 | 0.042 | 0.014 | 0.005 | 0.002 | 0.001 | 0.001 |
| 4 | 0.555 | 0.200 | 0.067 | 0.024 | 0.009 | 0.004 | 0.002 | 0.001 |
| 5 |  | 0.267 | 0.097 | 0.036 | 0.015 | 0.006 | 0.003 | 0.002 |
| 6 |  | 0.355 | 0.139 | 0.054 | 0.023 | 0.010 | 0.005 | 0.002 |
| 7 |  | 0.444 | 0.188 | 0.077 | 0.033 | 0.015 | 0.007 | 0.004 |
| 8 |  | 0.556 | 0.249 | 0.107 | 0.047 | 0.021 | 0.010 | 0.005 |
| 9 |  |  | 0.315 | 0.141 | 0.064 | 0.030 | 0.014 | 0.007 |
| 10 |  |  | 0.388 | 0.184 | 0.086 | 0.041 | 0.020 | 0.011 |
| 11 |  |  | 0.461 | 0.230 | 0.111 | 0.054 | 0.027 | 0.014 |
| 12 |  |  | 0.539 | 0.285 | 0.142 | 0.071 | 0.036 | 0.019 |
| 13 |  |  |  | 0.341 | 0.177 | 0.090 | 0.047 | 0.025 |
| 14 |  |  |  | 0.404 | 0.218 | 0.114 | 0.060 | 0.033 |
| 15 |  |  |  | 0.467 | 0.262 | 0.141 | 0.076 | 0.042 |
| 16 |  |  |  | 0.533 | 0.311 | 0.173 | 0.095 | 0.052 |
| 17 |  |  |  |  | 0.362 | 0.207 | 0.116 | 0.065 |
| 18 |  |  |  |  | 0.416 | 0.245 | 0.140 | 0.080 |
| 19 |  |  |  |  | 0.472 | 0.286 | 0.168 | 0.097 |
| 20 |  |  |  |  | 0.528 | 0.331 | 0.198 | 0.117 |
| 21 |  |  |  |  |  | 0.377 | 0.232 | 0.139 |
| 22 |  |  |  |  |  | 0.426 | 0.268 | 0.164 |
| 23 |  |  |  |  |  | 0.475 | 0.306 | 0.191 |
| 24 |  |  |  |  |  | 0.525 | 0.347 | 0.221 |
| 25 |  |  |  |  |  |  | 0.389 | 0.253 |
| 26 |  |  |  |  |  |  | 0.433 | 0.287 |
| 27 |  |  |  |  |  |  | 0.477 | 0.323 |
| 28 |  |  |  |  |  |  | 0.523 | 0.361 |
| 29 |  |  |  |  |  |  |  | 0.400 |
| 30 |  |  |  |  |  |  |  | 0.440 |
| 31 |  |  |  |  |  |  |  | 0.480 |
| 32 |  |  |  |  |  |  |  | 0.520 |


| $n 2=9$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ | $\mathrm{n} 1=8$ | $\mathrm{n} 1=9$ |
| 0 | 0.100 | 0.018 | 0.004 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 1 | 0.200 | 0.036 | 0.009 | 0.003 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | 0.300 | 0.073 | 0.018 | 0.006 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 3 | 0.400 | 0.109 | 0.032 | 0.010 | 0.004 | 0.001 | 0.001 | 0.000 | 0.000 |
| 4 | 0.500 | 0.164 | 0.050 | 0.017 | 0.006 | 0.002 | 0.001 | 0.001 | 0.000 |
| 5 |  | 0.218 | 0.073 | 0.025 | 0.009 | 0.004 | 0.002 | 0.001 | 0.000 |
| 6 |  | 0.291 | 0.105 | 0.038 | 0.014 | 0.006 | 0.003 | 0.001 | 0.001 |
| 7 |  | 0.364 | 0.141 | 0.053 | 0.021 | 0.009 | 0.004 | 0.002 | 0.001 |
| 8 |  | 0.455 | 0.186 | 0.074 | 0.030 | 0.013 | 0.006 | 0.003 | 0.001 |
| 9 |  | 0.545 | 0.241 | 0.099 | 0.041 | 0.018 | 0.008 | 0.004 | 0.002 |
| 10 |  |  | 0.300 | 0.130 | 0.056 | 0.025 | 0.011 | 0.005 | 0.003 |
| 11 |  |  | 0.364 | 0.165 | 0.073 | 0.033 | 0.016 | 0.008 | 0.004 |
| 12 |  |  | 0.432 | 0.207 | 0.095 | 0.044 | 0.021 | 0.010 | 0.005 |
| 13 |  |  | 0.500 | 0.252 | 0.120 | 0.057 | 0.027 | 0.014 | 0.007 |
| 14 |  |  |  | 0.302 | 0.149 | 0.072 | 0.036 | 0.018 | 0.009 |
| 15 |  |  |  | 0.356 | 0.182 | 0.090 | 0.045 | 0.023 | 0.012 |
| 16 |  |  |  | 0.413 | 0.219 | 0.112 | 0.057 | 0.029 | 0.016 |
| 17 |  |  |  | 0.470 | 0.259 | 0.136 | 0.071 | 0.037 | 0.020 |
| 18 |  |  |  | 0.530 | 0.303 | 0.164 | 0.087 | 0.046 | 0.025 |
| 19 |  |  |  |  | 0.350 | 0.194 | 0.105 | 0.057 | 0.031 |
| 20 |  |  |  |  | 0.399 | 0.228 | 0.126 | 0.069 | 0.039 |
| 21 |  |  |  |  | 0.449 | 0.264 | 0.150 | 0.084 | 0.047 |
| 22 |  |  |  |  | 0.500 | 0.303 | 0.176 | 0.100 | 0.057 |
| 23 |  |  |  |  |  | 0.344 | 0.204 | 0.118 | 0.068 |
| 24 |  |  |  |  |  | 0.388 | 0.235 | 0.138 | 0.081 |
| 25 |  |  |  |  |  | 0.432 | 0.268 | 0.160 | 0.095 |
| 26 |  |  |  |  |  | 0.477 | 0.303 | 0.185 | 0.111 |
| 27 |  |  |  |  |  | 0.523 | 0.340 | 0.211 | 0.129 |
| 28 |  |  |  |  |  |  | 0.379 | 0.240 | 0.149 |
| 29 |  |  |  |  |  |  | 0.419 | 0.270 | 0.170 |
| 30 |  |  |  |  |  |  | 0.459 | 0.303 | 0.193 |
| 31 |  |  |  |  |  |  | 0.500 | 0.336 | 0.218 |
| 32 |  |  |  |  |  |  |  | 0.371 | 0.245 |
| 33 |  |  |  |  |  |  |  | 0.407 | 0.273 |
| 34 |  |  |  |  |  |  |  | 0.444 | 0.302 |
| 35 |  |  |  |  |  |  |  | 0.481 | 0.333 |
| 36 |  |  |  |  |  |  |  | 0.519 | 0.365 |
| 37 |  |  |  |  |  |  |  |  | 0.398 |
| 38 |  |  |  |  |  |  |  |  | 0.431 |
| 39 |  |  |  |  |  |  |  |  | 0.466 |
| 40 |  |  |  |  |  |  |  |  | 0.500 |


| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ | $\mathrm{n} 1=8$ | $\mathrm{n} 1=9$ | $\mathrm{n} 1=10$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.091 | 0.015 | 0.004 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| 1 | 0.182 | 0.030 | 0.007 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | 0.273 | 0.061 | 0.014 | 0.004 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 3 | 0.364 | 0.091 | 0.024 | 0.007 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 4 | 0.455 | 0.137 | 0.038 | 0.012 | 0.004 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 5 | 0.545 | 0.182 | 0.056 | 0.018 | 0.006 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 6 |  | 0.243 | 0.081 | 0.027 | 0.010 | 0.004 | 0.002 | 0.001 | 0.000 | 0.000 |
| 7 |  | 0.303 | 0.108 | 0.038 | 0.014 | 0.005 | 0.002 | 0.001 | 0.001 | 0.000 |
| 8 |  | 0.379 | 0.143 | 0.053 | 0.020 | 0.008 | 0.003 | 0.002 | 0.001 | 0.000 |
| 9 |  | 0.455 | 0.185 | 0.071 | 0.027 | 0.011 | 0.005 | 0.002 | 0.001 | 0.001 |
| 10 |  | 0.545 | 0.234 | 0.094 | 0.037 | 0.016 | 0.007 | 0.003 | 0.002 | 0.001 |
| 11 |  |  | 0.287 | 0.120 | 0.049 | 0.021 | 0.009 | 0.004 | 0.002 | 0.001 |
| 12 |  |  | 0.346 | 0.152 | 0.065 | 0.028 | 0.012 | 0.006 | 0.003 | 0.001 |
| 13 |  |  | 0.405 | 0.187 | 0.082 | 0.036 | 0.017 | 0.008 | 0.004 | 0.002 |
| 14 |  |  | 0.469 | 0.227 | 0.103 | 0.047 | 0.021 | 0.010 | 0.005 | 0.003 |
| 15 |  |  | 0.531 | 0.270 | 0.127 | 0.059 | 0.028 | 0.013 | 0.007 | 0.003 |
| 16 |  |  |  | 0.318 | 0.155 | 0.074 | 0.035 | 0.017 | 0.009 | 0.004 |
| 17 |  |  |  | 0.367 | 0.185 | 0.090 | 0.044 | 0.022 | 0.011 | 0.006 |
| 18 |  |  |  | 0.420 | 0.220 | 0.110 | 0.054 | 0.027 | 0.014 | 0.007 |
| 19 |  |  |  | 0.472 | 0.256 | 0.132 | 0.066 | 0.034 | 0.018 | 0.009 |
| 20 |  |  |  | 0.527 | 0.297 | 0.157 | 0.081 | 0.042 | 0.022 | 0.012 |
| 21 |  |  |  |  | 0.339 | 0.184 | 0.096 | 0.051 | 0.027 | 0.014 |
| 22 |  |  |  |  | 0.384 | 0.214 | 0.115 | 0.061 | 0.033 | 0.018 |
| 23 |  |  |  |  | 0.429 | 0.246 | 0.135 | 0.073 | 0.039 | 0.021 |
| 24 |  |  |  |  | 0.476 | 0.281 | 0.157 | 0.086 | 0.047 | 0.026 |
| 25 |  |  |  |  | 0.524 | 0.318 | 0.182 | 0.102 | 0.056 | 0.031 |
| 26 |  |  |  |  |  | 0.356 | 0.208 | 0.119 | 0.067 | 0.038 |
| 27 |  |  |  |  |  | 0.396 | 0.237 | 0.137 | 0.078 | 0.044 |
| 28 |  |  |  |  |  | 0.438 | 0.268 | 0.158 | 0.091 | 0.052 |
| 29 |  |  |  |  |  | 0.479 | 0.300 | 0.180 | 0.105 | 0.061 |
| 30 |  |  |  |  |  | 0.521 | 0.334 | 0.204 | 0.121 | 0.071 |
| 31 |  |  |  |  |  |  | 0.369 | 0.230 | 0.139 | 0.083 |
| 32 |  |  |  |  |  |  | 0.406 | 0.257 | 0.158 | 0.095 |
| 33 |  |  |  |  |  |  | 0.443 | 0.286 | 0.178 | 0.109 |
| 34 |  |  |  |  |  |  | 0.481 | 0.317 | 0.200 | 0.123 |
| 35 |  |  |  |  |  |  | 0.519 | 0.348 | 0.223 | 0.140 |
| 36 |  |  |  |  |  |  |  | 0.381 | 0.248 | 0.157 |
| 37 |  |  |  |  |  |  |  | 0.414 | 0.274 | 0.176 |
| 38 |  |  |  |  |  |  |  | 0.448 | 0.302 | 0.196 |
| 39 |  |  |  |  |  |  |  | 0.483 | 0.330 | 0.218 |
| 40 |  |  |  |  |  |  |  | 0.517 | 0.360 | 0.241 |
| 41 |  |  |  |  |  |  |  |  | 0.390 | 0.264 |
| 42 |  |  |  |  |  |  |  |  | 0.421 | 0.289 |
| 43 |  |  |  |  |  |  |  |  | 0.452 | 0.315 |
| 44 |  |  |  |  |  |  |  |  | 0.484 | 0.342 |
| 45 |  |  |  |  |  |  |  |  | 0.516 | 0.370 |
| 46 |  |  |  |  |  |  |  |  |  | 0.398 |
| 47 |  |  |  |  |  |  |  |  |  | 0.427 |
| 48 |  |  |  |  |  |  |  |  |  | 0.456 |
| 49 |  |  |  |  |  |  |  |  |  | 0.485 |
| 50 |  |  |  |  |  |  |  |  |  | 0.515 |

# Tables for CAS Exam LC 

## Updated 2013

The following tables will be provided to the candidate with the exam. The tables are reprinted with the permission of the Society of Actuaries.

## Tables of the Normal Distribution



Values of $\mathbf{z}$ for selected values of $\operatorname{Pr}(\mathbf{Z}<\mathbf{z})$

| z | 0.842 | 1.036 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{Pr}(\mathrm{Z}<\mathrm{z})$ | 0.800 | 0.850 | 0.900 | 0.950 | 0.975 | 0.990 | 0.995 |

Illustrative Life Table: Basic Functions and Single Benefit Premiums at $\boldsymbol{i}=0.06$

| $\boldsymbol{x}$ | $I_{x}$ | $1000 q_{x}$ | $\ddot{z}_{\boldsymbol{x}}$ | 1000 $A_{x}$ | $1000\left(2 A_{x}\right)$ | $1000{ }_{5} E_{x}$ | $1000{ }_{10} E_{x}$ | $1000{ }_{20} E_{x}$ | $\boldsymbol{x}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 10,000,000 | 20.42 | 16.8010 | 49.00 | 25.92 | 728.54 | 541.95 | 299.89 | 0 |
| 5 | 9,749,503 | 0.98 | 17.0379 | 35.59 | 8.45 | 743.89 | 553.48 | 305.90 | 5 |
| 10 | 9,705,588 | 0.85 | 16.9119 | 42.72 | 9.37 | 744.04 | 553.34 | 305.24 | 10 |
| 15 | 9,663,731 | 0.91 | 16.7384 | 52.55 | 11.33 | 743.71 | 552.69 | 303.96 | 15 |
| 20 | 9,617,802 | 1.03 | 16.5133 | 65.28 | 14.30 | 743.16 | 551.64 | 301.93 | 20 |
| 21 | 9,607,896 | 1.06 | 16.4611 | 68.24 | 15.06 | 743.01 | 551.36 | 301.40 | 21 |
| 22 | 9,597,695 | 1.10 | 16.4061 | 71.35 | 15.87 | 742.86 | 551.06 | 300.82 | 22 |
| 23 | 9,587,169 | 1.13 | 16.3484 | 74.62 | 16.76 | 742.68 | 550.73 | 300.19 | 23 |
| 24 | 9,576,288 | 1.18 | 16.2878 | 78.05 | 17.71 | 742.49 | 550.36 | 299.49 | 24 |
| 25 | 9,565,017 | 1.22 | 16.2242 | 81.65 | 18.75 | 742.29 | 549.97 | 298.73 | 25 |
| 26 | 9,553,319 | 1.27 | 16.1574 | 85.43 | 19.87 | 742.06 | 549.53 | 297.90 | 26 |
| 27 | 9,541,153 | 1.33 | 16.0873 | 89.40 | 21.07 | 741.81 | 549.05 | 297.00 | 27 |
| 28 | 9,528,475 | 1.39 | 16.0139 | 93.56 | 22.38 | 741.54 | 548.53 | 296.01 | 28 |
| 29 | 9,515,235 | 1.46 | 15.9368 | 97.92 | 23.79 | 741.24 | 547.96 | 294.92 | 29 |
| 30 | 9,501,381 | 1.53 | 15.8561 | 102.48 | 25.31 | 740.91 | 547.33 | 293.74 | 30 |
| 31 | 9,486,854 | 1.61 | 15.7716 | 107.27 | 26.95 | 740.55 | 546.65 | 292.45 | 31 |
| 32 | 9,471,591 | 1.70 | 15.6831 | 112.28 | 28.72 | 740.16 | 545.90 | 291.04 | 32 |
| 33 | 9,455,522 | 1.79 | 15.5906 | 117.51 | 30.63 | 739.72 | 545.07 | 289.50 | 33 |
| 34 | 9,438,571 | 1.90 | 15.4938 | 122.99 | 32.68 | 739.25 | 544.17 | 287.82 | 34 |
| 35 | 9,420,657 | 2.01 | 15.3926 | 128.72 | 34.88 | 738.73 | 543.18 | 286.00 | 35 |
| 36 | 9,401,688 | 2.14 | 15.2870 | 134.70 | 37.26 | 738.16 | 542.11 | 284.00 | 36 |
| 37 | 9,381,566 | 2.28 | 15.1767 | 140.94 | 39.81 | 737.54 | 540.92 | 281.84 | 37 |
| 38 | 9,360,184 | 2.43 | 15.0616 | 147.46 | 42.55 | 736.86 | 539.63 | 279.48 | 38 |
| 39 | 9,337,427 | 2.60 | 14.9416 | 154.25 | 45.48 | 736.11 | 538.22 | 276.92 | 39 |
| 40 | 9,313,166 | 2.78 | 14.8166 | 161.32 | 48.63 | 735.29 | 536.67 | 274.14 | 40 |
| 41 | 9,287,264 | 2.98 | 14.6864 | 168.69 | 52.01 | 734.40 | 534.99 | 271.12 | 41 |
| 42 | 9,259,571 | 3.20 | 14.5510 | 176.36 | 55.62 | 733.42 | 533.14 | 267.85 | 42 |
| 43 | 9,229,925 | 3.44 | 14.4102 | 184.33 | 59.48 | 732.34 | 531.12 | 264.31 | 43 |
| 44 | 9,198,149 | 3.71 | 14.2639 | 192.61 | 63.61 | 731.17 | 528.92 | 260.48 | 44 |
| 45 | 9,164,051 | 4.00 | 14.1121 | 201.20 | 68.02 | 729.88 | 526.52 | 256.34 | 45 |
| 46 | 9,127,426 | 4.31 | 13.9546 | 210.12 | 72.72 | 728.47 | 523.89 | 251.88 | 46 |
| 47 | 9,088,049 | 4.66 | 13.7914 | 219.36 | 77.73 | 726.93 | 521.03 | 247.08 | 47 |
| 48 | 9,045,679 | 5.04 | 13.6224 | 228.92 | 83.06 | 725.24 | 517.91 | 241.93 | 48 |
| 49 | 9,000,057 | 5.46 | 13.4475 | 238.82 | 88.73 | 723.39 | 514.51 | 236.39 | 49 |
| 50 | 8,950,901 | 5.92 | 13.2668 | 249.05 | 94.76 | 721.37 | 510.81 | 230.47 | 50 |
| 51 | 8,897,913 | 6.42 | 13.0803 | 259.61 | 101.15 | 719.17 | 506.78 | 224.15 | 51 |
| 52 | 8,840,770 | 6.97 | 12.8879 | 270.50 | 107.92 | 716.76 | 502.40 | 217.42 | 52 |
| 53 | 8,779,128 | 7.58 | 12.6896 | 281.72 | 115.09 | 714.12 | 497.64 | 210.27 | 53 |
| 54 | 8,712,621 | 8.24 | 12.4856 | 293.27 | 122.67 | 711.24 | 492.47 | 202.70 | 54 |
| 55 | 8,640,861 | 8.96 | 12.2758 | 305.14 | 130.67 | 708.10 | 486.86 | 194.72 | 55 |
| 56 | 8,563,435 | 9.75 | 12.0604 | 317.33 | 139.11 | 704.67 | 480.79 | 186.32 | 56 |
| 57 | 8,479,908 | 10.62 | 11.8395 | 329.84 | 147.99 | 700.93 | 474.22 | 177.53 | 57 |
| 58 | 8,389,826 | 11.58 | 11.6133 | 342.65 | 157.33 | 696.85 | 467.12 | 168.37 | 58 |
| 59 | 8,292,713 | 12.62 | 11.3818 | 355.75 | 167.13 | 692.41 | 459.46 | 158.87 | 59 |
| 60 | 8,188,074 | 13.76 | 11.1454 | 369.13 | 177.41 | 687.56 | 451.20 | 149.06 | 60 |
| 61 | 8,075,403 | 15.01 | 10.9041 | 382.79 | 188.17 | 682.29 | 442.31 | 139.00 | 61 |
| 62 | 7,954,179 | 16.38 | 10.6584 | 396.70 | 199.41 | 676.56 | 432.77 | 128.75 | 62 |
| 63 | 7,823,879 | 17.88 | 10.4084 | 410.85 | 211.13 | 670.33 | 422.54 | 118.38 | 63 |
| 64 | 7,683,979 | 19.52 | 10.1544 | 425.22 | 223.34 | 663.56 | 411.61 | 107.97 | 64 |
| 65 | 7,533,964 | 21.32 | 9.8969 | 439.80 | 236.03 | 656.23 | 399.94 | 97.60 | 65 |

Illustrative Life Table: Basic Functions and Single Benefit Premiums at $\boldsymbol{i}=0.06$

| $\boldsymbol{X}$ | $I_{x}$ | $1000{ }^{1} x$ | $\ddot{a}_{x}$ | 1000 $A_{x}$ | $1000\left({ }^{2} A_{x}\right)$ | $1000{ }_{5} E_{x}$ | $1000{ }_{10} E_{x}$ | $1000{ }_{20} E_{x}$ | $x$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 66 | 7,373,338 | 23.29 | 9.6362 | 454.56 | 249.20 | 648.27 | 387.53 | 87.37 | 66 |
| 67 | 7,201,635 | 25.44 | 9.3726 | 469.47 | 262.83 | 639.66 | 374.36 | 77.38 | 67 |
| 68 | 7,018,432 | 27.79 | 9.1066 | 484.53 | 276.92 | 630.35 | 360.44 | 67.74 | 68 |
| 69 | 6,823,367 | 30.37 | 8.8387 | 499.70 | 291.46 | 620.30 | 345.77 | 58.54 | 69 |
| 70 | 6,616,155 | 33.18 | 8.5693 | 514.95 | 306.42 | 609.46 | 330.37 | 49.88 | 70 |
| 71 | 6,396,609 | 36.26 | 8.2988 | 530.26 | 321.78 | 597.79 | 314.27 | 41.86 | 71 |
| 72 | 6,164,663 | 39.62 | 8.0278 | 545.60 | 337.54 | 585.25 | 297.51 | 34.53 | 72 |
| 73 | 5,920,394 | 43.30 | 7.7568 | 560.93 | 353.64 | 571.81 | 280.17 | 27.96 | 73 |
| 74 | 5,664,051 | 47.31 | 7.4864 | 576.24 | 370.08 | 557.43 | 262.31 | 22.19 | 74 |
| 75 | 5,396,081 | 51.69 | 7.2170 | 591.49 | 386.81 | 542.07 | 244.03 | 17.22 | 75 |
| 76 | 5,117,152 | 56.47 | 6.9493 | 606.65 | 403.80 | 525.71 | 225.46 | 13.04 | 76 |
| 77 | 4,828,182 | 61.68 | 6.6836 | 621.68 | 421.02 | 508.35 | 206.71 | 9.61 | 77 |
| 78 | 4,530,360 | 67.37 | 6.4207 | 636.56 | 438.42 | 489.97 | 187.94 | 6.88 | 78 |
| 79 | 4,225,163 | 73.56 | 6.1610 | 651.26 | 455.95 | 470.57 | 169.31 | 4.77 | 79 |
| 80 | 3,914,365 | 80.30 | 5.9050 | 665.75 | 473.59 | 450.19 | 151.00 | 3.19 | 80 |
| 81 | 3,600,038 | 87.64 | 5.6533 | 680.00 | 491.27 | 428.86 | 133.19 | 2.05 | 81 |
| 82 | 3,284,542 | 95.61 | 5.4063 | 693.98 | 508.96 | 406.62 | 116.06 | 1.27 | 82 |
| 83 | 2,970,496 | 104.28 | 5.1645 | 707.67 | 526.60 | 383.57 | 99.81 | 0.75 | 83 |
| 84 | 2,660,734 | 113.69 | 4.9282 | 721.04 | 544.15 | 359.79 | 84.59 | 0.42 | 84 |
| 85 | 2,358,246 | 123.89 | 4.6980 | 734.07 | 561.57 | 335.40 | 70.56 | 0.22 | 85 |
| 86 | 2,066,090 | 134.94 | 4.4742 | 746.74 | 578.80 | 310.56 | 57.83 | 0.11 | 86 |
| 87 | 1,787,299 | 146.89 | 4.2571 | 759.03 | 595.79 | 285.44 | 46.50 | 0.05 | 87 |
| 88 | 1,524,758 | 159.81 | 4.0470 | 770.92 | 612.51 | 260.21 | 36.61 | 0.02 | 88 |
| 89 | 1,281,083 | 173.75 | 3.8442 | 782.41 | 628.92 | 235.11 | 28.17 | 0.01 | 89 |
| 90 | 1,058,491 | 188.77 | 3.6488 | 793.46 | 644.96 | 210.36 | 21.13 | 0.00 | 90 |
| 91 | 858,676 | 204.93 | 3.4611 | 804.09 | 660.61 | 186.21 | 15.41 | 0.00 | 91 |
| 92 | 682,707 | 222.27 | 3.2812 | 814.27 | 675.83 | 162.90 | 10.91 | 0.00 | 92 |
| 93 | 530,959 | 240.86 | 3.1091 | 824.01 | 690.59 | 140.69 | 7.47 | 0.00 | 93 |
| 94 | 403,072 | 260.73 | 2.9450 | 833.30 | 704.86 | 119.79 | 4.93 | 0.00 | 94 |
| 95 | 297,981 | 281.91 | 2.7888 | 842.14 | 718.61 | 100.43 | 3.13 | 0.00 | 95 |
| 96 | 213,977 | 304.45 | 2.6406 | 850.53 | 731.83 | 82.78 | 1.90 | 0.00 | 96 |
| 97 | 148,832 | 328.34 | 2.5002 | 858.48 | 744.50 | 66.97 | 1.10 | 0.00 | 97 |
| 98 | 99,965 | 353.60 | 2.3676 | 865.99 | 756.60 | 53.09 | 0.60 | 0.00 | 98 |
| 99 | 64,617 | 380.20 | 2.2426 | 873.06 | 768.13 | 41.14 | 0.31 | 0.00 | 99 |
| 100 | 40,049 | 408.12 | 2.1252 | 879.70 | 779.08 | 31.12 | 0.15 | 0.00 | 100 |
| 101 | 23,705 | 437.28 | 2.0152 | 885.93 | 789.44 | 22.91 | 0.07 | 0.00 | 101 |
| 102 | 13,339 | 467.61 | 1.9123 | 891.76 | 799.21 | 16.37 | 0.03 | 0.00 | 102 |
| 103 | 7,101 | 498.99 | 1.8164 | 897.19 | 808.41 | 11.33 | 0.01 | 0.00 | 103 |
| 104 | 3,558 | 531.28 | 1.7273 | 902.23 | 817.02 | 7.56 | 0.00 | 0.00 | 104 |
| 105 | 1,668 | 564.29 | 1.6447 | 906.90 | 825.06 | 4.86 | 0.00 | 0.00 | 105 |
| 106 | 727 | 597.83 | 1.5685 | 911.22 | 832.53 | 2.99 | 0.00 | 0.00 | 106 |
| 107 | 292 | 631.64 | 1.4984 | 915.19 | 839.46 | 1.76 | 0.00 | 0.00 | 107 |
| 108 | 108 | 665.45 | 1.4341 | 918.82 | 845.84 | 0.98 | 0.00 | 0.00 | 108 |
| 109 | 36 | 698.97 | 1.3755 | 922.14 | 851.69 | 0.52 | 0.00 | 0.00 | 109 |
| 110 | 11 | 731.87 | 1.3223 | 925.15 | 857.04 | 0.26 | 0.00 | 0.00 | 110 |

Interest Functions

| Interest Functions at i=0.06 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $m$ | $i^{(m)}$ | $d^{(m)}$ | $i / i^{(m)}$ | $d / d^{(m)}$ | $\alpha(m)$ | $\beta(m)$ |
| 1 | 0.06000 | 0.05660 | 1.00000 | 1.00000 | 1.00000 | 0.00000 |
| 2 | 0.05913 | 0.05743 | 1.01478 | 0.98564 | 1.00021 | 0.25739 |
| 4 | 0.05870 | 0.05785 | 1.02223 | 0.97852 | 1.00027 | 0.38424 |
| 12 | 0.05841 | 0.05813 | 1.02721 | 0.97378 | 1.00028 | 0.46812 |
| $\infty$ | 0.05827 | 0.05827 | 1.02971 | 0.97142 | 1.00028 | 0.50985 |

Special Note: Unless specified, the force of interest is constant in each question .

Casualty Actuarial Society<br>AND THE Canadian Institute of Actuaries

Steven D. Armstrong Vice President-Admissions

William Wilder
Chairperson
Examination Committee
Jason Russ
Assistant Chairperson
Examination Committee

October 29, 2015

## INSTRUCTIONS TO CANDIDATES

1. This 50 point examination consists of 25 multiple choice questions worth 2 points each.
2. To answer the multiple choice questions, use the short-answer card provided and a number 2 or HB pencil only.

- Fill in that it is fall 2015 and that the exam name is ST.
- Darken the spaces corresponding to your Candidate ID number. Five rows are available. If your Candidate ID number is fewer than 5 digits, include leading zeros. For example, if your Candidate ID number is 987 , consider that your Candidate ID number is 00987 , enter a zero on the first row, a zero on the second row, 9 on the third row, 8 on the fourth row, and 7 on the fifth [last] row. Write in your Candidate ID number next to the place where you darken the spaces for your Candidate ID number. Your name, or any other identifying mark, must not appear on the short-answer card.
- Mark your short-answer card during the examination period. No additional time will be allowed for this after the exam has ended. Make your marks dark and fill in the spaces completely.
- For each of the multiple choice questions, select the one best answer and fill in the corresponding letter. One quarter of the point value of the question will be subtracted for each incorrect answer. No points will be added or subtracted for responses left blank.

3. Do all problems until you reach the last page of the examination where "END OF EXAMINATION" is marked.
4. Prior to the start of the exam you will have a ten-minute reading period in which you can silently read the questions and check the exam booklet for missing or defective pages. Writing will NOT be permitted during this time and you will not be permitted to hold pens or pencils. You will also not be allowed to use calculators. The supervisor has additional exams for those candidates who have defective exam booklets.

- Verify that you have a copy of "Tables for CAS Exam ST" included in your exam packet.
- Candidates should not interpolate in the tables unless explicitly instructed to do so in the problem, rather, a candidate should round the result that would be used to enter a given table to the same level of precision as shown in the table and use the result in the table that is nearest to that indicated by rounded result. For example, if a candidate is using the Tables of the Normal Distribution to find a significance level and has a Z value of 1.903 , the candidate should round to 1.90 to find cumulative probability in the Normal table.
- Candidates should employ a non-parametric test unless otherwise specified in the problem, or when there is a standard distribution that is logically or commonly associated with the random variable in question. Examples of problems with a logical or commonly associated distribution would include exponential wait times for Poisson processes and applications of the Central Limit Theorem.

5. Your Examination Envelope is pre-labeled with your Candidate ID number, name, exam number, and test center. Do not remove this label. Keep a record of your Candidate ID number for future inquiries regarding this exam.
6. Candidates must remain in the examination center until the examination has concluded. The examination starts after the reading period is complete. You may leave the examination room to use the restroom with permission from the supervisor.
7. At the end of the examination, place the short-answer card in the Examination Envelope. Nothing written in the examination booklet will be graded. Only the short-answer card will be graded. Also place any included reference materials in the Examination Envelope. BEFORE YOU TURN THE EXAMINATION ENVELOPE IN TO THE SUPERVISOR, BE SURE TO SIGN IT IN THE SPACE PROVIDED ABOVE THE CUT-OUT WINDOW.
8. If you have brought a self-addressed, stamped envelope, you may put the examination booklet and scrap paper inside and submit it separately to the supervisor. It will be mailed to you. Do not put the self-addressed stamped envelope inside the Examination Envelope. Interoffice mail is not acceptable.

If you do not have a self-addressed, stamped envelope, please place the examination booklet in the Examination Envelope and seal the envelope. You may not take it with you. Do not put scrap paper in the Examination Envelope. The supervisor will collect your scrap paper.

Candidates may obtain a copy of the examination from the CAS Web Site.
All extra answer sheets, scrap paper, etc. must be returned to the supervisor for disposal.
9. Candidates must not give or receive assistance of any kind during the examination. Any cheating, any attempt to cheat, assisting others to cheat, or participating therein, or other improper conduct will result in the Casualty Actuarial Society and the Canadian Institute of Actuaries disqualifying the candidate's paper, and such other disciplinary action as may be deemed appropriate within the guidelines of the CAS Policy on Examination Discipline.
10. The exam survey is available on the CAS Web Site in the "Admissions/Exams" section. Please submit your survey by November 14, 2015.

## END OF INSTRUCTIONS

## 2015 Exam S Syllabus Statistics and Probabilistic Models

The syllabus for this four-hour multiple-choice exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as calculating the likelihood ratio test when there is no closed-form solution, but that the candidate would still be expected to explain conceptually in the context of an examination.

KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the preliminary examinations, provide sufficient resources to allow the candidate to demonstrate proficiency with respect to the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.

Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.

A thorough knowledge of calculus and probability is assumed, as is familiarity with discounting cash flows. While some problems may have an insurance or risk management theme, no prior knowledge of insurance terminology is expected.

The Probability Models section (Section A) covers Stochastic Processes, Markov Chains and Survival Models along with a simplified version of Life Contingencies. Survival models are covered in depth as part of probability modeling in generic terms. Markov Chains provide the means to model how an entity can move through different states. Life Contingencies problems can be viewed as discounted cash flow problems that include the effect of probability of payment, and are covered through a Study Note linking the generic survival model concepts to a subset of life actuarial concepts to illustrate how to calculate annuities or single premium insurance amounts.

In general, the material covered under the Statistics section (Section B) covers topics that would be commonly found in a second semester course of a two semester Probability \& Statistics sequence at the undergraduate level. Coverage of the topics listed under the Statistics section will vary by college and the candidate may need to supplement that course work with additional reading and problem solving work from the suggested textbooks listed at the end of Section B.

The Extended Linear Model section (Section C) covers Generalized Linear Models, a predictive modeling technique commonly used to construct classification plans. Ordinary least squares is covered as one member of the exponential family under the Generalized Linear Models section. Many textbooks covering this topic, including the textbook on the syllabus, use statistical software to illustrate the concepts covered in examples, since using a calculator to solve a realistic problem is impractical. While it is not required that the candidates learn a statistical language for the purposes of this examination, learning the basic concepts of a statistical language will be useful in applying the techniques on this exam in practice.

The Time Series section (Section D) covers an introduction to modeling activity over time like financial results or stock prices using the Auto Regressive Integrated Moving Average (ARIMA) where activity in a given time period may be linked to activity in subsequent time periods. That connection between adjacent time periods violates one of the assumptions behind the Extended Linear Model techniques, but the ARIMA approach incorporates that linkage as an aid in predicting future results.

The CAS will test the candidate's knowledge of topics that are presented in the learning objectives. Thus, the candidate should expect that each exam will cover a large proportion of the learning objectives and associated knowledge statements and syllabus readings, and that all of these will be tested at least once over the course of a few years-but each one may not be covered on each exam.

A variety of tables will be provided to the candidate with the exam. The tables include values for the illustrative life tables, standard normal distribution, abridged inventories of discrete and continuous probability distributions, Chi-square Distribution, $t$-Distribution, $F$-Distribution, Normal Distribution as well as the tables required to perform the Signed-Rank test and Mann Whitney tests from the non-parametric section. Since they will be included with the examination, candidates will not be allowed to bring copies of the tables into the examination room.

A guessing adjustment will be used in grading this exam. Details are provided under "Guessing Adjustment" in the "Examination Rules-The Examination" section of the Syllabus of Basic Education.

Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from the CAS website.

Changes made since this syllabus was first published are highlighted in red below. Please check the "Syllabus Update" for this exam for any further changes to this syllabus.

