# A Practical Approach to Risk Margins in the Measurement of Insurance Liabilities for Property and Casualty (General Insurance) under Developing International Financial Reporting Standards 

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#### Abstract

The International Accounting Standards Board (IASB) and the Financial Accounting Standards Board (FASB) continue to debate and refine the financial reporting standards that will emerge from Phase II of their joint project on insurance contracts. The changes to the measurement of insurance liabilities for financial reporting are potentially quite significant for most insurance organizations around the world.

The paper presents the authors' views on practical approaches to consider in calculating risk margins in the measurement of insurance liabilities for property and casualty (also referred to as general insurance or non-life) insurance contracts. In particular, the paper focuses on the use of an approach to estimate risk margins that: recognizes risk and uncertainty in the amount and timing of future payments needed to satisfy insurance liabilities; (2) reflects an objective assessment and measurement of risk for insurance liabilities and the price of risk in terms of the amount an insurer would rationally pay to be relieved of the insurance contract obligations that underlie such liabilities; and (3) provides useful financial information for users of IFRS financial statements.


## 1. BACKGROUND, SCOPE AND LIMITATIONS

### 1.1 Background

The concept of risk as an actuarial consideration in the valuation of insurance liabilities has been well understood by the actuarial profession. However, for property and casualty insurance, also known as general insurance or non-life insurance, it is not common practice in many countries to include explicit risk margins or other risk adjustments for general purpose financial reporting. Actuarial practices in a few countries have established what sometimes are referred to as "technical prudential" provisions, typically to satisfy the solvency requirements of insurance regulators/supervisors. Such technical provisions have included a margin or provision for adverse deviations that reflect the risk that the actual amount ultimately paid to extinguish the liabilities could be greater than the expected value estimate of liabilities.

In practice, actuaries have used a variety of technical methods and assumptions to consider such risks, and in many situations risk margins have been implicitly embedded in the assumptions or the selection or interpretation of the results of analyses or models. In the U.S. and certain other jurisdictions, the lack of sufficient adjustments for the time value of money has also been considered to provide an implicit risk margin. Generally Accepted Accounting Principles (GAAP) in most countries have used the amounts established in the financial statements filed with insurance regulators/supervisors, resulting in some jurisdictions including explicit risk margins in their financial statements while others have no explicit risk provisions or risk adjustments. The International Accounting Standards Board (IASB), in developing International Financial Reporting Standard No. 4 (IFRS 4) for insurance contracts, has questioned the inconsistencies in practices applied to determine insurance liabilities in different countries. Such inconsistencies have, in part, been the result of differences in the objectives of insurance regulators/supervisors and the interpretation of accounting guidance as it applies to various types of insurance.

Based on a goal of establishing common principles-based global standards for financial reporting, the IASB has worked for several years on a project to develop standards that would be adopted in most countries, including the U.S., which would provide a common set of principles for the financial reporting of insurance contracts. One of the areas with significant impact to actuaries is the measurement of insurance liabilities under IFRS 4.

There is an extensive discussion of risk margins in a research paper (IAA, 2009), entitled Measurement of Liabilities for Insurance Contracts: Current Estimates and Riske Margins. Many different views and examples of how risk margins might be considered are presented. In this paper, the concept of a risk margin for non-life insurance liabilities is further explored through the application of actuarial research to U.S. insurance company financial statement data available from public sources.

Based on the IASB's 2007 Discussion Paper (DP), Preliminary Views on Insurance Contracts (IASB, 2007) and subsequent discussions of the IASB Board, explicit risk margins, or an explicit risk adjustment, have been included in many of the alternatives for the measurement basis for insurance liabilities. Consequently, while the final IFRS 4 guidance is not known at the time this paper was written, practical actuarial approaches to risk margins can be developed based on the latest alternatives being discussed by the IASB and FASB. This paper pursues the concepts of "current fulfillment value" and "the amount the entity would rationally pay to be relieved of risk", and the resulting implications for estimating a risk adjustment in the measurement of insurance liabilities.

In January 2010, the discussion papers written by the technical staff of the IASB and FASB (IASB reference agenda 6A / FASB memo agenda 35A) refer to "a risk adjustment for the effects of
uncertainty about the amount and timing of future cash flows." Such "risk adjustment" in the measurement of insurance liabilities is described by the IASB/FASB as one of the "building blocks" to be used to "portray a current assessment of the insurer's obligation." In these latest discussions the IASB/FASB has replaced the term "risk margin" with "risk adjustment". Since the difference in terminology is not significant to the actuarial approaches developed in this paper, the authors have retained the term risk margin. Based on the authors' understanding of the IASB/FASB's use of the term "risk adjustment", that term is essentially synonymous with the term "risk margin" as used in this paper. The actuarial techniques presented in this paper to develop a risk margin are intended to meet the same objectives of a risk adjustment as described in the IASB/FASB documents.

### 1.2 Scope and Limitations

The intent of this paper is to discuss the elements needed for practical actuarial models that can be used to derive risk margins to be included in the measurement of insurance liabilities, to illustrate the results of a one practical model using actual data, and to provide some key observations on the relationships and sensitivities of risk margins to the input data.

This paper shows how to apply the research about a model of loss reserve risk and a model for the market price of risk that can be used to reflect market input from actual non-life insurance company data. The paper will present the results of the application of these models to actual insurance company data reported by major U.S. insurers to insurance regulators/supervisors through December 31, 2008. Five major lines of insurance were selected, for which published data from the largest 100 insurers (based on recent premium volume) in each line was available in sufficient detail to provide a reasonable basis for the analysis. These lines of insurance, as defined by U.S. insurance regulators/supervisors, include:

- Private Passenger Auto Liability (motor insurance for liability to third parties)
- Commercial Auto Liability (motor insurance for business/transport, for liability to third parties)
- Commercial Multi-Peril (combination policies with property insurance and standard third party liability insurance, excludes personal lines policies)
- Other Liability Occurrence (various types of commercial third party liability insurance, excluding motor, products liability, medical malpractice and insurance with claims made coverage, such as directors \& officers or errors \& omissions)
- Workers Compensation (including coverage for lost wages and medical cost resulting from work related injuries)

This paper does not include exhaustive testing of the approach presented. The authors recognize that such testing, including back-testing of the methodology to prior years' data, is needed to further understand the strengths and weaknesses of this methodology. There are a wide variety of alternative models and methods to estimate probability distributions for post-claim insurance liabilities, as well as to develop the parameter estimates or parameter assumptions for the probability distribution. In practice, actuaries will need to select the models or methods that provide an appropriate representation of the probability distributions of the cash flows underlying insurance liabilities. In addition, the reader should recognize that the primary available indicators of the market price of risk are limited to active market transactions, such as new insurance policies and renewal policies that are subject to re-pricing by the insurer at renewal. Consequently, there is a
variety of market transaction data that could be used to evaluate the market price of risk, but it is clearly not a single static value.

Insurance markets can vary widely across different insurance product features, policyholder risk characteristics, local market conditions, underwriting practices, pricing practices, etc. Consequently, any representation of the market value of risk for use in estimating risk margins will be an aggregated average, or central value, over a portfolio of insurance contracts for a particular time period. Furthermore, from time to time unanticipated types of losses can emerge under non-life insurance contracts; for example asbestos and environmental claims were clearly not originally considered in the insurance contract provisions, the underwriting, or the pricing of policies when the exposure to such claims was unknown. Such situations would necessitate adjustments to the historical data used in estimating the market value of risk and to the technical approach for estimating the probability distribution appropriate for the unpaid losses from such unanticipated types of claims.

Over the past several years, considerable research and many ideas have been developed and published involving stochastic loss reserve models, loss reserve ranges, loss reserve risk, and models to quantify risk margins or the price/cost of risk. These advancements in actuarial science and practice have made it possible to develop the approach suggested in this paper for estimating risk margins. This approach can help actuaries in their roles as technical specialists in the measurement of insurance liabilities as may be required under the Phase II development of IFRS for insurance contracts.

## 2. INTRODUCTION

This paper will consider various concepts from certain actuarial research papers written in the last ten years to suggest practical methods to determine explicit risk margins to be included in the measurement of insurance liabilities from unpaid non-life claims. More specifically, the paper focuses on the application of risk margins for post-claim insurance liabilities arising from property and casualty (general or non-life) insurance claims. IFRS 4 also addresses the measurement of preclaims insurance liabilities, which are beyond the scope of this paper. For ease of reference, the term "non-life" will be used to in lieu of "property and casualty or general insurance", recognizing that the term non-life refers to claims from specific types of insurance contracts.

Actuaries frequently refer to insurance liabilities for unpaid claims as reserves for unpaid losses and loss adjustment expenses, or simply, loss reserves. "Technical provisions" or "loss provisions" are other terms sometimes used for loss reserves. However, the elements considered in the basis of the valuation of insurance liabilities have varied depending on local practice or on the understanding of what should be reflected in the loss reserves. The expected value of unpaid claim amounts, the discount for the time value of money, and risk margins are the typical elements that have be considered for the valuation. However, there has been a diversity of practice in which elements are included and how they are determined. This paper will focus on the risk element as a separate, explicit element in the valuation and will demonstrate a proposed methodology for the determination of the risk element.

The main challenges considered in this paper are:
(1) How to determine a basic and practical stochastic risk model for unpaid claim amounts for most standard lines of non-life insurance;
(2) How to utilize insurance market inputs on pricing levels, particularly the market level of profitability, based on available insurance industry data in the U.S.;
(3) How to determine a basic and practical risk model for the insurance market risk associated with the market inputs on pricing levels;
(4) How to use the insurance market inputs from (2) and the insurance market risk model from (3) to calibrate a value of risk parameter, $\lambda$, that can be applied to the stochastic risk model from (1) to compute risk margins for a portfolio of unpaid claims;
(5) How to relate the risk model to the cost of capital; and
(6) How to validate the risk margin results by sensitivity testing.

Results are also presented by applying the approach outlined in the paper to recent U.S. insurance company data for many of the largest 100 insurance groups in each of five non-life lines of insurance.

### 2.1 Organization of This Paper

The organization of the remainder of this paper consists of eight sections:
Section 3. Risk Margins for Financial Reporting
Section 4. Reserve Risk Distributions
Section 5. Insurance Market Inputs and Risk Distributions
Section 6. Risk Margins and the Cost of Capital
Section 7. Valuation of Insurance Market Risk using a Risk Transform
Section 8. Application of a Risk Transform for Reserve Risk Margins
Section 9. Testing of Approach on Data from Largest 100 U.S. Insurers
Section 10. Results, Conclusions and Areas for Additional Research
The remainder of the paper includes a series of exhibits showing the results of the testing of the risk margin method using historical U.S. data and an appendix which has additional analysis of the historical adequacy of estimated ultimate losses using the same dataset compiled for the testing of the risk margin method.

## 3. RISK MARGINS FOR FINANCIAL REPORTING

Risk margins, along with discounting, have emerged as controversial concepts in non-life financial reporting. This is evident from the diversity of practice that has existed for many years across various jurisdictions with respect to risk margins and discounting. Some jurisdictions, such as Australia and Canada, have included risk margins and discounting in their financial reporting requirements for several years. Others, like the U.S., generally ignore discounting and avoid explicit
risk margins, although implicit risk margins may be embedded in some commonly used processes to select estimates for financial statement values. The controversy is also evident in the insurance industry's overwhelmingly negative responses to the current exit value approach suggested for the reporting of insurance contract liabilities in the IASB's 2007 Discussion Paper (DP), Preliminary Views on Insurance Contracts (IASB, 2007).

The IASB/FASB has articulated certain measurement principles for insurance liabilities, based on a foundation consisting of building blocks. The first of the building blocks is that the measurement should be unbiased and determined from current data and information. This principle is intended to clarify that a measurement with these attributes is not locked in based on assumptions made when the policy was issued. Furthermore, any level of prudence or conservatism included explicitly or implicitly in the assumptions or methods used for this measurement would be inconsistent with this principle. The second building block is that the measurement should recognize the time value of money. The third building block is that the measurement should include a risk adjustment (risk margin) for the effects of uncertainty about the amount and the timing of the future cash flows associated with fulfillment of the contract obligations.

One of the proposed criteria that have emerged for the risk element in the measurement of the value of insurance liabilities is the amount an insurer would rationally pay to be relieved of the insurance contract obligations that underlie such liabilities. It is recognized that, based on the status of historical and current markets, insurance liabilities are not traded in open market transactions. Consequently, the valuation of such liabilities cannot be determined simply by reference to market transactions. Absent a developed market where the trading of such liabilities is significant enough to be a reliable indication of value, a measurement objective was needed that recognizes the economic value of these liabilities and that is relevant to financial reporting and the users of financial reports.

The IASB has proposed a building block approach for the measurement of insurance liabilities which has gone through a few iterations. The version below was provided in the IASB/FASB staff paper (IASB agenda reference 6A / FASB reference 35A) addressing the measurement objective and risk adjustment for the January 2010 joint boards meeting. That staff paper describes the boards' current thinking about the measurement approach which should portray a current assessment of the insurer's obligation, using building blocks which include:

1) the unbiased, probability-weighted average of future cash flows expected to arise as the insurer fulfills the obligation;
2) the time value of money; and
3) a risk adjustment (a risk margin)

The IASB's position is grounded in the premise that the values reported for insurance contracts in financial statements should reflect economic value. The boards are considering the measurement of that value from the entity's perspective, in terms of the cost of the resources necessary to fulfill its contract obligations.

One additional building block has been added to the three listed above:
4) an amount that eliminates any gain at inception of the contract.

This fourth building block is a separate concept to address the recognition of gains from insurance transactions. However, this fourth building block can be impacted by the result of the other three building blocks. The focus of this paper is on the third building block, which will require significant actuarial input and analysis.

### 3.1 Current Exit Value

In the DP, the IASB uses the expression "current exit value" to describe a measurement basis for insurance liabilities. Current exit value (CEV) is defined as the amount the insurer would expect to pay at the reporting date to transfer its remaining contractual rights and obligations immediately to another entity. Since there is no observable market for trading insurance liabilities, and consequently no observable market pricing of insurance liabilities, there is a need to estimate the value for these quantities using an approach such as the building blocks established by the IASB. In the DP, the IASB uses the expression "current exit value" to describe a measurement basis. CEV is defined as the amount the insurer would expect to pay at the reporting date to transfer its remaining contractual rights and obligations immediately to another entity.

Many of the non-life insurers who responded to the DP take the position that the approach suggested by the IASB will not provide more useful information in relation to the U.S. GAAP model. Concerns from these insurers include the fact that the model is very different from U.S. GAAP and therefore will have uncertain impact on financial statements; it is untested and could result in significant implementation cost; and it is based on a hypothetical market for insurance liabilities that does not exist. This last point is mentioned by many respondents to the DP. Insurers intend to fulfill their obligations to the policyholder - they do not intend to trade these liabilities on the open market and in most cases are precluded from doing so, thereby calling the exit value concept into question. The strong preference in the majority of the U.S. non-life insurer responses was to maintain the U.S. GAAP approach of undiscounted reserves with no explicit risk margin.

### 3.2 Developments concerning Risk Margins Subsequent to the DP

Several developments have occurred since the 2007 release of the DP. The FASB joined the Insurance Contracts project, signaling a strong likelihood of U.S. GAAP and IFRS convergence. The IASB moved away from the "current exit value" measurement basis and has given serious consideration to two alternative models. One is based on the updated model in IAS 37 Provisions, Contingent Liabilities, and Contingent Assets. The other is based on a current fulfillment value model. The boards and their staff have been developing these concepts in tandem with the intent to have a consistent approach taken in IAS 37 and for Phase II of the Insurance Contracts Project.

### 3.3 IAS 37 Model

In July 2009, the IASB/FASB Staff paper on the Insurance Contracts - Project Measurement Approaches for Insurance Contracts (IASB/FASB, 2009 pp. 7, Paragraph 27) stated, "The measurement objective of the IAS 37 project builds on the amount an insurer would rationally pay to be relieved of an obligation." This statement of the measurement objective proposes that the measurement should not require estimation of the amount a third party would demand for taking over the liability. This is illustrated by the following sentence in the staff paper appendix regarding the updated IAS 37 model (IASB/FASB, 2009 pp .17 , paragraph A9), "The risk margin would reflect the amount at which an insurer would be indifferent between keeping a risk and transferring or settling the risk immediately." Hence, the risk margin would be measured from the perspective of the insurer who currently holds the liability. This perspective of the IAS 37 model is that of the insurer rather than a hypothetical market participant. This clarification potentially alleviates the concerns expressed by critics of the CEV model.

In January 2010, the IASB issued an Exposure Draft of Proposed Amendments to the Measurement of Liabilities in IAS 37 (IASB, 2010). The IAS 37 Exposure Draft defines the amount
an entity would rationally pay at the end of the reporting period to be relieved of the present obligation in terms of the lowest of three values:
a) The present value of the resources required to fulfill the obligation;
b) The amount the entity would have to pay to cancel the obligation; and
c) The amount the entity would have to pay to transfer the obligation to a third party.

One of those values (c) is the CEV. Rather than discarding the CEV, the IASB has retained it as one alternative for meeting this measurement objective. The other values include the current fulfillment value (a), restated in terms of the "value of resources required", and the settlement value (b). The determination of these values will involve consideration of the appropriateness, relevance and reliability of the approaches and assumptions needed to estimate them. This paper explores a practical approach to the estimation of the current fulfillment value (a), but could also be applied to estimating (c).