## A. Probability Models (Stochastic Processes and Survival Models)

Range of weight for Section A: 20-40 percent

Candidates should be able to solve problems using stochastic processes. They should be able to determine the probabilities and distributions associated with these processes. Specifically, candidates should be able to use a Poisson process in these applications. Survival models are simply an extension of the stochastic process probability models where one is estimating the future lifetime of an entity given assumptions on the distribution function used to describe the likelihood of survival. Markov Chains are a useful tool to model movement between states in a given process and underlie modern Bayesian MCMC models. The Study Note will re-cast the generic survival model learning objectives to link those concepts to life actuarial symbols to help ensure P\&C actuaries can communicate with life actuaries on basic concepts, but we should recognize that many disciplines like engineering or computer science incorporate survival models in their work. Life Contingencies problems can be viewed as discounted cash flow problems that can be set up and solved using Markov Chain concepts or simply viewed as three matrices in a spreadsheet indicating payment amount, likelihood of payment and discount effect by time period as illustrated by Learning Objective 7.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Understand and apply the properties of Poisson processes: <br> - For increments in the homogeneous case <br> - For interval times in the homogeneous case <br> - For increments in the non-homogeneous case <br> - Resulting from special types of events in the Poisson process <br> - Resulting from sums of independent Poisson processes <br> Range of weight: $0-5$ percent | a. Poisson process <br> b. Non-homogeneous Poisson process <br> c. Memoryless property of Exponential and Poisson <br> d. Relationship between Exponential and Gamma <br> e. Relationship between Exponential and Poisson |
| 2. For any Poisson process and the inter arrival and waiting distributions associated with the Poisson process, calculate: <br> - Expected values <br> - Variances <br> - Probabilities <br> Range of weight: $0-5$ percent | a. Probability calculations for Poisson process <br> b. Conditional distribution of arrival times <br> c. Greedy algorithms |
| 3. For a compound Poisson process, calculate moments associated with the value of the process at a given time. <br> Range of weight: $0-5$ percent | a. Compound Poisson process mean and variance <br> b. Normal approximation and hypothesis testing |
| READINGS |  |
| Ross 5.3-5.4 <br> Daniel |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 4. Apply the Poisson Process concepts to calculate the hazard function and related survival model concepts <br> - Relationship between hazard rate, probability density function and cumulative distribution function <br> - Effect of memoryless nature of Poisson distribution on survival time estimation <br> Range of weight: 2-8 percent | a. Failure time random variables <br> b. Cumulative distribution functions <br> c. Survival functions <br> d. Probability density functions <br> e. Hazard functions and relationship to Exponential distribution <br> f. Relationships between failure time random variables in the functions above |
| READINGS |  |
| Ross 5.2 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 5. Given the joint distribution of more than one source of failure in a system (or life) and using Poisson Process assumptions: <br> - Calculate probabilities and moments associated with functions of these random variables' variances. <br> - Understand difference between a series system (joint life) and parallel system (last survivor) when calculating expected time to failure or probability of failure by a certain time <br> - Understand the effect of multiple sources of failure (multiple decrement) on expected system time to failure (expected lifetime) <br> Range of weight: 2-8 percent | a. Joint distribution of failure times <br> b. Probabilities and moments <br> c. Time until failure of the system (life) <br> d. Time until failure of the system (life) from a specific cause <br> e. Time until failure of the system (life) for parallel or series systems with multiple components <br> f. Paths that lead to parallel or series system failure for systems with multiple components <br> g. Relationship between failure time and minimal path and minimal cut sets <br> h. Bridge system and defining path to failure <br> i. Random graphs and defining path to failure <br> j. Effect of multiple sources of failure (multiple decrements) on failure time calculations (competing risk) <br> k. Non-uniform probability of component failure (multiple decrement) <br> 1. Method of inclusion and exclusion as applied to failure time estimates <br> m . Expected system lifetime as function of component lifetime and properties of expected lifetime estimates |
| READINGS |  |
| Ross 9.1-9.6 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 6. For discrete and continuous Markov Chains under both homogeneous and nonhomogenous states <br> - Definition of a Markov Chain <br> - Chapman-Kolmogorov Equations for nstep transition calculations <br> - Accessible states <br> - Ergodic Markov Chains and limiting probabilities <br> - Markov Chain Monte Carlo Methods <br> Range of weight: 2-10 percent | a. Random Walk <br> b. Classification of states and classes of states (absorbing, accessible, transition, irreducible, and recurrent) <br> c. Transition step probabilities <br> d. Stationary probabilities <br> e. Recurrent vs. transient states <br> f. Gamblers ruin problem <br> g. Branching Processes <br> h. Metropolis-Hastings algorithm <br> i. Gibbs sampler <br> j. Birth-Death process <br> k. Homogeneous transition probabilities <br> 1. Memoryless property of Markov Chains <br> m. Limiting probabilities |
| READINGS |  |
| Ross 4.1-4.9 and 6.1-6.5 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 7. Solve Life Contingency problems using a life table in a spreadsheet as the combined result of discount, probability of payment and amount of payment vectors. Understand the linkage between the life table and the corresponding probability models. <br> - Calculate annuities for discrete time <br> - Calculate life insurance single net premiums (or property/casualty pure premiums) for discrete time <br> - Solve for net level premiums (not including fractional lives) <br> Range of weight: 2-8 percent | a. Discounted cash flow <br> b. Relationship between annuity values and insurance premiums <br> c. Life table linkage to probability models <br> d. Equivalence property |
| READINGS |  |
| Struppeck |  |

## B. Statistics

Range of weight for Section B: 20-40 percent
Candidates should have a thorough understanding of the concepts typically covered in the $2^{\text {nd }}$ semester of a two semester undergraduate sequence in Probability and Statistics. The specific topics to be tested are described below. Mastering the concepts listed under section B is necessary to understand the concepts behind the Generalized Linear Models presented under Section C.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Perform point estimation of statistical parameters using Maximum likelihood estimation ("MLE"). <br> Apply criteria to the estimates such as: <br> - Consistency <br> - Unbiasedness <br> - Sufficiency <br> - Efficiency <br> - Minimum variance <br> - Mean square error <br> Range of weight: 5-10 percent | a. Equations for MLE of mean, variance from a sample <br> b. Estimation of mean and variance based on sample <br> c. General equations for MLE of parameters <br> d. Recognition of consistency property of estimators and alternative measures of consistency <br> e. Application of criteria for measurement when estimating parameters through minimization of variance, mean square error <br> f. Definition of statistical bias and recognition of estimators that are unbiased or biased <br> g. Application of Rao-Cramer Lower Bound and Efficiency <br> h. Relationship between Sufficiency and Minimum Variance <br> i. Develop and estimate a sufficient statistic for a distribution <br> j. Factorization Criterion for sufficiency <br> k. Application of Rao-Cramer Lower Bound and Fisher Information <br> 1. Application of MVUE for the exponential class of distributions |


| 2. Test statistical hypotheses including Type I and Type II errors using: <br> - Neyman-Pearson lemma <br> - Likelihood ratio tests <br> - First principles <br> Apply Neyman-Pearson lemma to construct likelihood ratio equation. <br> Use critical values from a sampling distribution to test means and variances <br> Range of weight: 5-10 percent | a. Presentation of fundamental inequalities based on general assumptions and normal assumptions <br> b. Definition of Type I and Type II errors <br> c. Significance levels <br> d. One-sided versus two-sided tests <br> e. Estimation of sample sizes under normality to control for Type I and Type II errors <br> f. Determination of critical regions <br> g. Definition and measurement of likelihood ratio tests <br> h. Determining parameters and testing using tabular values <br> i. Recognizing when to apply likelihood ratio tests versus chi-square or other goodness of fit tests <br> j. Apply paired t -test to two samples <br> k. Test for difference in variance under Normal distribution between two samples through application of F-test <br> 1. Test of significance of means from two samples under Normal distribution assumption in both large and small sample cases <br> m . Test for significance of difference in proportions between two samples under Binomial distribution assumption in both large and small sample case <br> n. Application of contingency tables to test independence between effects <br> o. Asymptotic relationship between likelihood ratio tests and the Chi-Square distribution <br> p. Application of Neyman-Pearson lemma to Uniformly Most Powerful hypothesis tests <br> q. Equivalence between critical regions and confidence intervals |
| :---: | :---: |
| 3. Calculate order statistics of a sample for a given distribution and use non-parametric statistics to describe a data set. <br> Range of weight: 5-10 percent | a. General form for distribution of $\mathrm{n}^{\text {th }}$ largest element of a set <br> b. Application to a given distributional form <br> c. Calculate Spearman's Rho and Kendall's Tau and understand how those correlation measures differ from the Pearson correlation coefficient <br> d. Apply rank order statistics using Sign-Rank Wilcoxon for matched pair tests <br> e. Apply rank order statistics using Sign Test for matched pairs and comparison of distributions with or without Normal approximation <br> f. Apply rank order statistics using Mann-WhitneyWilcoxon Procedure <br> g. Application of QQ Plots to evaluate goodness of fit <br> h. Relationship between Man-Whitney U test and Wilcoxon's rank sum |


| 4. Bayesian Statistics parameter estimation for conjugate prior and posterior distributions: <br> - Beta-Binomial <br> - Normal-Normal <br> - Gamma-Poisson <br> Range of weight: 5-10 percent | a. Calculate Bayesian Point Estimates for the three conjugate prior distributions listed on the Learning Objective <br> b. Calculate Bayesian Interval estimates for the Normal-Normal distribution and special cases of the other conjugate prior distributions listed on the Learning Objective <br> c. Difference between confidence interval and Bayesian credible interval <br> d. Posterior mean as weighted average of posterior distribution and observations <br> e. Bayes Theorem <br> f. Effect of changing variance of observations or prior distribution on posterior distribution parameters |
| :---: | :---: |
| READINGS |  |
| There is no single required text for Section B. No single text provides complete coverage of all learning objectives and knowledge statements. Each of the following textbooks has very good coverage of the syllabus material, but there may be other introductory statistics textbooks that cover much of the material as well: |  |
| Hogg, McKean, and Craig |  |
| Wackerly, Mendenhall, and Scheaffer |  |
| For a mapping of the sections of these texts to the learning objectives, candidates should refer to the "Knowledge Statement Mapping for Exam S" document posted on the CAS website under the Syllabus Material section for this exam. |  |

## C. Extended Linear Models

## Range of weight for Section C: 25-40 percent

This section covers the Generalized Linear Model and treats Ordinary Least Squares as one type of a Generalized Linear Model that may be used when the dependent variable follows the Normal distribution. The models presented in this section all assume that the underlying data consists of independent and identically distributed observations from a member of the exponential distribution family. Also, we assume there is a formula describing the behavior of the dependent variable can be described as a linear process of the dependent variables after applying a link function. The specific topics to be tested are described below.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Understand the assumptions behind different forms of the Generalized Linear Model under the exponential family assuming independent and identically distributed observations and be able to select the appropriate model from list below: <br> - Ordinary Least Squares <br> - Generalized Linear Model <br> - ANOVA <br> Range of weight: 5-10 percent | a. Understand the relationship between mean and variance by model family member <br> b. Understand how to select the appropriate distribution function for the dependent variable and the implication for the appropriate model form <br> c. Link Functions (Identity, Log, Logit, Power, Inverse) <br> d. (Natural) Exponential Family (Binomial, Normal, Exponential, Gamma, Poisson, Inverse Gaussian, Negative Binomial, Tweedie) <br> e. Canonical Forms of link function and effect of non-canonical link function on bias <br> f. Tweedie relationship to Gamma-Poisson |
| 2. Evaluate models developed using Generalized Linear Model approach <br> Range of weight: 5-10 percent | a. Raw and studentized Residuals <br> b. $R^{2}$ statistic <br> c. Cook's Distance and outliers <br> d. Influential points <br> e. Leverage <br> f. Akaike's Information /Criterion (AIC) and BIC(penalized log likelihood measures) <br> g. Standardized/Studentized Residuals <br> h. Deviance Residuals and relationship to likelihood <br> i. PP Plots <br> j. Type III Sequential Chi-Square test <br> k. T-test and Wald test for significance of regression coefficients <br> 1. Prediction intervals for response variable <br> m. Mean square error and standard error <br> n. Calculation and validity of $F$ test to compare two models (under OLS) <br> o. Evaluate appropriateness of underlying assumptions including: <br> - Homoscedasticity <br> - Autocorrelation of residuals |

$\left.\left.\begin{array}{|l|ll|}\hline \text { 3. } \begin{array}{l}\text { Understand the algorithms behind the } \\ \text { numerical solutions for the different forms } \\ \text { of the GLM family to enable interpretation } \\ \text { of output from the statistical software } \\ \text { employed in modeling and to make } \\ \text { appropriate modeling choices when } \\ \text { selecting modeling options. }\end{array} & \begin{array}{ll}\text { a. } \\ \text { b. } \\ \text { c. }\end{array} & \begin{array}{l}\text { Maximum Likelihood } \\ \text { Fisher Scoring (iterative weighted least squares) } \\ \text { Quasi-Likelihood and relationship to maximum } \\ \text { likelihood }\end{array} \\ \text { Range of weight: 5-10 percent }\end{array}\right] \begin{array}{lll|}\text { Collinearity (Aliasing) and model stability }\end{array}\right]$

## D. Time Series with Constant Variance

Range of weight for Section D: 5-10 percent
This section will cover basic applications of the Auto Regressive Integrated Moving Average time series model. The specific topics to be tested are described below.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Use time series to model trends <br> a. Estimation, data analysis and forecasting <br> b. Forecast errors and confidence intervals | a. Mean-reverting time series <br> b. Elimination of trends using differencing <br> c. Relationship between seasonality and autocorrelation |
| 2. Model relationships of current and past values of a statistic / metric. <br> a. Estimation, data analysis and forecasting <br> b. Forecast errors and confidence intervals | a. Calculation and use of lag $k$ autocorrelation statistic and cross correlation statistics in determining model structure <br> b. Stationary series <br> c. Autoregressive models of order 1, AR(1) <br> d. Autoregressive integrated moving average models (ARIMA) <br> - AR(p) models <br> - Moving average models (MA) <br> - Autoregressive moving average models (ARMA) <br> - ARIMA models <br> e. Invertible time series and relationship between AR and MA models <br> f. Converting between AR and MA models <br> g. Interpretation of auto-correlation function as aid to model selection (AR vs. MA and number of lags to include in model) <br> h. Relationship between time series input and item modeled for AR vs. MA |
| 3. Understand forecasts produced by ARIMA | a. Forecast using ARIMA models <br> b. One step ahead prediction vs. many step ahead projection <br> c. Change in variance in prediction by AR vs. MA model |
| READINGS |  |
| Exam questions from this section may contain snippets of simple R code and illustrative output of the type shown in the text. Candidates should understand the general functionality of the R commands listed in the "Summary of commands used in examples" sections at the end of chapters 1-4 and 6. Candidates will not be asked to write R code, nor will they be required to interpret complex applications or complete R programs. |  |

## Complete Text References for Exam S

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning <br> Objectives | Source |
| :--- | :--- | ---: | ---: |
| Cowpertwait, Paul S. P., and Metcalfe, Andrew N., <br> Introductory Time Series with R, 2009, Springer | Cowpertwait | D1-D3 | B <br> NEW |
| Daniel, J.W., "Poisson processes (and mixture <br> distributions)," Study Note, June 2008. | Daniel | A1-A3 | OP |
| de Jong, P., and Heller, G., Generalized Linear Models for <br> Insurance Data, 2008, Cambridge | de Jong | C1-C4 | B <br> NEw |
| Hogg, R.V.; McKean, J.W.; and Craig, A.T., Introduction to <br> Mathematical Statistics (Seventh Edition), 2013, Prentice <br> Hall. | Hogg, <br> McKean, and <br> Craig | B1-B4 | BO |
| Rosenberg, M. and Guszcza, J., Overview of Linear Models, <br> excerpted from the text Predictive Modeling Applications in <br> Actuarial Science, 2014, Cambridge. | Rosenberg | C2 | OP <br> NEW <br> Ross, Sheldon M., Introduction to Probability Models <br> (Eleventh Edition), 2014, Academic Press <br> Struppeck, T., Life Contingencies, Study Note, October <br> 2014. <br> Wackerly, D.; Mendenhall, W.; and Scheaffer, R., <br> Mathematical Statistics with Applications,(7th edition), <br> 2008, Cengage LearningStruppeck <br> Mendenhall, <br> and Scheaffer |
| A1-A6 | A7 | OP <br> NEW | B1-B4 | | BO |
| ---: |

## Source Key

B Book—may be purchased from the publisher or bookstore or borrowed from the CAS Library.
BO Book (Optional)—may be purchased from the publisher or bookstore.
NEW Indicates new or updated material.
OP All text references marked as Online Publications will be available on a web page titled Complete Text References.

## Publishers and Distributors

Contact information is furnished for those who wish to purchase the text references cited for in the syllabus. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

Academic Press, 200 Wheeler Road, Burlington, MA, 01803, website:
http:/www.academicpressbooks.com
Actex Publications (Mad River Books), 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com; Website: www.actexmadriver.com.
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| KNOWLEDGE STATEMENT MAPPING FOR EXAM S |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | CAS Recommended Texts |  |  |  |
|  |  |  | Hogg, | Wackerly, | Other Texts* |  |
|  |  |  | McKean \& | Mendenhal \& | Hogg \& |  |
|  |  |  | Craig (7th) | Scheafer (7th) | Tannis (9th) | Marx (5th) |
| L.O. |  | Knowledge Statement | Section |  |  |  |
| B. 1 | a. | Equations for MLE of mean, variance from a sample | 6.1 | 9.7 | 6.1 | 5.1-5.2 |
| B. 1 | b. | Estimation of mean and variance based on sample | 2.8 | 8.6-8.9 | 2.3 | 5.1-5.2 |
| B. 1 | c. | General equations for MLE of parameters | 4.1, 6.1 | 9.7 | 6.1 | 5.1-5.2 |
| B. 1 | d. | Recognition of consistency property of estimators and alternative measures of consistency | 5.1 | 9.3 |  | 5.7 |
| B. 1 | e. | Application of criteria for measurement when estimating parameters through minimization of variance, mean square error | 7.1 | 8.2 |  | 5.5 |
| B. 1 | f. | Definition of statistical bias and recognition of estimators that are unbiased or biased | 4.1 | 8.2 | 6.1 | 5.4 |
| B. 1 | g. | Application of Rao-Cramer Lower Bound and Efficiency | 6.2 | 9.5 | 10.7 | 5.5 |
| B. 1 | h. | Relationship between Sufficiency and Minimum Variance | 7.3, 7.4 | 9.5 | 10.1 | 5.6 |
| B. 1 | i. | Develop and estimate a sufficient statistic for a distribution | 7.2 | 9.4 | 10.1 | 5.6 |
| B. 1 | j. | Factorization Criterion for sufficiency | 7.2 | 9.4 | 10.1 | 5.6 |
| B. 1 | k. | Application of Rao-Cramer Lower Bound and Fisher Information | 6.2, 6.4 | 9.5 |  | 5.5 |
| B. 1 | 1. | Application of MVUE for the exponential class of distributions | 7.3-7.5 | 9.8 | 6.1 | 5.2 |
| B. 2 | a. | Presentation of fundamental inequalities based on general assumptions and normal assumptions | 4.5 | 10.2 | 7.1 | 6.2 |
| B. 2 | b. | Definition of Type I and Type II errors | 4.5, 8.1 | 10.2 | 7.1 | 6.4 |
| B. 2 | c. | Significance levels | 4.5, 8.1 | 10.2 | 7.1 | 6.2 |
| B. 2 | d. | One-sided versus two-sided tests | 4.6, 6.2 | 10.2 | 7.1 | 6.2 |
| B. 2 | e. | Estimation of sample sizes under normality to control for Type I and Type II errors | 4.5 | 10.2 | 7.2 | 6.4 |
| B. 2 | f. | Determination of critical regions | 4.5 | 10.2 | 7.1 | 6.2 |
| B. 2 | g. | Definition and measurement of likelihood ratio tests | $6.3,8.1,8.2,8.3$ | 10.11 | 10.4 | 6.5 |
| B. 2 | h. | Determining parameters and testing using tabular values | 4.5, 4.6 |  | 7.1-7.4, 10.3-10.4 | 6.2, 7.3, 7.4 |
| B. 2 | i. | Recognizing when to apply likelihood ratio tests versus chi-square or other goodness of fit tests | 4.7 |  | 7.1-7.4, 10.3-10.4 | 10.1, 10.3-10.4 |
| B. 2 | j. | Apply paired t-test to two samples |  | 12.3 | 7.2 | 8.2, 13.3 |
| B. 2 | k. | Test for difference in variance under Normal distribution between two samples through application of F-test | 8.3 | 10.9 | 7.4 | 7.1-7.4 |
| B. 2 | 1. | Test of significance of means from two samples under Normal distribution assumption in both large and small sample cases | 4.5, 4.6, 5.3 | 10.8 | 7.3 | 7.2 |
| B. 2 | m . | Test for significance of difference in proportions between two samples under Binomial distribution assumption in both large and small sample case | 4.5, 4.6, 5.3 | 10.8 | 7.1 | 8.1-8.2, 9.4 |
| B. 2 | n. | Application of contingency tables to test independence between effects | 4.7 | 14.4 | 8.2 | 10.5 |
| B. 2 | o. | Asymptotic relationship between likelihood ratio tests and the Chi-Square distribution | 6.3, 6.5 |  | 10.4 | 7.3 |
| B. 2 | p. | Application of Neyman-Pearson lemma to Uniformly Most Powerful hypothesis tests | 6.4, 8.1 | 10.1 | 10.3 |  |
| B. 2 | q. | Equivalence between critical regions and confidence intervals | 4.6 | 10.5 | 7.1 | 9.5 |
| B. 3 | a. | General form for distribution of nth largest element of a set | 4.4 | 6.7 | 8.3 | 3.10 |
| B. 3 | b. | Application to a given distributional form | 4.4 | 6.7 | 8.3 | 3.10 |
| B. 3 | c. | Calculate Spearman's Rho and Kendall's Tau and understand how those correlation measures differ from the Pearson correlation coefficent | 10.8 | 15.10-15.11 |  |  |
| B. 3 | d. | Apply rank order statistics using Sign-Rank Wilcoxon | 10.3 | 15.3 | 8.5 | 14.3 |
| B. 3 | e. | Apply rank order statistics using Sign Test | 10.2 | 15.4 | 8.5 | 14.2 |
| B. 3 | f. | Apply rank order statistics using Mann-Whitney-Wilcoxon Procedure | 10.4 | 15.3 | 8.5 |  |
| B. 3 | g . | QQ Plots | 4.4 |  |  |  |
| B. 4 | a. | Calculate Bayesian Point Estimates for the three conjugate prior distributions listed on the Learning Objective | 11.1, 11.2, 11.3 | 16.2 | 9.2 | 5.8 |
| B. 4 | b. | Calculate Bayesian Interval estimates for the three conjugate prior distributions listed on the Learning Objective | 11.1, 11.2, 11.3 | 16.3 | 9.2 | 5.8 |
|  |  |  |  |  |  |  |
|  |  | *Publisher information for these texts is as follows: |  |  |  |  |
|  |  | Hogg, R.V.; and Tanis, E., Probability and Statistical Inference (Ninth Edition), 2014, Prentice Hall. |  |  |  |  |
|  |  | Larsen, R.J.; and Marx, M.L., An Introduction to Mathematical Statistics and Its Applications (Fifth Edition), 2012, Pearson Education, Inc. |  |  |  |  |

## Tables for CAS Exam S

The following tables will be provided to the candidate with the exam. The tables on pages 2 through 15 are reprinted with the permission of the Society of Actuaries; the tables on pages 16 through 25 are copyright material of the Casualty Actuarial Society.

We are furnishing a set of tables for statistical tests as well as a set of distribution functions for Exam S. We do not have a single authoritative textbook for Statistics. The format of the tables may vary from one textbook to the next. The nomenclature used to describe distribution functions may vary from one textbook to the next. To avoid confusion on the part of the candidates we will use the tables and distribution functions definitions that follow when writing exam questions for Exam S.

## Tables of the Normal Distribution



Values of $\mathbf{z}$ for selected values of $\operatorname{Pr}(\mathbf{Z}<\mathbf{z})$

| z | 0.842 | 1.036 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{Pr}(\mathrm{Z}<\mathrm{z})$ | 0.800 | 0.850 | 0.900 | 0.950 | 0.975 | 0.990 | 0.995 |

## Illustrative Life Table: Basic Functions and Single Benefit Premiums at $\boldsymbol{i}=0.06$

| $\boldsymbol{x}$ | $I_{x}$ | $1000 q_{x}$ | $\ddot{a}_{x}$ | $1000 A_{x}$ | $\left.1000{ }^{2} A_{x}\right)$ | $1000{ }_{5} E_{x}$ | $1000{ }_{10} E_{x}$ | $1000{ }_{20} E_{x}$ | $\boldsymbol{x}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 10,000,000 | 20.42 | 16.8010 | 49.00 | 25.92 | 728.54 | 541.95 | 299.89 | 0 |
| 5 | 9,749,503 | 0.98 | 17.0379 | 35.59 | 8.45 | 743.89 | 553.48 | 305.90 | 5 |
| 10 | 9,705,588 | 0.85 | 16.9119 | 42.72 | 9.37 | 744.04 | 553.34 | 305.24 | 10 |
| 15 | 9,663,731 | 0.91 | 16.7384 | 52.55 | 11.33 | 743.71 | 552.69 | 303.96 | 15 |
| 20 | 9,617,802 | 1.03 | 16.5133 | 65.28 | 14.30 | 743.16 | 551.64 | 301.93 | 20 |
| 21 | 9,607,896 | 1.06 | 16.4611 | 68.24 | 15.06 | 743.01 | 551.36 | 301.40 | 21 |
| 22 | 9,597,695 | 1.10 | 16.4061 | 71.35 | 15.87 | 742.86 | 551.06 | 300.82 | 22 |
| 23 | 9,587,169 | 1.13 | 16.3484 | 74.62 | 16.76 | 742.68 | 550.73 | 300.19 | 23 |
| 24 | 9,576,288 | 1.18 | 16.2878 | 78.05 | 17.71 | 742.49 | 550.36 | 299.49 | 24 |
| 25 | 9,565,017 | 1.22 | 16.2242 | 81.65 | 18.75 | 742.29 | 549.97 | 298.73 | 25 |
| 26 | 9,553,319 | 1.27 | 16.1574 | 85.43 | 19.87 | 742.06 | 549.53 | 297.90 | 26 |
| 27 | 9,541,153 | 1.33 | 16.0873 | 89.40 | 21.07 | 741.81 | 549.05 | 297.00 | 27 |
| 28 | 9,528,475 | 1.39 | 16.0139 | 93.56 | 22.38 | 741.54 | 548.53 | 296.01 | 28 |
| 29 | 9,515,235 | 1.46 | 15.9368 | 97.92 | 23.79 | 741.24 | 547.96 | 294.92 | 29 |
| 30 | 9,501,381 | 1.53 | 15.8561 | 102.48 | 25.31 | 740.91 | 547.33 | 293.74 | 30 |
| 31 | 9,486,854 | 1.61 | 15.7716 | 107.27 | 26.95 | 740.55 | 546.65 | 292.45 | 31 |
| 32 | 9,471,591 | 1.70 | 15.6831 | 112.28 | 28.72 | 740.16 | 545.90 | 291.04 | 32 |
| 33 | 9,455,522 | 1.79 | 15.5906 | 117.51 | 30.63 | 739.72 | 545.07 | 289.50 | 33 |
| 34 | 9,438,571 | 1.90 | 15.4938 | 122.99 | 32.68 | 739.25 | 544.17 | 287.82 | 34 |
| 35 | 9,420,657 | 2.01 | 15.3926 | 128.72 | 34.88 | 738.73 | 543.18 | 286.00 | 35 |
| 36 | 9,401,688 | 2.14 | 15.2870 | 134.70 | 37.26 | 738.16 | 542.11 | 284.00 | 36 |
| 37 | 9,381,566 | 2.28 | 15.1767 | 140.94 | 39.81 | 737.54 | 540.92 | 281.84 | 37 |
| 38 | 9,360,184 | 2.43 | 15.0616 | 147.46 | 42.55 | 736.86 | 539.63 | 279.48 | 38 |
| 39 | 9,337,427 | 2.60 | 14.9416 | 154.25 | 45.48 | 736.11 | 538.22 | 276.92 | 39 |
| 40 | 9,313,166 | 2.78 | 14.8166 | 161.32 | 48.63 | 735.29 | 536.67 | 274.14 | 40 |
| 41 | 9,287,264 | 2.98 | 14.6864 | 168.69 | 52.01 | 734.40 | 534.99 | 271.12 | 41 |
| 42 | 9,259,571 | 3.20 | 14.5510 | 176.36 | 55.62 | 733.42 | 533.14 | 267.85 | 42 |
| 43 | 9,229,925 | 3.44 | 14.4102 | 184.33 | 59.48 | 732.34 | 531.12 | 264.31 | 43 |
| 44 | 9,198,149 | 3.71 | 14.2639 | 192.61 | 63.61 | 731.17 | 528.92 | 260.48 | 44 |
| 45 | 9,164,051 | 4.00 | 14.1121 | 201.20 | 68.02 | 729.88 | 526.52 | 256.34 | 45 |
| 46 | 9,127,426 | 4.31 | 13.9546 | 210.12 | 72.72 | 728.47 | 523.89 | 251.88 | 46 |
| 47 | 9,088,049 | 4.66 | 13.7914 | 219.36 | 77.73 | 726.93 | 521.03 | 247.08 | 47 |
| 48 | 9,045,679 | 5.04 | 13.6224 | 228.92 | 83.06 | 725.24 | 517.91 | 241.93 | 48 |
| 49 | 9,000,057 | 5.46 | 13.4475 | 238.82 | 88.73 | 723.39 | 514.51 | 236.39 | 49 |
| 50 | 8,950,901 | 5.92 | 13.2668 | 249.05 | 94.76 | 721.37 | 510.81 | 230.47 | 50 |
| 51 | 8,897,913 | 6.42 | 13.0803 | 259.61 | 101.15 | 719.17 | 506.78 | 224.15 | 51 |
| 52 | 8,840,770 | 6.97 | 12.8879 | 270.50 | 107.92 | 716.76 | 502.40 | 217.42 | 52 |
| 53 | 8,779,128 | 7.58 | 12.6896 | 281.72 | 115.09 | 714.12 | 497.64 | 210.27 | 53 |
| 54 | 8,712,621 | 8.24 | 12.4856 | 293.27 | 122.67 | 711.24 | 492.47 | 202.70 | 54 |
| 55 | 8,640,861 | 8.96 | 12.2758 | 305.14 | 130.67 | 708.10 | 486.86 | 194.72 | 55 |
| 56 | 8,563,435 | 9.75 | 12.0604 | 317.33 | 139.11 | 704.67 | 480.79 | 186.32 | 56 |
| 57 | 8,479,908 | 10.62 | 11.8395 | 329.84 | 147.99 | 700.93 | 474.22 | 177.53 | 57 |
| 58 | 8,389,826 | 11.58 | 11.6133 | 342.65 | 157.33 | 696.85 | 467.12 | 168.37 | 58 |
| 59 | 8,292,713 | 12.62 | 11.3818 | 355.75 | 167.13 | 692.41 | 459.46 | 158.87 | 59 |
| 60 | 8,188,074 | 13.76 | 11.1454 | 369.13 | 177.41 | 687.56 | 451.20 | 149.06 | 60 |
| 61 | 8,075,403 | 15.01 | 10.9041 | 382.79 | 188.17 | 682.29 | 442.31 | 139.00 | 61 |
| 62 | 7,954,179 | 16.38 | 10.6584 | 396.70 | 199.41 | 676.56 | 432.77 | 128.75 | 62 |
| 63 | 7,823,879 | 17.88 | 10.4084 | 410.85 | 211.13 | 670.33 | 422.54 | 118.38 | 63 |
| 64 | 7,683,979 | 19.52 | 10.1544 | 425.22 | 223.34 | 663.56 | 411.61 | 107.97 | 64 |
| 65 | 7,533,964 | 21.32 | 9.8969 | 439.80 | 236.03 | 656.23 | 399.94 | 97.60 | 65 |

Illustrative Life Table: Basic Functions and Single Benefit Premiums at $\boldsymbol{i}=0.06$

| $\boldsymbol{X}$ | $I_{x}$ | $1000{ }^{1} x$ | $\ddot{a}_{x}$ | 1000 $A_{x}$ | $1000\left({ }^{2} A_{x}\right)$ | $1000{ }_{5} E_{x}$ | $1000{ }_{10} E_{x}$ | $1000{ }_{20} E_{x}$ | $x$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 66 | 7,373,338 | 23.29 | 9.6362 | 454.56 | 249.20 | 648.27 | 387.53 | 87.37 | 66 |
| 67 | 7,201,635 | 25.44 | 9.3726 | 469.47 | 262.83 | 639.66 | 374.36 | 77.38 | 67 |
| 68 | 7,018,432 | 27.79 | 9.1066 | 484.53 | 276.92 | 630.35 | 360.44 | 67.74 | 68 |
| 69 | 6,823,367 | 30.37 | 8.8387 | 499.70 | 291.46 | 620.30 | 345.77 | 58.54 | 69 |
| 70 | 6,616,155 | 33.18 | 8.5693 | 514.95 | 306.42 | 609.46 | 330.37 | 49.88 | 70 |
| 71 | 6,396,609 | 36.26 | 8.2988 | 530.26 | 321.78 | 597.79 | 314.27 | 41.86 | 71 |
| 72 | 6,164,663 | 39.62 | 8.0278 | 545.60 | 337.54 | 585.25 | 297.51 | 34.53 | 72 |
| 73 | 5,920,394 | 43.30 | 7.7568 | 560.93 | 353.64 | 571.81 | 280.17 | 27.96 | 73 |
| 74 | 5,664,051 | 47.31 | 7.4864 | 576.24 | 370.08 | 557.43 | 262.31 | 22.19 | 74 |
| 75 | 5,396,081 | 51.69 | 7.2170 | 591.49 | 386.81 | 542.07 | 244.03 | 17.22 | 75 |
| 76 | 5,117,152 | 56.47 | 6.9493 | 606.65 | 403.80 | 525.71 | 225.46 | 13.04 | 76 |
| 77 | 4,828,182 | 61.68 | 6.6836 | 621.68 | 421.02 | 508.35 | 206.71 | 9.61 | 77 |
| 78 | 4,530,360 | 67.37 | 6.4207 | 636.56 | 438.42 | 489.97 | 187.94 | 6.88 | 78 |
| 79 | 4,225,163 | 73.56 | 6.1610 | 651.26 | 455.95 | 470.57 | 169.31 | 4.77 | 79 |
| 80 | 3,914,365 | 80.30 | 5.9050 | 665.75 | 473.59 | 450.19 | 151.00 | 3.19 | 80 |
| 81 | 3,600,038 | 87.64 | 5.6533 | 680.00 | 491.27 | 428.86 | 133.19 | 2.05 | 81 |
| 82 | 3,284,542 | 95.61 | 5.4063 | 693.98 | 508.96 | 406.62 | 116.06 | 1.27 | 82 |
| 83 | 2,970,496 | 104.28 | 5.1645 | 707.67 | 526.60 | 383.57 | 99.81 | 0.75 | 83 |
| 84 | 2,660,734 | 113.69 | 4.9282 | 721.04 | 544.15 | 359.79 | 84.59 | 0.42 | 84 |
| 85 | 2,358,246 | 123.89 | 4.6980 | 734.07 | 561.57 | 335.40 | 70.56 | 0.22 | 85 |
| 86 | 2,066,090 | 134.94 | 4.4742 | 746.74 | 578.80 | 310.56 | 57.83 | 0.11 | 86 |
| 87 | 1,787,299 | 146.89 | 4.2571 | 759.03 | 595.79 | 285.44 | 46.50 | 0.05 | 87 |
| 88 | 1,524,758 | 159.81 | 4.0470 | 770.92 | 612.51 | 260.21 | 36.61 | 0.02 | 88 |
| 89 | 1,281,083 | 173.75 | 3.8442 | 782.41 | 628.92 | 235.11 | 28.17 | 0.01 | 89 |
| 90 | 1,058,491 | 188.77 | 3.6488 | 793.46 | 644.96 | 210.36 | 21.13 | 0.00 | 90 |
| 91 | 858,676 | 204.93 | 3.4611 | 804.09 | 660.61 | 186.21 | 15.41 | 0.00 | 91 |
| 92 | 682,707 | 222.27 | 3.2812 | 814.27 | 675.83 | 162.90 | 10.91 | 0.00 | 92 |
| 93 | 530,959 | 240.86 | 3.1091 | 824.01 | 690.59 | 140.69 | 7.47 | 0.00 | 93 |
| 94 | 403,072 | 260.73 | 2.9450 | 833.30 | 704.86 | 119.79 | 4.93 | 0.00 | 94 |
| 95 | 297,981 | 281.91 | 2.7888 | 842.14 | 718.61 | 100.43 | 3.13 | 0.00 | 95 |
| 96 | 213,977 | 304.45 | 2.6406 | 850.53 | 731.83 | 82.78 | 1.90 | 0.00 | 96 |
| 97 | 148,832 | 328.34 | 2.5002 | 858.48 | 744.50 | 66.97 | 1.10 | 0.00 | 97 |
| 98 | 99,965 | 353.60 | 2.3676 | 865.99 | 756.60 | 53.09 | 0.60 | 0.00 | 98 |
| 99 | 64,617 | 380.20 | 2.2426 | 873.06 | 768.13 | 41.14 | 0.31 | 0.00 | 99 |
| 100 | 40,049 | 408.12 | 2.1252 | 879.70 | 779.08 | 31.12 | 0.15 | 0.00 | 100 |
| 101 | 23,705 | 437.28 | 2.0152 | 885.93 | 789.44 | 22.91 | 0.07 | 0.00 | 101 |
| 102 | 13,339 | 467.61 | 1.9123 | 891.76 | 799.21 | 16.37 | 0.03 | 0.00 | 102 |
| 103 | 7,101 | 498.99 | 1.8164 | 897.19 | 808.41 | 11.33 | 0.01 | 0.00 | 103 |
| 104 | 3,558 | 531.28 | 1.7273 | 902.23 | 817.02 | 7.56 | 0.00 | 0.00 | 104 |
| 105 | 1,668 | 564.29 | 1.6447 | 906.90 | 825.06 | 4.86 | 0.00 | 0.00 | 105 |
| 106 | 727 | 597.83 | 1.5685 | 911.22 | 832.53 | 2.99 | 0.00 | 0.00 | 106 |
| 107 | 292 | 631.64 | 1.4984 | 915.19 | 839.46 | 1.76 | 0.00 | 0.00 | 107 |
| 108 | 108 | 665.45 | 1.4341 | 918.82 | 845.84 | 0.98 | 0.00 | 0.00 | 108 |
| 109 | 36 | 698.97 | 1.3755 | 922.14 | 851.69 | 0.52 | 0.00 | 0.00 | 109 |
| 110 | 11 | 731.87 | 1.3223 | 925.15 | 857.04 | 0.26 | 0.00 | 0.00 | 110 |


| $m$ | Interest Functions at i=0.06 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $i^{(m)}$ | $d^{(m)}$ | $i / i^{(m)}$ | $d / d^{(m)}$ | $\alpha(m)$ | $\beta(m)$ |
| 1 | 0.06000 | 0.05660 | 1.00000 | 1.00000 | 1.00000 | 0.00000 |
| 2 | 0.05913 | 0.05743 | 1.01478 | 0.98564 | 1.00021 | 0.25739 |
| 4 | 0.05870 | 0.05785 | 1.02223 | 0.97852 | 1.00027 | 0.38424 |
| 12 | 0.05841 | 0.05813 | 1.02721 | 0.97378 | 1.00028 | 0.46812 |
| $\infty$ | 0.05827 | 0.05827 | 1.02971 | 0.97142 | 1.00028 | 0.50985 |

Special Note: Unless specified, the force of interest is constant in each question.