### 3.4 Current Fulfillment Value

Current fulfillment value (CFV) is defined as the expected present value of the resources required to fulfill the obligations to the policyholder over time. The definition of CFV does not appear to require explicit risk margins. However, two insurance contracts may have the same expected present value yet contain underlying fulfillment obligations with significantly different uncertain cash flows. This difference in uncertain cash flows indicates that the expected present values alone do not fully capture the economic impact on the holder of the obligations. Consequently, the IASB has held to the position that an explicit risk element is a necessary component in the measurement model that is ultimately adopted for insurance contracts.

The January 2010 IASB Exposure Draft for IAS 37 amendments (IASB, 2010) uses the notion of "the present value of the resources required to fulfill the obligation". That Exposure Draft includes a description of the two elements of the calculation of this value:
"(a) the expected outflows of resources and the time value of money; and
(b) the risk that the actual outflows of resources might ultimately differ from those expected."
Therefore, the CFV concept appears to have emerged as a consistent approach under both IAS 37 and Phase II of the Insurance Contracts Project.

### 3.5 Summary

While the measurement basis for insurance contracts is still under debate as of the writing of this paper, there is a need for actuaries to develop a common set of techniques which could be used to estimate explicit risk margins. The estimation of risk margins could become an integral part of the financial reporting process for non-life insurance contracts. Financial and actuarial literature is rich with discussion of risk margins, particularly in recent years as the topic has taken on additional importance with the development of the IFRS on insurance contracts. However, there are not many practical examples and tools which can be used by non-life insurers to estimate risk margins as the IASB/FASB has defined them for financial reporting under IFRS. This paper attempts to provide such practical examples and tools.

## 4. INSURANCE LIABILITY RISK DISTRIBUTIONS

A first step to estimating an explicit risk margin is to determine the underlying risk model for unpaid claim amounts. There are many methods and models to choose from for the purpose of developing an appropriate model of the risk inherent in insurance liabilities. For insurance liabilities related to unpaid claims, typically referred to as reserves for unpaid losses or unpaid losses and loss adjustment expenses, most actuarial approaches applicable to non-life risks produce estimates of a central value, such as the mean. Also, uncertainty in such actuarial central estimates is typically reflected in a range of estimates that represents a range of values that are considered, by the actuary, to be reasonable for the intended use(s) of the estimates. The elements that drive the uncertainty, and hence the range of estimates, typically include the credibility of the data, missing or data reliability issues, changes in pattern of claim payments and claim estimates (e.g., case reserves), volatility in development patterns, shifts in patterns, changes in litigation risk, inflationary impacts on historical data versus future impacts, and differences in operations (e.g., underwriting, claims administration, mix of claim types, etc.).

Given the wide range of possible uncertainty elements, it can be quite a technical challenge to create a risk distribution model that sufficiently captures the drivers of uncertainty into a mathematical model or an analytical method. When the phenomenon being measured is not well behaved based on available data, models or methods that attempt to capture that risk in quantitative terms are subject to model specification risk, primarily due to either a model/method that is too simple or one that is over-specified (over-parameterized). Validation can also be a challenge due to data limitations, changes in the drivers of uncertainty over time, or other conditions. Also, for purposes of incorporating a risk margin for financial reporting valuation, one of the important features of measurement is the reliability of the estimate, in addition to the relevance and transparency of the estimate.

### 4.1 The Rehman-Klugman Method

The methodology explored in this paper attempts to link the risk margin directly to the uncertainty in the actuarial estimates. Given the importance of reliability and uncertainty, one particular actuarial approach to developing risk distributions is worth further exploration. In a recent paper (Rehman, et al., 2009), the authors review the current literature and discuss the work of many others with similar observations about risk quantification models for non-life losses. In doing so, the authors present a risk modeling approach that is based on an analysis of actuarial estimates themselves, rather than the underlying loss data. This approach is significant in the context of financial reporting. The uncertainty of the actuarial estimates, specifically for unpaid claims, should reflect evidence about the past reliability of the actuarial estimates, particularly when such evidence suggests the uncertainty in the actuarial estimates is greater or lesser than can be attributed to the risk probability distribution of the unpaid claims. This is the essence of the Rehman-Klugman (RK) approach. Furthermore, as these authors point out, their approach to quantifying uncertainty is independent of the method used to determine the unpaid claim estimates.

The R-K methodology produces a probability distribution model of unpaid claim liabilities based on the logarithms of the development factors (also known as age-to-age factors or link ratios) from the traditional loss development method (also known as the chain ladder method). By applying this approach to the successive annual (end of year) estimates of ultimate losses by accident year, the result is a probability model of the reliability of the actuarial estimates of ultimate losses. In order to
provide a more complete view of uncertainty in actuarial estimates, the R-K paper notes that the various sources of uncertainty, namely process risk, parameter risk and model risk, are "intertwined and thus hard to separate." Therefore, their approach attempts to take a higher level view of the uncertainty:
"Each reserve set in the past is an estimate of its distribution and thus its errors can be estimated from the historical errors made in the estimations. Because the ultimates will converge to the true value, the errors made along the way reflect all sources of error" (Rehman, et al., 2009 p. 3)

The R-K approach also can be applied if new actuarial methods for estimating ultimate losses are found to be more reliable. If a new or improved actuarial estimation method can be used to restate the historical estimates of ultimate losses by accident year for prior development periods, the R-K method can then be applied to the restated data.

In essence, the R-K approach creates a framework that analyzes the "errors", i.e., the differences between actual and estimated values, using statistical tools from regression analysis and analysis of variance. Consequently, the R-K approach is based on a stochastic model of these errors, which focuses on the reliability of the estimation process in statistical terms and is independent of the actuarial method or methods used to develop the ultimate loss estimates in the first place. Thus, by using the results of the $\mathrm{R}-\mathrm{K}$ method for measuring the total variability in the estimates, the resulting risk margins will directly reflect the reliability of the estimates. Consequently, for entities whose estimates of ultimate losses indicate volatility which are higher or lower than other entities, their risk margins will be higher or lower than such other entities.

### 4.2 Assumptions and Limitations to the R-K Approach

It should be noted that there are limitations and assumptions stated by the authors of the R-K method as conditions for use of the method.

The principal assumptions are that:
(1) The underlying loss development process has not changed over time;
(2) The reserving methodology has not changed over time;
(3) The estimates of ultimate losses are the result of consistent application of a specific methodology;
(4) The estimates of ultimate losses do not contain ad hoc adjustments; and
(5) The estimates of ultimate losses do not contain margins or other provisions.

### 4.3 Impact of Changes in Historical Conditions

If the R-K method is used to determine risk margins when the above mentioned assumptions do not hold, there may be some concern about the estimated risk margins. However, it should be possible to evaluate whether the historical conditions, relative to these assumptions, would tend to increase or decrease the uncertainty estimates. In many cases, historical conditions that are not consistent with these assumptions would tend to increase the uncertainty estimates. Consequently, if the historical data can be adjusted to lessen the impact of those inconsistencies, then lower
estimates of uncertainty should be produced. If such adjustments are not possible, then the estimates of uncertainty and the resultant risk margins will simply reflect the risk as evidenced by such history. In the context of financial reporting the risk margins would reflect the level of risk indicated by the historical evidence if a lower level of risk cannot be reasonably quantified. The risk margins developed using such data would still provide useful information to users of the financial statements since those margins would reflect the current information about the historical reliability of the entity's estimates of their ultimate losses.

Another issue for financial reporting concerning these assumptions is whether the historical conditions, or the current conditions, would result in the underestimation (or overestimation) of the risk margins. Consequently, it is important to identify changes in conditions that could result in higher (or lower) uncertainty in the estimates than is reflected in the historical data.

### 4.4 Insufficient Historical Data

Also, in cases where an entity is a new insurer or has only recently started writing business in a line of insurance, there could be insufficient historical data from which to make an estimate of the uncertainty of the ultimate losses. These situations would usually require the application of considerable judgment in order to develop assumptions or a model that might be relevant to quantifying uncertainty in ultimate loss estimates. While the R-K approach does not provide a solution to these situations, there can be some useful results of applying the method to industry data in order to provide a starting point for the development of risk margins through the use of external data and judgment. In section 9, results are presented from applying the R-K method to the largest 100 U.S. insurance groups in each of five lines of insurance selected for this paper. Some of the 100 U.S. insurance groups in the data set do not have sufficient historical data to apply the R-K method. However, the results of applying the R-K method for the remaining insurers provide a potentially useful set of data on the range of uncertainty measurement among a large group of insurers.

The application of the R-K methodology to U.S. insurance group data shows that this methodology produces results that tend to be fairly consistent among most entities. As might be expected, there are a few results for individual insurers that appear to be outliers and would need further analysis before making any conclusions about those specific entities. Also, some of the insurers have fewer years available in their data set or are missing data for certain data elements. Nonetheless, the overall results appear to be quite good considering the use of published data that has various changes, adjustments and differences reflected in this data for each insurer over the 22 years of data used (1987-2008).

### 4.5 Number and Size of Reserve Segments

In their paper, the authors of the R-K method also discuss some of the issues surrounding "reserve segments" and the possibility of combining lines of insurance for the application of the method. In practice, actuaries tend to prefer dividing their data into a large number of reserve segments for purposes of estimating ultimate losses. While this practice is well established and provides insights recognized as important in providing more reliable estimates of ultimate losses, there is a significant difference in selecting the appropriate data set for purposes of quantifying uncertainty in the estimates of ultimate losses. The R-K approach suggests that such segments, or even entire lines of insurance, should be combined in order to recognize that there are underlying correlations between segments or lines of insurance. Moreover, in practice, actuaries would typically use the same, or very similar, methods for estimating ultimate losses by segment or by line.

Consequently, there can be significant correlation in the estimates of ultimate losses due to the actuarial estimation process itself.

The aggregation of reserve segments for purposes of estimating risk margins will need to comply with the final IFRS 4 guidelines. Based on observations of the IASB/FASB's initial views on this aggregation issue at the time of the writing of this paper, it appears that the aggregation guidelines might be based on the comparability of the underlying business being aggregated with respect to the similarity of the cash flows, or perhaps the similarity of the uncertainty in the cash flows. Consequently, the R-K method may also be useful as a possible tool for testing the comparability between business segments with respect to the uncertainty associated with the liability estimates for those segments.

The R-K methodology can be applied independent of whatever techniques might be considered by the actuary in estimating the ultimate losses. Consequently, the R-K method can be used as a tool to compare the results of different methods, to test for correlations between methods, or to provide a statistical basis for selecting a range of estimated ultimate losses.

### 4.6 Level of Aggregation and Diversification

If the measurement objective for financial reporting is to reflect the amount that an entity would rationally pay to be relieved of the obligations, then the approach to estimating risk margins should be capable of being computed at some aggregated level of uncertainty. The R-K approach is quite flexible in this regard, either by combining data before applying the method, or by further analyses, or assumptions, to obtain the parameters applicable to the combined risk of multiple segments or lines. Also, this approach provides a means to quantify the impact of diversification, and thus a means to allocate such impact for internal profitability or performance measurement. In addition, this approach could be adapted to estimate risk margins that properly measure the gross insurance liabilities before reinsurance while also measuring the asset value for ceded reinsurance recoveries, and result in an appropriate balance sheet position, net of reinsurance. Non-life insurers purchase reinsurance using a wide variety of structures, terms and conditions that can be quite different from the underlying insurance policies. For example, the purchase of catastrophe reinsurance can be on a portfolio basis, or on a stop loss basis. Also, reinsurance protection may apply to only portions of an insurer's business segments or may apply to multiple segments or lines of insurance.

This paper demonstrates a methodology for estimating risk margins applied to individual lines of insurance, but the basic methodology can be further adapted to accommodate various divisions or aggregations of business segments or lines of insurance. It may be possible to use the methodology to evaluate the impact of reinsurance by applying the method to estimates of ultimate losses that are gross of reinsurance vs. net of reinsurance. However, as discussed further below, there can be significant limitations on the viability of the method when it is applied to low frequency lines of insurance, particularly when high severity claims make up most of the losses.

### 4.7 The Lognormal Assumption

The R-K approach is dependent on a lognormal probability distribution assumption. The validity of this assumption is easily tested because the natural logarithm values can be checked for normality using standard statistics or by graphical means. The research for this paper used actual historical data on approximately 500 data sets, each with up to 22 years of data. Based on this research, the lognormal assumption performed quite well. When the R-K method is applied to most lines of insurance, the normality assumptions (in log scale) can be expected to produce fairly consistent
results. However, the method may not perform well when applied to datasets with very low claim frequency or extreme claim severity due to the possible divergence from normality.

For lines of insurance with very low claim frequency and extreme claim severity, more research would be needed to test, or otherwise evaluate, the expected performance of the R-K method. The obvious statistical problem with very low claim frequency is that there are very few past observations containing actual claims to test the model or method. Also, with extreme claim severity, the presence of a few extreme claims in the historical data, or the lack of such claims, are likely to indicate a very low reliability of ultimate loss estimates. Given the nature of the low claim frequency and extreme severity lines of insurance, including insurance or reinsurance on an excess of loss basis, the expectations of outcomes would be a very high probability of zero losses, but very high losses if they do occur. As the authors of the R-K point out, the methodology relies on an underlying process (approximately normal) that has some regularity in terms of a sufficient number of events and a reasonable frequency of changes in estimates. Consequently, the estimation of risk distributions for insurance liabilities with very low frequency or extreme severity characteristics will likely require an alternative approach to the R-K method. The lines of insurance tested in this paper did not have such characteristics.

### 4.8 Mechanics of the R-K Approach

To illustrate the use of the R-K method for a given dataset, consider a data triangle consisting of estimates of ultimate losses for several accident years at annual valuations.
$\left.\begin{array}{|c|c|c|c|c|l|l|l|l|}\hline \begin{array}{c}\text { Accident } \\ \text { Year }\end{array} & \begin{array}{c}12 \\ \text { months }\end{array} & \begin{array}{c}24 \\ \text { months }\end{array} & \begin{array}{c}36 \\ \text { months }\end{array} & \begin{array}{c}48 \\ \text { months }\end{array} & \begin{array}{c}60 \\ \text { months }\end{array} & \begin{array}{c}72 \\ \text { months }\end{array} & \begin{array}{c}84 \\ \text { months }\end{array} & \begin{array}{c}96 \\ \text { months }\end{array}\end{array} \begin{array}{c}108 \\ \text { months }\end{array}\right)$

The R-K method uses the typical ratios of successive values (development periods 12 to 24,24 to 36, etc.) for each accident year, but applies the ratios to estimated ultimate losses and takes the log of each ratio. These $\log$ ratios are then considered to be random variables for each development period, where each accident year is treated as a sample observation of that random variable.

| Accident Year | $12 \text { to } 24$ months | 24 to 36 months | 36 to 48 months | 48 to 60 months | Etc. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2000 | $\ln \left(\mathrm{U}^{24}{ }_{00} / \mathrm{U}^{12}{ }_{00}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{00} / \mathrm{U}^{24}{ }_{00}\right)$ | $\ln \left(\mathrm{U}^{48}{ }_{00} / \mathrm{U}^{36}{ }_{00}\right)$ | $\ln \left(\mathrm{U}^{60}{ }_{00} / \mathrm{U}^{48}{ }_{00}\right)$ | $\ldots$ |
| 2001 | $\ln \left(\mathrm{U}^{24}{ }_{01} / \mathrm{U}^{12}{ }_{01}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{01} / \mathrm{U}^{24}{ }_{01}\right)$ | $\ln \left(\mathrm{U}^{48}{ }_{01} / \mathrm{U}^{36}{ }_{01}\right)$ | $\ln \left(\mathrm{U}^{60}{ }_{01} / \mathrm{U}^{48}{ }_{01}\right)$ | $\cdots$ |
| 2002 | $\ln \left(\mathrm{U}^{24}{ }_{02} / \mathrm{U}^{12}{ }_{02}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{02} / \mathrm{U}^{24}{ }_{02}\right)$ | $\ln \left(\mathrm{U}^{48}{ }_{02} / \mathrm{U}^{36}{ }_{02}\right)$ | $\ln \left(\mathrm{U}^{60}{ }_{02} / \mathrm{U}^{48}{ }_{02}\right)$ | $\cdots$ |
| 2003 | $\ln \left(\mathrm{U}^{24}{ }_{03} / \mathrm{U}^{12}{ }_{03}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{03} / \mathrm{U}^{24}{ }_{03}\right)$ | $\ln \left(\mathrm{U}^{48}{ }_{03} / \mathrm{U}^{36}{ }_{03}\right)$ | $\ln \left(\mathrm{U}^{60}{ }_{03} / \mathrm{U}^{48}{ }_{03}\right)$ | $\cdots$ |
| 2004 | $\ln \left(\mathrm{U}^{24}{ }_{04} / \mathrm{U}^{12}{ }_{04}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{04} / \mathrm{U}^{24}{ }_{04}\right)$ | $\ln \left(\mathrm{U}^{48}{ }_{04} / \mathrm{U}^{36}{ }_{04}\right)$ | $\ln \left(\mathrm{U}^{60}{ }_{04} / \mathrm{U}^{48}{ }_{04}\right)$ |  |
| 2005 | $\ln \left(\mathrm{U}^{24}{ }_{05} / \mathrm{U}^{12}{ }_{05}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{05} / \mathrm{U}^{24}{ }_{05}\right)$ | $\ln \left(\mathrm{U}^{48}{ }_{05} / \mathrm{U}^{36}{ }_{05}\right)$ |  |  |
| 2006 | $\ln \left(\mathrm{U}^{24}{ }_{06} / \mathrm{U}^{12}{ }_{06}\right)$ | $\ln \left(\mathrm{U}^{36}{ }_{06} / \mathrm{U}^{24}{ }_{06}\right)$ |  |  |  |
| 2007 | $\ln \left(\mathrm{U}^{24}{ }_{07} / \mathrm{U}^{12}{ }_{07}\right)$ |  |  |  |  |
| Average | $\frac{\sum \ln \left(\mathrm{U}^{24} / \mathrm{U}^{12}\right)}{\mathrm{N}_{1}}$ | $\frac{\sum \ln \left(\mathrm{U}^{36} / \mathrm{U}^{24}\right)}{\mathrm{N}_{2}}$ | $\frac{\Sigma \ln \left(\mathrm{U}^{48} / \mathrm{U}^{36}\right)}{\mathrm{N}_{3}}$ | $\frac{\sum \ln \left(\mathrm{U}^{60} / \mathrm{U}^{48}\right)}{\mathrm{N}_{4}}$ | $\cdots$ |