Excerpts from the Appendices to Loss Models: From Data to Decisions, 2nd edition

April 21, 2005

## Appendix A

## An Inventory of Continuous Distributions

## A. 1 Introduction

The incomplete gamma function is given by

$$
\begin{gathered}
\Gamma(\alpha ; x)=\frac{1}{\Gamma(\alpha)} \int_{0}^{x} t^{\alpha-1} e^{-t} d t, \quad \alpha>0, x>0 \\
\text { with } \Gamma(\alpha)=\int_{0}^{\infty} t^{\alpha-1} e^{-t} d t, \quad \alpha>0
\end{gathered}
$$

Also, define

$$
G(\alpha ; x)=\int_{x}^{\infty} t^{\alpha-1} e^{-t} d t, \quad x>0
$$

Integration by parts produces the relationship

$$
G(\alpha ; x)=-\frac{x^{\alpha} e^{-x}}{\alpha}+\frac{1}{\alpha} G(\alpha+1 ; x)
$$

For negative $\alpha$, this can repeated until the first argument is postive, say at $\alpha+k$. Then the incomplete gamma function can be evaluated from

$$
G(\alpha+k ; x)=\Gamma(\alpha+k)[1-\Gamma(\alpha+k ; x)] .
$$

The incomplete beta function is given by

$$
\beta(a, b ; x)=\frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} \int_{0}^{x} t^{a-1}(1-t)^{b-1} d t, \quad a>0, b>0,0<x<1
$$

## A. 2 Transformed beta family

## A.2.3 Three-parameter distributions

A.2.3.1 Generalized Pareto (beta of the second kind) - $\alpha, \theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\Gamma(\alpha+\tau)}{\Gamma(\alpha) \Gamma(\tau)} \frac{\theta^{\alpha} x^{\tau-1}}{(x+\theta)^{\alpha+\tau}} \quad \quad F(x)=\beta(\tau, \alpha ; u), \quad u=\frac{x}{x+\theta} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k) \Gamma(\alpha-k)}{\Gamma(\alpha) \Gamma(\tau)}, \quad-\tau<k<\alpha \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \tau(\tau+1) \cdots(\tau+k-1)}{(\alpha-1) \cdots(\alpha-k)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k) \Gamma(\alpha-k)}{\Gamma(\alpha) \Gamma(\tau)} \beta(\tau+k, \alpha-k ; u)+x^{k}[1-F(x)], \quad k>-\tau \\
\text { mode } & =\theta \frac{\tau-1}{\alpha+1}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

A.2.3.2 Burr (Burr Type XII, Singh-Maddala) - $\alpha, \theta, \gamma$

$$
\begin{aligned}
f(x) & =\frac{\alpha \gamma(x / \theta)^{\gamma}}{x\left[1+(x / \theta)^{\gamma} \alpha^{\alpha+1}\right.} \quad F(x)=1-u^{\alpha}, \quad u=\frac{1}{1+(x / \theta)^{\gamma}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \gamma) \Gamma(\alpha-k / \gamma)}{\Gamma(\alpha)}, \quad-\gamma<k<\alpha \gamma \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \gamma) \Gamma(\alpha-k / \gamma)}{\Gamma(\alpha)} \beta(1+k / \gamma, \alpha-k / \gamma ; 1-u)+x^{k} u^{\alpha}, \quad k>-\gamma \\
\text { mode } & =\theta\left(\frac{\gamma-1}{\alpha \gamma+1}\right)^{1 / \gamma}, \quad \gamma>1, \text { else } 0
\end{aligned}
$$

A.2.3.3 Inverse Burr (Dagum) - $\tau, \theta, \gamma$

$$
\begin{aligned}
f(x) & =\frac{\tau \gamma(x / \theta)^{\gamma \tau}}{x\left[1+(x / \theta)^{\gamma}\right]^{\tau+1}} \quad F(x)=u^{\tau}, \quad u=\frac{(x / \theta)^{\gamma}}{1+(x / \theta)^{\gamma}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \gamma) \Gamma(1-k / \gamma)}{\Gamma(\tau)}, \quad-\tau \gamma<k<\gamma \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \gamma) \Gamma(1-k / \gamma)}{\Gamma(\tau)} \beta(\tau+k / \gamma, 1-k / \gamma ; u)+x^{k}\left[1-u^{\tau}\right], \quad k>-\tau \gamma \\
\text { mode } & =\theta\left(\frac{\tau \gamma-1}{\gamma+1}\right)^{1 / \gamma}, \quad \tau \gamma>1, \text { else } 0
\end{aligned}
$$

## A.2.4 Two-parameter distributions

## A.2.4.1 Pareto- $\alpha, \theta$

$$
\begin{aligned}
f(x) & =\frac{\alpha \theta^{\alpha}}{(x+\theta)^{\alpha+1}} \quad F(x)=1-\left(\frac{\theta}{x+\theta}\right)^{\alpha} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(k+1) \Gamma(\alpha-k)}{\Gamma(\alpha)}, \quad-1<k<\alpha \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} k!}{(\alpha-1) \cdots(\alpha-k)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}[X \wedge x] & =\frac{\theta}{\alpha-1}\left[1-\left(\frac{\theta}{x+\theta}\right)^{\alpha-1}\right], \quad \alpha \neq 1 \\
\mathrm{E}[X \wedge x] & =-\theta \ln \left(\frac{\theta}{x+\theta}\right), \quad \alpha=1 \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(k+1) \Gamma(\alpha-k)}{\Gamma(\alpha)} \beta[k+1, \alpha-k ; x /(x+\theta)]+x^{k}\left(\frac{\theta}{x+\theta}\right)^{\alpha}, \quad \text { all } k \\
\text { mode } & =0
\end{aligned}
$$

## A.2.4.2 Inverse Pareto- $\tau, \theta$

$$
\begin{aligned}
f(x) & =\frac{\tau \theta x^{\tau-1}}{(x+\theta)^{\tau+1}} \quad F(x)=\left(\frac{x}{x+\theta}\right)^{\tau} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k) \Gamma(1-k)}{\Gamma(\tau)}, \quad-\tau<k<1 \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k}(-k)!}{(\tau-1) \cdots(\tau+k)}, \quad \text { if } k \text { is a negative integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \tau \int_{0}^{x /(x+\theta)} y^{\tau+k-1}(1-y)^{-k} d y+x^{k}\left[1-\left(\frac{x}{x+\theta}\right)^{\tau}\right], \quad k>-\tau \\
\text { mode } & =\theta \frac{\tau-1}{2}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

## A.2.4.3 Loglogistic (Fisk)- $\gamma, \theta$

$$
\begin{aligned}
f(x) & =\frac{\gamma(x / \theta)^{\gamma}}{x\left[1+(x / \theta)^{\gamma}\right]^{2}} \quad F(x)=u, \quad u=\frac{(x / \theta)^{\gamma}}{1+(x / \theta)^{\gamma}} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1+k / \gamma) \Gamma(1-k / \gamma), \quad-\gamma<k<\gamma \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(1+k / \gamma) \Gamma(1-k / \gamma) \beta(1+k / \gamma, 1-k / \gamma ; u)+x^{k}(1-u), \quad k>-\gamma \\
\text { mode } & =\theta\left(\frac{\gamma-1}{\gamma+1}\right)^{1 / \gamma}, \quad \gamma>1, \text { else } 0
\end{aligned}
$$

## A.2.4.4 Paralogistic- $\alpha, \theta$

This is a Burr distribution with $\gamma=\alpha$.

$$
\begin{aligned}
f(x) & =\frac{\alpha^{2}(x / \theta)^{\alpha}}{x\left[1+(x / \theta)^{\alpha}\right]^{\alpha+1}} \quad F(x)=1-u^{\alpha}, \quad u=\frac{1}{1+(x / \theta)^{\alpha}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \alpha) \Gamma(\alpha-k / \alpha)}{\Gamma(\alpha)}, \quad-\alpha<k<\alpha^{2} \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(1+k / \alpha) \Gamma(\alpha-k / \alpha)}{\Gamma(\alpha)} \beta(1+k / \alpha, \alpha-k / \alpha ; 1-u)+x^{k} u^{\alpha}, \quad k>-\alpha \\
\text { mode } & =\theta\left(\frac{\alpha-1}{\alpha^{2}+1}\right)^{1 / \alpha}, \quad \alpha>1, \text { else } 0
\end{aligned}
$$

## A.2.4.5 Inverse paralogistic- $\tau, \theta$

This is an inverse Burr distribution with $\gamma=\tau$.

$$
\begin{aligned}
f(x) & =\frac{\tau^{2}(x / \theta)^{\tau^{2}}}{x\left[1+(x / \theta)^{\tau}\right]^{\tau+1}} \quad F(x)=u^{\tau}, \quad u=\frac{(x / \theta)^{\tau}}{1+(x / \theta)^{\tau}} \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \tau) \Gamma(1-k / \tau)}{\Gamma(\tau)}, \quad-\tau^{2}<k<\tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\tau+k / \tau) \Gamma(1-k / \tau)}{\Gamma(\tau)} \beta(\tau+k / \tau, 1-k / \tau ; u)+x^{k}\left[1-u^{\tau}\right], \quad k>-\tau^{2} \\
\text { mode } & =\theta(\tau-1)^{1 / \tau}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

## A. 3 Transformed gamma family

## A.3.2 Two-parameter distributions

A.3.2.1 Gamma- $\alpha, \theta$

$$
\begin{aligned}
f(x) & =\frac{(x / \theta)^{\alpha} e^{-x / \theta}}{x \Gamma(\alpha)} \quad F(x)=\Gamma(\alpha ; x / \theta) \\
M(t) & =(1-\theta t)^{-\alpha}, \quad t<1 / \theta \quad \mathrm{E}\left[X^{k}\right]=\frac{\theta^{k} \Gamma(\alpha+k)}{\Gamma(\alpha)}, \quad k>-\alpha \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k}(\alpha+k-1) \cdots \alpha, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\alpha+k)}{\Gamma(\alpha)} \Gamma(\alpha+k ; x / \theta)+x^{k}[1-\Gamma(\alpha ; x / \theta)], \quad k>-\alpha \\
& =\alpha(\alpha+1) \cdots(\alpha+k-1) \theta^{k} \Gamma(\alpha+k ; x / \theta)+x^{k}[1-\Gamma(\alpha ; x / \theta)], \quad k \text { an integer } \\
\text { mode } & =\theta(\alpha-1), \quad \alpha>1, \text { else } 0
\end{aligned}
$$

## A.3.2.2 Inverse gamma (Vinci) - $\alpha, \theta$

$$
\begin{aligned}
f(x) & =\frac{(\theta / x)^{\alpha} e^{-\theta / x}}{x \Gamma(\alpha)} \quad F(x)=1-\Gamma(\alpha ; \theta / x) \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(\alpha-k)}{\Gamma(\alpha)}, \quad k<\alpha \quad \mathrm{E}\left[X^{k}\right]=\frac{\theta^{k}}{(\alpha-1) \cdots(\alpha-k)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(\alpha-k)}{\Gamma(\alpha)}[1-\Gamma(\alpha-k ; \theta / x)]+x^{k} \Gamma(\alpha ; \theta / x) \\
& =\frac{\theta^{k} \Gamma(\alpha-k)}{\Gamma(\alpha)} G(\alpha-k ; \theta / x)+x^{k} \Gamma(\alpha ; \theta / x), \text { all } k \\
\text { mode } & =\theta /(\alpha+1)
\end{aligned}
$$

## A.3.2.3 Weibull- $\theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\tau(x / \theta)^{\tau} e^{-(x / \theta)^{\tau}}}{x} \quad F(x)=1-e^{-(x / \theta)^{\tau}} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1+k / \tau), \quad k>-\tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(1+k / \tau) \Gamma\left[1+k / \tau ;(x / \theta)^{\tau}\right]+x^{k} e^{-(x / \theta)^{\tau}}, \quad k>-\tau \\
\text { mode } & =\theta\left(\frac{\tau-1}{\tau}\right)^{1 / \tau}, \quad \tau>1, \text { else } 0
\end{aligned}
$$

## A.3.2.4 Inverse Weibull (log Gompertz) - $\theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\tau(\theta / x)^{\tau} e^{-(\theta / x)^{\tau}}}{x} \quad F(x)=e^{-(\theta / x)^{\tau}} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1-k / \tau), \quad k<\tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(1-k / \tau)\left\{1-\Gamma\left[1-k / \tau ;(\theta / x)^{\tau}\right]\right\}+x^{k}\left[1-e^{-(\theta / x)^{\tau}}\right], \quad \text { all } k \\
& =\theta^{k} \Gamma(1-k / \tau) G\left[1-k / \tau ;(\theta / x)^{\tau}\right]+x^{k}\left[1-e^{-(\theta / x)^{\tau}}\right] \\
\text { mode } & =\theta\left(\frac{\tau}{\tau+1}\right)^{1 / \tau}
\end{aligned}
$$

## A.3.3 One-parameter distributions

## A.3.3.1 Exponential- $\theta$

$$
\begin{aligned}
f(x) & =\frac{e^{-x / \theta}}{\theta} \quad F(x)=1-e^{-x / \theta} \\
M(t) & =(1-\theta t)^{-1} \quad \mathrm{E}\left[X^{k}\right]=\theta^{k} \Gamma(k+1), \quad k>-1 \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} k!, \quad \text { if } k \text { is an integer } \\
\mathrm{E}[X \wedge x] & =\theta\left(1-e^{-x / \theta}\right) \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} \Gamma(k+1) \Gamma(k+1 ; x / \theta)+x^{k} e^{-x / \theta}, \quad k>-1 \\
& =\theta^{k} k!\Gamma(k+1 ; x / \theta)+x^{k} e^{-x / \theta}, \quad k \text { an integer } \\
\text { mode } & =0
\end{aligned}
$$

## A.3.3.2 Inverse exponential- $\theta$

$$
\begin{aligned}
f(x) & =\frac{\theta e^{-\theta / x}}{x^{2}} \quad F(x)=e^{-\theta / x} \\
\mathrm{E}\left[X^{k}\right] & =\theta^{k} \Gamma(1-k), \quad k<1 \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\theta^{k} G(1-k ; \theta / x)+x^{k}\left(1-e^{-\theta / x}\right), \quad \text { all } k \\
\text { mode } & =\theta / 2
\end{aligned}
$$

## A. 4 Other distributions

## A.4.1.1 Lognormal- $\mu, \sigma$ ( $\mu$ can be negative)

$$
\begin{aligned}
f(x) & =\frac{1}{x \sigma \sqrt{2 \pi}} \exp \left(-z^{2} / 2\right)=\phi(z) /(\sigma x), \quad z=\frac{\ln x-\mu}{\sigma} \quad F(x)=\Phi(z) \\
\mathrm{E}\left[X^{k}\right] & =\exp \left(k \mu+k^{2} \sigma^{2} / 2\right) \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\exp \left(k \mu+k^{2} \sigma^{2} / 2\right) \Phi\left(\frac{\ln x-\mu-k \sigma^{2}}{\sigma}\right)+x^{k}[1-F(x)] \\
\text { mode } & =\exp \left(\mu-\sigma^{2}\right)
\end{aligned}
$$

## A.4.1.2 Inverse Gaussian- $\mu, \theta$

$$
\begin{aligned}
f(x) & =\left(\frac{\theta}{2 \pi x^{3}}\right)^{1 / 2} \exp \left(-\frac{\theta z^{2}}{2 x}\right), \quad z=\frac{x-\mu}{\mu} \\
F(x) & =\Phi\left[z\left(\frac{\theta}{x}\right)^{1 / 2}\right]+\exp \left(\frac{2 \theta}{\mu}\right) \Phi\left[-y\left(\frac{\theta}{x}\right)^{1 / 2}\right], \quad y=\frac{x+\mu}{\mu} \\
M(t) & =\exp \left[\frac{\theta}{\mu}\left(1-\sqrt{1-\frac{2 t \mu^{2}}{\theta}}\right)\right], \quad t<\frac{\theta}{2 \mu^{2}}, \quad \mathrm{E}[X]=\mu, \quad \operatorname{Var}[X]=\mu^{3} / \theta \\
\mathrm{E}[X \wedge x] & =x-\mu z \Phi\left[z\left(\frac{\theta}{x}\right)^{1 / 2}\right]-\mu y \exp \left(\frac{2 \theta}{\mu}\right) \Phi\left[-y\left(\frac{\theta}{x}\right)^{1 / 2}\right]
\end{aligned}
$$

## A.4.1.3 log-t-r, $\mu, \sigma$ ( $\mu$ can be negative)

Let $Y$ have a $t$ distribution with $r$ degrees of freedom. Then $X=\exp (\sigma Y+\mu)$ has the $\log -t$ distribution. Positive moments do not exist for this distribution. Just as the $t$ distribution has a heavier tail than the normal distribution, this distribution has a heavier tail than the lognormal distribution.

$$
\begin{aligned}
& f(x)=\frac{\Gamma\left(\frac{r+1}{2}\right)}{x \sigma \sqrt{\pi r} \Gamma\left(\frac{r}{2}\right)\left[1+\frac{1}{r}\left(\frac{\ln x-\mu}{\sigma}\right)^{2}\right]^{(r+1) / 2}} \\
& F(x)=F_{r}\left(\frac{\ln x-\mu}{\sigma}\right) \text { with } F_{r}(t) \text { the cdf of a } t \text { distribution with } r \text { d.f., }
\end{aligned}
$$

## APPENDIX A. AN INVENTORY OF CONTINUOUS DISTRIBUTIONS

$$
F(x)= \begin{cases}\frac{1}{2} \beta\left[\frac{r}{2}, \frac{1}{2} ; \frac{r}{r+\left(\frac{\ln x-\mu}{\sigma}\right)^{2}}\right], & 0<x \leq e^{\mu}, \\ 1-\frac{1}{2} \beta\left[\frac{r}{2}, \frac{1}{2} ; \frac{r}{r+\left(\frac{\ln x-\mu}{\sigma}\right)^{2}}\right], & x \geq e^{\mu} .\end{cases}
$$

## A.4.1.4 Single-parameter Pareto- $\alpha, \theta$

$$
\begin{array}{rlrl}
f(x) & =\frac{\alpha \theta^{\alpha}}{x^{\alpha+1}}, \quad x>\theta & F(x)=1-(\theta / x)^{\alpha}, \quad x>\theta \\
\mathrm{E}\left[X^{k}\right] & =\frac{\alpha \theta^{k}}{\alpha-k}, \quad k<\alpha & & \mathrm{E}\left[(X \wedge x)^{k}\right]=\frac{\alpha \theta^{k}}{\alpha-k}-\frac{k \theta^{\alpha}}{(\alpha-k) x^{\alpha-k}} \\
\text { mode } & =\theta & &
\end{array}
$$

Note: Although there appears to be two parameters, only $\alpha$ is a true parameter. The value of $\theta$ must be set in advance.

## A. 5 Distributions with finite support

For these two distributions, the scale parameter $\theta$ is assumed known.

## A.5.1.1 Generalized beta- $a, b, \theta, \tau$

$$
\begin{aligned}
f(x) & =\frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} u^{a}(1-u)^{b-1} \frac{\tau}{x}, \quad 0<x<\theta, \quad u=(x / \theta)^{\tau} \\
F(x) & =\beta(a, b ; u) \\
\mathrm{E}\left[X^{k}\right] & =\frac{\theta^{k} \Gamma(a+b) \Gamma(a+k / \tau)}{\Gamma(a) \Gamma(a+b+k / \tau)}, \quad k>-a \tau \\
\mathrm{E}\left[(X \wedge x)^{k}\right] & =\frac{\theta^{k} \Gamma(a+b) \Gamma(a+k / \tau)}{\Gamma(a) \Gamma(a+b+k / \tau)} \beta(a+k / \tau, b ; u)+x^{k}[1-\beta(a, b ; u)]
\end{aligned}
$$

A.5.1.2 beta- $a, b, \theta$

$$
\begin{aligned}
f(x)= & \frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} u^{a}(1-u)^{b-1} \frac{1}{x}, \quad 0<x<\theta, \quad u=x / \theta \\
F(x)= & \beta(a, b ; u) \\
\mathrm{E}\left[X^{k}\right]= & \frac{\theta^{k} \Gamma(a+b) \Gamma(a+k)}{\Gamma(a) \Gamma(a+b+k)}, \quad k>-a \\
\mathrm{E}\left[X^{k}\right]= & \frac{\theta^{k} a(a+1) \cdots(a+k-1)}{(a+b)(a+b+1) \cdots(a+b+k-1)}, \quad \text { if } k \text { is an integer } \\
\mathrm{E}\left[(X \wedge x)^{k}\right]= & \frac{\theta^{k} a(a+1) \cdots(a+k-1)}{(a+b)(a+b+1) \cdots(a+b+k-1)} \beta(a+k, b ; u) \\
& +x^{k}[1-\beta(a, b ; u)]
\end{aligned}
$$

## Appendix B

## An Inventory of Discrete Distributions

## B. 2 The ( $a, b, 0$ ) class

B.2.1.1 Poisson- $\lambda$

$$
\begin{array}{rlrlr}
p_{0} & =e^{-\lambda}, \quad a=0, \quad b=\lambda & p_{k}=\frac{e^{-\lambda} \lambda^{k}}{k!} \\
\mathrm{E}[N] & =\lambda, \quad \operatorname{Var}[N]=\lambda & P(z)=e^{\lambda(z-1)}
\end{array}
$$

B.2.1.2 Geometric- $\beta$

$$
\begin{array}{rlrc}
p_{0} & =\frac{1}{1+\beta}, \quad a=\frac{\beta}{1+\beta}, \quad b=0 & p_{k}=\frac{\beta^{k}}{(1+\beta)^{k+1}} \\
\mathrm{E}[N] & =\beta, \quad \operatorname{Var}[N]=\beta(1+\beta) & P(z)=[1-\beta(z-1)]^{-1} .
\end{array}
$$

This is a special case of the negative binomial with $r=1$.
B.2.1.3 Binomial- $q, m,(0<q<1, m$ an integer $)$

$$
\begin{aligned}
p_{0} & =(1-q)^{m}, \quad a=-\frac{q}{1-q}, \quad b=\frac{(m+1) q}{1-q} \\
p_{k} & =\binom{m}{k} q^{k}(1-q)^{m-k}, \quad k=0,1, \ldots, m \\
\mathrm{E}[N] & =m q, \quad \operatorname{Var}[N]=m q(1-q) \quad P(z)=[1+q(z-1)]^{m} .
\end{aligned}
$$

B.2.1.4 Negative binomial- $\beta, r$

$$
\begin{aligned}
p_{0} & =(1+\beta)^{-r}, \quad a=\frac{\beta}{1+\beta}, \quad b=\frac{(r-1) \beta}{1+\beta} \\
p_{k} & =\frac{r(r+1) \cdots(r+k-1) \beta^{k}}{k!(1+\beta)^{r+k}} \\
\mathrm{E}[N] & =r \beta, \quad \operatorname{Var}[N]=r \beta(1+\beta) \quad P(z)=[1-\beta(z-1)]^{-r}
\end{aligned}
$$

Approximate critical values of T in the Wilcoxon Matched-Pairs, Signed-Rank Test

| One-sided | Two-sided | $\mathrm{n}=5$ | $\mathrm{n}=6$ | $\mathrm{n}=7$ | $\mathrm{n}=8$ | $\mathrm{n}=9$ | $\mathrm{n}=10$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 0 | 2 | 3 | 5 | 8 | 10 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ |  | 0 | 2 | 3 | 5 | 8 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ |  |  | 0 | 1 | 3 | 5 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ |  |  |  | 0 | 1 | 3 |
| One-sided | Two-sided | $\mathrm{n}=11$ | $\mathrm{n}=12$ | $\mathrm{n}=13$ | $\mathrm{n}=14$ | $\mathrm{n}=15$ | $\mathrm{n}=16$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 13 | 17 | 21 | 25 | 30 | 35 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 10 | 13 | 17 | 21 | 25 | 29 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 7 | 9 | 12 | 15 | 19 | 23 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 5 | 7 | 9 | 12 | 15 | 19 |
| One-sided | Two-sided | $\mathrm{n}=17$ | $\mathrm{n}=18$ | $\mathrm{n}=19$ | $\mathrm{n}=20$ | $\mathrm{n}=21$ | $\mathrm{n}=22$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 41 | 47 | 53 | 60 | 67 | 75 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 34 | 40 | 46 | 52 | 58 | 65 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 27 | 32 | 37 | 43 | 49 | 55 |
| $P=.005$ | $\mathrm{P}=.01$ | 23 | 27 | 32 | 37 | 42 | 48 |
| One-sided | Two-sided | $\mathrm{n}=23$ | $\mathrm{n}=24$ | $\mathrm{n}=25$ | $\mathrm{n}=26$ | $\mathrm{n}=27$ | $\mathrm{n}=28$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 83 | 91 | 100 | 110 | 119 | 130 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 73 | 81 | 89 | 98 | 107 | 116 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 62 | 69 | 76 | 84 | 92 | 101 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 54 | 61 | 68 | 75 | 83 | 91 |
| One-sided | Two-sided | $\mathrm{n}=29$ | $\mathrm{n}=30$ | $\mathrm{n}=31$ | $\mathrm{n}=32$ | $\mathrm{n}=33$ | $\mathrm{n}=34$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 140 | 151 | 163 | 175 | 187 | 200 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 126 | 137 | 147 | 159 | 170 | 182 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 110 | 120 | 130 | 140 | 151 | 162 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 100 | 109 | 118 | 128 | 138 | 148 |
| One-sided | Two-sided | $\mathrm{n}=35$ | $\mathrm{n}=36$ | $\mathrm{n}=37$ | $\mathrm{n}=38$ | $\mathrm{n}=39$ | $\mathrm{n}=40$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 213 | 227 | 241 | 256 | 271 | 286 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 195 | 208 | 221 | 235 | 249 | 264 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 173 | 185 | 198 | 211 | 224 | 237 |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 159 | 171 | 182 | 194 | 207 | 220 |
| One-sided | Two-sided | $\mathrm{n}=41$ | $\mathrm{n}=42$ | $\mathrm{n}=43$ | $\mathrm{n}=44$ | $\mathrm{n}=45$ | $\mathrm{n}=46$ |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 302 | 319 | 336 | 353 | 371 | 389 |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 279 | 294 | 310 | 327 | 343 | 361 |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 252 | 266 | 281 | 296 | 312 | 328 |
| $P=.005$ | $\mathrm{P}=.01$ | 233 | 247 | 261 | 276 | 291 | 306 |
| One-sided | Two-sided | $\mathrm{n}=47$ | $\mathrm{n}=48$ | $\mathrm{n}=49$ | $\mathrm{n}=50$ |  |  |
| $\mathrm{P}=.05$ | $\mathrm{P}=.10$ | 407 | 426 | 446 | 466 |  |  |
| $\mathrm{P}=.025$ | $\mathrm{P}=.05$ | 378 | 396 | 415 | 434 |  |  |
| $\mathrm{P}=.01$ | $\mathrm{P}=.02$ | 345 | 362 | 379 | 397 |  |  |
| $\mathrm{P}=.005$ | $\mathrm{P}=.01$ | 322 | 339 | 355 | 373 |  |  |

For use on the CAS actuarial examinations

Tail areas (two-sided) for t-distributions

|  | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| df |  |  |  |  |  |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 |
| 35 | 1.306 | 1.690 | 2.030 | 2.438 | 2.724 |
| 40 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 |
| 45 | 1.301 | 1.679 | 2.014 | 2.412 | 2.690 |
| 50 | 1.299 | 1.676 | 2.009 | 2.403 | 2.678 |
| 55 | 1.297 | 1.673 | 2.004 | 2.396 | 2.668 |
| 60 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 |
| 70 | 1.294 | 1.667 | 1.994 | 2.381 | 2.648 |
| 80 | 1.292 | 1.664 | 1.990 | 2.374 | 2.639 |
| 90 | 1.291 | 1.662 | 1.987 | 2.368 | 2.632 |
| 100 | 1.290 | 1.660 | 1.984 | 2.364 | 2.626 |
| 120 | 1.289 | 1.658 | 1.980 | 2.358 | 2.617 |
| 400 | 1.284 | 1.649 | 1.966 | 2.336 | 2.588 |
| Inf | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |

[^6]Selected Upper-tail areas for F-distributions

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Numerator df | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 14 | 16 | 20 | 24 | 30 | 40 | 50 | 75 | 100 | 200 | 500 | $\operatorname{lnf}$ |

df Upper-ta






```
|2.351
```





| 14.04 | 12.142 | 11.344 | 10.899 | 10.616 | 10.419 | 10.274 | 10.162 | 10.074 | 10.003 | 9.944 | 9.894 | 9.815 | 9.755 | 9.67 | 9.612 | 9.554 | 9.495 | 9.46 | 9.412 | 9.388 | 9.352 | 9.33 | 9.315 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 212 | 16 | 0.02 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




| 4.06 | 3.78 | 3.619 | 3.52 | 3.453 | 3.405 | 3.368 | 3.339 | 3.316 | 3.297 | 3.282 | 3.268 | 3.247 | 3.23 | 3.207 | 3.191 | 3.174 | 3.157 | 3.147 | 3.133 | 3.126 | 3.116 | 3.109 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 3.105 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6.608 | 5.786 | 5.409 | 5.192 | 5.05 | 4.95 | 4.876 | 4.818 | 4.772 | 4.735 | 4.704 | 4.678 | 4.636 | 4.604 | 4.558 | 4.527 | 4.496 | 4.464 | 4.444 | 4.418 | 4.405 | 4.385 | 4.373 |
| 4.365 | 0.05 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |



| 11.323 | 9.454 | 8.67 | 8.233 | 7.953 | 7.758 | 7.614 | 7.503 | 7.415 | 7.344 | 7.285 | 7.235 | 7.156 | 7.095 | 7.009 | 6.951 | 6.893 | 6.833 | 6.797 | 6.749 | 6.724 | 6.687 | 6.665 | 6.65 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 16.258 | 13.274 | 12.06 | 11.392 | 10.967 | 10.672 | 10.456 | 10.289 | 10.158 | 10.051 | 9.963 | 9.888 | 9.77 | 9.68 | 9.553 | 9.466 | 9.379 | 9.291 | 9.238 | 9.166 | 9.13 | 9.075 | 9.042 | 9.02 |


| 2.077 | 2.13 | 2.113 | 2.092 | 2.076 | 2.062 | 2.051 | 2.042 | 2.034 | 2.028 | 2.022 | 2.018 | 2.01 | 2.004 | 1.995 | 1.989 | 1.982 | 1.976 | 1.972 | 1.966 | 1.963 | 1.959 | 1.956 | 1.954 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 3.776 | 3.463 | 3.289 | 3.181 | 3.108 | 3.055 | 3.014 | 2.983 | 2.958 | 2.937 | 2.92 | 2.905 | 2.881 | 2.863 | 2.836 | 2.818 | 2.8 | 2.781 | 2.77 | 2.754 | 2.746 | 2.734 | 2.727 | 2.722 |



| 5.987 | 5.143 | 4.757 | 4.534 | 4.387 | 4.284 | 4.207 | 4.147 | 4.099 | 4.06 | 4.027 | 4 | 3.956 | 3.922 | 3.874 | 3.841 | 3.808 | 3.774 | 3.754 | 3.726 | 3.712 | 3.69 | 3.678 | 3.669 | 0.05 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 9.876 | 8.052 | 7.287 | 6.859 | 6.585 | 6.393 | 6.251 | 6.141 | 6.055 | 5.984 | 5.925 | 5.876 | 5.797 | 5.737 | 5.651 | 5.593 | 5.534 | 5.474 | 5.438 | 5.389 | 5.364 | 5.327 | 5.304 | 5.289 | 0.02 |
| 1.5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




| 3.589 | 3.257 | 3.074 | 2.961 | 2.883 | 2.827 | 2.785 | 2.752 | 2.725 | 2.703 | 2.684 | 2.668 | 2.643 | 2.623 | 2.595 | 2.575 | 2.555 | 2.535 | 2.523 | 2.506 | 2.497 | 2.484 | 2.476 | 2.471 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.591 | 4.737 | 4.347 | 4.12 | 3.972 | 3.866 | 3.787 | 3.726 | 3.677 | 3.637 | 3.603 | 3.575 | 3.529 | 3.494 | 3.445 | 3.41 | 3.376 | 3.34 | 3.319 | 3.29 | 3.275 | 3.252 | 3.239 | 3.23 | 0.05 |






| 3.458 | 3.113 | 2.924 | 2.806 | 2.726 | 2.668 | 2.624 | 2.589 | 2.561 | 2.538 | 2.519 | 2.502 | 2.475 | 2.455 | 2.425 | 2.404 | 2.383 | 2.361 | 2.348 | 2.33 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.318 | 4.459 | 4.066 | 3.338 | 3.687 | 3.581 | 3.5 | 3.438 | 3.388 | 3.347 | 3.313 | 3.284 | 3.237 | 3.202 | 3.15 | 3.115 | 307 | 2.298 | 2.293 |  |
|  | 0.10 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 5.318 | 4.459 | 4.066 | 3.838 | 3.687 | 3.581 | 3.5 | 3.438 | 3.388 | 3.347 | 3.313 | 3.284 | 3.237 | 3.202 | 3.15 | 3.115 | 3.079 | 3.043 | 3.02 | 2.99 | 2.975 | 2.951 | 2.937 | 2.928 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 8389 | 6.637 | 5 | 0.051 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 8.389 | 6.637 | 5.901 | 5.489 | 5.223 | 5.036 | 4.897 | 4.79 | 4.705 | 4.635 | 4.577 | 4.528 | 4.449 | 4.389 | 4.304 | 4.245 | 4.186 | 4.125 | 4.088 | 4.038 | 4.013 | 3.975 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 11.259 | 8.649 | 7.591 | 7.006 | 6.632 | 6.371 | 6.178 | 6.029 | 5.911 | 5.814 | 5.734 | 5.667 | 5.559 | 5.477 | 5.359 | 5.279 | 5.198 | 5.116 | 5.065 | 4.998 | 4.963 | 4.911 |



| 3.36 | 3.006 | 2.813 | 2.693 | 2.611 | 2.551 | 2.505 | 2.469 | 2.44 | 2.416 | 2.396 | 2.379 | 2.351 | 2.329 | 2.298 | 2.277 | 2.255 | 2.232 | 2.218 | 2.199 | 2.189 | 2.174 | 2.165 | 2.159 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.117 | 4.256 | 3.863 | 3.633 | 3.482 | 3.374 | 3.293 | 3.23 | 3.179 | 3.137 | 3.102 | 3.073 | 3.025 | 2.989 | 2.936 | 2.9 | 2.864 | 2.826 | 2.803 | 2.771 | 2.756 | 2.731 | 2.717 | 2.707 |
| .0 .05 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




Selected Upper-tail areas for F-distributions

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Numerator df | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 14 | 16 | 20 | 24 | 30 | 40 | 50 | 75 | 100 | 200 | 500 | $\operatorname{lnf}$ |

df Upper-ta






```
|2.351
```





| 14.04 | 12.142 | 11.344 | 10.899 | 10.616 | 10.419 | 10.274 | 10.162 | 10.074 | 10.003 | 9.944 | 9.894 | 9.815 | 9.755 | 9.67 | 9.612 | 9.554 | 9.495 | 9.46 | 9.412 | 9.388 | 9.352 | 9.33 | 9.315 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 212 | 16 | 0.02 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




| 4.06 | 3.78 | 3.619 | 3.52 | 3.453 | 3.405 | 3.368 | 3.339 | 3.316 | 3.297 | 3.282 | 3.268 | 3.247 | 3.23 | 3.207 | 3.191 | 3.174 | 3.157 | 3.147 | 3.133 | 3.126 | 3.116 | 3.109 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 3.105 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6.608 | 5.786 | 5.409 | 5.192 | 5.05 | 4.95 | 4.876 | 4.818 | 4.772 | 4.735 | 4.704 | 4.678 | 4.636 | 4.604 | 4.558 | 4.527 | 4.496 | 4.464 | 4.444 | 4.418 | 4.405 | 4.385 | 4.373 |
| 4.365 | 0.05 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |



| 11.323 | 9.454 | 8.67 | 8.233 | 7.953 | 7.758 | 7.614 | 7.503 | 7.415 | 7.344 | 7.285 | 7.235 | 7.156 | 7.095 | 7.009 | 6.951 | 6.893 | 6.833 | 6.797 | 6.749 | 6.724 | 6.687 | 6.665 | 6.65 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 16.258 | 13.274 | 12.06 | 11.392 | 10.967 | 10.672 | 10.456 | 10.289 | 10.158 | 10.051 | 9.963 | 9.888 | 9.77 | 9.68 | 9.553 | 9.466 | 9.379 | 9.291 | 9.238 | 9.166 | 9.13 | 9.075 | 9.042 | 9.02 |


| 2.077 | 2.13 | 2.113 | 2.092 | 2.076 | 2.062 | 2.051 | 2.042 | 2.034 | 2.028 | 2.022 | 2.018 | 2.01 | 2.004 | 1.995 | 1.989 | 1.982 | 1.976 | 1.972 | 1.966 | 1.963 | 1.959 | 1.956 | 1.954 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 3.776 | 3.463 | 3.289 | 3.181 | 3.108 | 3.055 | 3.014 | 2.983 | 2.958 | 2.937 | 2.92 | 2.905 | 2.881 | 2.863 | 2.836 | 2.818 | 2.8 | 2.781 | 2.77 | 2.754 | 2.746 | 2.734 | 2.727 | 2.722 |



| 5.987 | 5.143 | 4.757 | 4.534 | 4.387 | 4.284 | 4.207 | 4.147 | 4.099 | 4.06 | 4.027 | 4 | 3.956 | 3.922 | 3.874 | 3.841 | 3.808 | 3.774 | 3.754 | 3.726 | 3.712 | 3.69 | 3.678 | 3.669 | 0.05 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 9.876 | 8.052 | 7.287 | 6.859 | 6.585 | 6.393 | 6.251 | 6.141 | 6.055 | 5.984 | 5.925 | 5.876 | 5.797 | 5.737 | 5.651 | 5.593 | 5.534 | 5.474 | 5.438 | 5.389 | 5.364 | 5.327 | 5.304 | 5.289 | 0.02 |
| 1.5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |




| 3.589 | 3.257 | 3.074 | 2.961 | 2.883 | 2.827 | 2.785 | 2.752 | 2.725 | 2.703 | 2.684 | 2.668 | 2.643 | 2.623 | 2.595 | 2.575 | 2.555 | 2.535 | 2.523 | 2.506 | 2.497 | 2.484 | 2.476 | 2.471 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.591 | 4.737 | 4.347 | 4.12 | 3.972 | 3.866 | 3.787 | 3.726 | 3.677 | 3.637 | 3.603 | 3.575 | 3.529 | 3.494 | 3.445 | 3.41 | 3.376 | 3.34 | 3.319 | 3.29 | 3.275 | 3.252 | 3.239 | 3.23 | 0.05 |






| 3.458 | 3.113 | 2.924 | 2.806 | 2.726 | 2.668 | 2.624 | 2.589 | 2.561 | 2.538 | 2.519 | 2.502 | 2.475 | 2.455 | 2.425 | 2.404 | 2.383 | 2.361 | 2.348 | 2.33 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.318 | 4.459 | 4.066 | 3.338 | 3.687 | 3.581 | 3.5 | 3.438 | 3.388 | 3.347 | 3.313 | 3.284 | 3.237 | 3.202 | 3.15 | 3.115 | 307 | 2.298 | 2.293 |  |
|  | 0.10 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 5.318 | 4.459 | 4.066 | 3.838 | 3.687 | 3.581 | 3.5 | 3.438 | 3.388 | 3.347 | 3.313 | 3.284 | 3.237 | 3.202 | 3.15 | 3.115 | 3.079 | 3.043 | 3.02 | 2.99 | 2.975 | 2.951 | 2.937 | 2.928 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 8389 | 6.637 | 5 | 0.051 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 8.389 | 6.637 | 5.901 | 5.489 | 5.223 | 5.036 | 4.897 | 4.79 | 4.705 | 4.635 | 4.577 | 4.528 | 4.449 | 4.389 | 4.304 | 4.245 | 4.186 | 4.125 | 4.088 | 4.038 | 4.013 | 3.975 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 11.259 | 8.649 | 7.591 | 7.006 | 6.632 | 6.371 | 6.178 | 6.029 | 5.911 | 5.814 | 5.734 | 5.667 | 5.559 | 5.477 | 5.359 | 5.279 | 5.198 | 5.116 | 5.065 | 4.998 | 4.963 | 4.911 |



| 3.36 | 3.006 | 2.813 | 2.693 | 2.611 | 2.551 | 2.505 | 2.469 | 2.44 | 2.416 | 2.396 | 2.379 | 2.351 | 2.329 | 2.298 | 2.277 | 2.255 | 2.232 | 2.218 | 2.199 | 2.189 | 2.174 | 2.165 | 2.159 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 5.117 | 4.256 | 3.863 | 3.633 | 3.482 | 3.374 | 3.293 | 3.23 | 3.179 | 3.137 | 3.102 | 3.073 | 3.025 | 2.989 | 2.936 | 2.9 | 2.864 | 2.826 | 2.803 | 2.771 | 2.756 | 2.731 | 2.717 | 2.707 |
| .0 .05 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |





### 0.02

0.01
0.02
0.200.10
0.050.05
0.02
0.010.200.050.05
0.020.01

 \begin{tabular}{|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|r|}
\hline


\hline 6.773 \& 5.135 \& 4.447 \& 4.058 \& 3.805 \& 3.626 \& 3.492 \& 3.387 \& 3.303 \& 3.235 \& 3.177 \& 3.128 \& 3.049 \& 2.988 \& 2.9 \& 2.84 \& 2.777 \& 2.713 \& 2.674 \& 2.62 \& 2.592 \& 2.55 \& 2.524 \& 2.506 <br>
\hline 8.683 \& 6.359 \& 5.417 \& 4.893 \& 4.556 \& 4.318 \& 4.142 \& 4.004 \& 3.895 \& 3.805 \& 3.73 \& 3.666 \& 3.564 \& 3.485 \& 3.372 \& 3.294 \& 3.214 \& 3.132 \& 3.081 \& 3.012 \& 2.977 \& 2.923 \& 2.891 \& 2.868 <br>
\hline
\end{tabular}

| 1.787 | 1.783 | 1.736 | 1.696 | 1.665 | 1.641 | 1.621 | 1.605 | 1.591 | 1.58 | 1.57 | 1.561 | 1.547 | 1.536 | 1.519 | 1.507 | 1.494 | 1.481 | 1.472 | 1.46 | 1.454 | 1.445 | 1.439 | 1.435 |
| :--- | :--- | :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: || 4.494 | 3.634 | 3.239 | 3.007 | 2.852 | 2.741 | 2.657 | 2.591 | 2.538 | 2.494 | 2.456 | 2.425 | 2.373 | 2.333 | 2.276 | 2.235 | 2.194 | 2.151 | 2.124 | 2.087 | 2.068 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |





| 4.414 | 3.555 | 3.16 | 2.928 | 2.773 | 2.661 | 2.577 | 2.51 | 2.456 | 2.412 | 2.374 | 2.342 | 2.29 | 2.25 | 2.191 | 2.15 | 2.107 | 2.063 | 2.035 | 1.998 | 1.978 | 1.948 | 1.929 | 1.917 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 6.515 | 4.9 | 4.221 | 3.837 | 3.586 | 3.408 | 3.275 | 3.171 | 3.087 | 3.018 | 2.96 | 2.911 | 2.832 | 2.77 | 2.682 | 2.62 | 2.557 | 2.491 | 2.45 | 2.395 | 2.366 | 2.322 | 2.295 | 2.277 | 0.02 |


| 6.515 | 4.9 | 4.221 | 3.837 | 3.566 | 3.408 | 3.275 | 3.171 | 3.087 | 3.018 | 2.96 | 2.911 | 2.832 | 2.77 | 2.682 | 2.62 | 2.557 | 2.491 | 2.45 | 2.395 | 2.366 | 2.322 | 2.295 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 8.285 | 6.013 | 5.092 | 4.579 | 4.248 | 4.015 | 3.841 | 3.705 | 3.597 | 3.508 | 3.434 | 3.371 | 3.269 | 3.19 | 3.077 | 2.999 | 2.919 | 2.835 | 2.784 | 2.714 | 2.678 | 2.623 | 2.589 |




| 4.381 | 3.522 | 3.127 | 2.895 | 2.74 | 2.628 | 2.544 | 2.477 | 2.423 | 2.378 | 2.34 | 2.308 | 2.256 | 2.215 | 2.155 | 2.114 | 2.071 | 2.026 | 1.999 | 1.96 | 1.94 | 1.91 | 1.891 | 1.878 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 6.449 | 4.84 | 4.164 | 3.781 | 3.531 | 3.353 | 3.22 | 3.116 | 3.032 | 2.963 | 2.906 | 2.856 | 2.777 | 2.715 | 2.626 | 2.564 | 2.501 | 2.434 | 2.394 | 2.337 | 2.308 | 2.264 | 2.236 | 2.218 |



| Numerator df | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 14 | 16 | 20 | 24 | 30 | 40 | 50 | 75 | 100 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |



Lower-tail areas for Chi-square distributions

|  | 0.005 | 0.010 | 0.025 | 0.050 | 0.950 | 0.975 | 0.990 | 0.995 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.00 | 0.00 | 0.00 | 0.00 | 3.84 | 5.02 | 6.63 | 7.88 |
| 2 | 0.01 | 0.02 | 0.05 | 0.10 | 5.99 | 7.38 | 9.21 | 10.60 |
| 3 | 0.07 | 0.11 | 0.22 | 0.35 | 7.81 | 9.35 | 11.34 | 12.84 |
| 4 | 0.21 | 0.30 | 0.48 | 0.71 | 9.49 | 11.14 | 13.28 | 14.86 |
| 5 | 0.41 | 0.55 | 0.83 | 1.15 | 11.07 | 12.83 | 15.09 | 16.75 |
| 6 | 0.68 | 0.87 | 1.24 | 1.64 | 12.59 | 14.45 | 16.81 | 18.55 |
| 7 | 0.99 | 1.24 | 1.69 | 2.17 | 14.07 | 16.01 | 18.48 | 20.28 |
| 8 | 1.34 | 1.65 | 2.18 | 2.73 | 15.51 | 17.53 | 20.09 | 21.95 |
| 9 | 1.73 | 2.09 | 2.70 | 3.33 | 16.92 | 19.02 | 21.67 | 23.59 |
| 10 | 2.16 | 2.56 | 3.25 | 3.94 | 18.31 | 20.48 | 23.21 | 25.19 |
| 11 | 2.60 | 3.05 | 3.82 | 4.57 | 19.68 | 21.92 | 24.72 | 26.76 |
| 12 | 3.07 | 3.57 | 4.40 | 5.23 | 21.03 | 23.34 | 26.22 | 28.30 |
| 13 | 3.57 | 4.11 | 5.01 | 5.89 | 22.36 | 24.74 | 27.69 | 29.82 |
| 14 | 4.07 | 4.66 | 5.63 | 6.57 | 23.68 | 26.12 | 29.14 | 31.32 |
| 15 | 4.60 | 5.23 | 6.26 | 7.26 | 25.00 | 27.49 | 30.58 | 32.80 |
| 16 | 5.14 | 5.81 | 6.91 | 7.96 | 26.30 | 28.85 | 32.00 | 34.27 |
| 17 | 5.70 | 6.41 | 7.56 | 8.67 | 27.59 | 30.19 | 33.41 | 35.72 |
| 18 | 6.26 | 7.01 | 8.23 | 9.39 | 28.87 | 31.53 | 34.81 | 37.16 |
| 19 | 6.84 | 7.63 | 8.91 | 10.12 | 30.14 | 32.85 | 36.19 | 38.58 |
| 20 | 7.43 | 8.26 | 9.59 | 10.85 | 31.41 | 34.17 | 37.57 | 40.00 |
| 21 | 8.03 | 8.90 | 10.28 | 11.59 | 32.67 | 35.48 | 38.93 | 41.40 |
| 22 | 8.64 | 9.54 | 10.98 | 12.34 | 33.92 | 36.78 | 40.29 | 42.80 |
| 23 | 9.26 | 10.20 | 11.69 | 13.09 | 35.17 | 38.08 | 41.64 | 44.18 |
| 24 | 9.89 | 10.86 | 12.40 | 13.85 | 36.42 | 39.36 | 42.98 | 45.56 |
| 25 | 10.52 | 11.52 | 13.12 | 14.61 | 37.65 | 40.65 | 44.31 | 46.93 |
| 26 | 11.16 | 12.20 | 13.84 | 15.38 | 38.89 | 41.92 | 45.64 | 48.29 |
| 27 | 11.81 | 12.88 | 14.57 | 16.15 | 40.11 | 43.19 | 46.96 | 49.64 |
| 28 | 12.46 | 13.56 | 15.31 | 16.93 | 41.34 | 44.46 | 48.28 | 50.99 |
| 29 | 13.12 | 14.26 | 16.05 | 17.71 | 42.56 | 45.72 | 49.59 | 52.34 |
| 30 | 13.79 | 14.95 | 16.79 | 18.49 | 43.77 | 46.98 | 50.89 | 53.67 |
| 31 | 14.46 | 15.66 | 17.54 | 19.28 | 44.99 | 48.23 | 52.19 | 55.00 |
| 32 | 15.13 | 16.36 | 18.29 | 20.07 | 46.19 | 49.48 | 53.49 | 56.33 |
| 33 | 15.82 | 17.07 | 19.05 | 20.87 | 47.40 | 50.73 | 54.78 | 57.65 |
| 34 | 16.50 | 17.79 | 19.81 | 21.66 | 48.60 | 51.97 | 56.06 | 58.96 |
| 35 | 17.19 | 18.51 | 20.57 | 22.47 | 49.80 | 53.20 | 57.34 | 60.27 |
| 36 | 17.89 | 19.23 | 21.34 | 23.27 | 51.00 | 54.44 | 58.62 | 61.58 |
| 37 | 18.59 | 19.96 | 22.11 | 24.07 | 52.19 | 55.67 | 59.89 | 62.88 |
| 38 | 19.29 | 20.69 | 22.88 | 24.88 | 53.38 | 56.90 | 61.16 | 64.18 |
| 39 | 20.00 | 21.43 | 23.65 | 25.70 | 54.57 | 58.12 | 62.43 | 65.48 |
| 40 | 20.71 | 22.16 | 24.43 | 26.51 | 55.76 | 59.34 | 63.69 | 66.77 |
| 41 | 21.42 | 22.91 | 25.21 | 27.33 | 56.94 | 60.56 | 64.95 | 68.05 |
| 42 | 22.14 | 23.65 | 26.00 | 28.14 | 58.12 | 61.78 | 66.21 | 69.34 |
| 43 | 22.86 | 24.40 | 26.79 | 28.96 | 59.30 | 62.99 | 67.46 | 70.62 |
| 44 | 23.58 | 25.15 | 27.57 | 29.79 | 60.48 | 64.20 | 68.71 | 71.89 |
| 45 | 24.31 | 25.90 | 28.37 | 30.61 | 61.66 | 65.41 | 69.96 | 73.17 |
| 46 | 25.04 | 26.66 | 29.16 | 31.44 | 62.83 | 66.62 | 71.20 | 74.44 |
| 47 | 25.77 | 27.42 | 29.96 | 32.27 | 64.00 | 67.82 | 72.44 | 75.70 |
| 48 | 26.51 | 28.18 | 30.75 | 33.10 | 65.17 | 69.02 | 73.68 | 76.97 |
| 49 | 27.25 | 28.94 | 31.55 | 33.93 | 66.34 | 70.22 | 74.92 | 78.23 |
| 50 | 27.99 | 29.71 | 32.36 | 34.76 | 67.50 | 71.42 | 76.15 | 79.49 |

For use on the CAS exams

| $\mathrm{n} 2=3$ |  |  |  |  |
| ---: | :---: | ---: | ---: | ---: |
|  |  |  |  |  |
| U0 |  | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ |
|  | 0 | 0.250 | 0.100 | 0.050 |
| 1 | 0.500 | 0.200 | 0.100 |  |
| 2 |  | 0.400 | 0.200 |  |
| 3 |  | 0.600 | 0.350 |  |
|  |  |  |  | 0.500 |

$n 2=4$

U0 |  | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ |
| ---: | ---: | ---: | ---: | ---: |
| 0 | 0.200 | 0.067 | 0.029 | 0.014 |
| 1 | 0.400 | 0.134 | 0.057 | 0.029 |
| 2 | 0.600 | 0.267 | 0.114 | 0.057 |
| 3 |  | 0.400 | 0.200 | 0.100 |
| 4 |  | 0.600 | 0.314 | 0.172 |
| 5 |  |  | 0.428 | 0.243 |
| 6 |  |  | 0.572 | 0.343 |
| 7 |  |  |  | 0.443 |
| 8 |  |  |  | 0.557 |

| $\mathrm{n} 2=5$ |  |  |  |  |  | $=6$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ |
| 0 | 0.167 | 0.048 | 0.018 | 0.008 | 0.004 | 0 | 0.143 | 0.036 | 0.012 | 0.005 | 0.002 | 0.001 |
| 1 | 0.334 | 0.095 | 0.036 | 0.016 | 0.008 | 1 | 0.286 | 0.071 | 0.024 | 0.009 | 0.004 | 0.002 |
| 2 | 0.500 | 0.191 | 0.071 | 0.032 | 0.016 | 2 | 0.429 | 0.143 | 0.048 | 0.019 | 0.009 | 0.004 |
| 3 |  | 0.286 | 0.125 | 0.056 | 0.028 | 3 | 0.571 | 0.214 | 0.083 | 0.033 | 0.015 | 0.008 |
| 4 |  | 0.429 | 0.197 | 0.095 | 0.048 | 4 |  | 0.321 | 0.131 | 0.057 | 0.026 | 0.013 |
| 5 |  | 0.571 | 0.286 | 0.143 | 0.075 | 5 |  | 0.428 | 0.191 | 0.086 | 0.041 | 0.021 |
| 6 |  |  | 0.393 | 0.206 | 0.111 | 6 |  | 0.572 | 0.274 | 0.129 | 0.063 | 0.033 |
| 7 |  |  | 0.500 | 0.278 | 0.155 | 7 |  |  | 0.357 | 0.176 | 0.089 | 0.047 |
| 8 |  |  |  | 0.365 | 0.210 | 8 |  |  | 0.452 | 0.238 | 0.123 | 0.066 |
| 9 |  |  |  | 0.452 | 0.274 | 9 |  |  | 0.548 | 0.305 | 0.164 | 0.090 |
| 10 |  |  |  | 0.548 | 0.345 | 10 |  |  |  | 0.381 | 0.214 | 0.120 |
| 11 |  |  |  |  | 0.421 | 11 |  |  |  | 0.457 | 0.268 | 0.155 |
| 12 |  |  |  |  | 0.500 | 12 |  |  |  | 0.543 | 0.331 | 0.197 |
|  |  |  |  |  |  | 13 |  |  |  |  | 0.396 | 0.242 |
|  |  |  |  |  |  | 14 |  |  |  |  | 0.465 | 0.294 |
|  |  |  |  |  |  | 15 |  |  |  |  | 0.535 | 0.349 |
|  |  |  |  |  |  | 16 |  |  |  |  |  | 0.409 |
|  |  |  |  |  |  | 17 |  |  |  |  |  | 0.469 |
|  |  |  |  |  |  | 18 |  |  |  |  |  | 0.531 |

$\mathrm{n} 2=7$

U0 |  | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ |
| ---: | :--- | ---: | :--- | ---: | ---: | ---: | ---: |
| 0 | 0.125 | 0.028 | 0.008 | 0.003 | 0.001 | 0.001 | 0.000 |
| 1 | 0.250 | 0.056 | 0.017 | 0.006 | 0.003 | 0.001 | 0.001 |
| 2 | 0.375 | 0.111 | 0.033 | 0.012 | 0.005 | 0.002 | 0.001 |
| 3 | 0.500 | 0.167 | 0.058 | 0.021 | 0.009 | 0.004 | 0.002 |
| 4 |  | 0.250 | 0.092 | 0.036 | 0.015 | 0.007 | 0.004 |
| 5 |  | 0.333 | 0.133 | 0.054 | 0.024 | 0.011 | 0.005 |
| 6 |  | 0.444 | 0.192 | 0.082 | 0.037 | 0.018 | 0.009 |
| 7 |  | 0.556 | 0.258 | 0.115 | 0.053 | 0.026 | 0.013 |
| 8 |  |  | 0.333 | 0.158 | 0.074 | 0.037 | 0.019 |
| 9 |  |  | 0.417 | 0.206 | 0.101 | 0.051 | 0.027 |
| 10 |  |  | 0.500 | 0.264 | 0.134 | 0.069 | 0.036 |
| 11 |  |  |  | 0.324 | 0.172 | 0.090 | 0.049 |
| 12 |  |  |  | 0.394 | 0.216 | 0.117 | 0.064 |
| 13 |  |  |  | 0.464 | 0.265 | 0.148 | 0.083 |
| 14 |  |  |  |  | 0.536 | 0.319 | 0.183 |
| 15 |  |  |  |  | 0.378 | 0.223 | 0.133 |
| 16 |  |  |  |  | 0.500 | 0.367 | 0.159 |
| 17 |  |  |  |  |  | 0.365 | 0.191 |
| 18 |  |  |  |  |  | 0.228 |  |
| 19 |  |  |  |  |  | 0.418 | 0.268 |
| 20 |  |  |  |  |  | 0.310 |  |
| 21 |  |  |  |  |  |  | 0.355 |
| 22 |  |  |  |  |  |  | 0.403 |
| 23 |  |  |  |  |  |  |  |
| 24 |  |  |  |  |  |  |  |

| $\mathrm{n} 2=8$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ | $\mathrm{n} 1=8$ |
| 0 | 0.111 | 0.022 | 0.006 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 1 | 0.223 | 0.044 | 0.012 | 0.004 | 0.002 | 0.001 | 0.000 | 0.000 |
| 2 | 0.334 | 0.089 | 0.024 | 0.008 | 0.003 | 0.001 | 0.001 | 0.000 |
| 3 | 0.445 | 0.133 | 0.042 | 0.014 | 0.005 | 0.002 | 0.001 | 0.001 |
| 4 | 0.555 | 0.200 | 0.067 | 0.024 | 0.009 | 0.004 | 0.002 | 0.001 |
| 5 |  | 0.267 | 0.097 | 0.036 | 0.015 | 0.006 | 0.003 | 0.002 |
| 6 |  | 0.355 | 0.139 | 0.054 | 0.023 | 0.010 | 0.005 | 0.002 |
| 7 |  | 0.444 | 0.188 | 0.077 | 0.033 | 0.015 | 0.007 | 0.004 |
| 8 |  | 0.556 | 0.249 | 0.107 | 0.047 | 0.021 | 0.010 | 0.005 |
| 9 |  |  | 0.315 | 0.141 | 0.064 | 0.030 | 0.014 | 0.007 |
| 10 |  |  | 0.388 | 0.184 | 0.086 | 0.041 | 0.020 | 0.011 |
| 11 |  |  | 0.461 | 0.230 | 0.111 | 0.054 | 0.027 | 0.014 |
| 12 |  |  | 0.539 | 0.285 | 0.142 | 0.071 | 0.036 | 0.019 |
| 13 |  |  |  | 0.341 | 0.177 | 0.090 | 0.047 | 0.025 |
| 14 |  |  |  | 0.404 | 0.218 | 0.114 | 0.060 | 0.033 |
| 15 |  |  |  | 0.467 | 0.262 | 0.141 | 0.076 | 0.042 |
| 16 |  |  |  | 0.533 | 0.311 | 0.173 | 0.095 | 0.052 |
| 17 |  |  |  |  | 0.362 | 0.207 | 0.116 | 0.065 |
| 18 |  |  |  |  | 0.416 | 0.245 | 0.140 | 0.080 |
| 19 |  |  |  |  | 0.472 | 0.286 | 0.168 | 0.097 |
| 20 |  |  |  |  | 0.528 | 0.331 | 0.198 | 0.117 |
| 21 |  |  |  |  |  | 0.377 | 0.232 | 0.139 |
| 22 |  |  |  |  |  | 0.426 | 0.268 | 0.164 |
| 23 |  |  |  |  |  | 0.475 | 0.306 | 0.191 |
| 24 |  |  |  |  |  | 0.525 | 0.347 | 0.221 |
| 25 |  |  |  |  |  |  | 0.389 | 0.253 |
| 26 |  |  |  |  |  |  | 0.433 | 0.287 |
| 27 |  |  |  |  |  |  | 0.477 | 0.323 |
| 28 |  |  |  |  |  |  | 0.523 | 0.361 |
| 29 |  |  |  |  |  |  |  | 0.400 |
| 30 |  |  |  |  |  |  |  | 0.440 |
| 31 |  |  |  |  |  |  |  | 0.480 |
| 32 |  |  |  |  |  |  |  | 0.520 |


| $\mathrm{n} 2=9$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ | $\mathrm{n} 1=8$ | $\mathrm{n} 1=9$ |
| 0 | 0.100 | 0.018 | 0.004 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 1 | 0.200 | 0.036 | 0.009 | 0.003 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | 0.300 | 0.073 | 0.018 | 0.006 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 3 | 0.400 | 0.109 | 0.032 | 0.010 | 0.004 | 0.001 | 0.001 | 0.000 | 0.000 |
| 4 | 0.500 | 0.164 | 0.050 | 0.017 | 0.006 | 0.002 | 0.001 | 0.001 | 0.000 |
| 5 |  | 0.218 | 0.073 | 0.025 | 0.009 | 0.004 | 0.002 | 0.001 | 0.000 |
| 6 |  | 0.291 | 0.105 | 0.038 | 0.014 | 0.006 | 0.003 | 0.001 | 0.001 |
| 7 |  | 0.364 | 0.141 | 0.053 | 0.021 | 0.009 | 0.004 | 0.002 | 0.001 |
| 8 |  | 0.455 | 0.186 | 0.074 | 0.030 | 0.013 | 0.006 | 0.003 | 0.001 |
| 9 |  | 0.545 | 0.241 | 0.099 | 0.041 | 0.018 | 0.008 | 0.004 | 0.002 |
| 10 |  |  | 0.300 | 0.130 | 0.056 | 0.025 | 0.011 | 0.005 | 0.003 |
| 11 |  |  | 0.364 | 0.165 | 0.073 | 0.033 | 0.016 | 0.008 | 0.004 |
| 12 |  |  | 0.432 | 0.207 | 0.095 | 0.044 | 0.021 | 0.010 | 0.005 |
| 13 |  |  | 0.500 | 0.252 | 0.120 | 0.057 | 0.027 | 0.014 | 0.007 |
| 14 |  |  |  | 0.302 | 0.149 | 0.072 | 0.036 | 0.018 | 0.009 |
| 15 |  |  |  | 0.356 | 0.182 | 0.090 | 0.045 | 0.023 | 0.012 |
| 16 |  |  |  | 0.413 | 0.219 | 0.112 | 0.057 | 0.029 | 0.016 |
| 17 |  |  |  | 0.470 | 0.259 | 0.136 | 0.071 | 0.037 | 0.020 |
| 18 |  |  |  | 0.530 | 0.303 | 0.164 | 0.087 | 0.046 | 0.025 |
| 19 |  |  |  |  | 0.350 | 0.194 | 0.105 | 0.057 | 0.031 |
| 20 |  |  |  |  | 0.399 | 0.228 | 0.126 | 0.069 | 0.039 |
| 21 |  |  |  |  | 0.449 | 0.264 | 0.150 | 0.084 | 0.047 |
| 22 |  |  |  |  | 0.500 | 0.303 | 0.176 | 0.100 | 0.057 |
| 23 |  |  |  |  |  | 0.344 | 0.204 | 0.118 | 0.068 |
| 24 |  |  |  |  |  | 0.388 | 0.235 | 0.138 | 0.081 |
| 25 |  |  |  |  |  | 0.432 | 0.268 | 0.160 | 0.095 |
| 26 |  |  |  |  |  | 0.477 | 0.303 | 0.185 | 0.111 |
| 27 |  |  |  |  |  | 0.523 | 0.340 | 0.211 | 0.129 |
| 28 |  |  |  |  |  |  | 0.379 | 0.240 | 0.149 |
| 29 |  |  |  |  |  |  | 0.419 | 0.270 | 0.170 |
| 30 |  |  |  |  |  |  | 0.459 | 0.303 | 0.193 |
| 31 |  |  |  |  |  |  | 0.500 | 0.336 | 0.218 |
| 32 |  |  |  |  |  |  |  | 0.371 | 0.245 |
| 33 |  |  |  |  |  |  |  | 0.407 | 0.273 |
| 34 |  |  |  |  |  |  |  | 0.444 | 0.302 |
| 35 |  |  |  |  |  |  |  | 0.481 | 0.333 |
| 36 |  |  |  |  |  |  |  | 0.519 | 0.365 |
| 37 |  |  |  |  |  |  |  |  | 0.398 |
| 38 |  |  |  |  |  |  |  |  | 0.431 |
| 39 |  |  |  |  |  |  |  |  | 0.466 |
| 40 |  |  |  |  |  |  |  |  | 0.500 |


| U0 | $\mathrm{n} 1=1$ | $\mathrm{n} 1=2$ | $\mathrm{n} 1=3$ | $\mathrm{n} 1=4$ | $\mathrm{n} 1=5$ | $\mathrm{n} 1=6$ | $\mathrm{n} 1=7$ | $\mathrm{n} 1=8$ | $\mathrm{n} 1=9$ | $\mathrm{n} 1=10$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.091 | 0.015 | 0.004 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| 1 | 0.182 | 0.030 | 0.007 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | 0.273 | 0.061 | 0.014 | 0.004 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 3 | 0.364 | 0.091 | 0.024 | 0.007 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 |
| 4 | 0.455 | 0.137 | 0.038 | 0.012 | 0.004 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 5 | 0.545 | 0.182 | 0.056 | 0.018 | 0.006 | 0.002 | 0.001 | 0.000 | 0.000 | 0.000 |
| 6 |  | 0.243 | 0.081 | 0.027 | 0.010 | 0.004 | 0.002 | 0.001 | 0.000 | 0.000 |
| 7 |  | 0.303 | 0.108 | 0.038 | 0.014 | 0.005 | 0.002 | 0.001 | 0.001 | 0.000 |
| 8 |  | 0.379 | 0.143 | 0.053 | 0.020 | 0.008 | 0.003 | 0.002 | 0.001 | 0.000 |
| 9 |  | 0.455 | 0.185 | 0.071 | 0.027 | 0.011 | 0.005 | 0.002 | 0.001 | 0.001 |
| 10 |  | 0.545 | 0.234 | 0.094 | 0.037 | 0.016 | 0.007 | 0.003 | 0.002 | 0.001 |
| 11 |  |  | 0.287 | 0.120 | 0.049 | 0.021 | 0.009 | 0.004 | 0.002 | 0.001 |
| 12 |  |  | 0.346 | 0.152 | 0.065 | 0.028 | 0.012 | 0.006 | 0.003 | 0.001 |
| 13 |  |  | 0.405 | 0.187 | 0.082 | 0.036 | 0.017 | 0.008 | 0.004 | 0.002 |
| 14 |  |  | 0.469 | 0.227 | 0.103 | 0.047 | 0.021 | 0.010 | 0.005 | 0.003 |
| 15 |  |  | 0.531 | 0.270 | 0.127 | 0.059 | 0.028 | 0.013 | 0.007 | 0.003 |
| 16 |  |  |  | 0.318 | 0.155 | 0.074 | 0.035 | 0.017 | 0.009 | 0.004 |
| 17 |  |  |  | 0.367 | 0.185 | 0.090 | 0.044 | 0.022 | 0.011 | 0.006 |
| 18 |  |  |  | 0.420 | 0.220 | 0.110 | 0.054 | 0.027 | 0.014 | 0.007 |
| 19 |  |  |  | 0.472 | 0.256 | 0.132 | 0.066 | 0.034 | 0.018 | 0.009 |
| 20 |  |  |  | 0.527 | 0.297 | 0.157 | 0.081 | 0.042 | 0.022 | 0.012 |
| 21 |  |  |  |  | 0.339 | 0.184 | 0.096 | 0.051 | 0.027 | 0.014 |
| 22 |  |  |  |  | 0.384 | 0.214 | 0.115 | 0.061 | 0.033 | 0.018 |
| 23 |  |  |  |  | 0.429 | 0.246 | 0.135 | 0.073 | 0.039 | 0.021 |
| 24 |  |  |  |  | 0.476 | 0.281 | 0.157 | 0.086 | 0.047 | 0.026 |
| 25 |  |  |  |  | 0.524 | 0.318 | 0.182 | 0.102 | 0.056 | 0.031 |
| 26 |  |  |  |  |  | 0.356 | 0.208 | 0.119 | 0.067 | 0.038 |
| 27 |  |  |  |  |  | 0.396 | 0.237 | 0.137 | 0.078 | 0.044 |
| 28 |  |  |  |  |  | 0.438 | 0.268 | 0.158 | 0.091 | 0.052 |
| 29 |  |  |  |  |  | 0.479 | 0.300 | 0.180 | 0.105 | 0.061 |
| 30 |  |  |  |  |  | 0.521 | 0.334 | 0.204 | 0.121 | 0.071 |
| 31 |  |  |  |  |  |  | 0.369 | 0.230 | 0.139 | 0.083 |
| 32 |  |  |  |  |  |  | 0.406 | 0.257 | 0.158 | 0.095 |
| 33 |  |  |  |  |  |  | 0.443 | 0.286 | 0.178 | 0.109 |
| 34 |  |  |  |  |  |  | 0.481 | 0.317 | 0.200 | 0.123 |
| 35 |  |  |  |  |  |  | 0.519 | 0.348 | 0.223 | 0.140 |
| 36 |  |  |  |  |  |  |  | 0.381 | 0.248 | 0.157 |
| 37 |  |  |  |  |  |  |  | 0.414 | 0.274 | 0.176 |
| 38 |  |  |  |  |  |  |  | 0.448 | 0.302 | 0.196 |
| 39 |  |  |  |  |  |  |  | 0.483 | 0.330 | 0.218 |
| 40 |  |  |  |  |  |  |  | 0.517 | 0.360 | 0.241 |
| 41 |  |  |  |  |  |  |  |  | 0.390 | 0.264 |
| 42 |  |  |  |  |  |  |  |  | 0.421 | 0.289 |
| 43 |  |  |  |  |  |  |  |  | 0.452 | 0.315 |
| 44 |  |  |  |  |  |  |  |  | 0.484 | 0.342 |
| 45 |  |  |  |  |  |  |  |  | 0.516 | 0.370 |
| 46 |  |  |  |  |  |  |  |  |  | 0.398 |
| 47 |  |  |  |  |  |  |  |  |  | 0.427 |
| 48 |  |  |  |  |  |  |  |  |  | 0.456 |
| 49 |  |  |  |  |  |  |  |  |  | 0.485 |
| 50 |  |  |  |  |  |  |  |  |  | 0.515 |

Here is the rule for Exam S which will be printed for the Fall 2015 Syllabus:
*Note: To receive credit for the new Exam S on Statistics and Probabilistic Models during the transition, the candidate must have credit for Exams ST and LC ${ }^{\dagger}$ and the Applied Statistical Methods VEE. At the time of transition, if a candidate has credit for either Exam ST or Exam LC, but not both, the candidate will be allowed to take just the exam for which he or she is missing credit in order to obtain partial credit for the new exam. This option will be available for a transition period of two sittings after the official conversion to the new education structure (i.e., Fall 2015 and Spring 2016). Credit for the Applied Statistical Methods VEE will be accepted through August 2016. After August 2016, candidates must contact the CAS Office to verify and add the Applied Statistical Methods VEE, or course equivalent, credit to their transcript. If the candidate has not completed Exam ST, Exam LC, and the Applied Statistical Methods VEE by this date, the candidate will need to pass the full version of Exam $S$ to receive credit. Candidates with credit for neither Exam ST nor Exam LC on August 31, 2015 will not be permitted to sit for Exams ST or LC during the transition period and will need to pass the full version of Exam $S$ to receive credit.

The following table summarizes the above:

| Candidate Credit on August 31, 2015 |  |  | Action Required by August 31, 2016 to Earn Credit for new Exam S |
| :---: | :---: | :---: | :---: |
| Exam ST | Exam LC | Stats VEE |  |
| $\checkmark$ | $\checkmark$ | $\checkmark$ | Credit granted. No candidate action required. |
| $\checkmark$ | $\checkmark$ |  | Complete the Applied Statistical Methods VEE. |
| $\checkmark$ |  | $\checkmark$ | Pass Exam LC. |
| $\checkmark$ |  |  | Pass Exam LC and complete the Applied Statistical Methods VEE. |
|  | $\checkmark$ | $\checkmark$ | Pass Exam ST. |
|  | $\checkmark$ |  | Pass Exam ST and complete the Applied Statistical Methods VEE. |
|  |  | $\checkmark$ | Candidate must take full Exam S. |
|  |  |  | Candidate must take full Exam S. |

${ }^{\dagger}$ The CAS has also granted waivers for Exam LC to candidates who have:

- passed SOA Exam MLC;
- passed the Institute and Faculty of Actuaries (U.K.), Actuaries Institute (Australia), or Institute of Actuaries of IndiaSubject CT5; or
- passed the Actuarial Society of South Africa Course A203; or
- received a waiver granted by the Canadian Institute of Actuaries University Accreditation Program.

For those students who have credit for Exam ST by August 31, 2015, the CAS will continue to grant Exam LC waivers through December 31, 2016 for exams passed before August 31, 2016.

## CAS Online Course 1, Second Edition Risk Management and Insurance Operations

Notice about the $1^{\text {st }}$ and $2^{\text {nd }}$ Editions<br>1st Edition: The original CAS Online Course 1 (CA1, $1^{\text {st }}$ Edition) was revised effective September 1, 2014. Although the 1st Edition of CA1 is no longer available for sale after August 31, 2014, for those who purchased the $1^{\text {st }}$ Edition, the original online course will be available and unchanged through June 15,2015 . The exam for the $1^{\text {st }}$ Edition of CA1 will be offered through June 15, 2015.<br>2nd Edition: CA1, $2^{\text {nd }}$ Edition, is the current version that was effective on September 1, 2014. Exams on this content will be offered for the first time on January 15, 2015.

Risk Management and Insurance Operations is called Online Course 1 by the CAS and CA1, $2^{\text {nd }}$ Edition, by The Institutes. (Prometric lists this course as CAS1 on its Web site under The Institutes.)

Online Course 1/CA1 prepares CAS candidates for a two-hour, seventy-five-point multiple-choice examination. The online course and exam were developed collaboratively with The Institutes. The online course is available through the Casualty Actuarial Society Online Courses Web Page on The Institutes' Web Site. Similarly, the exam is administered by The Institutes at Prometric test centers during four, two-month testing windows annually.
The CAS will grant a waiver of CAS Online Course 1 to those who have the Chartered Property Casualty Underwriter (CPCU) designation.
The study material for CAS Course 1/CA1 is contained in the online course access. The fee for access to the online course includes one attempt at passing the exam. Candidates are required to purchase the online course to obtain access to the exam. Exam retakes may be purchased separately if needed.

Purchasing the course requires that candidates declare the testing window in which they are planning to take the exam. To register for the exam, a candidate must:

- Call The Institutes at (800) 644-2101 or (610) 644-2100, extension 6000, to register for the exam itself. This will place the candidate on an eligibility list for Prometric.
- Then make an appointment with Prometric for a specific date and time during the testing window. Early registration for the exam is strongly encouraged as seats fill quickly. There is a $\$ 105$ fee for changing testing windows.
- Schedule your appointment when you know you will be ready to sit for the exam. Effective January 1,2012 , Prometric will charge a $\$ 50$ fee to candidates who reschedule their appointments between 3 to 12 business days of a test date. Changes to the appointment date/time are not permitted within 3 business days of the appointment.
Questions or concerns regarding CAS Online Course 1/CA1 should be directed to The Institutes' Customer Service Department at (800) 644-2101 or (610) 644-2100, extension 6000, or CustomerService@TheInstitutes.org.


## Assignment 1: Introduction to Risk Management

| MODULE TITLE | LEARNING OBJECTIVE |
| :---: | :---: |
| Understanding and Quantifying Risk | Describe each of the following in the context of risk: <br> - Uncertainty <br> - Possibility <br> - Possibility compared with probability |
| Classifications of Risk | Explain how the following classifications of risk apply and how they help in risk management: <br> - Pure and speculative risk <br> - Subjective and objective risk <br> - Diversifiable and nondiversifiable risk <br> - Quadrants of risk (hazard, operational, financial, and strategic) |
| Financial Consequences of Risk | Describe the three financial consequences of risk. |
| Basic Purpose and Scope of Risk Management | Describe the basic purpose and scope of risk management in terms of the following: <br> - How risk management is practiced by individuals and organizations <br> - The basic distinction between traditional risk management and enterprise-wide risk management |
| Loss Exposures | Describe the following elements of property, liability, personnel, and net income loss exposures: <br> - Assets exposed to loss <br> - Causes of loss, including associated hazards <br> - Financial consequences of loss |
| Risk Management Benefits | Describe the benefits of risk management and how it reduces the financial consequences of risk for individuals, organizations, and society. |
| Risk Management Program Goals | Summarize pre-loss and post-loss risk management program goals and the conflicts that can arise as they are implemented. |
| The Risk Management Process | Describe each of the steps in the risk management process |

## Assignment 2: Risk Control

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Risk Control Techniques | Describe the six categories of risk control techniques <br> in terms of the following: |
|  | - Whether each reduces loss frequency, reduces loss <br> severity, or makes losses more predictable <br> -How each can be used to address a particular loss <br> exposure <br> - How they differ from one another |


| Risk Control Goals | Explain how an organization can use risk control <br> techniques and measures to achieve the following risk <br> control goals: <br> - Implement effective and efficient risk control |
| :--- | :--- |
|  | measures <br> - Comply with legal requirements <br> - Promote life safety <br> - Ensure business continuity |
| Application of Risk Control Techniques | Explain how risk control techniques can be applied to <br> property, liability, personnel, and net income loss <br> exposures. |
| Business Continuity Management | Describe business continuity management in terms of <br> its scope, the process used to implement it, and the <br> contents of a typical business continuity plan. |

Assignment 3: Risk Financing

| MODULE TITLE | LEARNING OBJECTIVE |
| :---: | :---: |
| Risk Financing Goals | Explain how individuals or organizations can achieve their overall and risk management goals by fulfilling the following risk financing goals: <br> - Pay for losses <br> - Manage the cost of risk <br> - Manage cash flow variability <br> - Maintain an appropriate level of liquidity <br> - Comply with legal requirements |
| Retention and Transfer | Describe the following aspects of retention and transfer: <br> - Retention funding measures <br> - Limitations on risk transfer measures <br> - The advantages of both retention and transfer |
| Selecting Appropriate Risk Financing Measures | Explain how the following can affect the selection of the appropriate risk financing measure: <br> - Ability of a risk financing measure to meet risk financing goals <br> - Loss exposure characteristics <br> - Characteristics specific to an individual or organization |
| Risk Financing Measures | Explain how an organization meets its risk financing goals by using the following risk financing measures: <br> - Guaranteed cost insurance <br> - Self-insurance <br> - Large deductible plans <br> - Captives <br> - Finite risk plans <br> - Pools <br> - Retrospective rating plans <br> - Hold-harmless agreements <br> - Capital market solutions |

## Assignment 4: Enterprise-Wide Risk Management

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Traditional Risk Management Versus ERM | Contrast traditional risk management and ERM. |
| Improving Strategic Decision Making With <br> ERM | Explain how an organization can improve its strategic <br> decision making by incorporating enterprise-wide <br> risk management (ERM). |
| ERM in Approaching Business Uncertainties | Explain why ERM is an effective approach to use to <br> face business uncertainties. |
| Major Risk Management Frameworks and <br> Standards | Summarize the main risk management frameworks <br> and standards. |

Assignment 5: Insurance as a Risk Management Technique

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| How Insurance Reduces Risk | Explain how insurance reduces risk through pooling. |
| Benefits of Insurance | Explain how insurance benefits individuals, <br> organizations, and society. |
| Characteristics of an Ideally Insurable Loss <br> Exposure | Explain why each of the six characteristics of an <br> ideally insurable loss exposure is important to the <br> insurance mechanism. |
| Insurability of Commercial Loss Exposures | Explain how the six characteristics of an ideally <br> insurable loss exposure apply to commercial loss <br> exposures. |
| Insurability of Personal Loss Exposures | Explain how the six characteristics of an ideally <br> insurable loss exposure apply to personal loss <br> exposures. |
| Government Insurance Programs | Explain how state and federal governments are <br> involved in the insurance market and the rationale <br> for, and level of, their involvement. |

Assignment 6: Overview of Insurance Operations

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Classifications of Insurers | Explain how insurers have organized to provide <br> property-casualty insurance. |
| Insurer Goals | Describe the major goals of an insurer. |
| Constraints on Achieving Insurer Goals | Describe the internal and external constraints that <br> impede insurers from achieving their major goals. |
| Measuring Insurer Performance | Describe the measurements used to evaluate how <br> successful an insurer is at meeting its established <br> goals. |
| Functional View of Insurance | Describe the core and supporting functions performed <br> by insurers. |

Assignment 7: Insurance Marketing and Distribution

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Property-Casualty Insurance Marketplace | Describe the following attributes of the competitive <br> property-casualty insurance marketplace: <br> distinguishing characteristics of insurance customers, <br> insurer marketing differentiations, and unique factors <br> in the insurance marketplace. |
| Insurer Marketing Activities | Explain how typical insurer marketing activities are <br> performed and why they are performed. |
| Insurance Distributions Systems and Channels | Describe the main types of insurance distribution <br> systems and channels, including the principal <br> characteristics that distinguish one distribution <br> system from another. |
| Functions of Insurance Producers | Describe the functions performed by insurance <br> producers. |
| Distribution System and Channel Selection for <br> Insurance Marketing | Describe the key factors an insurer should evaluate <br> during the distribution-system and distribution- <br> channel selection process. |

## Assignment 8: The Underwriting Function

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Purpose of Underwriting | Describe the purpose of underwriting. |
| Underwriting Activities | Describe the underwriting activities typically <br> performed by line and staff underwriters. |
| Underwriting Authority | Describe the importance of compliance with <br> underwriting authority in individual account <br> selection. |
| Constraints in Establishing Underwriting Policy | Describe the constraining factors considered in the <br> establishment of underwriting policy. |
| Implementing Underwriting Policy | Describe the purposes that underwriting guidelines <br> and underwriting audits serve. |
| Steps in the Underwriting Process | Summarize the steps in the underwriting process and <br> the purpose of each. |
| Measuring Underwriting Results | Explain how an insurer's underwriting results are <br> measured and how financial measures can be <br> distorted. |

## Assignment 9: Underwriting Property and Liability Insurance

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Underwriting Property Insurance Using the <br> COPE Model | Describe in detail each of the COPE factors used to <br> evaluate property loss exposures. |
| Property Policy Provision Underwriting <br> Considerations | Explain how insurable interest, policy provisions for <br> valuing losses, and insurance to value affect a loss <br> payment amount under property insurance. |


| Measures of Potential Loss Severity | Explain how underwriters use policy amount, amount <br> subject, normal loss expectancy (NLE), probable <br> maximum loss (PML), and maximum foreseeable <br> loss (MFL) to measure potential loss severity. |
| :--- | :--- |
| Underwriting Business Income and Extra <br> Expense Coverage | Describe the underwriting considerations for business <br> income and extra expense coverage. |
| Underwriting Commercial Crime Insurance | Describe the underwriting considerations and risk <br> control techniques associated with employee <br> dishonesty and crimes committed by others. |
| Underwriting Commercial General Liability <br> Insurance | Describe the loss exposures and the underwriting <br> considerations for commercial general liability <br> insurance. |
| Underwriting Personal and Commercial Auto <br> Insurance | Describe the underwriting considerations for personal <br> and commercial auto insurance. |
| Underwriting Workers Compensation Insurance | Describe the underwriting considerations for workers <br> compensation insurance. |
| Underwriting Umbrella and Excess Liability | Describe the underwriting considerations for <br> umbrella and excess liability insurance. |
| Insurance |  |

Assignment 10: Risk Control and Premium Auditing

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Insurer Risk Control Goals | Describe the goals of insurer risk control activities. |
| Risk Control Services Provided by Insurers | Describe the risk control services provided by <br> insurers. |
| Cooperation Between Risk Control and Other <br> Insurer Functions | Explain how risk control cooperates with other <br> insurer functions. |
| Reasons for Premium Auditing | Explain why premium audits are conducted. |
| Premium Auditing Process | Describe the premium auditing process. |
| Importance of Accurate Premium Audits | Explain why premium audits must be accurate. |
| Premium Auditing Contributions | Explain how premium auditing contributes to other <br> insurer functions. |

Assignment 11: The Claim Function

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Overview of the Claim Function | Identify the goals of the claim function; the users of <br> claim information, and the parties with whom claim <br> personnel interact. |
| Claim Department Structure, Personnel, and <br> Performance | Describe the claim departments in terms of the <br> following: <br> - How they are structured |
|  | - The types and functions of claim personnel |
|  | - How their performance can be measured |


| Measures Used to Ensure Regulatory | Explain how the following measures are used to <br> ensure regulatory compliance: <br> Compliance |
| :--- | :--- |
|  | Claim guidelines, policies, and procedures <br> - Controls <br> - <br> - Supervisor and manager reviews <br> Claim audits |
| Activities in the Claim Handling Process | Summarize the activities performed in the claim <br> handling process and the purpose of each. |
| The Framework for Coverage Analysis and the <br> Claim Handling Process Case Study | Given a claim scenario, demonstrate how a claim <br> reprentative can use the claim handling process and <br> framework for coverage analysis to resolve a claim. |
|  |  |

## Assignment 12: Adjusting Property and Liability Claims

| MODULE TITLE | LEARNING ObJECTIVE |
| :---: | :---: |
| Property Claim Handling Process | Explain how and why the activities in the framework for handling property claims are accomplished. |
| Handling Specific Types of Property Claims | Describe the challenges of handling the following types of property claims: <br> - Residential dwelling claims <br> - Residential personal property claims <br> - Commercial structure claims <br> - Business income claims <br> - Merchandise claims <br> - Transportation and bailment claims <br> - Catastrophe claims |
| Liability Claim Handling Process | Explain how and why the activities in the framework for handling a liability claim are accomplished. |
| Handling Specific Types of Liability Claims | Describe the challenges of handling each of the following types of claims: <br> - Auto bodily injury liability claims <br> - Auto property damage claims <br> - Premises liability claims <br> - Operations liability claims <br> - Products liability claims <br> - Workers compensation claims <br> - Professional liability claims |

## Assignment 13: Reinsurance Principles and Concepts

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Reinsurance and Its Functions | Describe reinsurance and its principal functions. |
| Reinsurance Sources | Describe the three sources of reinsurance. |
| Reinsurance Transactions | Describe treaty reinsurance and facultative <br> reinsurance. |
| Types of Pro Rata and Excess of Loss <br> Reinsurance | Summarize the types of pro rata reinsurance and <br> excess of loss reinsurance and their uses. |
| Alternatives to Traditional Reinsurance | Describe finite risk reinsurance and other methods <br> that rely on capital markets as alternatives to <br> traditional and non-traditional reinsurance. |
| Reinsurance Program Design | Describe the factors that should be considered in the <br> design of a reinsurance program. |
| Reinsurance Program Design Case Studies | Given a case, identify the reinsurance needs of an <br> insurer and recommend an appropriate reinsurance <br> program to meet those needs. |

Assignment 14: Insurer Strategic Management

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Strategic Management Process | Describe the strategic management process. |
| The Five Forces and SWOT Methods of <br> Analyzing the Environment | Explain how the Five Forces and SWOT methods can <br> be used to analyze the environment in which an <br> insurer operates. |
| Determining Strategy at Different <br> Organizational Levels | Explain how strategies are developed at the corporate, <br> business, functional, and operational levels. |
| Insurers Global Expansion | Describe the strategic reasons, considerations, and <br> approaches for insurers to expand their operations <br> globally. |
| Strategic Management Case Study | Given information about an insurer's business <br> strategies, conduct a SWOT analysis to evaluate its <br> strategy. |

## Assignment 15: The Underwriting Cycle

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| The Insurance Underwriting Cycle | Describe the phases of the insurance underwriting <br> cycle and the strategies normally used by insurers and <br> producers during each phase. |
| Financial Factors Influencing the Underwriting <br> Cycle | Explain how the following financial factors influence <br> underwriting cycles <br> - Investment income <br> - Capacity <br> - Return on equity <br> - Cash flow |
| Effects of Supply and Demand on the <br> Underwriting Cycle | Explain how the theory of demand and supply applies <br> to insurance and the underwriting cycle. |

## Assignment 16: Actuarial Data Management

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Data Quality | Summarize <br> - The concepts of data quality and information <br> quality <br> - The impact of data quality on the actuarial work <br> product |
| Principles of Data Quality | Given a principle of data quality, provide an example <br> that illustrates the principle. |
| Data Quality—ASOP No. 23 | Given a concept from the Actuarial Standard of <br> Practice No. 23, provide an example of its application <br> or use. |
| Life Cycle for Insurance Data | For each step in the life cycle for insurance data, <br> describe the purpose, the responsible parties, and <br> errors typically encountered. |
| Metadata | Summarize metadata including: <br> - How metadata are defined <br> - The actuary's role in creating and sharing |
| metadata |  |
| - How metadata are shared across an organization |  |
| - The data collected under different statistical plans |  |$|$| The Need for Aggregate Insurance Statistical |
| :--- |
| Explain the regulatory and business needs for <br> statistical data. |
| Types of Statistical Plans |
| Summarize the relationship of Statistical Plans to <br> insurance rating elements and the two basic types of <br> Statistical Plans: <br> - Summary-based Statistical Plans <br> - Transaction-based Statistical Plans |
| Insurance Data Elements: Date Fields and <br> Amount Fields in Statistical Plans |
| Describe the functions of the date field and amount <br> field data elements in a statistical plan. |


| Insurance Data Elements: Classification or <br> Rating Variable Fields and Exposure Data <br> Elements | Describe the following statistical plan data elements <br> by line of business: <br> - Classification and Rating Elements <br> - Exposure |
| :--- | :--- |
| Techniques and Applications to Improve <br> Information Quality | Summarize the following data quality analysis <br> concepts: <br> - Exploratory data analysis <br>  <br> - Data cubes <br> - Identifying missing data |
|  | - Descriptive statistics <br> - Box and whisker plots |
|  | Explain the following: <br> - The purpose and steps of data auditing <br> - An actuary's responsibility in assessing data <br> reasonability |
| Auditing Data and the Actuary's Responsibility |  |

## Study Materials for CAS Online Course 1

The online course itself contains learning objectives and all the educational material to meet these objectives and successfully complete the exam. The course fee includes one attempt at the exam.