Using the incremental development averages computed from the previous table, the cumulative log mean values are simply the sum of the incremental averages from each age ( n ) to "ultimate." This is similar to the typical cumulative multiplication of age-to-age development factors (also known as link ratios), but in this case the incremental values are added instead of multiplied.

$$
\begin{equation*}
\hat{\mu}_{\text {nto ult }}=\sum_{t=n}^{u l t} \text { Average Incremental } \ln \left(U^{t+12} / U^{t}\right) \tag{1}
\end{equation*}
$$

Since the basis for this model is a lognormal random variable for each incremental development period, the distribution of the sum of the incremental averages also requires an estimate of the variance of the sum. The R-K method uses a variance-covariance matrix as depicted below. The computation of the variances and covariance for each of the age-to-age incremental values can be easily implemented in a spreadsheet using the built-in functions.

|  | 12-24 months | 24-36 months | 36-48 months | Etc. |
| :---: | :---: | :---: | :---: | :---: |
| $12-24$ <br> months | $\operatorname{Var}\left[\ln \left(\frac{U^{24}}{U^{12}}\right)\right]$ | $\operatorname{Cov}\left[\ln \left(\frac{U^{24}}{U^{12}}\right), \ln \left(\frac{U^{36}}{U^{24}}\right)\right]$ | $\operatorname{Cov}\left[\ln \left(\frac{U^{24}}{U^{12}}\right), \ln \left(\frac{U^{48}}{U^{36}}\right)\right]$ | $\cdots$ |
| $\begin{gathered} 24-36 \\ \text { months } \end{gathered}$ | $\operatorname{Cov}\left[\ln \left(\frac{U^{24}}{U^{12}}\right), \ln \left(\frac{U^{36}}{U^{24}}\right)\right]$ | $\operatorname{Var}\left[\ln \left(\frac{U^{36}}{U^{24}}\right)\right]$ | $\operatorname{Cov}\left[\ln \left(\frac{U^{36}}{U^{24}}\right), \ln \left(\frac{U^{48}}{U^{36}}\right)\right]$ | $\cdots$ |
| $\begin{gathered} 36-48 \\ \text { months } \end{gathered}$ | $\operatorname{Cov}\left[\ln \left(\frac{U^{24}}{U^{12}}\right), \ln \left(\frac{U^{48}}{U^{36}}\right)\right]$ | $\operatorname{Cov}\left[\ln \left(\frac{U^{36}}{U^{24}}\right), \ln \left(\frac{U^{48}}{U^{36}}\right)\right]$ | $\operatorname{Var}\left[\ln \left(\frac{U^{48}}{U^{36}}\right)\right]$ | $\ldots$ |
| Etc. | ... | $\ldots$ | $\ldots$ | $\ldots$ |

By applying the R-K method to historical data, the parameters of a lognormal distribution, $\mu$ and $\sigma$, are estimated for each accident year based on the latest maturity applicable to each accident year. The lognormal parameters for each accident year produce an expected adjustment factor from the mean of the fitted lognormal probability distribution which can be applied to the latest value of estimated ultimate losses for each accident year. In addition, the fitted distribution can be used to represent the probability distributions of ultimate loss outcomes by accident year. Since the paid loss amounts are fixed and known at the latest evaluation date, the outcomes of the insurance liabilities for the unpaid losses are simply the ultimate loss outcomes less the known paid loss amounts at the evaluation date. Then, the distributions from each accident year can be combined to produce an aggregate probability distribution for the total insurance liabilities for unpaid losses of all open accident years as of the latest valuation date.

The aggregate probability distribution for all accident years is the sum of the individual accident years. Since a lognormal distribution was used for each accident year, the sum of the results would not be lognormal. However, as mentioned by Rehman and Klugman, the results can be easily simulated. The results for this paper were obtained by a 500 sample simulation for each accident year and the simulation results were evaluated for normality (in the $\log$ scale). The evaluations consistently indicated that the sum of the simulated accident year results was a reasonably good fit to a lognormal. The 500 simulation size appeared to be sufficient to support these research results. The sensitivity of the results to a larger number of simulations was tested by running multiple 500 simulation computations and observing no significant changes in the results.

### 4.9 Consideration of Independence between Accident Years

One area of additional consideration is whether the estimates for each of the accident years are independent. The R-K method implicitly assumes independence by adding the random variables for each accident year in order to arrive at a total probability distribution for the unpaid losses, without adjustment for covariance between accident years. Another recent paper (Underwood, et al., 2009), A Top-Down Approach to Understanding Uncertainty in Loss Ratio Estimation, explores a measure of
estimation error for ultimate insurance losses which is very similar to Rehman and Klugman, arriving at a similar lognormal model of estimated ultimate loss ratios. However, Underwood and Zhu analyzed cross sectional data by company to study the probability distribution of errors in the estimates of ultimate loss ratios by accident year. They produced results from their research that indicated a time series relationship in the sample average log errors across accident years. These results suggest that there may be some correlation in the estimates of ultimate losses between accident years. Also, similar time series analyses for the cross sectional datasets used in the research for this paper suggest a similar relationship between accident years for the estimated mean of the log of the ratio of the estimates of ultimate losses as of different maturities.

Underwood and Zhu found a linear relationship between the absolute value of the estimated mean of the log ratio and the standard deviation of the errors for the one line of insurance they studied, but the results of the analysis for this paper did not indicate such a relationship. Rather, the standard deviation estimates from the datasets used for this paper were fairly constant by accident year and appeared to be independent of the value of the estimated mean (See the summary of results in the Appendix).

The assumption of independence between accident years in the R-K method was not specifically tested. However, the results for this paper did not suggest that the independence assumption would produce an underestimate or overestimate of the total variance for the unpaid losses of multiple accident years. However, further research may be needed to support this conclusion more generally.

### 4.10 Policy Year or Underwriting Year Data in lieu of Accident Year Data

The R-K methodology is not dependent on using loss data organized by accident year. Policy year or underwriting year data could be substituted for accident year. Since the R-K methodology is testing for the uncertainty in the estimates of ultimate losses, the data can be organized by grouping claims, such as by the accident date or loss date of the claims, or by grouping policies, such as for policies underwritten with effective or renewal dates during particular time periods. Other groupings may also be used, if needed.

In order to meet financial reporting requirements, the insurance liabilities may need to be separated into estimates of loss reserves (post claim) and estimates of policy/premium reserves (preclaim). At the time of the writing of this paper, the IASB/FASB was discussing the measurement of insurance liabilities on the basis of net cash flows that reflect the cash outflows related to the obligations under the insurance contracts offset by future cash inflows related to the insurer's rights under insurance contracts. The final IFRS 4 guidelines may suggest that risk margins are also on a similar net basis. As mentioned in Section 2, the scope of this paper does not include consideration of pre-claim liabilities, nor does it include consideration of the netting of risk margins based on cash inflows and outflows.

### 4.11 Summary

This section has discussed the possible uses and limitations of the R-K methodology as one practical means of estimating a risk probability distribution for the value of the resources required to fulfill the present obligations. This risk distribution can then be used to estimate a value for the risk that the actual outflows of resources might ultimately differ from those expected. In the next section, a pricing model for risk will be explored that could be used to incorporate market inputs in assessing a current market value for such risk.

## 5. INSURANCE MARKET INPUTS AND RISK DISTRIBUTIONS

This section describes a basis for incorporating insurance market inputs into the process of estimating risk margins. The objective of using market data is to find a basis for the value of a liability with uncertain outcomes that reflects the economic value of the obligations underlying the liability. While the outcomes of the relevant obligations are uncertain, they can generally be described by probability distributions that are tractable. The question of the value of insurance obligations is typically considered in the context of the pricing of insurance. Also, some would consider the value question to be related to the cost of satisfying or being relieved of the obligations. Whether economic value is considered to be the cost or the price of a set of cash flows, the primary element to be considered is the appropriate value adjustment to the insurance liability for the uncertainty of the cash flows.

### 5.1 Use of Industry Profitability Data to Indicate Market Pricing Levels

Market pricing data provides relevant information about the value of the obligations under an insurance contract, including consideration of the uncertainty of the cash flows. The premiums charged by insurers will include compensation for the expected expenses, the expected losses (or benefits) to be paid to, or on behalf of, the policyholders, and the expected profit for the risk taken by the insurers, including the cost of capital committed to support the solvency of the insurer in the event that the uncertain losses and expenses might exceed the premiums charged. In a stable market, the premiums will not be significantly greater than the minimum that the market requires as compensation to take on the risk of insuring policyholders for their claims (and benefits) provided by a particular type of insurance. However, insurance markets are not always stable and there can be underwriting cycles where the premiums may fall, leading to lower profits (or losses), or where premiums may rise, leading to higher profits.

Market changes can be attributable to many factors, such as the number of competitors in the market, changes in the measurable or perceived risks covered by the type of insurance policy, inflationary changes affecting the expenses or claims (benefits) covered by the type of insurance policy, changes in the market cost of capital, changes in market investment yields, etc. Consequently, it would be quite challenging to develop market inputs to estimating appropriate risk margins if one were to attempt to determine the individual drivers of market changes.

For the purpose of this paper, the market input for expected profit is defined as the aggregate level of profitability for a line of insurance based on aggregate industry (U.S.) statistics. This approach does not attempt to adjust for the desired level of profitability, or a particular cost of capital, but rather reported aggregate industry insurance data by line of insurance are used to determine the most recent level of profitability available in the broad market for common lines of insurance. This approach should be fairly robust in most insurance market cycles, but may need to be modified when insurance market cycles are clearly inconsistent with the general economy.

### 5.2 Determining the Market Level of Profitability

The proposed approach for determining the market level of profit uses the following basic equation:

$$
\begin{equation*}
\text { Profit }=\frac{(1-\text { Expense Ratio })}{(1+\text { ULAE Factor })}-P V \text { Factor } \cdot \text { Ultimate Loss } \& A L A E \text { Ratio } \tag{2}
\end{equation*}
$$

where,
Expense Ratio $=$ all expenses except loss adjustment expenses, a ratio to premium
ULAE Factor $=$ Unallocated Loss Adjustment Expenses, a factor on Loss \& ALAE
Ultimate Loss \& ALAE Ratio $=$ Losses and Allocated Loss Adjustment Expenses, a ratio to premium (sometimes simply referred to as the Ultimate Loss Ratio)

PV (Present Value) Factor $=$ discounting factor that reflects the time value of money, the cash flows associated with the payment of Loss \& ALAE, and the current applicable discount rate(s), a factor on Loss \& ALAE
Profit $=$ a ratio to premium representing the present value of the aggregate profit on a portfolio of transactions.

Under this depiction of profit from insurance contracts, the variable with the most significant uncertainty is the Ultimate Loss \& ALAE Ratio. Therefore, given the linear relationship between Profit and the Ultimate Loss \& ALAE Ratio, the Profit variable is also subject to a similar level of uncertainty. There may be additional uncertainty in the Profit due to uncertainty in the other variables. However, the typical situation for major lines of insurance would indicate that such additional uncertainty is de minimus.

The R-K method provides estimated parameters for the probability distribution of the Ultimate Loss \& ALAE Ratio. However, the R-K method starts with an estimated Ultimate Loss \& ALAE Ratio as of a certain maturity. The earliest maturity considered would be the end of the accident period, 12 months in the typical case of an accident year. This does not take into consideration the variability of results between the inception of the accident period and 12 months later. Additional uncertainty exists as a result of this variability not being captured in methodologies that use data commencing 12 months after the inception of the accident period. Consequently, the probability distribution of the Profit variable should also consider the distribution of the estimated Ultimate Loss \& ALAE Ratio as of 12 months. If we consider the lognormal distribution for the estimated ultimate loss \& ALAE ratio as of 12 months, then the R-K method can be combined with this loss ratio distribution to produce a lognormal distribution of the Ultimate Loss \& ALAE Ratio variable, which then produces the probability distribution of the Profit variable.

Using data from annual reports filed with U.S. insurance supervisors/regulators (NAIC Annual Statements), the profitability of each of the five lines of insurance considered in this paper for each accident year was estimated. The data for each accident year includes premiums, estimated ultimate losses and allocated loss adjustment expenses, expense ratio, estimated ultimate loss and loss adjustment expense ratio, paid loss development history, and estimated ultimate loss development history. All data elements were on a net basis after reinsurance. While gross data would have been preferable, the available data sources only provided all needed data elements on a net basis.

After adjusting the historical data for significant systematic trends in loss ratios (see Exhibits), the $\log$ of the estimated ultimate loss \& ALAE ratios as of 12 months by accident year are analyzed and then used to estimate the parameters of a probability distribution for those loss ratios. Next, the
parameters from the R-K method for the distribution of errors in the 12 months to ultimate link ratios were used to develop a revised loss ratio distribution. Since the loss ratios and the errors in link ratios are both estimated using lognormal distributions, the result of combining the two distributions is also lognormal. However, in order to get the total variance of the product of these two lognormal variables, the needed covariance of the two variables is estimated from the historical loss \& ALAE ratio data and the results of the R-K method.

$$
\begin{equation*}
\operatorname{Cov}(X, Y)=\sum_{i=1}^{n} \frac{\left(X_{i}-\hat{\mu}_{X}\right)\left(Y_{i}-\hat{\mu}_{Y}\right)}{(n-1)} \tag{3}
\end{equation*}
$$

where,

$$
\begin{aligned}
& X=\text { logarithm of accident year loss \& ALAE ratio, estimated ultimate as of } 12 \text { months } \\
& Y= \\
& \quad \text { ultimate } \\
& \hat{\mu}_{X}=\text { sample mean of } \mathrm{X} \\
& \hat{\mu}_{Y}=\text { sample mean of } \mathrm{Y}
\end{aligned}
$$

Based on the combined loss ratio distribution, the latest accident year loss ratio distribution can be expressed as:

$$
\begin{equation*}
\text { Loss Ratio ~Lognormal }\left(\mu_{A Y}, \sigma_{A Y}\right) \tag{4}
\end{equation*}
$$

where,
$\mu_{A Y}=$ mean of the probability distribution for the logarithm of the accident year loss ratio
$\mu_{A Y}=\mu_{X}+\mu_{Y}$
$\sigma_{A Y}^{2}=$ variance of the probability distribution for the logarithm of the accident year loss ratio
$\sigma_{A Y}^{2}=\sigma_{X}^{2}+\sigma_{Y}^{2}+2 \cdot \operatorname{Cov}(X, Y)$

The Profit variable has the form,

$$
\begin{equation*}
\text { Profit }=\frac{(1-E R)}{(1+U L A E)}-P V \cdot L R \tag{5}
\end{equation*}
$$

This formulation can then be used to represent the market level of profitability, i.e. the pricing factor, for the most recent period. Since the loss ratio distribution represents a basis for measuring risk and uncertainty, the current average pricing factor in the market can be used to represent the
current insurance market value of risk, and to calibrate the value parameter associated with a measure of risk and uncertainty.

### 5.3 Summary

In this paper, a pricing factor based on estimated industry profitability is explored as the basis for estimating risk margins for the risk and uncertainty associated with the total unpaid losses, based on the probability distribution of the total unpaid losses. In section 7, the profit formula will be used with a risk transform function, applied to a probability distribution function, to calibrate an insurance market value of risk parameter, $\lambda$, that can be applied to the unpaid loss risk model and compute risk margins for a portfolio of unpaid losses.

The next section explores how the cost of capital can be considered in the determination of risk margins. The cost of capital has emerged as the preferred approach to determining risk margins. This next section explores some of the issues involved with the cost of capital and how risk margins are related to an entity's economic capital and cost of capital.

## 6. RISK MARGINS AND THE COST OF CAPITAL

A basic economic premise of market pricing behavior is that capital providers require a return on the capital they provide, and this return is expected to be commensurate with the level of risk. Cost of capital is a well-accepted concept and is commonly used as a conceptual framework in both nonlife and life insurance pricing applications. In the context of the IASB's three building block approach for the measurement of insurance liabilities, the third building block, a risk margin, reflects the economic impact of the uncertainty in the estimates. Consequently, there appears to be a strong preference to use cost of capital methods to estimate market-consistent risk margins for insurance contracts under IFRS. Conceptually at least, an appropriate risk margin can be based on the present value of the insurer's cost of the capital attributable to supporting the insurance liabilities of the insurer (IASB, $2007 \mathrm{pp} .63-67$ ).