The following printed materials are supplemental and may also be purchased from The Institutes, but are not required:

- Textbook contains material that is identical to the online course-only in a hardcopy format.
- Review Notes is a condensed version of the textbook.
- Course Guide contains sample questions and answers.
- Flashcards contain key words and phrases.

The materials described above may be purchased individually or in various package combinations.
Questions about potentially defective questions or material should be directed to The Institutes' Customer Service Department at (800) 644-2101 or (610) 644-2100, extension 6000, or CustomerService@TheInstitutes.org.

## Publisher and Distributor

CAS Online Course 1/CA1 is available through The Institutes.
The Institutes, 720 Providence Road, Suite 100, Malvern, PA 19355-3433; telephone: (800) 6442101 or (610) 644-2100 extension 6000; E-mail: CustomerService@TheInstitutes.org; Web Site Page for CAS Online Courses: www.aicpcu.org/cas.htm.

## Exam Results

Candidates taking this computer-based test will receive unofficial pass/fail results at the conclusion of their exam. The unofficial pass/fail result will be displayed on the computer screen at the conclusion of the exam. In most test centers, a printed copy of the candidate's unofficial pass/fail result will be available upon completion of the computer-based test from the proctor in the administrative area outside the testing room. The candidate, however, should carefully read the result that is displayed on the computer screen at the conclusion of the exam.
When the official grades have been processed, candidates will receive an e-mail from The Institutes stating that their grades are available. Candidates may then log into their account on The Institutes Web Site (www.TheInstitutes.org) to access their grades. The grade report for each candidate will show the candidate's overall score on the exam in ten point increments (e.g., 60 to $69 \%, 70$ to $79 \%$, and so on). It will similarly show the candidate's performance by assignment using those same ten point increments.

Numeric scores are not released. Approximately three weeks after the close of the testing window, The Institutes will send a copy of the grades directly to the CAS Office to be added to the candidates’ admissions records.

# CAS Online Course 2, Third Edition Insurance Accounting, Coverage Analysis, Insurance Law, and Insurance Regulation 

Notice about the 3rd Edition of CA2 Replacing the 2nd Edition of CA2

3rd Edition: The CA2, 3rd Edition, reflects changes in commercial coverage forms and the addition of a new assignment on life insurance, annuities and health insurance. The 3rd Edition will be available on September 1, 2015. The exams on this content will be offered for the first time on January 15, 2016

2nd Edition: The CA2, 2nd Edition will no longer be sold after August 31, 2015. Candidates who have purchased the 2nd edition will be able to access the course and take the exam on this content through June 15, 2016. (Please note: CAS Candidates have access to the online modules for one year from the date of purchase.)

Insurance Accounting, Coverage Analysis, Insurance Law, and Insurance Regulation is called Online Course 2 by the CAS and CA2, $3{ }^{\text {rd }}$ Edition, by The Institutes. Prometric lists this course as CAS2 on its website under The Institutes.
Online Course 2/CA2 prepares CAS candidates for a two-hour, seventy-five-point, multiple-choice examination. The online course and exam were developed collaboratively with The Institutes. The online course is available through the Casualty Actuarial Society Online Courses Web page on The Institutes' website. Similarly, the exam is administered by The Institutes at Prometric test centers during four, two-month testing windows annually.
The study material for CAS Course 2/CA2 is contained in the online course access. The fee for access to the online course includes one attempt at passing the exam. Candidates are required to purchase the online course to obtain access to the exam. Exam retakes may be purchased separately if needed.
Purchasing the course requires that candidates declare the testing window in which they are planning to take the exam. To register for the exam, a candidate must:

- Call The Institutes at (800) 644-2101 or (610) 644-2100, extension 6000 , to register for the exam itself. This will place the candidate on an eligibility list for Prometric.
- Then make an appointment with Prometric for a specific date and time during the testing window. Early registration for the exam is strongly encouraged as seats fill quickly. There is a $\$ 110$ fee for changing testing windows.
- Schedule your appointment when you know you will be ready to sit for the exam. Prometric will charge a $\$ 50$ fee to candidates who reschedule their appointments between 3 to 12 business days of a test date. Changes to the appointment date/time are not permitted within 3 business days of the appointment.

Questions or concerns regarding CAS Online Course 2/CA2 should be directed to The Institutes' Customer Service Department at (800) 644-2101 or (610) 644-2100, extension 6000, or CustomerService@TheInstitutes.org.

Assignment 1: Introductory Insurance Accounting

| MODULE TITLE | LEARNING ObJECTIVE |
| :---: | :---: |
| Qualitative Accounting Information Criteria | Explain the following qualitative accounting information criteria: <br> - Understandability <br> - Relevance <br> - Reliability <br> - Comparability and consistency <br> - Lack of bias <br> - Cost-benefit effectiveness |
| Types of Accounting Frameworks | Describe the frameworks and the intended users and focus of each of the following sets of accounting frameworks: <br> - Generally Accepted Accounting Principles (GAAP) accounting <br> - Regulatory/supervisory accounting <br> - Tax accounting <br> - Management accounting |
| Accounting Frameworks and Rule Hierarchies | Explain the concept of a rule hierarchy and the sources of the following accounting frameworks: <br> - Generally Accepted Accounting Principles (GAAP) <br> - Regulatory/supervisory accounting <br> - Tax accounting |
| Selected Accounting Concepts | Summarize the following accounting concepts: <br> - Fair value versus historical cost <br> - Recognition versus measurement <br> - Deferral-matching versus asset-liability <br> - Impairment <br> - Revenue recognition <br> - Reporting segment <br> - Liquidation versus going concern <br> - Change in accounting principle versus change in accounting estimate <br> - Principle-based versus rule-based |
| Fundamentals of Insurer Financial Statements | Describe the purpose and primary components of these key schedules of an insurer's financial statements: <br> - Balance sheet <br> - Income statement <br> - Cash flow statement <br> - Notes and disclosures |
| Premium Accounting-Revenue Recognition | Explain how and when insurers recognize premium revenue in their financial statements under deferralmatching and asset-liability approaches. |


| Premium Accounting-Types of Written Premium | Distinguish between the various types of written premium and policy transactions that may not be classified as premium. |
| :---: | :---: |
| Other Premium Accounting Issues | Summarize the implications of these premium accounting issues: <br> - Financing-premiums versus service charges <br> - Earning premium before it is written <br> - Extended reporting endorsements (definite versus indefinite periods) <br> - Reinsurance lags <br> - Large deductible credits |
| Unearned Premium | Summarize the purpose of unearned premium and these issues associated with how premiums are earned over time: <br> - Pro rata and non-pro rata approaches to earning premium <br> - Multiyear policies <br> - Liability adequacy test and the premium deficiency reserve |
| The Relationship Between Loss Reserves and the Unearned Premium Reserve | Explain the relationship between loss reserves and the unearned premium reserve. |
| Loss and Loss Adjustment Expense Accounting | Describe the following issues related to loss and loss adjustment expense (LAE) accounting: <br> - Loss accounts <br> - Loss cycle <br> - Paid loss versus cash payment <br> - Recoverable amounts <br> - Accounting for discounted reserves <br> - Self-insurer issues |
| Reinsurance Accounting Basics | Explain the accounting and financial reporting considerations, including how values in insurers' financial reports are influenced by lags in the reporting of reinsurance transactions and bordereau reporting, for these types of reinsurance: <br> - Assumed reinsurance <br> - Ceded reinsurance <br> - Commutations <br> - Prospective versus retroactive reinsurance |
| Deposit Accounting | Explain the conditions under which an accounting framework may require deposit accounting for an insurance contract, and the operation of three general forms of deposit accounting rules. |

## Assignment 2: Insurance Policy Analysis

| MODULE TITLE | LEARNING OBJECTIVE |
| :---: | :---: |
| Distinguishing Characteristics of Insurance Policies | Describe the following characteristics of insurance policies, including common exceptions to these characteristics. <br> - Indemnity <br> - Utmost good faith <br> - Fortuitous losses <br> - Contract of adhesion <br> - Exchange of unequal amounts <br> - Conditional <br> - Nontransferable |
| Structure of Insurance Policies | Describe these approaches to insurance policy structure and how they can affect policy analysis: <br> - Self-contained and modular policies <br> - Preprinted and manuscript policies <br> - Standard and nonstandard forms <br> - Endorsements and other related documents |
| Types of Policy Provisions | Describe the purpose(s) and characteristics of each of these types of policy provisions in a propertycasualty insurance policy: <br> - Declarations <br> - Definitions <br> - Insuring agreements <br> - Exclusions <br> - Conditions <br> - Miscellaneous provisions |
| Insurance Policy Analysis | Describe the primary methods of insurance policy analysis. |

## Assignment 3: Common Policy Concepts

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Insurable Interest | Given a case, evaluate one or more entities' insurable <br> interests. |
| Insurance to Value | Explain why insurance to value is important to <br> property insurers, how insurers encourage insurance <br> to value, and what insureds can do to address the <br> problems associated with maintaining insurance to <br> value. |
| Property Valuation Methods | Explain how property is valued under each of the <br> following valuation methods in property insurance <br> policies: <br> $\bullet$ Actual cash value <br> - Replacement cost <br> $\bullet$ - Agreed value <br> - Functional valuation |


| Valuation of Liability Claims | Explain how the amount payable for a claim covered <br> under a liability insurance policy is determined. |
| :--- | :--- |
| Reasons for Property Deductibles | Explain how deductibles in property insurance benefit <br> the insured. |
| Liability Deductibles and Self-Insured <br> Retentions | Explain when and why deductibles and self-insured <br> retentions are appropriate for use in liability <br> insurance. |
| Other Sources Of Recovery | Describe the multiple sources of recovery that may be <br> available to an insurance policyholder for a covered <br> loss. |

Assignment 4: Personal Auto Policy: Liability, Medical Payments, and Uninsured Motorist Coverage

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Overview of the Personal Auto Policy | Summarize the sections of the Personal Auto Policy. |
| Declarations | Identify the types of information typically contained <br> on the declarations page of a personal auto policy. |
| Definitions | Define the words and phrases included in the <br> definitions section of the Personal Auto Policy. |
| Part A - Liability Coverage | Summarize each of the provisions in Part A- <br> Liability Coverage of the Personal Auto Policy. |
| Part A - Liability Coverage Case | Given a case describing an auto liability claim, <br> determine whether Part A-Liability Coverage of the <br> Personal Auto Policy would cover the claim and, if <br> so, the amount the insurer would pay for the claim. |
| Part B - Medical Payments Coverage | Summarize each of the provisions in Part B- <br> Medical Payments Coverage of the Personal Auto <br> Policy. |
| Part B - Medical Payments Coverage Case | Given a case describing an auto medical payments <br> claim, determine whether Part B - Medical Payments <br> Coverage of the Personal Auto Policy would cover <br> the claim and, if so, the amount the insurer would pay <br> for the claim. |
| Part C - Uninsured Motorists Coverage | Summarize each of the provisions in Part C-- <br> Uninsured Motorists Coverage of the Personal Auto <br> Policy. |
| UM/UIM Endorsements and State Variations | Describe underinsured motorists coverage in terms <br> of: <br> - Its purpose <br> - The ways in which it can vary by state |
| Part C - Uninsured Motorists Coverage Case | Given a case describing an uninsured motorists claim, <br> determine whether Part C-Uninsured Motorists <br> Coverage of the Personal Auto Policy would cover <br> the claim and, if so, the amount the insurer would pay <br> for the claim. |

## Assignment 5: Personal Auto Policy: Physical Damage, Duties After an Accident, Endorsements, General Provisions

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Part D - Damage to Your Auto Coverage | Summarize each of the provisions in Part D-- <br> Damage to Your Auto of the Personal Auto Policy. |
| Part D - Damage to Your Auto Coverage Case | Given a case describing an auto physical damage <br> claim, determine whether Part D-Coverage for <br> Damage to Your Auto of the Personal Auto Policy <br> would cover the claim and, if so, the amount the <br> insurer would pay for the claim. |
| Part E - Duties After an Accident or Loss | Identify the insured's duties following an auto <br> accident or loss (Part E) covered by the Personal <br> Auto Policy. |
| Part F - General Provisions | Summarize each of the general provisions in Part F of <br> the Personal Auto Policy. |
| Common Endorsements to the Personal Auto <br> Policy | Identify the Personal Auto Policy endorsements that <br> are used to handle common auto loss exposures. |
| Personal Auto Coverage Case | Given a case describing an auto claim, determine <br> whether the Personal Auto Policy would cover the <br> claim and, if so, the amount the insurer would pay for <br> the claim. |

Assignment 6: Homeowners Property Coverage

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| ISO Homeowners Program | Describe how individuals and families can use the <br> ISO Homeowners insurance program to address their <br> personal risk management needs. |
| Homeowners Program Structure | Summarize these aspects of the 2011 Homeowners <br> Program: <br> - Structure of the Homeowners Policy (HO-3) <br> - <br> - Key changes in the ISO 2011 Program Revision <br> - Factors important to rating homeowners <br> insurance |
| HO-3 Section I - Property Coverages | Determine whether the 2011 HO-3 policy provisions <br> in the following Section I - Property Coverages <br> provide coverage for a given loss or loss exposure: <br> - Coverage A - Dwelling |
|  | - Coverage B - Other Structures <br> - Coverage C - Personal Property |
|  | - Coverage D - Loss of Use <br> - Additional Coverages |
| HO-3 Section I - Perils Insured Against and <br> Exclusions | Summarize each of the 2011 HO-3 policy provisions: <br> - Perils Insured Against <br> - Exclusions |


| HO-3 Section I - Conditions | Summarize each of the 2011 HO-3 policy provisions <br> in Section I - Conditions. |
| :--- | :--- |
| 2011 HO-3 Section I - Property Coverage Case | Given a scenario describing a homeowners property <br> claim, determine whether the 2011 HO-3 Policy <br> Section I - Property Coverages would cover the <br> claim, and if so, the amount the insurer would pay for <br> the claim. |

Assignment 7: Homeowners Liability, Conditions, Coverage Forms, and Endorsements

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| HO-3 Section II - Liability Coverages | Determine whether the 2011 HO-3 Policy provisions <br> in the following Section II - Liability Coverages <br> provide coverage for a given loss or loss exposure: <br> - Coverage E - Personal Liability <br> - Coverage F - Medical Payments to Others <br> - Additional Coverages |
| HO-3 Section II - Exclusions | Determine whether one or more exclusions preclude <br> the coverage provided by Section II of the 2011 HO-3 <br> policy provisions in Section II - Exclusions. |
| HO-3 Section II - Conditions | Summarize each of these 2011 HO-3 policy <br> provisions: <br> - Conditions applicable to Section II |
|  | - Conditions applicable to Sections I and II |
| Homeowners Coverage Forms and Causes of the coverage provided by each of the <br> Loss Comparison Summary to the HO-3 <br> following 2011 Homeowners policies to the coverage <br> provided by the 2011 HO-3 policy: <br> $\bullet$ <br> - HO-2 Broad Form |  |
| - HO-5 Comprehensive Form |  |
| - HO-4 Contents Broad Form |  |
| - HO-6 Unit-Owners Form |  |
| - HO-8 Modified Coverage Form |  |

## Assignment 8: Life Insurance, Annuities and Health Insurance

| MODULE TITLE | LEARNING OBJECTIVE |
| :---: | :---: |
| Premature Death Loss Exposures | Describe the financial impact of the premature death personal loss exposure on the following types of family structures: <br> - Singles without children <br> - Single-parent families <br> - Two-income families <br> - Traditional families <br> - Blended families <br> - Sandwiched families |
| Types of Life Insurance | Summarize the various types of life insurance. |
| Sources of Life Insurance | Summarize the distinguishing characteristics of life insurance provided by each of the following sources: individual life insurance, group life insurance, and government-provided life insurance. |
| Common Life Insurance Contractual Provisions and Riders | Summarize the common life insurance contractual provisions and riders. |
| Individual Annuities | Summarize the various types of individual annuities. |
| Disability and Health-Related Personal Loss Exposures | Describe the financial impact of disability and other health-related personal loss exposures on individuals and families. |
| Disability Income Insurance | Summarize the distinguishing characteristics of each of the following types of disability income insurance: <br> - Individual disability income insurance <br> - Group disability income insurance <br> - Social Security disability income program |
| Health Insurance Plans | Describe the characteristics of the following nongovernment programs for providing healthcare benefits: <br> - Traditional health insurance plans <br> - Managed-care plans <br> - Consumer-directed health plans |

## Assignment 9: Commercial Property Insurance, Part I

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Overview of the Commercial Property Insurance | Describe commercial property insurance in terms of <br> these elements: |
|  | - The major categories of loss exposures that can <br> be covered |
|  | The components of a commercial property <br> coverage part |


| BPP Covered Property | Determine whether a described item of property qualifies as Covered Property under one or more of these categories in the Building and Personal Property Coverage Form: <br> - Building <br> - Your Business Personal Property <br> - Personal Property of Others |
| :---: | :---: |
| BPP Additional Coverages and Coverage Extensions | Determine which of the additional coverages and coverage extensions of the Building and Personal Property Coverage Form apply to a described loss. |
| Causes of Loss-Basic Form and Broad Form | Determine whether the cause of a described loss is a covered cause of loss under either the Causes of Loss-Basic Form or the Causes of Loss-Broad Form. |
| Cause of Loss-Special Form | Determine whether the cause of a described loss is a Covered Cause of Loss under the Causes of LossSpecial Form. |
| BPP Limits of Insurance and Deductibles | Apply the Limits of Insurance and Deductible provisions of the Building and Personal Property Coverage Form to a described loss. |

## Assignment 10: Commercial Property Insurance, Part II

| MODULE TITLE | LEARNING ObJECTIVE |
| :---: | :---: |
| BPP Loss Conditions and Additional Conditions | Explain how each of the Loss Conditions and Additional Conditions affects coverage under the Building and Personal Property Coverage Form. |
| BPP: Optional Coverages | Explain how each of the following optional coverages described in the BPP modifies the basic coverage of the BPP: <br> - Agreed Value <br> - Inflation Guard <br> - Replacement Cost <br> - Extension of Replacement Cost to Personal Property of Others |
| Commercial Property Conditions | Summarize each of the Commercial Property Conditions. |
| Common Policy Conditions | Explain how each of the conditions contained in the Common Policy Conditions affects coverage under a commercial property coverage part. |
| Commercial Property Endorsements | Explain how each of these documents modifies the Building and Personal Property Coverage Form: <br> - Ordinance or Law Coverage endorsement <br> - Spoilage Coverage endorsement <br> - Flood Coverage endorsement <br> - Earthquake and Volcanic Eruption Coverage endorsement <br> - Peak Season Limit of Insurance endorsement <br> - Value Reporting Form |


| Factors Affecting Commercial Property <br> Premiums | Identify the factors that affect commercial property <br> insurance premiums |
| :--- | :--- |
| Determining Whether the BPP Covers a Loss | Given a case, determine whether, and for what <br> amount, a described loss would be covered by a <br> commercial property coverage part that includes the <br> Building and Personal Property Coverage Form and <br> any of the three causes of loss forms. |

## Assignment 11: Commercial General Liability Insurance, Part I

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Overview of Commercial General Liability <br> Insurance | Describe commercial general liability insurance in <br> terms of these elements: <br> The types of losses that can be covered by <br> general liability insurance <br> The components of a commercial general liability <br> coverage part |
| CGL Coverage A-Insuring Agreement | Determine whether a described claim meets the <br> conditions imposed by the Coverage A insuring <br> agreement of the Commercial General Liability <br> Coverage Form (occurrence version). |
| CGL Coverage A-Exclusions | Determine whether any of the exclusions applicable <br> to Coverage A of the Commercial General Liability <br> Coverage Form eliminate coverage for a described <br> claim. |
| CGL Coverage B-Personal and Advertising <br> Injury Liability | Determine whether a described claim meets the <br> conditions imposed by the Coverage B insuring <br> agreement of the Commercial General Liability <br> Coverage Form and whether any of the Coverage B <br> exclusions eliminate coverage for the claim. |
| CGL Coverage C-Medical Payments | Determine whether a described claim meets the <br> conditions imposed by the Coverage C insuring <br> agreement of the Commercial General Liability <br> Coverage Form, and whether any of the Coverage C <br> exclusions eliminate coverage for the claim. |
| CGL Supplementary Payments | Summarize the supplementary payments of the <br> Commercial General Liability Coverage Form. |

## Assignment 12: Commercial General Liability Insurance, Part II

$\left.\left.\begin{array}{|l|l|}\hline \text { MODULE TITLE } & \text { LEARNING OBJECTIVE } \\ \hline \text { CGL Who Is an Insured Provisions } & \begin{array}{l}\text { Determine whether a described person organization is } \\ \text { an insured under the Commercial General Liability } \\ \text { Coverage Form. }\end{array} \\ \hline \text { CGL Limits of Insurance } & \begin{array}{l}\text { Explain how the following limits of insurance in the } \\ \text { CGL Coverage Form are applied: } \\ \bullet \text { Each occurrence limit } \\ \bullet \text { Personal and advertising injury limit } \\ \bullet \text { Damage to premises rented to you limit }\end{array} \\ & \begin{array}{l}\text { - Medical expense limit } \\ \bullet \text { General aggregate limit }\end{array} \\ \hline \text { CGL Products-completed operations aggregate limit }\end{array} \right\rvert\, \begin{array}{l}\text { Apply the Commercial General Liability Conditions } \\ \text { to claims or other interactions between the insurer } \\ \text { and the insured. }\end{array}\right\}$

## Assignment 13: Specialty Coverages

| MODULE TITLE | LEARNING OBJECTIVE |
| :---: | :---: |
| Commercial Excess and Umbrella Liability Insurance | Describe commercial excess liability insurance and commercial umbrella liability insurance in terms of these characteristics: <br> - The three basic types of commercial excess liability insurance <br> - The provisions commonly found in commercial umbrella liability policies that distinguish them from other types of commercial liability policies |
| Professional Liability and Management Liability Insurance | Describe professional liability insurance and management liability insurance in terms of these aspects: <br> - How they differ from each other <br> - How they differ from commercial general liability policies <br> - The common types of professional and management liability policies |


| Environmental Insurance | Describe the purpose and characteristics of each of these types of environmental insurance policies: <br> - Site-specific environmental impairment liability (EIL) policies <br> - Underground storage tank compliance policies <br> - Remediation stop-loss policies <br> - Contractors pollution liability policies <br> - Environmental professional errors and omissions liability policies |
| :---: | :---: |
| Aircraft Insurance | Describe aircraft insurance in terms of these characteristics: <br> - The purposes-of-use categories that insurers used to classify aircraft <br> - The coverages that can be included in an aircraft policy |
| Cyber Risk Insurance | Describe the types of losses that can be covered by each of the insuring agreements generally available in cyber risk insurance policies. |
| Insuring Foreign Operations | Explain how an organization domiciled in the United States can insure foreign loss exposures that would not be covered under standard property and liability insurance policies. |
| Terrorism Endorsements for Commercial Property and Liability Forms | Summarize the purpose and provisions of the terrorism endorsements developed by Insurance Services Office, Inc., and the National Council on Compensation Insurance, Inc. |
| Types of Surety Bonds | Summarize the guarantee provided by the particular types of surety bonds within the following bond classifications: <br> - Contract bonds <br> - License and permit bonds <br> - Public official bonds <br> - Court bonds <br> - Miscellaneous bonds |

## Assignment 14: Insurance Law, Part I

\(\left.\left.$$
\begin{array}{|l|l|}\hline \text { MODULE TITLE } & \text { LEARNING OBJECTIVE } \\
\hline \text { Tort Law } & \begin{array}{l}\text { Explain these concepts: } \\
\bullet \text { Tort as distinguished from other offenses } \\
\bullet \text { Classifications of tort } \\
\bullet\end{array} \\
\hline \text { Negligence Application of laws in tort cases }\end{array}
$$ \right\rvert\, \begin{array}{l}Describe negligence claims in terms of: <br>
\bullet The elements of negligence <br>

\bullet The required proof of negligence\end{array}\right]\)| Describe these defenses against negligence claims: |
| :--- |
| Comparative negligence, releases and exculpatory |
| clauses, immunity, statutes of limitations and repose, |
| tortfeasor's capacity. |


| Intentional Torts Part 1 of 2 | Describe these intentional torts, the circumstances under which they can occur, and common defenses to them: <br> - Battery <br> - Assault <br> - False imprisonment and false arrest <br> - Intentional infliction of emotional distress <br> - Defamation (libel and slander) <br> - Invasion of the right of privacy |
| :---: | :---: |
| Intentional Torts Part 2 of 2 | Describe these intentional torts, the circumstances under which they can occur, and common defenses to them: <br> - Fraud <br> - Bad faith, or outrage <br> - Interference with relationships between others <br> - Misuse of legal process <br> - Trespass <br> - Nuisance <br> - Conversion |
| Liability in Extraordinary Circumstances | Explain how liability attaches as a result of the unique circumstances presented by the following: <br> - Ultrahazardous activities <br> - Ownership and/or possession of animals <br> - Escape of toxic substances |

## Assignment 15: Insurance Law, Part II

| MODULE TITLE | LEARNING OBJECTIVE |
| :---: | :---: |
| Products Liability | Describe these causes of action for products liability and the possible defenses to them: <br> - Misrepresentation <br> - Breach of warranty <br> - Strict liability and negligence |
| Professional Liability | Describe professional and directors and officers liability. |
| Damages in Tort Suits | Describe the types of damages a court can award a plaintiff for a tort claim. |
| Equitable Remedies | Explain these equitable remedies: <br> - Specific performance <br> - Injunction |
| Factors Affecting Amounts and Payment of Damages | Summarize these legal concepts related to negligence damages and remedies: <br> - Restitutio in integrum <br> - Mitigation of damages <br> - Aggravated damages <br> - Structured settlements and judgments |


| Liability Concepts Affecting Tort Claims | Explain how any of these concepts can affect a tort claim: <br> - Joint tortfeasor's liability <br> - Expanded liability concepts <br> - Vicarious liability <br> - Good Samaritan issues <br> - Class actions |
| :---: | :---: |
| Trends in Tort Litigation | Summarize these trends in tort litigation: <br> - Class action litigation <br> - Litigation funding <br> - Punitive damages <br> - Tort reform |

Assignment 16: Insurance Regulation

| MODULE TITLE | LEARNING OBJECTIVE |
| :--- | :--- |
| Economic Impact of the Insurance Industry | Explain the economic impact of the insurance <br> industry. |
| The Objectives of Insurance Regulation | Describe the objectives of insurance regulation. |
| The Sources of Insurance Regulation | Describe the three sources from which insurance <br> regulatory powers originate: <br> - Legislation <br> - Judicial review <br> - Administrative agencies |
| The Structure of Insurance Regulations | Describe the structure of insurance regulations. |
| Elements of Rate Regulation and Ratemaking | Describe the following elements of rate regulation <br> and ratemaking: <br> - Purpose and unique qualities of the insurance <br> industry |
|  | - Actuarial ratemaking principles and considerations <br> in rate regulation |
|  | - Insurance advisory organizations |
| Types of Rate Regulations | Compare the following types of rate regulation: <br> - Prior approval <br> - File and use |
|  | - Use and file <br> - Open competition <br> - Flex rating |
| Effects of Rate Regulation on Insurers | Summarize the effects of rate regulation on these <br> aspects of insurance: <br> - Resources required for complying with rate <br> regulations |
| - The underwriting cycle |  |
| - Insurers' decision making regarding where to |  |
| operate |  |

## Study Materials for CAS Online Course 2

The online course itself contains learning objectives and all the educational material to meet these objectives and successfully complete the exam. The course fee includes one attempt at the exam.

The following printed materials are supplemental and may also be purchased from The Institutes, but are not required:

- Textbook contains material that is identical to the online course-only in a hardcopy format.
- Review Notes is a condensed version of the textbook.
- Course Guide contains sample questions and answers.
- Flashcards contain key words and phrases.

The materials described above may be purchased individually or in various package combinations.
Questions about potentially defective questions or material should be directed to The Institutes' Customer Service Department at (800) 644-2101 or (610) 644-2100, extension 6000, or CustomerService@TheInstitutes.org.

## Publisher and Distributor

CAS Online Course 2/CA2, 3rd Edition is available through The Institutes.
The Institutes, 720 Providence Road, Suite 100, Malvern, PA 19355-3433; telephone: (800) 6442101 or (610) 644-2100 extension 6000; e-mail: CustomerService@TheInstitutes.org; Web page for CAS Online Courses: www.aicpcu.org/cas.htm.

## Exam Results

Candidates taking this computer-based test will receive unofficial pass/fail results at the conclusion of their exam. The unofficial pass/fail result will be displayed on the computer screen at the conclusion of the exam. In most test centers, a printed copy of the candidate's unofficial pass/fail result will be available upon completion of the computer-based test from the proctor in the administrative area outside the testing room. The candidate, however, should carefully read the result that is displayed on the computer screen at the conclusion of the exam.

When the official grades have been processed, candidates will receive an e-mail from The Institutes stating that their grades are available. Candidates may then log into their account on The Institutes website (www.TheInstitutes.org) to access their grades. The grade report for each candidate will show the candidate's overall score on the exam in ten point increments (e.g., 60 to $69 \%, 70$ to $79 \%$, and so on). It will similarly show the candidate's performance by assignment using those same ten point increments. Numeric scores are not released. Approximately three weeks after the close of the testing window, The Institutes will send a copy of the grades directly to the CAS Office to be added to the candidates' admissions records.

## 2015 Exam 5 Syllabus Basic Techniques for Ratemaking and Estimating Claim Liabilities

The syllabus for this four-hour exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain conceptually in the context of an examination.

KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.

Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.

Items marked with a bold SK constitute the 2015 CAS Exam 5 Study Kit that may be purchased from the CAS Online Store. Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from the CAS website.

Please check the "Syllabus Updates" section of the CAS Website for any changes to the Syllabus.

## A. Basic Techniques for Ratemaking

## Range of weight for Section A: 50-60 percent

This section introduces the general principles of ratemaking as well as specific details regarding data requirements, calculations, key assumptions, and implementation-related issues. Candidates require a thorough understanding of basic ratemaking so that they will be able to analyze data, select appropriate techniques, and develop solutions to problems. This section addresses the advantages and disadvantages of the various ratemaking techniques as they are applied to specific situations and different lines of business. Classification of insureds for the purpose of risk stratification and other important ratemaking topics, such as coinsurance and catastrophe provisions, are also examined in this section.
Candidates are also expected to be knowledgeable in the calculation of policy premiums using manual rate pages. Excerpts from the ISO Personal Automobile Manual will be provided with the examination. Candidates are not required to memorize the details, but will be expected to be able to use them during the examination. Since they will be included with the examination, candidates will not be allowed to bring copies of the documents into the examination room.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1. Calculate a policy premium for a specified <br> risk using the rate pages provided. <br> Range of weight: $0-3$ percent | a. How to read and use manual rate pages |
| READINGS |  |
| ISO PAM <br> Werner \& Modlin, Chapter 2 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |  |
| :--- | :--- | :--- |
| 2.Describe, analyze, or design the information <br> requirements for ratemaking related to <br> exposures and demonstrate the use of <br> $\quad$ exposures in ratemaking. | a. Definition of exposure base <br> b. Characteristics of exposure bases <br> c. Relationship of exposures to coverage provisions |  |
| Range of weight: 2-6 percent | d. | Organization of data: calendar year, policy year, <br> accident year |
|  | e.Written exposure versus earned exposure versus <br> in-force exposure |  |
|  | f. Role of exposures in the ratemaking process <br> g. Influence of changes in exposures |  |
| READINGS |  |  |
| Werner \& Modlin, Chapters 1-4 |  |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Describe, analyze, or design the information requirements for ratemaking related to premiums and demonstrate the use of premiums in ratemaking. <br> Range of weight: 4-8 percent | a. Organization of data: calendar year, policy year, accident year <br> b. Written premium versus earned premium versus in-force premium <br> c. Relationship between earned premium and earned exposure <br> d. Policy terms <br> e. Effect of law changes <br> f. Effect of rate changes <br> g. Determinations of and application of premium trend <br> h. Adjustment for coverage and benefit level changes <br> i. Distributional shifts and changes in volume (i.e., trend over time) <br> j. Parallelogram method <br> k. Extension of exposures |
| READINGS |  |
| ASOP 13 <br> Werner \& Modlin, Chapters 1-3, 5, and Appendic | A-D |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 4. Describe, analyze, or design the information requirements for ratemaking related to loss and loss adjustment expenses and demonstrate the use of loss and loss adjustment expenses in ratemaking. <br> Range of weight: 8-12 percent | a. Organization of the data: calendar year, policy year, accident year, report year <br> b. Policy provisions <br> c. Occurrence coverage <br> d. Claims-made coverage: <br> - report lag <br> - coverage triggers <br> - principles of claims-made policies <br> - retroactive date <br> - tail coverage <br> e. Reported losses versus paid losses <br> f. Claim counts <br> g. Loss adjustment expense (allocated and unallocated expenses) <br> h. Loss development <br> i. Frequency trend <br> j. Severity trend <br> k. Pure premium trend <br> 1. Approaches to determining trend (e.g., exponential and linear analyses) <br> m. Relationship between trend and loss development <br> n. Effect of law changes <br> o. Effect of changes in mix of business <br> p. Adjustment for coverage and benefit level changes <br> q. Credibility criteria and formulae <br> r. Large loss adjustment |


|  | s. <br> t. <br> u.Reinsurance recoveries <br> Catastrophe adjustment |
| :--- | :--- | :--- |
| READINGS |  |
| ASOP 13 |  |
| Werner \& Modlin, Chapters $1,3,6,12,16$, and Appendices A-D |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 5. Calculate the underwriting expense provisions underlying the overall rate level indication. <br> Range of weight: 0-5 percent | a. Expense categories (e.g., commission, general, other acquisition, taxes, licenses, and fees) <br> b. Sources of data and selection criteria <br> c. Profit and contingency provisions <br> d. Net cost of reinsurance <br> e. Cost of capital <br> f. Fixed expenses and variable expenses <br> g. Differences in procedures for loss adjustment expenses versus underwriting expenses |
| READINGS |  |
| Werner \& Modlin, Chapters 1, 7, and Appendices A-D |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 6. Calculate the overall rate level indication | a. Statement of Principles, CAS |
| $\quad$using the pure premium and loss ratio <br> methods and argue the merits of each. | b. Assumptions of each method <br> c. $\quad$Mechanics associated with each method <br> (including organization of the data) <br> Range of weight: 3-6 percent |
| READINGS |  |
| CAS Principles |  |
| Werner \& Modlin, Chapters 1, 8, and Appendices A-D |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 7. Describe, analyze, and validate the considerations beyond the calculated costbased estimate of the rate when selecting a final rate change to implement. <br> Range of weight: 0-5 percent | a. Calculated cost-based rate <br> b. Regulatory constraints <br> c. Operational constraints <br> d. Marketing constraints: <br> - Competitive comparisons <br> - Close ratios <br> - Retention ratios <br> - Growth <br> - Distributional analysis <br> - Policyholder dislocation analysis <br> e. Lifetime value analysis <br> f. Optimized pricing <br> g. Underwriting cycles |
| READINGS |  |
| Werner \& Modlin, Chapter 13 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 8. Explain the purpose for segregating data | a. Risk Classification Statement of Principles, AAA |
| $\quad$ into homogeneous groups and summarize | b. Criteria for selection of classification grouping |
| the considerations for determining such | c. Credibility |
| $\quad$ groups. | d. Adverse Selection |
| Range of weight: 0-5 percent | e. Efficiency of class plan |
| READINGS |  |
| AAA |  |
| Werner \& Modlin, Chapter 9 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 9. Develop rating differentials for classification and territory and relativities for deductibles and increased limits. <br> Range of weight: 8-12 percent | a. Formulae and process for each rating differential or relativity <br> b. Credibility and complements of credibility <br> c. Off balance <br> d. Capping of change <br> e. Loss elimination <br> f. Basic limits versus total limits <br> g. Layers of loss <br> h. Expense adjustments <br> i. Fundamentals of univariate and multivariate relativity analyses |
| READINGS |  |
| Werner \& Modlin, Chapters 9-12, 15 and Appendices E-F |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 10. Assess the considerations for implementing | a. Rating algorithms |
| rates to achieve an organization's goals. | b. Rating variables and differentials |
| Range of weight: 0-3 percent | c. Fixed expenses, if applicable |
|  | d. Expense fee calculation |
|  | e. Calculation of final base rates |
|  | f. Minimum premiums |
|  | g. Non-pricing solutions |
| READINGS |  |
| Werner \& Modlin, Chapter 14 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 11. Calculate premium for policies with <br> coinsurance provisions. | a. $\quad$ Definition of coinsurance |
| Range of weight: 0-5 percent | b. Insurance to value |
|  | c. Common policy provisions |
|  | d. Layers of loss |
|  | e. Coverage issues |
|  | f. Guaranteed replacement cost |
| READINGS | g. Formula |
| Werner \& Modlin, Chapter 11 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 12. Perform basic individual risk rating | a. $\quad$ Purpose of individual risk rating |
| calculations. | b. |
| Range of weight: 0-5 percent | c. |

## B. Estimating Claim Liabilities

## Range of weight for Section B: 40-50 percent

This section explores basic techniques that actuaries use to estimate unpaid claims for both insurance entities and also for non-insurance entities that retain risk. The CAS Principles and the American Academy of Actuaries' Standards of Practice related to the estimation of unpaid claims are also examined in this section.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Describe, analyze, and validate the information requirements for estimating unpaid claims. <br> Range of weight: 2-6 percent | a. Types of data and their sources <br> b. Role of homogeneity and credibility of data in the process of estimating unpaid claims <br> c. Fundamentals of different types of insurance (e.g., long tail versus short tail lines of business, low frequency versus high frequency lines) <br> d. Organization of data: calendar year, accident year, policy year, underwriting year, report year <br> e. Insurer's environment <br> f. Importance of accurate estimates of unpaid claims |
| READINGS |  |
| Friedland, Chapters 1, 3, and 4, and Appendices A and B |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 2. Build and analyze claim development triangles. <br> Range of weight: 2-6 percent | a. Purposes of the development triangle <br> b. Development triangle as a diagnostic tool <br> c. Examples and uses of diagnostic development triangles: <br> - Claim and claim count <br> - Ratio of premium to claims <br> - Average values <br> - Ratios of claims and counts |
| READINGS |  |
| Friedland, Chapters 5 and 6 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Construct and appraise unpaid claims estimates using each of the following estimation techniques: <br> - Development technique, including case outstanding technique <br> - Expected claim technique <br> - Bornhuetter-Ferguson technique <br> - Cape Cod technique <br> - Frequency-Severity techniques <br> Range of weight: 12-16 percent | a. Standards of Practice, ASOP 43 <br> b. Statement of Principles, CAS <br> c. The claim process <br> d. Assumptions of each estimation technique <br> e. Mechanics associated with each technique (including organization of the data) <br> f. Reporting and payment patterns <br> g. When each techniques works and when it does not <br> h. Key terms: case outstanding, paid claims, reported claims, incurred but not reported, ultimate claims, claims related expenses, reported and closed claim counts, claim counts closed with no payment, insurance recoverables, exposures, experience period, maturity or age, and components of unpaid claim estimates |
| READINGS |  |
| Friedland, Chapters 1-12, 15, and Appendices A-B |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 4. Assess the influence of operating changes on the estimation of unpaid claims. <br> Range of weight: $0-5$ percent | a. How internal operating changes affect estimates of unpaid claims: <br> - Claims processing <br> - Underwriting and policy provisions <br> - Marketing <br> - Coding of claim counts and/or claim related expenses <br> - Treatment of recoveries such as policyholder deductibles and salvage and subrogation <br> - Reinsurance |
| READINGS |  |
| Friedland, Part 3 (Chapters 6-15) |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 5. Adjust data and/or estimation techniques for changes in the: <br> - Internal environment (e.g., claims processes that result in shift in the adequacy of case outstanding or shift in settlement rates, change in mix of business, change in rate level) <br> - External environment (e.g., inflationary or legal environment) <br> Range of weight: 3-7 percent | a. Effect on estimation techniques due to change in: rate levels, claim ratio, mix of business <br> b. Use of trend factors and tort reform factors in estimation techniques <br> c. Identification of changes in case outstanding adequacy <br> d. Adjustment for changes in case outstanding adequacy <br> e. Identification of changes in rate of claims settlement <br> f. Adjustment for changes in rate of claims settlement |
| READINGS |  |
| Friedland, Chapters 7-14 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 6. Estimate recoveries. <br> Range of weight: 0-5 percent | a. Salvage and subrogation <br> b. Reinsurance <br> c. Key assumptions of estimation techniques |
| READINGS |  |
| Friedland, Chapter 14 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 7. Estimate unpaid claim adjustment expenses. a. $\quad$ Organization of the data <br> Range of weight: 2-7 percent b. Estimation of unpaid ALAE |  |
|  | c. Estimation of unpaid ULAE <br> d. Key assumptions of estimation techniques <br> e. Strengths and weaknesses of the estimation <br> techniques for claim related expenses  |
| READINGS |  |
| Friedland, Chapters 1, 3, 16, and 17 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 8. Appraise and validate the results of the estimation process for adequacy and reasonableness. <br> Range of weight: 4-8 percent | a. Components of evaluation: <br> - Multiple methods <br> - Explanation of differences <br> - Test statistics (e.g., claim ratios, severities, pure premiums, frequencies, indicated unpaid claims) <br> b. Monitoring and interim valuations |
| READINGS |  |
| Friedland, Chapter 15 |  |

## Complete Text References for Exam 5

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning <br> Objective | Source |
| :--- | :--- | ---: | ---: |
| Actuarial Standards Board of the American Academy of <br> Actuaries, "Actuarial Standard of Practice No. 13, Trending <br> Procedures in Property/Casualty Insurance Ratemaking." | ASOP 13 | A3, A4 | OP |
| American Academy of Actuaries Committee on Risk <br> Classification, "Risk Classification Statement of Principles," June <br> 1980. (Available at no charge from the American Academy of <br> Actuaries at (202) 223-8196 or on the Academy's Website at <br> www.actuary.org.) | AAA | A8 | OP |
| Casualty Actuarial Society Committee on Ratemaking Principles, <br> Statement of Principles Regarding Property and Casualty <br> Insurance Ratemaking, Casualty Actuarial Society, May 1988. | CAS <br> Principles | A6 | OP |
| Friedland, J.F., Estimating Unpaid Claims Using Basic <br> Techniques, Casualty Actuarial Society, Third Version, July <br> 2010. Appendices A and B are integral parts of this reading. | Friedland | B1-B8 | OP |
| Insurance Services Office, Inc., Personal Automobile Manual <br> (Effective 6-98), General Rules 1-6 only. The entire manual is <br> included for completeness. | ISO PAM | A1 | SK |
| Werner, G, and Modlin, C., Basic Ratemaking, Casualty <br> Actuarial Society, Fourth Edition, October 2010. [The <br> Appendices are an integral part of the textbook and will be used <br> for creating questions.] |  <br> Modlin | A1-A12 | OP |

## Source Key

op All text references marked as Online Publications will be available on a web page titled Complete Text References.
sk Material in the 2015 CAS Study Kit.
Items printed in red indicate an update, clarification, or change.

## Publishers and Distributors

Contact information is furnished for those who wish to purchase the text references cited for Exam 5. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

Actex Publications (Mad River Books), 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com; Website: www.actexmadriver.com.
Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Website: www.actuarialbookstore.com.
Actuarial Standards Board, American Academy of Actuaries, 475 N. Martingale Road, Suite 600, Schaumburg, IL 60173; telephone: (847) 706-3513; fax: (847) 706-3599.

Casualty Actuarial Society, 4350 N. Fairfax Drive, Suite 250, Arlington, VA 22203; telephone: (703) 276-3100; fax: (703) 276-3108; e-mail: office@casact.org; Website: www.casact.org.

SlideRule Books, P.O. Box 69, Greenland, NH 03840; telephone: (877) 407-5433 or (603) 3736140; fax: (877) 417-5433 or (603) 430-1258; Website: www.sliderulebooks.com.

## Fall 2015 Exam 6-Canada Syllabus Regulation and Financial Reporting (Nation Specific)

The syllabus for this four-hour exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain ones that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain in the context of an examination.

KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.
READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the purpose, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.

Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination - the actual weight may fall outside the published range on any particular examination.
The overall section weights should be viewed as having more significance than the weights for the individual learning objective. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objective, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this examsyllabus.
In addition, this exam assumes that the candidate has completed Online Course 2. Online Course 2 contains fundamental background material for both Section A (Regulation of Insurance and Canadian Insurance Law) and Section C (Financial Reporting and Solvency).
Items marked with a bold SK or SKU constitute the Fall 2015 Exam 6-Canada Study Kit that may be purchased from the CAS Online Store. The Fall 2015 Update to the Spring 2015 Study Kit includes only the new items marked with a bold SKU; the Update may be purchased from the CAS Online Store. Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from the CAS website.
Please check the "Syllabus Updates" section of the CAS Web Site for any changes to the Syllabus.

The inherent nature of the material addressed in this nation-specific exam makes it subject to continual development and change. It is expected that the candidates will respond to exam questions based on the current syllabus presented below. Recognizing the changing nature of law, regulation, and financial reporting requirements, however, the Examination Committee will strive to acknowledge candidates who also respond with the current state in their solutions to examination questions.

## A. Regulation of Insurance and Canadian Insurance Law

## Range of weight for Section A: 15-20 percent

Candidates should understand the role of the insurance business as a supplier of a vital service. Because of the essential and highly technical nature of insurance, a system of regulatory controls has been established requiring insurers to demonstrate that they are providing fair and reliable services in accordance with the statutes and regulations of each jurisdiction.

The material in this section encompasses Canadian and U.S. insurance legislation and regulations including their historical development. Judicial decisions affect insurance regulation and insurance benefits to the extent they interpret the law and thereby modify regulatory behavior. Candidates are presented with a number of Canadian cases that have contributed to the development of legal precedents in the area of insurance.

| IFARNING OR.IFCTIVFS <br> 1. Describe the historical development of insurance legislation and regulations, including the division of responsibility between federal and provincial/state regulators. <br> Range of weight: 2-6 percent | KNOWI FDGF STATFMFNTS <br> a. British North America Act <br> b. Privy Council <br> c. Federal and provincial regulation of insurance <br> d. Office of the Superintendent of Financial Institutions <br> e. Foreign and provincial insurance companies <br> f. Nature of Canadian insurance regulations <br> g. History of U.S. insurance regulation |
| :---: | :---: |
| READINGS |  |
| Baer and Rendall |  |
| KPMG PACICC |  |
| Mayhall |  |
| McDonald |  |
| Noonan |  |


| 1FARNING OB.JECTIVES <br> 2. Discuss the current state of insurance regulation in Canada. <br> Range of weight: 5-10 percent | KNOWIEDGF STATEMENTS <br> a. Motor vehicle injury compensation systems <br> b. Rate regulation in Canada and its effects <br> c. Examples of Canadian automobile rate filing requirements <br> d. Reforms in Ontario automobile insurance <br> e. Use of credit scoring in ratemaking and underwriting practices <br> f. Market conduct <br> g. Solvency <br> h. Corporate Governance |
| :---: | :---: |
| READINGS |  |
| AAA Credit Scores <br> Alberta <br> CIA CSOP (Ratemaking, Section 2600) <br> FSCO Private Auto <br> FSCO Reforms <br> FSCO Reg. 664 <br> FSCO UBI <br> IBC Code of Conduct <br> KPMG et al. <br> KPMG PACICC <br> KPMG Regulatory Oversight <br> OSFI Corporate Governance <br> OSFI Supervisory Framework |  |
| IFARNING OR.TFC.TIVFS <br> 3. Discuss the issues, outcome, rationale and implications of landmark decisions for the insurance industry. <br> Range of weight: 5-10 percent | KNOWI FחGF STATFMFNTS <br> a. Specific landmark court decisions cited in the Readings section <br> b. Canadian cap for non-pecuniary general damages <br> 1. Trilogy of Supreme Court of Canada decisions <br> 2. Limits on damages <br> 3. Current state of cap <br> 4. Exceptions to cap |
| READINGS |  |
| Baer and Rendall <br> BC Credit <br> Davidson <br> Landmark Legal <br> McDonald |  |


| $\begin{aligned} & \text { TFARNING RPIFCTIVES } \\ & \text { 4. Describe the litigation environment with } \\ & \text { respect to insurance. } \\ & \text { Range of weight: } 2-6 \text { percent } \end{aligned}$ | KNOWIFDGE STATFMENTS <br> a. Trends in tort litigation, including tort reform and class action suits <br> b. Mass torts (e.g., asbestos) <br> c. Types of litigation costs <br> d. Canadian litigation system vs. other systems |
| :---: | :---: |
| READINGS |  |
| AAA Mass Torts |  |
| ATRA |  |
| Harris |  |
| KPMG et al. |  |
| Rand Asbestos |  |

## B. Government and Industry Insurance Programs

## Range of weight for Section B: 15-20 percent

This section focuses primarily on the identification of major Canadian insurance programs administered by government agencies and insurance industry organizations. The candidates are expected to have an understanding of the objectives, operations, and effectiveness of the following programs:

- Flood insurance
- Agricultural Insurance
- Employment insurance
- Health care insurance
- Residual personal insurance markets (e.g., auto, property)
- Workers compensation insurance
- Pension plans
- Guaranty funds including the Canadian Property and Casualty Insurance Compensation Corporation ("PACCIC")
- Terrorism Risk Insurance

| 1.ARNING OR.IECTIVFS Describe the origin and purpose of specific government and insurance industry programs. <br> Range of weight: 5-7 percent | KNOWILEDGE STATEMENTS <br> a. Reason for inception <br> b. Major historical developments <br> c. Philosophy of program |
| :---: | :---: |
| 2. Describe the operations and risk transfer process for each government and insurance industry program listed in the introduction to Section B and their interactions with the voluntary private insurance sector. <br> Range of weight: 5-7 percent | a. Funding mechanisms and sources of funding <br> b. Allocation/assignment of exposures and associated costs <br> c. Automobile residual market participation ratios <br> d. Eligibility provisions <br> e. Claim settlement and insurance coverage provisions <br> f. Welfare (subsidization) versus insurance principles <br> g. Private response to gap in government program <br> h. Government response to gap in private program |


| 3. Evaluate the effectiveness of a government and insurance industry program (actual, as listed in the introduction to Section B, or hypothetical). <br> Range of weight: 5-7 percent | a. How to measure performance of programs: <br> - Solvency <br> - Efficiencies <br> - Stability <br> - Viability and long term prospects <br> b. How well program meets its purpose <br> c. Effect of external factors (e.g., economic conditions, weather, regulation, etc.) |
| :---: | :---: |
| READINGS |  |
| Agricultural Programs CAS <br> Dibra and Leadbetter Dutil KPMG et al. <br> Morneau Shepell <br> PACICC <br> Swiss Re <br> Webel |  |

## C. Financial Reporting and Solvency

## Range of weight for Section C: 55-60 percent

This section addresses financial reporting and solvency issues. The intent is to address Canadian and global issues related to the reporting of financial results for property and casualty insurers. The core of the syllabus focuses on Canadian issues with an overview of relevant differences in other countries.
Candidates should have detailed knowledge of the contents, purposes, and recent changes in the Canadian Annual Return, including recent guidelines issued by the Office of the Superintendent of Financial Institutions (OSFI) and the provincial regulatory authorities. Specifically, candidates are expected to be knowledgeable of the sections of the Canadian Annual Return related to financial statements (such as the balance sheet and income statement), capital statements, insurance, and reinsurance.

This section is complemented by readings on solvency monitoring systems such as the Minimum Capital Test (MCT), Dynamic Capital AdequacyTesting (DCAT), and ORSA.
1FARNINGOR.JFCTIVES

1. Describe the element and prepare the
schedules of the Canadian Annual Return.
Range of weight: $25-35$ percent

KNOWLEPGE STATEMENTS
a. OSFIAnnual Return
b. Valuation of policy liabilities in accordance with accepted actuarial practice in Canada
c. Reinsurance accounting issues including risk transfer and effect of different types of reinsurance on financial statements.
d. Commutation
e. Calculation of excess (deficiency) ratio of net claim liabilities
f. Calculation of Earthquake Reserves

| READINGS |
| :--- |
| Blanchard and Klann |
| CCIR Instructions |
| CAS Financial Reporting |
| CIA Accounting Standards |
| CIA CSOP |
| CIA Disclosure |
| CIA Discounting |
| CIA Materiality |
| CIA MfAD |
| CIA Premium Liabilities |
| CIA Reinsurance Treatment |
| CIA Runoff |
| CIA Subsequent Events |
| CIA Taxes |
| CIA Valuation |
| Freihaut and Vendetti |
| IFRS 4 |
| OSFI Annual Return I |
| OSFI Annual Return II |
| OSFI Earthquake |
| OSFI Memorandum |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 2. Evaluate the financial health of an insurance entity based on various solvency frameworks. <br> Range of weight: 25-35 percent | a. MCT formulae <br> b. Definition of the components of the MCT <br> c. DCAT <br> - Purpose <br> - Satisfactory financial condition <br> - Plausible scenarios and ripple effects <br> - Management actions <br> d. Stress testing <br> e. Internal target capital ratios <br> f. MSA ratios <br> g. Key financial measures used by rating agencies <br> h. Rules-based and principles-based solvency regulation (ORSA, MCT and Solvency II) <br> i. A.M. Best rating system and BCAR |


| READINGS |
| :--- |
| AM Best Understanding BCAR |
| AM Best Catastrophe Analysis |
| CIA CSOP |
| CIA DCAT |
| CIA Valuation |
| Feldblum |
| KPMG Solvency II |
| MSA |
| OSFI Annual Return I |
| OSFI Annual Return II |
| OSFI Framework |
| OSFI MCT |
| OSFI Stress Testing |
| OSFI Target Capital |
| OSFI ORSA |

## D. Professional Responsibilities of the Actuary in Financial Reporting

Range of weight for Section D: 10-15 percent
This section focuses on the professional responsibilities of the appointed actuary related to the reporting of financial results by property and casualty insurers in Canada. The candidate will be required to understand the various statutory requirements of the appointed actuary under the Insurance Companies Act and the provincial insurance acts related to financial reporting and general corporate governance.

The material in this section encompasses sections of federal and provincial insurance laws and regulations, regulatory guidelines, and professional standards of practice and educational notes issued by the Canadian Institute of Actuaries that are related to the financial reporting of general insurers.

```
TFARNING OR.TFCTIVFS
    1. Explain the responsibilities of an actuary as
    defined by standards of practice, regulators,
    and insurance laws for financial reporting.
Range of weight: 10-15 percent
```

KNOWI FDGF STATENENTS
a. Statutory Actuarial Opinion
b. Contents of Statutory Reports of the Actuary
c. Standards of Practice
d. Educational Notes
e. Insurance Companies Act
f. Actuary and auditor relationship
g. Regulatory requirements

| READINGS |
| :--- |
| CIA Accounting Standards |
| CIA CSOP |
| CIA DCAT |
| CIA Disclosure |
| CIA Discounting |
| CIA Materiality |
| CIA MfAD |
| CIA Runoff |
| CIA Subsequent Events |
| CIA Taxes |
| CIA Valuation |
| ICA |
| KPMG PACICC |
| OSFI Earthquake |
| OSFI Memorandum |
| OSFI AA |

## Complete Text References for Exam 6-Canada

Text references are alphabetized by the citation column.

NOTE: The inherent nature of the material addressed in this nation-specific exam makes it subject to continual development and change. It is expected that the candidates will respond to exam questions based on the current syllabus presented below. Recognizing the changing nature of law, regulation, and financial reporting requirements, however, the Examination Committee will strive to acknowledge candidates who also respond with the current state in their solutions to examination questions.

| Citation | Abbreviation | Learning <br> Objective | Source |
| :--- | :--- | ---: | ---: |
| Chevalier, Sarah, "Agricultural Risk Management Programs <br> in Canada," October 2014. Note that the table on page <br> 6 is for reference only. | Agricultural <br> Programs | B1-3 | SEW |
| "Auto Insurance Grid Rate Calculator," Alberta <br> Automobile Insurance Rate Board, Candidates are only <br> responsible for the information displayed under the sections <br> titles "Background" and "Grid Premium for Basic <br> Coverage". | Alberta | A2 | OP <br> NEw |
| A.M. Best Company, Inc. A.M. Best Methodology, <br> "Understanding BCAR For Canadian Property/Casualty <br> Insurers," June 2015. | AM Best <br> Understanding <br> BCAR | C2 | OP |
| A.M. Best Company, Inc. A.M. Best Methodology, <br> "Catastrophe Analysis in A.M. Best Ratings,"November 3, <br> 2011. | AM Best <br> Catastrophe | C2 | OP |
| American Academy of Actuaries Mass Torts <br> Subcommittee, "Overview of Asbestos Claims Issues and <br> Trends," Mass Torts Subcommittee monograph, August <br> 2007,"pages 1-11. Candidates will not be responsible for <br> material in the exhibits. | AAA Mass Torts | A4 | OP |
| American Academy of Actuaries, "NAIC Public Hearing <br> on Credit-Based Insurance Scores," April 30, 2009. | AAA Credit <br> Scores | A2 | OP |
| "ATRA Tort Reform Record," CAS Study Note, December <br> 19, 2012. | ATRA | A4 | SK |


| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| Baer, M.G.; and Rendall, J.A., Cases on the Canadian Law of Insurance (Sixth Edition), Carswell, 2000, pp. 67-91, 93-100 302-304, 518-529, 821-827 and 829-831. Candidates are responsible for the following cases: Glenn v. Scottish Union and National Insurance Company Ltd. (Chapter 1); Regal Films Corporation Ltd. v. Glens Falls Insurance Company (Chapter 2); Fletcher v. MPIC (Chapter 8); Broadhurst and Ball v. American Home; and Dillon v. Guardian Insurance (Chapter 11). | Baer and Rendall | A1, A3 | SK |
| Blanchard, R.S.; and Klann, J., "Basic Reinsurance Accounting-Selected Topics," CAS Study Note, October 2012. | Blanchard and Klann | C1 | OP |
| Office of the Superintendent of Financial Institutions Canada, Annual Supplement, 2014, Approved by the Canadian Council of Insurance Regulators - P\&C-1, pp. 10.40, 10.41, 10.42, 10.60, $60.10,60.40,60.41,70.10,70.21,80.20$. NOTE: Please use the 2014 edition that has been archived on the CAS Web Site for educational purposes. | CCIR Instructions | C1 | OP NEW |
| Canadian Institute of Actuaries, Standards of Practice, 1620, 1630, 2200, 2400, 2500, and 2600. | CIA SOP | $\begin{gathered} \mathrm{A} 2, \mathrm{C} 1, \\ \mathrm{C} 2, \mathrm{D} 1 \end{gathered}$ | OP |
| Canadian Institute of Actuaries, "Educational Note: Subsequent Events," September 2012. | CIA <br> Subsequent Events | C1, D1 | OP |
| Canadian Institute of Actuaries, "Educational Note: Consideration of Future Income Taxes in the Valuation of Policy Liabilities," July 2005. | CIA Taxes | C1, D1 | OP |
| Canadian Institute of Actuaries, "Educational Note: Discounting," November 2010. | CIA Discounting | C1, D1 | OP |
| Canadian Institute of Actuaries, "Educational Note: Dynamic Capital Adequacy Testing," November 2013. Candidates are not responsible for details related to life insurance companies. | CIA DCAT | C2, D1 | OP |
| Canadian Institute of Actuaries, "Educational Note: Evaluation of the Runoff of P\&C Claim Liabilities when the Liabilities are Discounted in Accordance with Accepted Actuarial Practice," June 2011. | CIA Runoff | C1, D1 | OP |
| Canadian Institute of Actuaries, "Educational Note: Implications of CICA Accounting Standards 3855 and 1530," January 2007. | CIA <br> Accounting <br> Standards | C1, D1 | OP |
| Canadian Institute of Actuaries, "Educational Note: Guidance to the Appointed Actuary for Property and Casualty Insurers," October 2014. | $\begin{aligned} & \text { CIA } \\ & \text { Valuation } \end{aligned}$ | $\begin{array}{r} \hline \mathrm{C} 1, \mathrm{C} 2, \\ \mathrm{D} 1 \end{array}$ | OP |


| Citation | Abbreviation | Learning <br> Objective | Source |
| :--- | :--- | ---: | ---: |
| Canadian Institute of Actuaries, "Educational Note: Margins for <br> Adverse Deviations for Property-Casualty Insurance," December <br> 2009. | CIA MfAD | C1, D1 | OP |
| Canadian Institute of Actuaries, "Report: Materiality," October <br> 2007. Candidates are not responsible for material in the <br> Appendix. | CIA <br> Materiality | C1, D1 | OP |
| Canadian Institute of Actuaries," Educational Note: Premium <br> Liabilities," November 2014. | CIA <br> Premium <br> Liabilities | C1 | NEP <br> NEW |
| Canadian Institute of Actuaries, "Research Paper: Disclosure <br> Requirements IFRS 4-Insurance Contracts for P\&C Insurers," <br> October 2010. | CIA <br> Disclosure | C1, D1 | OP |
| Canadian Institute of Actuaries, "Report of the CIA Task Force <br> on the Appropriate Treatment of Reennurance," October 2007. <br> Candidates will be responsible for the following sections: Key <br> Principles of Risk Transfer (p. 11-12,, Qualitative Assessment <br> (pp. 13), Limitations of Risk Transfer (pp. 15-18) and Other <br> Issues (pp. 18-23). | CIA <br> Reinsurance <br> Treatment | C1 | OP |
| Canadian Underwriter, "B.C. judge quashes order requiring <br> insurer to review all credit score consent forms obtained since <br> 2004," May2013. | BC Credit | A3 | OP |
| CAS Study Note, "Government Insurers Study Note," October <br> 2013, pp. 1-5, excluding Crop Insurance. | CAS | B1-3 | OP |
| Davidson, J., "The Cap on Non Pecuniary General Damages: <br> Where is it Going and How Does it Affect Litigation?" | Davidson | A3 | OP |
| Dibra, S.; and Leadbetter, D., "Why insurers fail: The dynamics <br> of property and casualty insurance insolvency in Canada," <br> Property and Casualty Insurance Compensation Corporation, <br> 2007, excluding pp. 9-13, 33-40. | Dibra and <br> Leadbetter | B1-3 | OP |
| Dutil, R., "Facility Association," CAS Study Note, May 2008. | Dutil | B1-3 | OP |
| Feldblum, S., "Rating Agencies," CAS Study Note, October 3, <br> 2011, pp. 1-7 and 14-19. Candidates are not responsible for <br> Section 4, Appendices B-D, and the end notes. | Feldblum | C2 | OP |


| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| Financial Services Commission of Ontario, "Private Passenger Automobile Filing Guidelines-Major," October 2014. | FSCO <br> Private Auto | A2 | OP |
| Financial Services Commission of Ontario, "Providing more Choice to Consumers: What you need to know about changes to auto insurance in Ontario". | FSCO <br> Reforms | A2 | OP |
| Financial Services Commission of Ontario, "Regulation 664 of the Revised Regulations of Ontario 1990 Automobile Insurance made under the Ontario Insurance Act," last amended version under Ontario Regulation 291/10. | $\begin{aligned} & \text { FSCO Reg. } \\ & 664 \end{aligned}$ | A2 | OP |
| Financial Services Commission of Ontario, "Usage-Based Automobile Insurance Pricing in Ontario," Bulletin A-05/13, October 2013 | FSCO UBI | A2 | $\begin{gathered} \text { OP } \\ \text { NEW } \end{gathered}$ |
| Freihaut, D.; and Vendetti, P., "Common Pitfalls and Practical Considerations in Risk Transfer Analysis," Casualty Actuarial Society E-Forum, Spring 2009. Appendices A and B are for information only and will not be directly tested. | Freihaut and Vendetti | C1 | OP |
| Harris, C., "Tort Reform Tension," Canadian Underwriter.ca, August 2005. | Harris | A4 | OP |
| International Financial Reporting Standards Foundation, IFRS 4, "Insurance Contracts," as of 1 January 2015. [It is necessary to register (for free) on the IFRS Foundation Web Site in order to access the document.] | IFRS 4 | C1 | OP |
| Insurance Bureau of Canada, "Code of Conduct for Insurers' use of Credit Information (CODE)." | IBC Code of Conduct | A2 | OP |
| "Insurance Companies Act," Chapter 47, Sections 165(1), 165 (2), 203, 331(1), 331(2), 331(4), 346, 357-370, 464, 465, 476-$478,517,581,625-632,641,664,665,667(1), 667(2)$, and 674 (updated to July 1, 2013). | ICA | D1 | SK |
| KPMG, "Research Report - Best Practices for Actuarial Involvement in the Regulatory Oversight of Property and Casualty Insurance Rates," December 2012, pp. 14-31. | KPMG <br> Regulatory Oversight | A2 | SK |
| KPMG, Eckler Partners Ltd. \& Exactor Insurance Services, Inc., "Motor Vehicle Insurance in British Columbia-At the Crossroads, Volume II: Options and Choices," Section II excluding Section F. | KPMG et al. | $\begin{array}{r} \mathrm{A} 2, \mathrm{~A} 4, \\ \mathrm{~B} 1-3 \end{array}$ | SK |


| Citation | Abbreviation | Learning <br> Objective | Source |
| :--- | :--- | ---: | ---: |
| KPMG, "Property and Casualty Insurance Compensation <br> Corporation (PACICC), The P\&C Actuary's Role in Solvency <br> Monitoring," excluding pp. 2-3 and excluding Part 7. | KPMG <br> PACICC | A1, A2, <br> D1 | OP |
| KPMG, "Solvency II," pp. 3 to 8 only. Candidates will not be <br> responsible for discussions related to Risk Based Capital. | KPMG <br> Solvency II | C2 | OP |
| "Landmark Legal Insurance Cases in Canada" which covers the <br> following cases: Whiten v. Pilot Insurance Co.; Somersall v. <br> Friedman; Somersall v. Scottish and York; Sansalone v. <br> Wawanesa Mutual Insurance Co.; Nichols v. American Home <br> Assurance Co.; Amos v. Insurance Corporation of British <br> Columbia; KP Pacific Holdings Ltd. v. Guardian Insurance Co. <br> of Canada; Alie v. Bertrand \& Frere Construction Company <br> Limited; British Columbia v. Imperial Tobacco Canada Ltd.; <br> Resurface Corp. v. Hanke; and Morrow v. Zhang (Sections I, II, <br> III, IV, VI (E), VII, VIII, and IX.); PIPEDA Report of Findings <br> \#2012-005; Kusnierz v. Economical Mutual Insurance Company; <br> Aviva Canada Inc. v. Pastore. | Landmark <br> Legal |  | A3 |
| Mayhall, III, Van R. "A Brief Chronicle of Insurance Regulation <br> in the United States, Parts 1 and II." | Mayhall | SK |  |
| McDonald, B.R., Life Insurance Laws of Canada (Common Law <br> Provinces), Life Underwriters Association of Canada, 1995, pp. <br> A1-1, A2-1 to A2-9, B1-1 to B1-2, B2-1 to B2-3, and B4-1 to <br> B4-3. Candidates are responsible for all cases cited in this text. | McDonald | A1, A3 | SK |
| Morneau Shepell Handbook of Canadian Pension and Benefit <br> Plans (Fifteenth Edition), 2011, CCH Canadian Limited, <br> Chapters 3 (pages 57-67, 71-77 up to "DisabilityBenefits", 87- <br> 90 starting at "Funding and Future Contributions") and Chapters <br> 15-18. Candidates will not be responsible for specific values and <br> figures included in the text. | Morneau <br> Shepell | B1-3 | SK |
| MSA Research, Inc., "MSA Report on Property \& Casualty, <br> Canada, 2014," Section 3, pp. 1-10. | MSA | OP |  |


| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| Noonan, B., "Protecting the Pledge," Foundations of Regulation, Best's Review, October 2005. | Noonan | A1 | OP |
| Odomirok, K.C.; McFarlane, L.M.; Kennedy, G.L; and Brenden, J., Financial Reporting Through the Lens of a Property/ Casualty Actuary, Casualty Actuarial Society, 2014, Edition 4 Parts I, II, VII, and VIII | CAS Financial Reporting | C1 | OP |
| Office of the Superintendent of Financial Institutions Canada, Guideline E-15, "Appointed Actuary: Legal Requirements, Qualifications, and Peer Review," September 2012. | OSFI AA | D1 | OP |
| Office of the Superintendent of Financial Institutions Canada, "Corporate Governance," January 2013. | OSFI Corporate Governance | A2 | OP |
| Office of the Superintendent of Financial Institutions Canada, "Earthquake Exposure Sound Practices Guideline" Guideline B9, February 2013. | OSFI <br> Earthquake | C1, D1 | OP |
| Office of the Superintendent of Financial Institutions Canada, "Key Principles for the Future Direction of the Canadian Regulatory Capital Framework for Property and Casualty Insurance," January 2010. | OSFI <br> Framework | C2 | OP |
| Office of the Superintendent of Financial Institutions Canada Guideline, "Minimum Capital Test (MCT) for Federally Regulated Property and Casualty Insurance Companies, Effective January 1, 2015," September 2014. Candidates will not be required to memorize transition rules nor capital factors | OSFIMCT | C2 | OP |
| Office of the Superintendent of Financial Institutions Canada, "Memorandum for the Appointed Actuary's Report on Property and Casualty Insurance Business," 2014. | OSFI <br> Memorandum | C1, D1 | ( $\begin{array}{r}\text { OP } \\ \text { NEW }\end{array}$ |
| Office of the Superintendent of Financial Institutions Canada, "Own Risk and Solvency Assessment," January 2014. | OSFI ORSA | C2 | OP |
| Office of the Superintendent of Financial Institutions Canada Guideline, "Regulatory Capital and Internal Capital Targets," January 2014. | OSFI Target Capital | C2 | OP |
| Office of the Superintendent of Financial Institutions Canada Guideline E-18, "Stress Testing," December 2009. | OSFI Stress Testing | C2 | OP |
| Office of the Superintendent of Financial Institutions Canada, "Supervisory Framework," December 2010. | OSFI <br> Supervisory <br> Framework | A2 | $\begin{array}{r} \text { OP } \\ \text { NEW } \end{array}$ |


| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| Office of the Superintendent of Financial Institutions Canada, Sample Return, 2015 (Q1), Approved by the Canadian Council of Insurance Regulators - P\&C-1, pp. 20.10, 20.20, 20.30, 20.42, 20.54, 30.61, 30.62, 30.64, 30.66, 30.71, 30.73, 30.75, 30.77, $30.79,40.07,60.20,60.21,60.30,67.10,67.20,67.30,70.60$, $70.61,80.10$, NOTE: Please use the 2015 edition that has been archived on the CAS Web Site for educational purposes | OSFI Annual Return I | C1, C2 | $\begin{array}{r} \text { OP } \\ \text { NEW } \end{array}$ |
| Office of the Superintendent of Financial Institutions Canada, Annual Supplement, 2014, Approved by the Canadian Council of Insurance Regulators - P\&C-1, pp. 10.40, 10.41, 10.42, $10.60,60.10,60.40,60.41,70.10,70.21$. NOTE: Please use the 2014 edition that has been archived on the CAS Web Site for educational purposes. | OSFI Annual Return II | C1, C2 | $\begin{array}{r} \text { OP } \\ \text { NEW } \end{array}$ |
| Property and Casualty Insurance Compensation Corporation, "Guide to Compensation Plan for Property and Casualty Insurers," May 2010. | PACICC | B1-3 | OP |
| Rand Institute for Civil Justice, Research Brief, "Bankruptcy Trusts, Asbestos Compensation, and the Courts," 2011. | Rand Asbestos | A4 | OP |
| Swiss Re, "Making Flood Insurable for Canadian Homeowners," November 2010, Sections 3, 5, 6, 7, and 8. | Swiss Re | B1-3 | OP |
| Webel, Baird, "Terrorism Risk Insurance: Issue Analysis and Overview of Current Program," July 2014, Summary and pp. 113 (excluding the section "TRIA in the $113^{\text {th }}$ Congress (pp. 24)). | Webel | B1-3 | $\begin{array}{r} \hline \text { OP } \\ \text { NEW } \end{array}$ |

## Source Key

B Book-may be purchased from the publisher or bookstore or borrowed from the CAS Library.
NEW Indicates new or updated material.
OP All text references marked as Online Publications will be available on a web page titled Complete Text References.

SK Material included in the Fall 2015 CAS Study Kit.
SKU Material included in both the Fall 2015 CAS Study Kit and the Fall 2015 Update to the Spring 2015 Study Kit.

Items printed in red indicate an update, clarification, or change.

## Publishers and Distributors

Contact information is furnished for those who wish to purchase the text references cited for Exam 6Canada. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

ACTEX Publications, 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com; Web site: www.actexmadriver.com.
Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Web site: www.actuarialbookstore.com.
A.M. Best Company, Inc. Ambest Road, Oldwick, New Jersey, 00858 U.S.A; Website: www.ambest.com

American Academy of Actuaries, 1100 Seventeenth Street NW, Seventh Floor, Washington, DC 20036; telephone: (202) 223-8196; Web site: www.actuary.org.

American Institute for Chartered Property Casualty Underwriters, Order Department, P.O. Box 3016, 720 Providence Road, Malvern, PA 19355-0716; telephone: (610) 644-2100; fax: (610) 6409576.

Baer, M.G.; and Rendall, J.A., Cases on the Canadian Law of Insurance (Fifth Edition), 1995, Carswell, Attention: Customer and Order Services, One Corporate Plaza, 2075 Kennedy Road, Scarborough, Ontario M1T 3V4, Canada; telephone: (416) 609-3800 or (800) 387-5164; fax: (416) 298-5082; Web site: www.carswell.com.

Canadian Institute of Actuaries, Secretariat, Suite 820, 360 Albert Street, Ottawa, Ontario K1R 7X7, Canada; telephone: (613) 236-8196; fax: (613) 233-4552; Web site: www.actuaries.ca.
Casualty Actuarial Society Forum, Foundations of Casualty Actuarial Science (Fourth Edition), PCAS, and Discussion Paper Program, Casualty Actuarial Society, 4350 N. Fairfax Drive, Suite 250, Arlington, VA 22203; telephone: (703) 276-3100; fax: (703) 276-3108; e-mail: office@casact.org; Web site: www.casact.org.

Facility Association, 151 Yonge Street, $18^{\text {th }}$ Floor, Toronto, Ontario M5C 2W7, Canada; telephone: (416) 863-1750 or (800) 268-9572; fax: (416) 868-0894.

Financial Institutions Act, "Insurance Companies Act," Chapter 47, The Federal Publication, 388 King Street West, Toronto, Ontario M5V 1K2, Canada; telephone: (416) 860-1611.

Financial Services Commission of Ontario, 5160 Yonge Street, P.O. Box 85, North York, Ontario M2N 6L9, Canada; telephone: (416) 250-7250; fax: (416) 590-7070; Web site: www.ontarioinsurance.com.

Insurance Bureau of Canada, 240 Duncan Mill Road, Suite 700, Toronto, Ontario M3B 1Z4, Canada; telephone: (416) 445-5912; fax: (416) 445-2183.
Morneau Shepell Handbook of Canadian Pension and Benefit Plans (Fifteenth Edition), 2011, CCH Canadian Limited, 90 Shepherd East, Suite 300, North York, Ontario M2N 6X1, Canada; telephone: (416) 224-2248; fax: (800) 461-4131.

Office of the Superintendent of Financial Institutions Canada, 255 Albert Street, Ottawa, Ontario K1A 0H2 Canada; telephone: (613) 990-7788; fax: (613) 952-8219; Web site: www.osfi-bsif.gc.ca.

## Exam 6-Actuarial Institute of Chinese Taipei Regulation and Financial Reporting

The Actuarial Institute of Chinese Taipei (AICT) uses the Casualty Actuarial Society examinations for its property-casualty actuaries. The CAS Board of Directors approved specific AICT exams (i.e., current AICT Exam 6GA3 on Actuarial Standard of Practice and Accounting and Exam 6GB3 on Insurance Regulations and Discipline) as fulfilling the nation-specific requirement for CAS membership effective January 1, 2010.

In the 2011 transition to a revised basic education structure, learning objectives from the 2010 nationspecific exams were mapped to both the new Exam 6 on Regulation and Financial Reporting and new Online Course 2 on Insurance Accounting, Coverage Analysis, Insurance Law, and Insurance Regulation. Because the AICT continues to cover material from both new Exam 6 and new Online Course 2, candidates who have passed both AICT Exams 6GA3 and 6GB3 will be granted credit for both CAS Exam 6-Taiepi and Online Course 2.

For details on the administration of the AICT examinations, please contact:

Actuarial Institute of Chinese Taipei<br>10F.-1, No.216, Sec. 2<br>Nanchang Road, Zhongzheng District<br>Taipei 100<br>Taiwan (R.O.C.)<br>Telephone: 886-2-2364-9168<br>Fax: 886-2-3365-2283<br>E-mail: airc.org@gmail.com<br>Web Site in Chinese: http://www.airc.org.tw/2011/index.php<br>Web Site in English: http://airc.org.tw/newsfiles/AICT exam.pdf

## Applying for CAS Exam Credit

If a candidate has passed both parts of the AICT nation-specific exam (current AICT Exams 6GA3 and 6GB3) after January 1, 2010, then the candidate may apply for exam credit with the CAS. To receive credit for CAS Exam 6-Taipei and Online Course 2, the candidate should submit a written request to the Actuaries' Resource Center (arc@casact.org). The request must include the candidate's full legal name, contact information (including mailing address and telephone number), date of birth, and the administration (month/year of exam) that each of the AICT nation-specific exam parts was passed. The Actuaries' Resource Center will verify the exam information with the AICT and then update the candidate's record to reflect the credit as appropriate.