### 6.1 Challenges of the Cost of Capital Approach

Using a cost of capital approach to risk margins for the measurement of insurance liabilities presents several practical problems:
(1) To start with, the cost of capital is typically developed from two main components: (a) the amount of capital needed, and (b) the rate of return "cost" for the commitment of the capital (IASB, 2007 p. 79). However, neither of these two components is readily observable for a given set of insurance liabilities.
(2) The amount of regulatory capital needed is typically not the real economic capital needed to support the relevant obligations.
(3) The capital evaluation by rating agencies relates to the total operations, which can include other businesses unrelated to insurance operations, at the parent or group level, and consequently the use of rating agency capital does not provide a realistic market assessment of capital needed to support the risk associated with the insurance liabilities.
(4) If the overall capital for an insurer could be determined or calibrated based on market data, such overall capital would need to be decomposed and allocated in order to develop
risk margins for the appropriate groupings of insurance liabilities, such as line of insurance. A recent paper (Bodoff, 2009) suggests a method for the allocation of capital based on a percentile approach.
(5) Using a single rate of return on economic capital would seem to be an over-simplification in terms of economic impact since rates of return should vary depending on the risk associated with the potential amounts that the capital providers could gain or lose. Also, if each entity were able to determine their own specific capital needs and target rate of return on capital, this might produce an entity specific cost of capital with little or no market input and little, if any, calibration to market inputs.

These problems suggest the need for a more robust economic capital model and a more thorough evaluation of the applicable loss distributions in order to evaluate the probability distribution of returns on capital. Such a capital model would require some market basis for the validation of the model assumptions and parameters.

Another approach to resolving these issues about the cost of capital approach to risk margins is to consider the answers to three key questions:

1. How much capital is required to support the liabilities?
2. How is the capital released over time?
3. What is the cost of providing capital over the period that the capital is needed?

### 6.2 Basic Example of Cost of Capital Approach to Risk Margins

Several examples of the cost of capital method are given in (IAA, 2009) Measurement of Liabilities for Insurance Contracts: Current Estimates and Riske Margins. The assumptions used to derive the risk margin for a notional non-life insurance product, motor third party liability, are as follows:

IAA RISK MARGINS PAPER (IAA, 2009 p. 83)
MOTOR COST OF CAPITAL ASSUMPTIONS

| Initial Current Estimate of Liabilities | 100 |
| :--- | ---: |
| Cost of Capital (Target Rate of Return) | $6.0 \%$ |
| Initial Capital Requirement (\% of Liabilities) | $39 \%$ |
| Annual Increase to Capital \% Requirement | $10 \%$ |


| Discounted Unpaid \% (using 4\% discount rate) |  |
| :---: | ---: |
| End of Period |  |
| 1 | $58 \%$ |
| 2 | $27 \%$ |
| 3 | $6 \%$ |
| 4 | $2 \%$ |
| 5 | $0 \%$ |

Note that the capital requirement is related to the discounted current estimate and is assumed to increase as a percentage of the remaining liabilities as the liabilities mature. This assumption will be discussed in more detail later in this section. For questions 1 and 2, this example uses the initial capital requirement assumption ( $39 \%$ ) and the annual increase to this capital assumption ( $10 \%$ ). For question 3, the cost of capital rate of return is assumed to be $6.0 \%$ in this example.

With these assumptions in place, the risk margin at the beginning of the period can be illustrated using this cost of capital methodology as follows:

TABLE 1

RISK MARGIN USING COST OF CAPITAL METHODOLOGY - TIME 0

| Period | Current <br> Liability <br> Estimate | Capital <br> Requirement | Required <br> Capital | Cost of <br> Capital | Discounted <br> Cost of Capital |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 100 | $39 \%$ | 39 | 2.3 | 2.3 |
| 1 | 58 | $43 \%$ | 25 | 1.5 | 1.4 |
| 2 | 27 | $47 \%$ | 13 | 0.8 | 0.7 |
| 3 | 6 | $52 \%$ | 3 | 0.2 | 0.2 |
| 4 | 2 | $57 \%$ | 1 | 0.1 | 0.1 |
| 5 | 0 | $63 \%$ | 0 | 0.0 | 0.0 |
| Total (Risk Margin, Time 0) |  |  |  |  |  |
| \% of Current Estimate |  |  |  |  |  |

Note that the cost of capital rate of return is selected to be $6.0 \%$ of the required capital in each period and the resulting cost of capital amount at the end of each period is discounted to time 0 at the same $6.0 \%$ rate to determine the discounted amount of the cost of capital, which is the value used as the risk margin in this example.

For illustrative purposes, Table 2 below displays the computation of the risk margin at the end of the first period given no changes to the assumptions shown above. In practice, companies will update assumptions at the end of each period based on information available at that time, and therefore those assumptions would not be "locked-in" at the outset.

TABLE 2
RISK MARGIN USING COST OF CAPITAL METHODOLOGY - TIME 1

| Period | Current <br> Liability <br> Estimate | Capital <br> Requirement | Required <br> Capital | Cost of <br> Capital | Discounted Cost <br> of Capital |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 58 | $43 \%$ | 25 | 1.5 | 1.5 |
| 2 | 27 | $47 \%$ | 13 | 0.8 | 0.7 |
| 3 | 6 | $52 \%$ | 3 | 0.2 | 0.2 |
| 4 | 2 | $57 \%$ | 1 | 0.1 | 0.1 |
| 5 | 0 | $63 \%$ | 0 | 0.0 | 0.0 | | Total (Risk Margin, Time 1) |
| :--- |
| \% of Current Estimate |

The figures in Table 2 are identical to those in Table 1 for periods 1-5 with one exception, the discounted amount of the cost of capital. This is due to the fact that at time 1, the cost of capital amount is discounted back to the beginning of time 1 rather than time 0 . The resulting margin of 2.4 is stated as a percentage of the current estimate at the beginning of time 1 ( 58 in this example), resulting in the margin of $4.1 \%$ shown above.

This process will be repeated in each successive period. A summary of the indicated risk margins using this cost of capital approach, and holding all assumptions constant, is shown below in Table 3, taken from the IAA Risk Margins paper:

TABLE 3
COST OF CAPITAL RISK MARGINS - MOTOR LIABILITY

| Period since <br> reporting date | Liability | Capital \% | Capital | Cost of <br> capital | Risk <br> margin | Risk margin <br> as of <br> liability |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 100 | $39.1 \%$ | 39.1 | 2.3 | 4.5 | $4.5 \%$ |
| 1 | 58 | $43.0 \%$ | 25.0 | 1.5 | 2.4 | $4.1 \%$ |
| 2 | 27 | $47.3 \%$ | 12.8 | 0.8 | 1.0 | $3.6 \%$ |
| 3 | 6 | $52.1 \%$ | 3.1 | 0.2 | 0.2 | $4.1 \%$ |
| 4 | 2 | $57.3 \%$ | 1.1 | 0.1 | 0.1 | $3.3 \%$ |
| 5 | 0 | $63.0 \%$ | 0.0 | 0.0 | 0.0 | $0.0 \%$ |

### 6.3 Discussion of the Key Assumptions in Using Cost of Capital Approaches to Risk Margins

The three key assumptions required for cost of capital methods are discussed further below:

## Question 1: How much capital is required to support the liabilities?

The initial capital requirement in the example provided above in the IAA Risk Margins paper is based on a targeted amount of capital such that the sum of the capital and the current estimate of the liabilities will be sufficient to absorb the actual losses at the $99.5 \%$ confidence level. This is a percentile approach applied to the aggregate amount committed to support the insurance liabilities, the discounted value of the current estimate plus the amount of capital needed in addition to the current estimate in order to have sufficient funds in all cases up to the $99.5 \%$ aggregate probability of the outcomes from the liabilities. The capital needed to meet this requirement can be determined given the probability distribution of the liabilities. This is sometimes referred to as the Value at Risk (VaR) approach. Similar approaches include the "Tail Value at Risk" or "Conditional Tail Expectation" which provides some additional consideration in the capital measurement for the impact of extreme scenarios. Such approaches require a selected percentile which is not directly based on market behavior.

It is important to note that the IAA does not advocate this specific methodology for determining the answer to question 1. Instead, the $99.5 \%$ confidence level is used as an example of the VaR cost of capital methodology.

This paper presents another approach for consideration in determining capital requirements based on an economic capital approach that does not target a specific confidence level or VaR. Consider the concept of economic capital as the measurement of the amount of capital required to support the insurance liabilities, given the risk profile, i.e., the probability distribution, of those liabilities, as determined by a market participant. This concept is not based on targeted confidence levels or regulatory capital requirements, though those factors may enter into the market participant's judgment. Rather this concept of economic capital is based on the capital consideration, and the rate of return on that capital, which is consistent with how market participants would price a contract or group of contracts, with similar risk characteristics.