## Fall 2015 and Spring 2016 Exam 6-United States Syllabus Regulation and Financial Reporting (Nation Specific)

The syllabus for this four-hour exam is defined in the form of learning objectives, knowledge statements, and readings.
LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain ones that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain in an examination setting.
KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behavior, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.
Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination. The overall section weights should be viewed as having more significance than the individual learning objective weights. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the individual learning objective weights, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.
After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.
In addition, this exam assumes that the candidate has completed Online Course 2. Online Course 2 contains fundamental background material for both Section A (Regulation of Insurance and United States Insurance Law) and Section C (Financial Reporting and Taxation).
Items marked with a bold SK or SKU constitute the Fall 2015-Spring 2016 Exam 6-United States Study Kit that may be purchased from the CAS Online Store. The 2015 Update to the Fall 2014-Spring 2015 Study Kit includes only the new items marked with a bold SKU; the Update may be purchased from the CAS Online Store. Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from the CAS website.

Please check the "Syllabus Updates" section of the CAS Web Site for any changes to the Syllabus.

Section A of this examination covers insurance regulation with regards to property-casualty coverages, ratemaking, pricing, and solvency, and U.S. tort law as it affects the property-casualty business. Section B covers markets, coverages, and private and governmental programs for the property-casualty business in the United States. Section C covers the aspects of statutory, Generally Accepted Accounting Principles (GAAP), and International Financial Reporting Standards (IFRS) insurance accounting and taxation as these affect reserving and statutory reporting in the United States. Section D covers the professional responsibilities of the appointed actuary according to the Property and Casualty Annual Statement Instructions issued by the National Association of Insurance Commissioners (NAIC). Section E presents the general concepts of reinsurance accounting to the candidate.

The inherent nature of the material addressed in this nation-specific exam makes it subject to continual development and change. It is expected that the candidates will respond to exam questions based on the current syllabus presented below. Recognizing the changing nature of law, regulation, and financial reporting requirements, however, the Examination Committee will strive to acknowledge candidates who also respond with the current state in their solutions to examination questions.

## A. Regulation of Insurance and United States Insurance Law

Range of weight for Section A: 15-20\%
Candidates should understand that insurers are regulated by various governmental agencies because insurance is a valuable public service. An understanding of the dual U.S. state and federal regulatory system is required, along with the various state systems of regulation. The major areas of regulation for rate, contract terms, and solvency should be understood, as should the role of antitrust law as it pertains to insurance regulation.
Regulation as it affects insurance ratemaking in the U.S. is covered. Regulatory and political aspects of risk classification are also covered. Some learning objectives extend the topic to regulation and governmental actions designed to enhance the availability of insurance.
This section also covers the regulation for solvency in the U.S., including financial ratios tested by the National Association of Insurance Commissioners, Insurance Regulatory Information System (IRIS) tests and guaranty fund mechanisms set up by the various states. Also covered are risk-based capital calculations from the statutory blank and how they are used to monitor solvency.
U.S. tort law, while not a strictly actuarial subject, affects many areas of an actuary's work. The judicial role in the development of tort law is also covered.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1.Describe the historic development and the <br> current state of insurance regulation. <br> Range of weight: 3-7 percenta. Basis of insurance regulation <br> b. Functions of NAIC |  |
| READINGS | c. Antitrust provisions <br> d. Rate regulation |
| Kucera |  |
| McCarty <br> NAIC Solvency Regulatory Framework <br> Porter 1 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 2.Discuss the historic development of <br> solvency regulation; describe current <br> programs used to monitor solvency. <br> Range of weight: 3-7 percent | a.Solvency, including RBC, insolvency, insurance <br> department examination, and NAIC regulatory <br> tests such as IRIS <br> Receivership |
| READINGS | b. |
| Odomirok et al. <br> NAIC IRIS <br> NAIC Solvency Regulatory Framework <br> Porter 1 <br> Porter 2 <br> Vaughan (Economic Crisis) |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 3. Describe current regulation addressing | a.Surplus Lines Companies <br> specialized insurance topics. |
| Range of weight: 0-5 percent | b. Risk Retention Groups and Purchasing Groups |
|  | c. Captives <br> d. Admitted vs. Non-admitted Companies <br> e. Rating Agencies |
| READINGS |  |
| Feldblum (Rating Agencies) <br> GAO Report <br> Mayer Brown <br> NAIC Solvency Regulatory Framework <br> Porter 1 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 4.Discuss the issues, outcome, rationale, and <br> implications of landmark decisions and <br> antitrust laws for the insurance industry <br> including the division of responsibility <br> between federal and state regulators. | a.Federal and State Antitrust Laws (e.g. Sherman <br> Antitrust) |
| Range of weight: 3-7 percent | b.McCarran-Ferguson <br> c. |
| d.Southeastern Underwriters <br> Dodd-Frank Act <br> Gramm Leach Bliley Act <br> e. |  |
| READINGS | f. Paul vs. Virginia |
| g. Mass torts (e.g. asbestos) |  |
| Asbestos |  |
| Mayer Brown |  |
| NAIC Solvency Regulatory Framework |  |
| Porter 1 |  |
| Vaughan (Economic Crisis) |  |

## B. Government and Industry Insurance Programs

Range of weight for Section B: 10-15 percent
This section focuses on the identification of major United States insurance programs administered by government agencies and insurance industry organizations. The candidates are expected to have an understanding of the objectives, operations, and effectiveness of the following insurance programs:

- Flood insurance
- Crop Insurance
- Residual markets (e.g., auto, workers compensation, property)
- Workers compensation
- Automobile Plans (e.g., MD Fund)
- Guaranty funds
- Government Backstops, e.g., TRIA and FL Cat Fund

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1.Describe the origin and purpose of <br> government and industry insurance <br> programs. <br> Range of weight: 3-7 percent | a. Reason for inception <br> b. Major historical development <br> c. Philosophy of program |
| READINGS |  |
| Government Insurers Study Note <br> Hamilton and Ferguson <br> King <br> Porter 2 <br> Webel |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 2.Describe the operations and risk transfer <br> process for government/industry programs <br> and their interaction with voluntary private <br> insurance sector. | a. Funding mechanisms/sources <br> b. Allocation/assignment of exposures and <br> associated costs  |
| Range of weight: 3-7 percent | c.Claim settlement and insurance coverage <br> provisions |
| d.Welfare (subsidization) versus insurance <br> principles |  |
| READINGS |  |
| Government Insurers Study Note <br> Hamilton and Ferguson <br> King <br> Porter 2 <br> Webel |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Evaluate the effectiveness of a government/industry program. Range of weight: 3-7 percent | a. Solvency <br> b. Efficiencies <br> c. Stability <br> d. Viability/longer term prospects <br> e. How well program meets its purpose |
| READINGS |  |
| Government Insurers Study Note Hamilton and Ferguson <br> King <br> Porter 2 <br> Webel |  |

## C. Financial Reporting and Taxation

Range of weight for Section C: 35-55 percent
This section addresses financial reporting, solvency, and taxation issues. Candidates should have detailed knowledge of the contents, purposes, and recent changes in the NAIC Annual Statement and the Insurance Expense Exhibits. Knowledge of federal income tax treatment, including loss reserve discounting, is expected.
Candidates may find it valuable to review an actual insurer's Annual Statement to gain a more complete understanding of the key schedules, particularly the Notes to Financial Statements and General Interrogatories Sections. A candidate may review the Annual Statement of the company for which the candidate works or the Annual Statement of a publicly held company. There are links to publicly available Annual Statements of a few U.S. insurers in the citation for the NAIC Annual Statement Examples in the Complete Text References section below. Candidates are not responsible for the details of the companies' Annual Statement.

Candidates should understand the details of, and the reasons for, the differences between Generally Accepted Accounting Principles (GAAP), Statutory Accounting Principles (SAP), and International Financial Reporting Standards (IFRS).
This section is complemented by readings on solvency monitoring systems such as Risk Based Capital (RBC) and the IRIS ratios.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Describe the elements of the Annual Statement. Complete specific schedules and exhibits and use them to evaluate the financial health of an insurance entity. <br> Range of weight: 20-25 percent | a. Balance sheet <br> b. Income statement <br> c. Change in surplus <br> d. Schedule P <br> e. Insurance Expense Exhibit <br> f. Notes to financial statements <br> g. Reinsurance accounting including Schedule F <br> h. Underwriting and Investment Exhibit <br> i. Exhibit of Premiums and Losses (Statutory Page 14) |
| READINGS |  |
| 2014 IEE <br> Feldblum (Surplus) <br> NAIC Annual Statement <br> NAIC Annual Statement Examples NAIC SSAP 5R, $9,53,55,62 R$, and 65 Odomirok et al. |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 2. Using RBC formulas and IRIS ratios, | a. RBC formula |
| $\quad$ evaluate an insurer's financial health. | b. Components of RBC |
| Range of weight: 10-15 percent | c. IRIS ratios <br> d. Interaction of RBC and IRIS Ratios |
| READINGS |  |
| NAIC IRIS |  |
| Odomirok et al. |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 3. <br> Differentiate between various accounting <br> reporting principles and standards. <br> Range of weight: 5-10 percent | a. |
|  | b.U.S. Statutory Accounting Principles <br> Generally Accepted Accounting Principles (SEC <br> Filers) <br> Adjustments to go from SAP to GAAP <br> c. |
|  | d.Fair Value of claims liabilities, including Risk <br> Margins |
| READINGS | e.International Financial Reporting Standards <br> f. |
| DeFrain <br> Lindbergh and Seifert |  |
| NAIC APPM, Preamble |  |
| NAIC Solvency Regulatory Framework |  |
| Odomirok et al. |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |  |
| :--- | :--- | :--- |
| 4. Calculate specific elements of income tax | a. | Discounting |
| and evaluate their implications for a | b. | Elements of income tax calculation |
| property/casualty insurer. | c. | Statutory book income versus taxable income |
| Range of weight: 0-5 percent | d. Alternative minimum tax |  |
|  | e. | Deferred Tax Asset and Deferred Tax Liability |
|  | f. | Temporary vs. permanent differences |
| READINGS |  |  |
| Feldblum (Loss Reserve Discounting, Taxable Income, and Taxes and Investment Strategy) |  |  |
| Odomirok et al. |  |  |

## D. Professional Responsibilities of the Actuary in Financial Reporting

Range of weight for Section D: 15-20 percent
This section focuses on the professional responsibilities of the appointed actuary related to the reporting of financial results by property/casualty insurance companies in the United States of America. The identification of the appointed actuary is described in the Property and Casualty Annual Statement Instructions issued by the NAIC.

The candidate will be required to understand the various statutory requirements of the appointed actuary, and the appropriate professional standards and educational notes issued by the American Academy of Actuaries that are related to the financial reporting of property and casualty insurance companies.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Explain the responsibilities of an actuary as defined by standards of practice, regulators, and insurance laws for financial reporting. <br> Range of weight: 15-20 percent | a. Statutory Prescribed Statement of Actuarial Opinion <br> b. Standards of Practice <br> c. Actuarial Report <br> d. Actuary and auditor relationship <br> e. Materiality <br> f. Actuarial Opinion Summary |
| READINGS |  |
| AAA Materiality ASOP 20, 36, 41, and 43 COPLFR P\&C Practice Note Odomirok et al. |  |

## E. Reinsurance Accounting Principles

Range of weight for Section E: 5-10 percent
This section presents the general concepts of reinsurance accounting to the candidate. The candidate should become familiar with reinsurance accounting terminology and practice.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Describe reinsurance accounting terminology and practice, and evaluate considerations such as risk transfer testing and commutations. <br> Range of weight: 5-10 percent | a. Identification and evaluation of insurance and financing components of the contracts <br> b. Determination whether the contract qualifies for insurance accounting treatment or deposit accounting treatment (i.e., passes risk transfer), and understand impact on financial statements <br> c. Commutations-definition, motivations of parties, and accounting and tax treatment |
| READINGS |  |
| ASC 944-020-15 |  |
| Blanchard and Klann |  |
| Freihaut \& Vendetti |  |
| Klann |  |
| SSAP 62R |  |

## Complete Text References for Exam 6-United States

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| 2014 Insurance Expense Exhibit. | 2014 IEE | C1 | NEW |
| Actuarial Standards Board of the American Academy of Actuaries, "Actuarial Standard of Practice, No. 20, Discounting of Property/Casualty Unpaid Claim Estimates," September 2011. | ASOP 20 | D1 | OP |
| Actuarial Standards Board of the American Academy of Actuaries, "Actuarial Standard of Practice No. 36, Statements of Actuarial Opinion Regarding Property/Casualty Loss and Loss Adjustment Expense Reserves," Revised Ed. December 2010. | ASOP 36 | D1 | OP |
| Actuarial Standards Board of the American Academy of Actuaries, "Actuarial Standard of Practice No. 41, Actuarial Communications," December 2010. | ASOP 41 | D1 | OP |
| Actuarial Standards Board of the American Academy of Actuaries, "Actuarial Standard of Practice No. 43, Property/Casualty Unpaid Claim Estimates," May 2011. | ASOP 43 | D1 | OP |
| American Academy of Actuaries Mass Tort Subcommittee, "Overview of Asbestos Claims Issues and Trends," A Public Policy Monograph, August 2007, pp. 1-11. | Asbestos | A4 | OP |
| American Academy of Actuaries, Task Force on Materiality, "Materiality, Concepts on Professionalism," Discussion Paper, Professionalism Series, 2006, No. 8. | AAA <br> Materiality | D1 | OP |
| Blanchard, R.S.; and Klann, J., "Basic Reinsurance AccountingSelected Topics," CAS Study Note, October 2012. | Blanchard and Klann | E1 | OP |
| Committee on Property and Liability Financial Reporting, American Academy of Actuaries, "Property and Casualty Practice Note, Statements of Actuarial Opinion on P\&C Loss Reserves as of December 31, 2014." | COPLFR <br> P\&C <br> Practice <br> Note | D1 | $\begin{gathered} \hline \text { OP } \\ \text { NEW } \end{gathered}$ |
| DeFrain, K., "The Impact of International Financial Reporting Standards on U.S. Actuarial Practice," CAS Study Note, November 5, 2010. | DeFrain | C3 | OP |
| Feldblum, S., "Computing Taxable Income for Property-Casualty Insurance Companies," CAS Study Note, 2007, pp. 1-13, excluding appendices and end notes. | Feldblum (Taxable Income) | C4 | OP |
| Feldblum, S., "Federal Income Taxes and Investment Strategy," CAS Study Note, 2007, pp. 1-12, excluding Appendix and endnotes. | Feldblum (Taxes and Investment Strategy) | C4 | OP |
| Feldblum, S., "IRS Loss Reserve Discounting," CAS Study Note, 2007, pp. 1-13, including errata, excluding Appendix and endnotes. | Feldblum (Loss Reserve Discounting) | C4 | OP |


| Feldblum, S., "Rating Agencies," CAS Study Note, October 3, 2011, pp. 1-7 and 14-15(stop at Best's Capital Adequacy Ratio). Candidates are not responsible for Sections 4 \& 5, Appendices BD , and the endnotes. | Feldblum <br> (Rating <br> Agencies) | A3 | OP |
| :---: | :---: | :---: | :---: |
| Feldblum, S., "Statutory Surplus: Computation, Pricing and Valuation," CAS Study Note, June 2003. Candidates are not responsible for the endnotes. | Feldblum (Surplus) | C1 | OP |
| Financial Accounting Standards Board, Accounting Standards Codification 944, "Financial Guarantee Insurance Contracts," 2011, Section 15, Scope and Scope Exceptions, paragraphs 15-1 to $15-2 ; 15-5$ to $15-8 ; 15-34$ to $15-35 ; 15-41$ to $15-44$; and $15-49$ to 15-54. Candidates are not responsible for material relating to long-duration contracts and/or life insurance. | $\begin{aligned} & \text { ASC 944- } \\ & 020-15 \end{aligned}$ | E1 | SK |
| Freihaut, D.; and Vendetti, P., "Common Pitfalls and Practical Considerations in Risk Transfer Analysis," Casualty Actuarial Society E-Forum, Spring 2009. (Appendices A and B are for information only and will not be directly tested.) | Freihaut \& Vendetti | E1 | OP |
| "GAO Report to the Chairman, Committee on Financial Services, House of Representatives, Risk Retention Groups, Common Regulatory Standards and Greater Member Protections are Needed," United States Government Accountability Office, GAO-05-536," August, 2005, pp. 8-14. | GAO Report | A3 | OP |
| "Government Insurers Study Note," CAS Study Note, Updated September 2013, pp. 1-18 (stop at unemployment insurance). Candidates are not responsible for numbers or statistics in charts. | Government Insurers Study Note | $\mathrm{B} 1, \mathrm{~B} 2,$ B3 | OP |
| Hamilton, K.L.; and Ferguson, C.L., Personal Risk Management and Property-Liability Insurance (First Edition), American Institute for Chartered Property Casualty Underwriters, 2002, pp. 6.31-6.34 and 9.36-9.40. | Hamilton and Ferguson | $\mathrm{B} 1, \mathrm{~B} 2,$ <br> B3 | SK |
| King, R. "The National Flood Insurance Program: Status and Remaining Issues for Congress", February 6, 2013, pp. 1-32. | King | $\mathrm{B} 1, \mathrm{~B} 2$ <br> B3 | OP |
| Klann, J., "Reinsurance Commutation," 2013. | Klann | E1 | OP |
| Kucera, J., "NAIC Public Hearing on Credit-Based Insurance Scores," April 30, 2009, American Academy of Actuaries. | Kucera | A1 | OP |
| Lindbergh, D.L.; and Seifert, D.L., "A New Paradigm of Reporting on the Horizon, International Financial Reporting Standards (IFRS) and Implications for the Insurance Industry," Journal of Insurance Regulation, National Association of Insurance Commissioners, Volume 29, 2010, pp. 229-242. | Lindbergh and Seifert | C3 | SK |
| Mayer Brown, "Understanding the New Financial Reform Legislation: The Dodd-Frank Wall Street Reform and Consumer Protection Act," July 2010, pp. 55-63, excluding Section B and F4. The candidates are encouraged to read pages xv-xix to understand acronyms cited in the article. | Mayer Brown | A3, A4 | OP |


| McCarty, K.M., "Testimony of Kevin M. McCarty, Florida Insurance Commissioner, Florida Office of Insurance Regulation and Representing the National Association of Insurance Commissioners, Regarding: 'The Impact of Credit-Based Insurance Scoring on the Availability and Affordability of Insurance,' May 21, 2008," Subcommittee on Oversight and Investigations of the House Committee on Financial Services, excluding Appendices 1 and 2. | McCarty | A1 | OP |
| :---: | :---: | :---: | :---: |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Preamble. | NAIC APPM, Preamble | C3 | $\begin{aligned} & \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Statement of Statutory Accounting Principles 5R, "Liabilities, Contingencies, and Impairment of Assets," paragraphs 1-12, 26-29, and 33-34. | $\begin{aligned} & \text { NAIC SSAP } \\ & \text { 5R } \end{aligned}$ | C1 | $\begin{aligned} & \hline \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Statement of Statutory Accounting Principles 9, "Subsequent Events," paragraphs 1-8. | $\begin{aligned} & \text { NAIC SSAP } \\ & 9 \end{aligned}$ | C1 | $\begin{aligned} & \hline \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Statement of Statutory Accounting Principles 53, "Property Casualty ContractsPremiums," paragraphs 1-18. | $\begin{aligned} & \text { NAIC SSAP } \\ & 53 \end{aligned}$ | C1 | $\begin{aligned} & \hline \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Statement of Statutory Accounting Principles 55, "Unpaid Claims, Loss and Loss Adjustment Expenses," paragraphs 1-6 and 10-17. | $\begin{aligned} & \text { NAIC SSAP } \\ & 55 \end{aligned}$ | C1 | $\begin{aligned} & \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Statement of Statutory Accounting Principles 62R, "Property and Casualty Reinsurance," paragraphs $1-89$. | $\begin{aligned} & \text { NAIC SSAP } \\ & 62 R \end{aligned}$ | C1, E1 | $\begin{aligned} & \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, Accounting Practices and Procedures Manual, 2014, Statement of Statutory Accounting Principles 65, "Property and Casualty Contracts," paragraphs 1-45. | $\begin{aligned} & \text { NAIC SSAP } \\ & 65 \end{aligned}$ | C1 | $\begin{aligned} & \hline \text { SKU } \\ & \text { NEW } \end{aligned}$ |
| National Association of Insurance Commissioners, "NAIC Insurance Regulatory InformationSystem (IRIS) Ratios Manual," 2014, Section II, Property/Casualty Ratios, pp. 5-26. | NAIC IRIS | A2, C2 | $\begin{aligned} & \hline \text { SKU } \\ & \text { NEW } \end{aligned}$ |


| National Association of Insurance Commissioners, Official 2014 <br> NAIC Annual Statement Blanks, Property and Casualty, (both <br> individual and consolidated basis), pp. 2-13, Notes to the | NAIC Annual <br> Financial Statement p. 14 (refer to the Odomirok paper for the <br> Notes to cover); Schedules D (pp. SI03 through SI09), F (pp. <br> 20-29), H (pp. 30-33), and P (pp. 33-93). Candidates will be <br> expected to have knowledge of other sections of the annual <br> statement that are discussed in other Syllabus readings. <br> Candidates are not responsible for page numbers. [The "Notes to <br> the Financial Statement" are cited for reference only. Candidates <br> are responsible for the Notes as described in the Odomirok <br> reading where the Notes are referenced by title. If the 2015 |  |
| :--- | :--- | :--- |
| Annual Statement and the study materials differ, candidates may |  |  |$\quad$| NEW |
| :--- |
| base their answers on either.] |

## Source Key

B Book—may be purchased from the publisher or bookstore or borrowed from the CAS Library.
NEW Indicates new or updated material.
OP All text references marked as Online Publications will be available on a web page titled Complete Text References.

SK Material included in the Fall 2015-Spring 2016 Study Kit.
SKU Material included in both the Fall 2015-Spring 2016 CAS Study Kit and the 2015 Update to the Fall 2014-Spring 2015 Study Kit.

Items printed in red indicate an update, clarification, or change.

## Publishers and Distributors

Contact information is furnished for those who wish to purchase the text references cited for Exam 6-United States. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

Actex Publications (Mad River Books), 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail: retail@actexmadriver.com; Website: www.actexmadriver.com.

Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Web site: www.actuarialbookstore.com.

Actuarial Digest, P.O. Box 1127, Ponte Vedra, FL 32004.
American Institute for Chartered Property Casualty Underwriters, Order Department, P.O. Box 3016, 720 Providence Road, Malvern, PA 19355-0716; telephone: (610) 644-2100; fax: (610) 640-9576.

Association Form of the Annual Statement Blanks, Bowne Insurance Services, 1717 Arch Street, 31st Floor, Philadelphia, PA 19103; telephone: (215) 988-5690 or (800) 234-6859.

Casualty Actuarial Society E-Forum, Forum, Foundations of Casualty Actuarial Science (Fourth Edition), PCAS, and Discussion Paper Program, Casualty Actuarial Society, 4350 N. Fairfax Drive, Suite 250, Arlington, VA 22203; telephone: (703) 276-3100; fax: (703) 276-3108; e-mail: office@casact.org; Web site: www.casact.org.

Insurance Expense Exhibit, Bowne Insurance Services, 1717 Arch Street, 31st Floor, Philadelphia, PA 19103; telephone: (215) 988-5690 or (800) 223-3103.

Insurance Institute of America, 720 Providence Road, Malvern, PA 19355-0770; telephone: (610) 644-2100.

Journal of Insurance Regulation, National Association of Insurance Commissioners, $120 \mathrm{~W} .12^{\text {th }}$ Street, \#1100, Kansas City, MO 64105; telephone: (816) 842-3600.

Journal of Risk and Insurance, The, American Risk and Insurance Association, 716 Providence Road, P.O. Box 3028, Malvern, PA 19355; telephone: (610) 640-1997; fax: (610) 725-1007; Web site: www.aria.org.

NAIC Annual Statement Blanks, Property and Casualty may be obtained from Bowne Insurance Services, 1717 Arch Street, 31st Floor, Philadelphia, PA 19103; telephone: (215) 988-5690 or (800) 223-3103.

National Association of Insurance Commissioners, 120 W. 12th Street, \#1100, Kansas City, MO 64105; telephone: (816) 842-3600.
RR Donnelley, Two Logan Square, 18th Floor, Philadelphia, PA 19103; telephone: (215) 9885622 or (800) 234-6859 [for the NAIC Annual Statement Blanks, Property and Casualty and the Insurance Expense Exhibit (P\&C)].
Stanford University Press, 1450 Page Mill Road, Palo Alto, CA, 94304; telephone (800) 6212736; Web site: www.sup.org.

## 2015 Exam 7

## Estimation of Policy Liabilities, Insurance Company Valuation, and Enterprise Risk Management

The syllabus for this four-hour exam is defined in the form of learning objectives, knowledge statements, and readings.
LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain conceptually in the context of an examination.

KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.

Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination - the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.
After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.

Items marked with a bold SK or SKU constitute the 2015 CAS Exam 7 Study Kit that may be purchased from the CAS Online Store. Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from the CAS website. The 2015 Update to the 2014 Study Kit includes only the new items marked with a bold SKU and may be purchased from the CAS Online Store.

Please check the "Syllabus Update" for this exam for any changes to this syllabus.

## A. Estimation of Policy Liabilities

## Range of weight for Section A: 45-55 percent

This section focuses on advanced techniques that the actuary may need to estimate reserves for unpaid claims. The candidate is expected to be well versed in the basic Principles and Standards of Practice for unpaid claim estimation. This section addresses how actuarial concepts are adapted to evaluate liabilities arising in complex risk transfer agreements common in excess insurance and reinsurance contracts. Emphasis is placed on developing ranges around a best estimate.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1. Calculate unpaid claim estimates using <br> credibility models. | a. Application of credibility <br> Range of weight: 3-4 percent |
| b. Mechanics of the methods |  |
| READINGS | c. <br> d. |
| Brosius Testing results for reasonableness |  |
| Hürlimann |  |
| Mack (2000) |  |

## LEARNING OBJECTIVES

2. Estimate parameters and unpaid claims using claims development models related to loss reserving methods such as:

- Chain ladder

KNOWLEDGE STATEMENTS
a. Key assumptions of the models and testing of assumptions

- Cape Cod
- Chain ladder plus calendar-year effects
- Bornhuetter-Ferguson

3. Calculate the moments and percentiles of unpaid claim distributions implied by the models.
Range of weight: 16-18 percent
b. Original Mack chain ladder assumptions
c. Relationship of variance assumptions to methods of calculating development factors
d. Row-factor times column-factor models
e. Calendar-year effects in development factor models and in row-column factor models
f. Effect of trends and their interrelationship (e.g., calendar year, accident year, and development year trends)
g. Testing for and eliminating insignificant parameters
h. Testing whether the methods work and how well the models fit
i. Moments of the chain ladder unpaid claim estimate when factors are calculated based on different variance assumptions
j. Simulation of parameter percentiles and unpaid claims percentiles when models assume a distribution of residuals fit by MLE

## READINGS

Clark
Mack (1994)
Venter Factors

| EARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 4. Estimate unpaid claims for various layers of claims. <br> Range of weight: 3-4 percent | a. Methods for estimating unpaid claims in a deductible layer <br> b. Methods for estimating unlimited unpaid claims excess of a threshold <br> c. Methods for estimating unpaid claims excess of a retention but bounded by a limit <br> d. Relationships of development patterns among layers <br> e. Interrelationships between parameters for forecasting deductible, unlimited excess, layer excess and total claims |
| READINGS |  |
| Sahasrabuddhe Siewert |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 5. Describe the various sources of risk and uncertainty that are associated with the determination of reserves. Calculate risk margins that consider these sources of risk and uncertainty. <br> Range of weight for Learning Objectives A5-A10 collectively: 16-18 percent | a. Systemic risks and independent risks <br> b. Limitations of quantitative risk assessment <br> c. Risk correlations <br> d. Testing and evaluation of risk models |
| 6. Calculate the mean and prediction error of a reserve given an underlying statistical model. <br> Range of weight for Learning Objectives A5-A10 collectively: 16-18percent | a. Distributions and distribution-free models <br> b. Comparison of Chain Ladder stochastic models |
| 7. Derive predictive distributions using bootstrapping and simulation techniques. <br> Range of weight for Learning Objectives A5-A10 collectively: 16-18percent | a. Comparison of methods <br> b. Simulation using bootstrapping <br> c. Simulation from parameters <br> d. Bayesian methods |
| 8. Identify data issues and related model adjustments for reserving models. <br> 9. Test assumptions underlying reserve models. <br> 10. Develop a distribution of reserves using weights and multiple stochastic models. <br> Range of weight for Learning Objectives A5-A10 collectively: 16-18 percent | a. Bayesian methods <br> b. Adjustments to various reserving techniques <br> c. Comparison of ODP Bootstrap and GLM Bootstrap models |
| READINGS |  |
| Marshall et al Shapland and Leong Verrall |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 11. Compare and contrast reinsurance and primary reserving procedures. <br> 12. Adjust primary methods and data to be used for reinsurance reserving. <br> 13. Calculate ceded loss reserves using appropriate methods. <br> Range of weight for Learning Objectives A11-A13 collectively: 5-7 percent | a. Overview of reinsurance and primary reserving methods <br> b. Effect on assumptions from differences in information available to reinsurers <br> c. Stanard-Buhlmann method <br> d. Cape Cod method <br> e. Underlying business characteristics of reinsurance contracts e.g., concentration of exposures <br> f. Data structures: <br> - Ground up versus excess loss <br> - Accident year versus treaty year <br> g. Reinsurance reserving methods |
| READINGS |  |
| Patrik |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 14. Forecast Premium Reserves. Range of weight: 2-4 percent | a. Reserves for retrospective premiums <br> b. Reserves for unearned premiums for policies with non pro-rata earning patterns |
| READINGS |  |
| Teng and Perkins |  |

## B. Insurance Company Valuation

## Range of weight for Section B: 8-12 percent

This section focuses on methods used to determine the theoretical value of equity securities and extending the methodology to value property and casualty insurance companies. The candidate is expected to be proficient with the basic tools and techniques commonly used in the financial analysis of corporations as described in the knowledge requirements set forth for VEE-Corporate Finance.

| Learning Objectives | Knowledge Statements |
| :---: | :---: |
| 1. Calculate the effect of loss and expense reserve requirements and regulatory or rating agency capital requirements on the free cash flow to equity for a P\&C insurer. <br> Range of weight for Learning Objectives B1-B3 collectively: 8-12 percent | a. Free cash flow to equity for a P\&C insurer |
| 2. Value the equity of a P\&C insurer based on its expected future dividends, its free cash flow to equity, or its expected abnormal earnings <br> Range of weight for Learning Objectives B1-B3 collectively: 8-12 percent | a. Dividend Discount Model (DDM) <br> b. Free cash flow to equity for a P\&C insurer <br> c. Discounted Cash Flow (DCF) Valuation using free cash flow to equity (FCFE), including effect of alternative methods of estimating terminal values and reasons why this method is preferred over the free cash flow to the firm (FCFF) method for $\mathrm{P} \& \mathrm{C}$ insurers <br> d. Abnormal earnings <br> e. Abnormal Earnings Valuation (AE), including effect of alternative methods of estimating terminal values |
| 3. Value the equity of a firm using comparative or relative valuation methods based on multiples of selected financial variables obtained from either peer companies or from underlying fundamentals. <br> Range of weight for Learning Objectives B1-B3 collectively: -8-12 percent | a. Comparative valuation ratios including priceearnings, price-sales, price-book, price-cash flow <br> b. Relationship between the dividend discount model and the price-earnings (P-E) ratio <br> c. Relationship between the abnormal earnings valuation model and the price-book value (P-BV) ratio |
| READINGS |  |
| Goldfarb |  |

## C. Enterprise Risk Management

Range of weight for Section C: 35-45 percent
This section introduces the candidate to the concepts and basic techniques of Enterprise Risk Management (ERM). ERM seeks to integrate the entire landscape of risk that confronts a business. Topics include value of risk management and basic modeling concepts.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |  |
| :--- | :--- | :--- |
| 1. Demonstrate how insurance and financial | a. | Currency risk |
| risk can be analyzed quantitatively. | b. | Credit risk |
| Range of weight: 9-11 percent | c. | Spread risk |
|  | d. | Interest rate risk |
|  | e. | Equity risk |
|  | f. | Hazard/insurance risk |
| READINGS |  |  |
| Brehm et al |  |  |
| IAA |  |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 2. Describe the use of enterprise-wide risk modeling and aggregation techniques. <br> 3. Evaluate and select appropriate models to handle diverse risks, including stochastic approaches. <br> Range of weight: 9-11 percent | a. Incorporating the use of correlation <br> b. Evaluation and selection of appropriate copulas as part of the process of modeling multi-variate risks <br> c. Alternatives to copulas <br> d. Scenario analysis <br> e. Stress testing <br> f. Tail dependence and tail correlations <br> g. Low frequency/high severity events <br> h. Model and parameter risk |
| READINGS |  |
| Brehm et al Feldblum IAA Venter Copulas |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 4. Demonstrate the properties of various risk measures and their limitations. <br> 5. Describe how risk measures and risk modeling, including allocation, can affect strategic management. <br> Range of weight: 4-5 percent | a. (Semi) standard deviation <br> b. VaR and TVaR <br> c. Expected policyholder deficit and default put option <br> d. Risk-adjusted TVaR <br> e. OpVaR (including variations) <br> f. Distortion measures and probability transforms |
| READINGS |  |
| IAA <br> Venter and Underwood <br> Venter Non-tail Measures <br> Venter Strategic Management |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 6. Describe the rationale for, methods for, and effect of managing insurance and financial risks. <br> Range of weight: 8-10 percent | a. Selection of appropriate degree of risk <br> b. Risk optimization and value impact <br> c. Retention including estimated costs compared to benefits of risk transfer, value of specific risk, costs of financial distress, taxation, firm value, financing costs, and risk attitudes of debtholders, customers, employees, etc. |
| READINGS |  |
| IAA <br> Venter and Underwood |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 7. Describe operational risk and demonstrate possible mitigation and quantification methodology. <br> Range of weight: 1-2 percent | a. Types of operational risk <br> b. Examples <br> c. Quantification <br> d. Capital charges <br> d. Mitigation |
| READINGS |  |
| Brehm et al |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 8. Evaluate best practices in risk measurement, modeling, and management of various financial and non-financial risks faced by an entity. <br> Range of weight: 4-6 percent | a. Economic capital <br> b. Extreme events <br> c. Risks <br> d. Model structure |
| READINGS |  |
| Brehm et al |  |

## Complete Text References for Exam 7

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| Brehm, P.; Gluck, S.; Kreps, R.; Major, J.; Mango, D.; Shaw, R.; Venter, G.; White, S.; and Witcraft, S., Guy Carpenter, "Enterprise Risk Analysis for Property \& Liability Insurance Companies," Chapter 1, Sections 2.2, 2.3, 3.1, 3.2, 4.1,4.2, 5.2, 5.4, 6.2. (Note: Chapter 4.1 was included in the prior 2014 Syllabus as "Mango and Venter"). | Brehm et al | $\begin{array}{r} \hline \mathrm{C} 1, \mathrm{C} 2, \\ \mathrm{C} 3, \mathrm{C} 7, \\ \mathrm{C} 8 \end{array}$ | $\begin{aligned} & \hline \text { NEW } \\ & \text { SKU } \end{aligned}$ |
| Brosius, E., "Loss Development Using Credibility," CAS Study Note, March 1993. | Brosius | A1 | OP |
| Clark, D.R., "LDF Curve Fitting and Stochastic Reserving: A Maximum Likelihood Approach," Casualty Actuarial Society Forum, Fall 2003. | Clark | A2, A3 | OP |
| Feldblum, S., "Dependency Modeling," CAS Study Note, September 2010 (Updated March 25, 2013). | Feldblum | C2, C3 | OP |
| Goldfarb, R. "P\&C Insurance Company Valuation," CAS Study Note, October 2010. | Goldfarb | $\begin{array}{r} \mathrm{B} 1, \mathrm{~B} 2, \\ \mathrm{~B} 3 \end{array}$ | OP |
| Hürlimann, W., "Credible Loss Ratio Claims Reserves: The Benktander, Neuhaus and Mack Methods Revisited," Astin Bulletin 39(1), pp. 81-99, 2009. <br> Candidates are not responsible for mathematical proofs. | Hürlimann | A1 | OP |
| International Actuarial Association, "A Global Framework for Insurer Solvency Assessment," a research report of the Insurer Solvency Assessment Working Party, 2004, Chapters 1, 2, 5, 7, 8, and 9; Appendices B, D, E, H, and I. Including Errata. | IAA | $\begin{aligned} & \mathrm{C} 1, \mathrm{C} 2, \\ & \mathrm{C} 3, \mathrm{C} 4, \\ & \mathrm{C} 5, \mathrm{C} 6 \end{aligned}$ | OP |
| Mack, T., "Measuring the Variability of Chain Ladder Reserve Estimates," Casualty Actuarial Society Forum, Spring 1994. | Mack (1994) | A2, A3 | OP |
| Mack, T. "Credible Claims Reserve: The Benktander Method," ASTIN Bulletin, 2000, pp. 333-337. | Mack (2000) | A1 | OP |
| Marshall, K.; Collings, S.; Hodson, M.; and O’Dowd, C., "A Framework for Assessing Risk Margins," Institute of Actuaries of Australia 16th General Insurance Seminar, 9-12 November 2008, Coolum, Australia. | Marshall et al. | $\begin{aligned} & \text { A5- } \\ & \text { A10 } \end{aligned}$ | OP |
| Patrik, G.S., "Reinsurance," Foundations of Casualty Actuarial Science (Fourth Edition), Casualty Actuarial Society, 2001, Chapter 7, pp. 434-464 (section on Reinsurance Loss Reserving). | Patrik | $\begin{aligned} & \text { A11, } \\ & \text { A12, } \\ & \text { A13 } \end{aligned}$ | OP |
| Sahasrabuddhe, R., "Claims Development by Layer: The Relationship between Claims Development Patterns, Trend and Claim Size Models" Casualty Actuarial Society E-Forum, Fall 2010, Volume 1 (revised January 2, 2013). Including errata. | Sahasrabuddhe | A4 | OP |


| Shapland, M.; and Leong, J.W.K., "Bootstrap Modeling: Beyond the Basics," Casualty Actuarial Society E-Forum, Fall 2010. Including errata. | Shapland and Leong | $\begin{aligned} & \text { A5- } \\ & \text { A10 } \end{aligned}$ | OP |
| :---: | :---: | :---: | :---: |
| Siewert, J.J., "A Model for Reserving Workers Compensation High Deductibles," Casualty Actuarial Society Forum, Summer 1996, pp. 217-244. | Siewert | A4 | OP |
| Teng, M.T.S.; and Perkins, M.E., "Estimating the Premium Asset on Retrospectively Rated Policies," PCAS LXXXIII, 1996, pp. 611-647, excluding Section 5. Including discussion of paper: Feldblum, S., PCAS LXXXV, 1998, pp. 274-315, Sections 1 and 2 only. Candidates will not be held responsible for specific Annual Statement notation but will be responsible for concepts presented. | Teng and Perkins | A14 | OP |
| Venter, G.G., "ERM for Strategic Management-Status Report," Society of Actuaries, 2010. | Venter <br> Strategic <br> Management | C4, C5 | OP |
| Venter, G.G., "Non-tail Measures and Allocation of Risk Measures," CAS Study Note, 1/11/2010. | Venter Nontail Measures | C4, C5 | OP |
| Venter, G.G., "Tails of Copulas," PCAS LXXXIX, 2002, pp. 68-113. | Venter Copulas | C2 | OP |
| Venter, G.G., "Testing the Assumptions of Age-to-Age Factors," PCAS LXXXV, 1998, pp. 807-847. | Venter <br> Factors | A2, A3 | OP |
| Venter, G.G.; and Underwood, A., "Value of Risk Reduction," CAS Study Note, 2010. | Venter and Underwood | $\begin{array}{r} \mathrm{C} 4, \mathrm{C} 5, \\ \mathrm{C} 6 \end{array}$ | OP |
| Verrall, R.J., "Obtaining Predictive Distributions for Reserves Which Incorporate Expert Opinion," Variance, Vol. 1, Issue 1, 2007, Casualty Actuarial Society. Including errata. | Verrall | $\begin{aligned} & \text { A5- } \\ & \text { A10 } \end{aligned}$ | OP |

## Source Key

op All text references marked as Online Publications will be available on a web page titled Complete Text References.
NEW Indicates new or updated material.
sk Material included in the 2014 CAS Study Kit.
SKU Material included in the 2014 CAS Study Kit and the 2014 Update to the 2013 Study Kit.
Items printed in red indicate an update or change.

## Publishers and Distributors

Contact information is furnished for those who wish to purchase the text references cited for Exam 7. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

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Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Website: www.actuarialbookstore.com.

Casualty Actuarial Society, 4350 N. Fairfax Drive, Suite 250, Arlington, VA 22203; telephone: (703) 276-3100; fax: (703) 276-3108; e-mail: office@casact.org; Website: www.casact.org.

Institute and Faculty of Actuaries, Staple Inn Hall, High Holborn, London WC1V 7QJ, United Kingdom; telephone: +44 (0)20 7632 2111; Website: www.actuaries.org.uk.
Institute of Actuaries of Australia, Level 7 Challis House 4 Martin Place, Sydney NSW 2000, Australia; telephone: +61 (2) 9233 3466; Website: http://www.actuaries.asn.au.
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SlideRule Books, P.O. Box 69, Greenland, NH 03840; telephone: (877) 407-5433 or (605) 8455580; fax: (877) 417-5433 or (605) 845-7627; Website: www.sliderulebooks.com.

Society of Actuaries, 475 N. Martingale Road, Suite 600, Schaumburg, IL 60173; telephone: 847.706.3500; Website: www.soa.org.

## 2015 Exam 8 Syllabus Advanced Ratemaking

The syllabus for this four-hour exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain conceptually in the context of an examination.
KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.
Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.
Items marked with a bold SK constitute the 2015 CAS Exam 8 Study Kit that may be purchased from the CAS Online Store. Items marked with a bold OP (Online Publication) are available at no charge and may be downloaded from the CAS website.

Please check the "Syllabus Updates" section of the CAS Web Site for any changes to the Syllabus.
Candidates for Exam 8 are expected to have already acquired considerable technical knowledge and practical experience in insurance ratemaking. Therefore, this examination will assume a working knowledge of basic ratemaking and will deal with advanced topics. To some degree, the examination will deal with the types of practical problems that a fully qualified actuary, working in ratemaking, should be able to solve. The ability to apply ratemaking knowledge and experience may be tested through questions dealing with problems for which there are no generally recognized solutions.

The readings for Exam 8 should be studied for illustration of basic principles and theories, as well as for insight into advanced ratemaking problems and their solutions.

## A. Classification Ratemaking

Range of weight for Section A: 20-30 percent
In this exam, classification ratemaking and rate filings, which were introduced earlier in the syllabus, are treated in greater depth. The material in this section provides tools that enable the practitioner to go beyond mechanical construction to the comparison and evaluation of alternative classification schemes.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Identify and evaluate possible rate classes. Range of weight: 5-10 percent | a. Characteristics of appropriate classifications <br> b. Sampling techniques <br> c. Credibility considerations <br> d. Statistical significance <br> e. Cluster analysis |
| READINGS |  |
| AAA <br> Bailey \& Simon <br> Mahler 1 <br> Robertson |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 2.Measure statistical significance of possible <br> classes and estimate the loss costs of rating <br> $\quad$ classes. | a. |
| b. Multidimensional relativities |  |
| Range of weight: 5-10 percent | c. |
| READINGS | d. $\quad$ Holdibility technt Test |
| Bailey \& Simon |  |
| Couret \& Venter |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 3. Formularize and solve generalized linear | a. GLM assumptions compared to: |
| models (GLMs) for classification <br> ratemaking. | • One-way analysis <br> Range of weight: 5-10 percent |
|  | binimum bias procedures <br> b. Classical linear analysis <br> c. Aliasing and near-aliasing |
| READINGS |  |
| Anderson et al. |  |

## B. Excess, Deductible, and Individual Risk Rating

## Range of weight for Section B: 50-70 percent

One of the important functions performed by an actuary is rating individual risks. Prior to Exam 8 , most of the readings addressed group or classification risk rating. This section is intended to prepare candidates to design and manage excess, deductible, and individual risk rating systems.
The readings range from those that discuss the theoretical foundation of excess, deductible, and individual risk rating, to those that discuss the application of specific rating plans. Candidates are expected to apply these concepts in a creative and problem-solving manner.
The first subsection covers pricing for layers of loss including excess and deductible business while the following subsections cover individual risk rating consisting of:

Experience rating, in which prior individual risk experience is used to adjust rates prospectively.
Retrospective and loss sensitive rating, in which the insured will pay an amount (in premium or retained loss) that depends on the experience after the policy has been written.

Candidates are also expected to be knowledgeable in the application of individual risk rating plans currently in use. Excerpts from the NCCI Experience Rating Plan Manual for Workers Compensation and Employers Liability Insurance, NCCI Retrospective Rating Plan Manual for Workers Compensation and Employers Liability Insurance, and ISO Commercial General Liability Experience and Schedule Rating Plan will be provided with the examination. Candidates are not required to memorize the details, but will be expected to be able to use the details of these plans during the examination. Since the necessary excerpts will be included with the examination, candidates will not be allowed to bring copies of the documents into the examination room.

## Excess and Deductible Rating

Excess and deductible rating allows the insured to retain the risk of loss and loss expenses up to limits selected in advance.

This section builds on the material covered in the basic ratemaking section of Exam 5. Candidates should have a general knowledge and understanding of excess coverages and the problems inherent in pricing these coverages for different lines of business.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1. Apply frequency and severity distributions <br> to determine expected losses by layer of <br> insurance. | a.Severity distributions and their uses, including <br> increased limits factors (ILFs) and loss <br> elimination ratios (LERs) |
| Range of weight: 8-12 percent | b.Properties of ILFs and LERs <br> c. <br> Interaction among inflation, changes in layer, and <br> losses <br> Methods of estimating frequency and severity <br> distributions from losses <br> READINGS <br> Gillam \& Snader 1 <br> Lee 1 <br> Mahler 2 <br> Miccolisd.$\quad$ |

\(\left.$$
\begin{array}{|l|l|}\hline \text { LEARNING OBJECTIVES } & \text { KNOWLEDGE STATEMENTS } \\
\hline \begin{array}{ll}\text { 2. Estimate aggregate loss distributions. } \\
\text { Range of weight: 8-12 percent }\end{array} & \begin{array}{l}\text { a. } \\
\text { Techniques to estimate aggregate loss } \\
\text { distributions directly from aggregate data (e.g., } \\
\text { Table M, Table L) }\end{array}
$$ <br>
\hline READINGS \& bonstruction of an aggregate loss distribution <br>

from frequency and severity distributions\end{array}\right]\)| Brosius |
| :--- |
| Gillam \& Snader 2 |
| Lee 2 |
| Mahler 3 |
| Skurnick |

## Experience Rating

The primary goal of experience rating is the adjustment of an individual risk's rate to reflect the extent to which that risk's own experience identifies it as being different from other risks in the same class. The readings begin with principles and concepts, and then move to a discussion of plans in current use.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Adjust class rates based on individual risk experience and exposure. <br> Range of weight: 8-12 percent | a. Actuarial principles and concepts underlying the development of experience rating plans <br> b. Credibility concepts (e.g., maximum single loss) <br> c. Current NCCI and ISO experience rating plans <br> d. Schedule rating |
| READINGS |  |
| GillamGillam \& Snader 1ISONCCI 1Venter |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 4. Assess effectiveness of experience rating plans. <br> Range of weight: 5-10 percent | a. Off-balance factors <br> b. Evaluation techniques (e.g., quintile test) |
| READINGS |  |
| Gillam <br> Venter |  |

## Retrospective and Loss Sensitive Rating

Retrospective rating allows adjustment of individual risk premium after policy expiration in response to actual loss and expenses associated with the policy. The retrospective rating plans currently in use adjust the premium up or down within limits selected in advance.
$\left.\begin{array}{|l|l|}\hline \text { LEARNING OBJECTIVES } & \text { KNOWLEDGE STATEMENTS } \\ \hline \begin{array}{l}\text { 5. Construct a retrospectively rated plan. } \\ \text { Range of weight: } 8-12 \text { percent }\end{array} & \text { a. Actuarial principles and concepts underlying the } \\ \text { construction of a retrospective rating plan (e.g., } \\ \text { balance principle, construction of table of } \\ \text { insurance charges) }\end{array}\right\}$

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 6. Analyze the elements of a loss sensitive <br> rating plan. | a.Influence of the parameters and other elements of <br> the plan on the final price and potential <br> profitability of product |
| Range of weight: 8-12 percent | b.Influence of the parameters and other elements of <br> the plan on cost and cash flow to insured |
| READINGS |  |
| Fisher <br> Gillam \& Snader 2 <br> Lee 2 <br> Skurnick |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 7. Calculate the cost of the layer of risk given <br> the loss cost. | a.Variability of expenses by layer and policy <br> provisions <br> Range of weight: 4-6 percent |
| b.Large dollar deductible (LDD) and excess <br> policy provisions <br> c. |  |
| REAdvantages of LDD and excess policies |  |

## C. Catastrophic and Reinsurance Pricing

Range of weight for Section C: 15-20 percent

## Catastrophe Ratemaking

This subsection introduces candidates to the methods used to model losses due to catastrophic events for the purpose of generating a catastrophe risk load and to manage the total exposure from catastrophic events within an insurance portfolio.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Describe the components and structure of catastrophe models. | a. Hazard, exposure, vulnerability and loss modules <br> b. Exceedance Probability Curve <br> c. Simulation and modeling techniques |
| 2. Explain the use of catastrophe models in insurance ratemaking and portfolio management. <br> Range of weight for Learning Objectives C. 1 and C. 2 collectively: 4-6 percent | a. Insurability of catastrophe risks <br> b. Sources and nature of uncertainty in catastrophe modeling <br> c. Use of catastrophe models in insurance ratemaking <br> d. Use of catastrophe models in portfolio management |
| READING |  |
| Grossi \& Kunreuther, plus Errata for Section 2.4 |  |

## Reinsurance Ratemaking

This subsection introduces candidates to current and historical methods used to price reinsurance. The candidates will be familiar with many of these methods from the materials on primary insurance ratemaking; the emphasis here is on the application of these methods in pricing reinsurance contracts.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Determine the price of various types of reinsurance contracts. <br> Range of weight: 3-5 percent | a. Types of contracts, including excess of loss, quota share, surplus share, treaty, aggregate excess of loss, and facultative <br> b. Common methods for pricing reinsurance, including burn cost, exposure rating and experience rating <br> c. Reinsurance loss development and trend <br> d. Use of increased limit factors in reinsurance pricing <br> e. Evaluation of aggregate distribution models <br> f. Prospective and retrospective pricing in reinsurance |
| 4. Determine the effect of common contract provision on the price of reinsurance contracts. <br> Range of weight: 3-5 percent | a. Pricing for reinstatements, loss corridors, clash, profit and sliding scale commissions, and other common provisions in reinsurance contracts |
| 5. Specify, fit, and use loss distribution based exposure curves. <br> Range of weight: 3-5 percent | a. Define an exposure curve <br> b. Limited and unlimited distributions <br> c. Expected value and total loss probability <br> d. Use of MBBEFD class distributions as exposure curves |
| READING |  |
| Clark <br> Bernegger |  |

## Complete Text References for Exam 8

Text references are alphabetized by the citation column.

| Citation | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
| American Academy of Actuaries Committee on Risk Classification, "Risk Classification Statement of Principles," June 1980. [Available at no charge from the American Academy of Actuaries at (202) 223-8196 or on the Academy's Web Site at www.actuary.org.] | AAA | A1 | OP |
| Anderson, D.; Feldblum, S; Modlin, C; Schirmacher, D.; Schirmacher, E.; and Thandi, N., "A Practitioner's Guide to Generalized Linear Models" (Third Edition), CAS Study Note, February 2007, pp. 4-39 only. [Note: the study note edition is a revised version of a paper from the CAS Discussion Paper Program. Candidates must use the study note edition.] | Anderson et al. | A3 | OP |
| Bailey, R. A.; and Simon, L. J., "An Actuarial Note on the Credibility of Experience of a Single Private Passenger Car," PCAS XLVI, 1959, pp. 159-164. Including discussion of paper: Hazam, W. J., PCAS XLVII, 1960, pp. 150-152. |  <br> Simon | A1-A2 | OP |
| Bernegger, S., "Swiss Re Exposure Curves and the MBBEFD Distribution Class," ASTIN Bulletin, Vol. 27, No. 1, May 1997, pp. 99-111. | Bernegger | C3, C5 | OP |
| Brosius, J. E., "Table M Construction," CAS Study Note, 2002. | Brosius | B2, B5 | OP |
| Clark, D. R., "Basics of Reinsurance Pricing," CAS Study Note, Revised 2014. Candidates are not responsible for Section 6 of the paper. | Clark | C3, C4 | OP |
| Couret, J.; and Venter, G., "Using Multi-Dimensional Credibility to Estimate Class Frequency Vectors in Workers Compensation," ASTIN Bulletin, Vol. 38, No. 1, May 2008, pp. 72-85. | Couret \& Venter | A2 | OP |
| Fisher, G.K., "Pricing Aggregates on Deductible Policies," CAS Study Note, May 2002. | Fisher | B6, B7 | OP |
| Gillam, W. R., "Workers' Compensation Experience Rating: What Every Actuary Should Know," PCAS LXXIX, 1992, Sections 1-5, pp. 215-239. | Gillam | B3, B4 | OP |
| Gillam, W. R.; and Snader, R. H., "Fundamentals of Individual Risk Rating," National Council on Compensation Insurance (Study Note), 1992, Part I. | Gillam \& Snader 1 | B1, B3 | OP |
| Gillam, W. R.; and Snader, R. H., "Fundamentals of Individual Risk Rating," National Council on Compensation Insurance (Study Note), 1992, Part II. | Gillam \& Snader 2 | $\begin{array}{r} \hline \mathrm{B} 2, \mathrm{~B} 5, \\ \text { B6 } \end{array}$ | OP |
| Gillam, W. R.; and Snader, R.H., "Fundamentals of Individual Risk Rating," National Council on Compensation Insurance (Study Note), 1992, Part III. | Gillam \& Snader 3 | B7 | OP |


| Grossi, P.; and Kunreuther, H., Editors, Catastrophe Modeling: A <br> New Approach to Managing Risk, 2005, Springer, Chapters 2-6 <br> (excluding references at the end of each chapter). Errata 2.4. |  <br> Kunreuther | C1, C2 | B |
| :--- | :--- | ---: | ---: |
| Insurance Services Office, Inc., Commercial General Liability <br> Experience and Schedule Rating Plan, 2006. Excerpts from the <br> ISO Commercial General Liability Experience and Schedule <br> Rating Plan will be provided with the exam. Candidates are not <br> required to memorize the details, but will be expected to be able to <br> use them on the exam. Since they will be included with the exam, <br> candidates will not be allowed to bring copies of the documents <br> into the examination room. | ISO | B3 | SK |
| Lee, Y. S., "The Mathematics of Excess of Loss Coverages and <br> Retrospective Rating-A Graphical Approach," Sections 1-3, <br> PCAS LXXV, 1988, pp. 49-64. | Lee 1 | B1 | OP |
| Lee, Y. S., "The Mathematics of Excess of Loss Coverage and <br> Retrospective Rating-A Graphical Approach," Section 4, PCAS <br> LXXV, 1988, pp. 64-78. Candidates are not responsible for "Other <br> Applications" on pp. 75-76. | Lee 2 | B2, B5, |  |
| Mahler, H. C., "An Example of Credibility and Shifting Risk <br> Parameters," PCAS LXXVII, 1990, pp. 225-282. Candidates will <br> not be tested on the Appendices. | Mahler 1 | OP |  |
| Mahler, H. C., Discussion of "Retrospective Rating: 1997 Excess <br> Loss Factors," PCAS LXXXV, 1998, pp. 316-344. Appendices B- <br> D are for reference only; candidates do not need to memorize <br> formulas in Appendices B-D. Including Errata. | Mahler 2 | A1 | OP |
| Mahler, H. C., "Workers Compensation Excess Ratios: An <br> Alternative Method of Estimation," PCAS LXXXV, 1998, pp. <br> 132-156. | Mahler 3 | B1 | OP |
| Miccolis, R. S., "On the Theory of Increased Limits and Excess of <br> Loss Pricing," PCAS LXIV, 1977, pp. 27-59 excluding "Risk <br> Reduction by Layering" (pp. 45-49). Including discussion of <br> paper: Rosenberg, S., PCAS LXIV, 1977, pp. 60-73. | Miccolis | B2 | OP |
| National Council on Compensation Insurance, Experience Rating <br> Plan Manual for Workers Compensation and Employers Liability <br> Insurance. Candidates are responsible for only the excerpted <br> material included in the Study Kit. Candidates are not required to <br> memorize the details, but will be expected to be able to use them <br> on the examination. Since te required excerpts will be included <br> with the examination, candidates will not be allowed to bring <br> copies of the documents into the examination room. | NCCI 1 | B3 | SK |


| National Council on Compensation Insurance, Retrospective <br> Rating Plan Manual for Workers Compensation and Employers <br> Liability Insurance. Candidates are responsible for only the <br> excerpted material included in the Study Kit, excluding Part 2, <br> Section III, on cancellation provisions. Candidates are not required <br> to memorize the details, but will be expected to be able to se them <br> on the examination. Since the required excerpts will be included <br> with the examination, candidates will not be allowed to bring <br> copies of the documents into the examination room. | NCCI 2 | B5 | SK |
| :--- | :--- | ---: | ---: |
| Robertson, J.P., "NCCI's 2007 Hazard Group Mapping," <br> Variance, Vol. 3, Issue 2, 2009, Casualty Actuarial Society, pp. <br> 194-213. | Robertson | A1 | OP |
| Skurnick, D., "The California Table L," PCAS LXI, 1974, pp. 117- <br> 140. Including discussion of this paper: Gillam, W.R., PCAS <br> LXXX, 1993, pp. 353-365. | Skurnick | B2, B5, | OP |
| Teng, M.T.S., "Pricing Workers' Compensation Large Deductible <br> and Excess Insurance," Casualty Actuarial Society Forum, Winter <br> 1994, pp. 413-437. | Teng | B7 | OP |
| Venter, G.G., "Experience Rating-Equity and Predictive <br> Accuracy," NCCI Digest, April 1987, Volume II, Issue I, pp. 27- <br> 35. (Pages are shown as 1-9 in the Study Kit version.) | Venter | B3, B4 | SK |

## Source Key

B Book - may be purchased from the publisher or bookstore or borrowed from the CAS Library.
OP All text references marked as Online Publications will be available on a web page titled Complete Text References.

SK Material included in the 2015 CAS Study Kit.
Items printed in red indicate an update, clarification, or change.

## Publishers and Distributors

Contact information is furnished for those who wish to purchase the text references cited for Exam 8. Publishers and distributors are independent and listed for the convenience of candidates; inclusion does not constitute endorsement by the CAS.

Actex Publications (Mad River Books), 107 Groppo Drive, Suite A, P.O. Box 974, Winsted, CT 06098; telephone: (800) 282-2839 or (860) 379-5470; fax: (860) 738-3152; e-mail:
retail@actexmadriver.com; Website: www.actexmadriver.com.
Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 582-9672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Web site: www.actuarialbookstore.com.

American Academy of Actuaries, 1100 Seventeenth Street NW, Seventh Floor, Washington, DC 20036; telephone: (202) 223-8196; Web site: www.actuary.org.

Casualty Actuarial Society Forum, PCAS, Variance, and Discussion Paper Program, Casualty Actuarial Society, 4350 N. Fairfax Drive, Suite 250, Arlington, VA 22203; telephone: (703) 2763100; fax: (703) 276-3108; e-mail: office@casact.org; Web site: www.casact.org.

Insurance Services Office, Inc., 545 Washington Boulevard, Jersey City, NJ 07310-1686; telephone: (800) 888-4476.

National Council on Compensation Insurance, 901 Peninsula Corporate Circle, Boca Raton, FL 33487; telephone: (800) NCCI-123.

SlideRule Books, P.O. Box 69, Greenland, NH 03840; telephone: (877) 407-5433 or (603) 3736140; fax: (877) 417-5433 or (603) 430-1258; Web site: www.sliderulebooks.com.

## 2015 Exam 9 <br> Financial Risk and Rate of Return

The syllabus for this four-hour exam is defined in the form of learning objectives, knowledge statements, and readings.

LEARNING OBJECTIVES set forth, usually in broad terms, what the candidate should be able to do in actual practice. Included in these learning objectives are certain methodologies that may not be possible to perform on an examination, such as complex simulations, but that the candidate would still be expected to explain conceptually in the context of an examination.

KNOWLEDGE STATEMENTS identify some of the key terms, concepts, and methods that are associated with each learning objective. These knowledge statements are not intended to represent an exhaustive list of topics that may be tested, but they are illustrative of the scope of each learning objective.

READINGS support the learning objectives. It is intended that the readings, in conjunction with the material on the lower numbered examinations, provide sufficient resources to allow the candidate to perform the learning objectives. Some readings are cited for more than one learning objective. The Syllabus and Examination Committees emphasize that candidates are expected to use the readings cited in this Syllabus as their primary study materials.

Thus, the learning objectives, knowledge statements, and readings complement each other. The learning objectives define the behaviors, the knowledge statements illustrate more fully the intended scope of the learning objectives, and the readings provide the source material to achieve the learning objectives. Learning objectives should not be seen as independent units, but as building blocks for the understanding and integration of important competencies that the candidate will be able to demonstrate.
Note that the range of weights shown should be viewed as a guideline only. There is no intent that they be strictly adhered to on any given examination-the actual weight may fall outside the published range on any particular examination.

The overall section weights should be viewed as having more significance than the weights for the individual learning objectives. Over a number of years of examinations, absent changes, it is likely that the average of the weights for each individual overall section will be in the vicinity of the guideline weight. For the weights of individual learning objectives, such convergence is less likely. On a given examination, in which it is very possible that not every individual learning objective will be tested, there will be more divergence of guideline weights and actual weights. Questions on a given learning objective may be drawn from any of the listed readings, or a combination of the readings. There may be no questions from one or more readings on a particular exam.

After each set of learning objectives, the readings are listed in abbreviated form. Complete text references are provided at the end of this exam syllabus.

Items marked with a bold sk constitute the 2014 CAS Exam 9 Study Kit that may be purchased from the CAS Online Store. Items marked with a bold oP (Online Publication) are available at no charge and may be downloaded from the CAS website. Books and other publications marked with a bold в may be purchased from the publisher or a bookstore (with limited copies available to be borrowed from the CAS Library).
Please check the "Syllabus Update" for this exam for any changes to this syllabus.

Exam 9 focuses on a broad array of finance, investment, and financial risk management topics. This examination assumes a working knowledge of basic ratemaking, finance, probability and statistical modeling, liability and reserve risk, and insurance underwriting. The ability to apply this knowledge_and experience may be tested through questions dealing with problems for which there are no generally recognized solutions.

## TEXTS FOR THIS EXAM

There are two main texts: Investments (Tenth Edition) by Bodie, Kane, and Marcus and Options, Futures and Other Derivatives (Eighth Edition) by Hull. Investments contains references to various websites. Candidates are not responsible for the identity of the websites or the actual content of the websites except to the extent that the content is reproduced in the text. Candidates are also not responsible for any aspect of the Excel applications or the boxes entitled "E-Investments" that are usually placed at or towards the end of a chapter.

While, in general, it is suggested that the candidate cover the learning objectives in the order listed, some references to later chapters in texts may occur before references to earlier chapters. In these cases, the candidate may need to review the earlier chapters first and then return to the learning objectives that reference the later chapters.

For the Financial Risk and Rate of Return exam, the appendices are part of the material covered unless specifically excluded.
There are various numeric tables scattered throughout the readings, illustrating actual observations or hypothetical examples. Candidates are not responsible for the actual numeric values.

## BACKGROUND

Candidates may find it helpful to review Chapters 1-5 of Investments for background in financial markets and instruments as well as the Venter paper for background on liquidity risk.

## A. Portfolio Theory and Equilibrium in Capital Markets

## Range of weight for Section A: 20-30 percent

The portfolio theory portion of this section discusses the relationship between the risk and return for different combinations of risky and risk-free investments and discusses the effect of diversification on this relationship. Candidates are introduced to the manner in which investors might select a particular portfolio, from those available, that best suits their individual preferences for risk and return. In the portion of this section on equilibrium in capital markets, various equilibrium models are presented, including the Capital Asset Pricing Model (CAPM) and Arbitrage Pricing Theory (APT). The concept of market efficiency is presented to help candidates understand the factors that move market prices towards and away from the theoretical prices presented in these models.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Explain key concepts of risk: <br> - Appetite <br> - Tolerance <br> - Aversion <br> - Measurement <br> - Portfolio construction <br> - Strategies for monitoring <br> Range of weight: 0-5 percent | a. Utility functions, utility scores, and utility maximization <br> b. Risk aversion <br> c. Mean-variance criterion <br> d. Capital allocation line <br> e. Complete portfolio <br> f. Reward to volatility ratio (Sharpe ratio) <br> g. Passive versus active strategies: costs of active strategy and free-rider benefit |
| READINGS |  |
| BKM, Chapter 6 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 2. Calculate the expected value, variance, and covariance of returns of asset portfolios in a multi-dimensional setting. <br> Range of weight: 0-5 percent | a. Expected return and standard deviation for portfolios of risky and risk-free assets <br> b. Optimal risky portfolio <br> c. Optimal complete portfolio |
| 3. Describe the Markowitz Portfolio Selection Model. <br> Range of weight: 3-7 percent | a. Minimum variance frontier <br> b. Efficient frontier of risky assets <br> c. Optimal capital allocation line <br> d. Separation property <br> e. Asset allocation versus security selection |
| 4. Explain and demonstrate effects of various diversification strategies. <br> Range of weight: 0-5 percent | a. Systematic risk <br> b. Risk pooling <br> c. Risk sharing <br> d. Insurance principle |
| READINGS |  |
| BKM, Chapter 7 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 5. Explain and use the single factor models and compare/contrast the process of portfolio construction with the full covariance (Markowitz) model. <br> Range of weight: 3-7 percent | a. Markowitz model <br> b. Single factor model <br> c. Single index model <br> d. Systematic risk <br> e. Alpha, Beta estimating and forecasting <br> f. Covariance and correlation estimates for single index model <br> g. Risk premiums due to market and non-market factors <br> h. Parameter estimation risk <br> i. Macroeconomic factors |
| READINGS |  |
| BKM, Chapter 8 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 6. Explain the assumptions and construction of CAPM and use CAPM to calculate expected returns for risky securities. <br> Range of weight: 3-7 percent | a. CAPM assumptions <br> b. Market price of risk <br> c. Capital market line <br> d. Security market line <br> e. Extensions of CAPM <br> - Zero Beta CAPM <br> - CAPM with non-traded assets and labor income <br> - ICAPM <br> - CAPM with liquidity adjustments |
| 7. Compare/contrast CAPM and single index model and explain the assumptions that are modified under various extensions of CAPM. <br> Range of weight: 0-5 percent | a. CAPM <br> b. Single index model <br> c. Expected versus actual returns <br> d. Market portfolio versus market index |
| READINGS |  |
| BKM, Chapter 9 |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 8. Use APT to determine the expected return for a security and compare/contrast with CAPM and factor models. <br> Range of weight: 0-5 percent | a. Arbitrage and the Law of One Price <br> b. APT and its comparison to CAPM <br> c. Factor betas <br> d. Factor portfolios and factor risk premiums <br> e. Alternative factors in multifactor models |
| READINGS |  |
| BKM, Chapter 10 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 9. Explain market efficiency and its | a. Efficient market hypothesis |
| implications for portfolio management, | b. Random walk |
| and describe the various tests and studies | c. Technical analysis |
| of market efficiency. | d. Fundamental analysis |
| Range of weight: 0-5 percent | e. Passive investment strategy |
|  | f. Portfolio management |
| READINGS |  |
| BKM, Chapter 11 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 10. Explain the influence of behavioral <br> finance in understanding certain aspects <br> of market efficiency. | a. Information processing errors |
| Range of weight: 0-5 percent | b. Behavioral biases |
|  | c. Limits to arbitrage |
|  | d. Violations of Law of One Price |
|  | e. Behavioral critique |
| READINGS | f. Technical analysis |
| BKM, Chapter 12 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 11. Describe the use of historical data to test the CAPM and APT, the statistical limitations of these tests and the key findings of various studies. <br> Range of weight: 0-5 percent | a. Two-stage test of the expected return - beta relationship <br> b. Roll's critique <br> c. Important tests of CAPM and their results/conclusions <br> d. Accounting for Human Capital, Cyclical Variations, and Nontraded Business <br> e. Chen, Roll and Ross tests of APT <br> f. Fama and French's 3-Factor Model, including alternative explanations of the empirical results |
| 12. Describe the Equity Premium Puzzle and various explanations for the puzzle. <br> Range of weight: 0-5 percent | a. Equity Premium Puzzle <br> b. Expected vs. realized returns <br> c. Survivorship bias <br> d. Extensions of CAPM <br> e. Behavioral explanations |
| READINGS |  |
| BKM, Chapter 13 |  |

## B. Asset-Liability Management

## Range of weight for Section B: 15-25 percent

This section exposes the candidate to factors that influence the price sensitivity of fixed income securities and presents various ways in which a portfolio manager might manage the interest rate and cash flow risk in a portfolio of these instruments. The same concepts are also applied to the interest rate risk associated with a firm's liabilities and the interest rate risk associated with a firm's total market value, inclusive of their franchise value.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Explain the different Term Structure Theories. <br> Range of weight: 0-5 percent | a. Expectations hypothesis <br> b. Liquidity preference theory <br> c. Segmentation theory <br> d. Forward rate versus expected spot rate |
| 2. Determine U.S. Treasury zero rates at different maturities. <br> Range of weight: 3-7 percent | a. Bootstrap method for determining zero rates from coupon bonds using both continuous and semi-annual compounding <br> b. Determining forward rates from spot rates (zero rates) <br> c. Spot rates <br> d. Short rates <br> e. LIBOR zero rates <br> f. Forward Rate Agreements |
| READINGS |  |
| BKM, Chapter 15 Hull, Chapter 4 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Utilize various strategies to manage interest rate risk and cash flow risk in a bond portfolio. <br> Range of weight: 3-7 percent | a. Duration (Macaulay, modified, and effective) <br> b. Convexity <br> c. The effect of interest changes on bond prices <br> d. Immunization <br> e. Cash flow matching and dedication <br> f. Rebalancing <br> g. Use of interest rate swaps, mortgage-backed securities, and other derivative securities to alter the interest rate risk for a bond portfolio <br> h. Currency swaps |
| READINGS |  |
| BKM, Chapter 16 <br> Hull, Sections 4.8 and 4.9, and Chapter 7 |  |

$\left.\begin{array}{|l|l|}\hline \text { LEARNING OBJECTIVES } & \text { KNOWLEDGE STATEMENTS } \\ \hline \text { 4. } \begin{array}{l}\text { Calculate the Macaulay duration of loss } \\ \text { reserves and the Macaulay duration of the } \\ \text { surplus of a property and casualty (P\&C) } \\ \text { insurance company. }\end{array} & \begin{array}{l}\text { a. } \\ \text { b. }\end{array} \\ \hline \text { Range of weight: 0-5 percent }\end{array} \quad \begin{array}{l}\text { Relationship between surplus, asset, and liability } \\ \text { durations }\end{array}\right]$

## C. Financial Risk Management

Range of weight for Section C: 20-30 percent
This section addresses financial risks as well as risks related to the insurance industry from the financial economics perspective. The concepts and techniques presented in this section are important components in the field of enterprise risk management.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 1. Estimate the credit risk due to default and default correlation associated with fixed income securities. <br> Range of weight: $0-5$ percent | a. Default intensity or hazard rate <br> b. Unconditional default probability <br> c. Expected loss from default <br> d. Yield spread <br> e. Recovery rate <br> f. Relationship between asset volatility and equity volatility. <br> g. Merton's model <br> h. Credit ratings transition matrix <br> i. Use of Gaussian copula to simulate correlated ratings transitions for two bonds <br> j. CreditMetrics approach to estimating credit value at risk |
| 2. Describe the credit risk in derivatives transactions and various mechanisms to manage the risk. <br> Range of weight: $0-5$ percent | a. Counterparty default risk <br> b. Netting <br> c. Collateralization <br> d. Downgrade triggers |
| READINGS |  |
| Hull, Chapter 23 |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 3. Describe the reasons for the development of credit derivatives market, the valuation of credit derivative contracts, and the complexity of trading credit risks. Range of weight: $0-5$ percent | a. Credit default swaps (CDS) <br> b. Mark-to-market <br> c. Total Return Swaps <br> d. Collateralized debt obligation (CDO) and synthetic CDO <br> e. The role CDS played in the 2008 financial crisis |
| READINGS |  |
| Coval, Jurek, and Stafford Hull, Chapter 24 (24.1-24.9) |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 4. Describe liquidity risk and various mechanisms to manage the risk. <br> Range of weight: 0-5 percent | a. Liquidity risk <br> b. Sources of liquidity risk <br> c. Risk reduction techniques <br> d. Lessons from the recent economic crises |
| READINGS |  |
| Academy Venter |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- | :--- |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 7. Describe various risk measures and the need for practicing sound financial risk management. <br> Range of weight: $0-5$ percent | a. Capital structure and risk taking incentives <br> b. Regulation and rating agency <br> c. Value at risk (VaR) <br> d. Cash flow at risk <br> e. Shortfall risk <br> f. Risk-based capital <br> g. Expected policyholder deficit (EPD) <br> h. Capital associated with a constant EPD ratio <br> i. Risk-adjusted return on capital (RAROC), including alternative measures of income and alternative measures of risk-adjusted capital <br> j. Economic value added (EVA) <br> k. Friction costs, including agency costs and double taxation <br> 1. Lessons from past failures due to poor financial risk management <br> m . Manager incentives as motivations for hedging risk |
| READINGS |  |
| Butsic |  |
| Culp, Miller and Neves (excluding Appendix) |  |
| Cummins Capital |  |
| Goldfarb |  |
| Stulz |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 8. Describe the concept of economic capital (or risk capital) in the insurance industry and various methods of allocating the risk capital to business units or lines of business. <br> Range of weight: 0-5 percent | a. Financial and insurance risks <br> b. Economic capital or risk capital <br> c. Risk aggregation <br> d. Strengths and weaknesses of the various allocation methods using risk measures such as: <br> - Percentile (VaR) <br> - Conditional tail expectation (CTE) <br> - EPD Ratio <br> - Merton-Perold method <br> - Insolvency Put/EPD ratio risk measure <br> - Myers-Read method <br> - Co-Measures <br> - Co-CTE |
| 9. Apply the RAROC framework to risk management in the insurance industry. <br> Range of weight: $0-5$ percent | a. Economic profit as income measure <br> b. Cost of capital <br> c. RAROC <br> d. Additional risk margin in price <br> e. Multi-period capital commitment |
| 10. Assess the performance of business units and set prices for insurance policies on a risk-adjusted basis. <br> Range of weight: 0-5 percent | a. Economic profit as income measure <br> b. Cost of capital <br> c. RAROC <br> d. Additional risk margin in price <br> e. Multi-period capital commitment |
| READINGS |  |
| Cummins Capital Goldfarb |  |

## D. Rate of Return, Risk Loads, and Contingency Provision

## Range of weight for Section D: 25-35 percent

This section explores the relationship between insurance concepts (such as underwriting profits, premium-to-surplus ratios, and investment income) and financial concepts (such as interest rates, inflation rates, cost of capital, and risk premiums). The readings build on a background of finance as related to the insurance business, and deal with specific techniques used by actuaries to develop an appropriate profit loading in insurance prices.

Because insurance claims are fortuitous, the expected profit loaded in rates may not be realized. Some models discuss insured events that are predictable in time and amount while other models consider when insured events are uncertain, particularly where capacity is limited and/or sufficient diversification of exposure is impossible.

| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :--- | :--- |
| 1.Evaluate the internal rate of return <br> framework. <br> Range of weight: 3-7 percent | a.Inter-relationship between the product market <br> and financial market |
|  | b.Capital structure of insurance company <br> compared to other industries |
| d.Decision rule of the IRR model <br> distinction between equity flows and all other <br> cash flows |  |
|  | e.Impact of surplus allocation and timing on <br> equity flows |
| f.Methods of allocating surplus and impact on <br> IRR |  |
| Feldblum Financial | g.Potential pitfalls in IRR analysis |



| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 4. Describe the underwriting profit provision. Range of weight: 0-5 percent | a. Evolution of the profit provision <br> b. Policyholder versus stockholder return <br> c. Types of underwriting profit |
| 5. Calculate and compare the provision for underwriting profit in property and casualty insurance rates. <br> Range of weight: 3-7 percent | a. Calendar Year Investment Offset procedure <br> b. Present Value Offset procedure <br> c. Calendar Year Return on Equity method <br> d. Present Value of Income over Present Value of Equity method <br> e. Present Value Return on Cash Flow method <br> f. Risk-Adjusted Discounted Cash Flow method <br> g. Internal Rate of Return on Equity Flows method |
| READINGS |  |
| Robbin |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 6. Assess the risks of allocating surplus. Range of weight: 0-5 percent | a. Controversies regarding surplus allocation and leverage ratio <br> b. Sources of risks contributing to surplus need |
| 7. Analyze and calculate income and total rate of return <br> Range of weight: 0-5 percent | a. Measurement of the required rate of return <br> b. Capital structure and the required rate of return |
| READINGS |  |
| Roth |  |
| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| 8. Use investment-equivalent reinsurance pricing to determine risk loads. <br> Range of weight: 3-7 percent | a. Kreps' paradigm <br> b. Loss safety level <br> c. Swap technique <br> d. "Put" option technique <br> e. High excess layer <br> f. Effects of pooling |
| READINGS |  |
| Kreps |  |


| LEARNING OBJECTIVES | KNOWLEDGE STATEMENTS |
| :---: | :---: |
| 9. Calculate and compare the risk loads for property catastrophe insurance. <br> Range of weight: 3-7 percent | a. Order dependency <br> b. Marginal Surplus method <br> c. Marginal Variance method <br> d. Sub-additive and super-additive properties <br> e. Renewal additivity <br> f. Shapley Value method <br> g. Covariance Share method |
| READINGS |  |
| Mango |  |

## Complete Text References for Exam 9

Text references are alphabetized by the citation column.

| Citations | Abbreviation | Learning Objective | Source |
| :---: | :---: | :---: | :---: |
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## Source Key

B Book - may be purchased from the publisher or bookstore or borrowed from the CAS Library.
OP All text references marked as Online Publications will be available on a web page titled Complete Text References above..

SK Material included in the 2015 CAS Study Kit.
Items printed in red indicate an update, clarification, or change.

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e-mail: retail@actexmadriver.com; Website: www.actexmadriver.com.
Actuarial Bookstore, P.O. Box 69, Greenland, NH 03840; telephone: (800) 5829672 (U.S. only) or (603) 430-1252; fax: (603) 430-1258; Website: www.actuarialbookstore.com.

American Academy of Actuaries, 1850 M Street, NW, Suite 300, Washington,

DC 20036; telephone: (202) 223.8196; fax 202.872.1948; Website:
www.actuary.org.
American Risk and Insurance Association, 716 Providence Road, Malvern, PA 19355; telephone: (610) 640-1997; Website: aria@cpcuiia.org.

Bodie, Z.; Kane, A.; and Marcus, A.J., Investments (Tenth Edition), 2014, McGraw-Hill/Irwin, 860 Taylor Station Road, Blacklick, OH 43004; telephone: (800) 262-4729.

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SlideRule Books, P.O. Box 69, Greenland, NH 03840; telephone: (877) 4075433 or (603) 373-6140; fax: (877) 417-5433 or (603) 430-1258; Website: www.sliderulebooks.com.

Society of Actuaries, 475 N. Martingale Road, Suite 600, Schaumburg, IL 60173; telephone: 847.706.3500; Website: www.soa.org.


[^0]:    ${ }^{1}$ Exam LC and Exam ST will be offered through Spring 2016. See Transition Rules.

[^1]:    ${ }^{2}$ Candidates should review carefully the Transition Rules for Exam S as it relates to VEE-Applied Statistical Methods.

[^2]:    *Note: To receive credit for the new Exam 5 on Basic Techniques for Ratemaking and Estimating Claim Liabilities, the candidate must have credit for both old Exams 5 and 6. At the time of transition, if a candidate has credit for only one of the required exams (either old Exam 5 or Exam 6), the candidate will be allowed to take just the part of the exam for which he or she is missing credit (i.e., either the Basic Techniques for Ratemaking section or the Estimating Claim Liabilities section of the new exam) in order to obtain credit for the new exam. This option will be available for a transition period of two sittings after the official conversion to the new education structure (i.e., May 2011 and May 2012). If the candidate does not have credit for both halves of Exam 5 at the end of the transition period, the candidate would have to pass the full version of Exam 5 to receive credit.

[^3]:    LEARNING OBJECTIVES

    1. Use and apply the following concepts in a risk management context:

    - Probability functions and probability density functions
    - Cumulative distribution functions
    - Mode, median, percentiles, and moments
    - Variance and measures of dispersion
    - Moment generating functions
    - Transformations

[^4]:    *Note: The Exam 1 credit chart includes a new waiver for the Actuarial Society of South Africa.

[^5]:    For use on the CAS exams

[^6]:    For use on the CAS exams