## Question 2: How is the capital released over time?

To the extent the liabilities develop as expected, and capital is not required to absorb increases in the estimate of the liabilities, the capital supporting the liabilities may be released. The release of capital should theoretically mirror the reduction in aggregate risk of the liabilities. Thus, as claims are paid and the remaining liabilities are reduced over time, so too should the capital required to support those remaining liabilities be reduced (to the extent capital remains available given the current estimate). However, it is generally not the case that the capital release is directly proportional to the liability reduction. This is due to the fact that the relative risk of the remaining liabilities at different points in time can (and will) vary.

The assumption in the IAA Risk Margins example above is that the relative risk of the remaining liabilities is likely to increase over time; this is the reason for the assumption in the example of a $10 \%$ increase in the capital requirement as a percentage of remaining liabilities in each successive period. This assumption is based on the premise that relatively straightforward claims are settled in early periods and the remaining unpaid claims are more complex and the uncertainty in the value of those claims increases, albeit on a decreasing amount of the remaining liabilities. The $10 \%$ increase in the
capital requirement was shown only to illustrate its impact on risk margins, given the other assumptions made for the example.

## Question 3: What is the cost of capital?

The IAA Risk Margins paper uses $6 \%$ as the rate of return for the cost of capital in its example, but makes it clear that it does not advocate this or any other fixed assumption. In Market Value Margins for Insurance Liabilities in Financial Reporting and Solvency Application (Ernst \& Young, 2007), the point is made that the cost of capital should be inversely related to the capital requirement. This is consistent with the premise that there is a unique market risk margin given the risk profile of the liabilities, i.e., the probability distribution of the ultimate value of those liabilities. Thus, the key determinants of the appropriate risk margin in a cost of capital approach, the amount of capital needed and the rate of return on that capital, as required by market participants, should yield one answer. That one answer to risk margins based on the cost of capital represents the discounted present value of the product of the capital required and the rate of return on the capital.

Note that changing either the amount of capital needed or the rate of return required will result in a change in the opposite direction of the other variable. This is the reason why it has been suggested (IAA, 2009 p. 79) that benchmarks for cost of capital might include $6 \%$ at the $99.5^{\text {th }}$ percentile or $4 \%$ at the $99.95^{\text {th }}$ percentile, where the rate of return on capital assumption decreases as the percentile assumption increases.

Unfortunately, there is not a straightforward approach to estimate the cost of capital assumptions, and this is the reason why fixed assumptions, such as a $6 \%$ rate of return for a $99.5^{\text {th }}$ percentile have been used in both the financial and actuarial literature as well as in solvency regulation such as the Swiss Solvency Test. While these are useful benchmarks, what is lacking is a market basis for the determination of the cost of capital, particularly the rate of return, which reflects the risk of the liabilities, as might be measured by a probability distribution. Cost of capital can be viewed from multiple perspectives. From the point of view of the capital provider, a return on capital reflecting the risk of the endeavor is required in order to make the investment attractive. From the point of view of the insurer, this return must be provided, on average, in order to attract capital from investors. These two perspectives in theory should yield the same result.

### 6.4 Economic Capital

The amount of capital needed to support insurance liabilities is a major component of a cost of capital approach. However, economic value is usually defined in VaR terms, i.e., a certain percentile to provide a sufficient provision (i.e., financial resources such as investments in financial instruments) to minimize the solvency risk associated with the uncertain final cash flows needed to satisfy the obligations underlying the liabilities. This definition of economic capital therefore depends on the selected percentile (or similar criteria) which are defined in terms of insolvency risk, rather than market value. Hence, for purposes of using a cost of capital approach for risk margins, a different definition is needed to recognize that capital providers (investors) are at risk to losing their capital if the final cost of the unpaid claims exceeds the value provided for in the liabilities. For example, the value of the liabilities on a discounted basis will "provide for" a present value amount for the specific expected cash flows associated with the cost of claims. However, the investors may also receive a higher return on their capital if the final cost of the unpaid claims is less than the value provided for in the liabilities.

In other words, economic capital is not simply an amount borrowed at an interest rate which may or may not be repaid in full. Such a static view of capital as a sort of standby guarantee, increasing
for new risks and being released as risk declines, is based on the concept of solvency or stress scenarios used by rating agencies. While there is an element of market input to what level of capital is acceptable in the market, such an approach is significantly lacking because there is little, if any, reflection of the market pricing of risk and return. Consequently, risk margins that are based on this broader concept of economic capital should be derived from the probability distribution of gains and losses which emerge as the uncertain value of the unpaid claims liabilities matures and the uncertainty is resolved through the payment of these claims. Risk margins should not only reflect the expected value of the cost of the economic capital, but also the probability distribution of gains and losses.

This expanded view of risk margins, economic capital and the cost of capital suggests considering the determination of risk margins based on how the market prices insurance contracts. The pricing of insurance contracts involves the combinations of some costs that are known or can be estimated with reasonable certainty, and other costs, primarily the cost of claims, which are uncertain. This pricing also considers the amount of capital needed to support those insurance contracts until the cost of the claims is known. However, the usual approach for such pricing is to consider the profitability of the business, i.e., the rate of return which is available based on competitive prices in the marketplace. Thus, the participants in a competitive insurance market are assumed to understand the probability risk of the cost of claims (insurance losses) from the insurance policies sold in the marketplace, and the insurers price their policies accordingly. If the expected losses increase (or decrease), then the market prices will increase (or decrease). However, if the expected losses do not change, but there is a change in the risk distribution of losses being higher or lower than expected, then the prices should also respond accordingly.

This expanded view of economic capital describes the relationship between market profitability and the cost of capital in general terms. An additional consideration is the identification of situations where market pricing is not in equilibrium. In such cases, the question is whether the market pricing levels can be adjusted to estimate what the market variables would be in equilibrium. For example, because of underwriting cycles, competition, changes in perceptions of good and bad business, etc., there can be large fluctuations in profitability with little or no change in risk. In such situations, the estimate of the market value of risk should be adjusted, if possible, to reflect current expectations about what the level of profitability would be if the market were in equilibrium.

When there is evidence of a fairly stable market in equilibrium, or if market data were calibrated in some way to adjust for market equilibrium, then the objective is to use the market data to estimate the current market value of risk parameter. Based on recent industry average pricing for new or renewal insurance contracts, as reflected in estimates of profitability for recent accident years, the market value of risk parameter derived from the market data can be applied to the cash flow estimates for unpaid claims to calculate risk margins that are calibrated to the market.

### 6.5 Summary

Cost of capital approaches to risk margins have gained favor in the context of financial reporting and solvency monitoring due to their apparent consistency with pricing and because such approaches typically reflect a disciplined consideration of risk. This section has discussed the fundamental assumptions to consider when using a cost of capital methodology as well as some of the issues with finding practical approaches to applying a cost of capital approach to risk margins. In the next section, we will examine a methodology for determining risk margins based on a model for the quantification of a market value of risk parameter that is based on aggregate market data which is indicative of the estimated industry profit and risk, as reflected in insurance pricing.

## 7. VALUATION OF INSURANCE MARKET RISK USING A RISK TRANSFORM

Various methods and models have been discussed in the literature for the price of risk or the cost of risk. The terms "price of risk" and "cost of risk" may have different implications as a basis for valuing risk. The questions about the impact that risk has on value include what amount would willing buyers and sellers require to transfer such uncertain liabilities; what would be the settlement value of such liabilities; what is the maximum reasonable amount the holder of such liabilities would rationally pay to be relieved of such liabilities, etc. Consequently, the term "market value of risk" is adopted in this paper to address the question of the valuation of an uncertain quantity, unpaid claims, and to calibrate such valuation to a market basis that approximates how holders of such uncertain liabilities would value them. Since there is not a relevant reference market for insurance liabilities from unpaid losses, the current profit level for a large market of insurance can be utilized as the principal basis for calibration to a market basis, i.e., to determine a market value of risk parameter, $\lambda$.

### 7.1 The Wang Transform

Shaun Wang has written several papers (Wang, 1997) (Wang, 2002) on the application of a proportional hazard ( PH ) transform function to a probability distribution of outcomes. The resultant transformed probability distribution provides a mathematical representation, in probability terms, of the preferences associated with the various uncertain outcomes. The use of a probability distribution risk transform function allows for the computation of probability weighted expected values where the probabilities have been calibrated to risk preferences, such as the risk-based cost of capital. A particularly useful probability transform, the Wang Transform (Wang, 2002), has been developed based on a theoretical framework that connects the research from several other papers on the pricing of risk.

The Wang Transform has the following form for a liability variable (unpaid claims):

$$
\begin{equation*}
S^{*}(x)=\Phi\left(\Phi^{-1}(b \cdot S(x)+\lambda)\right) \tag{6}
\end{equation*}
$$

where,
$S(x)=1-F(x)$ for the original probability distribution function, $F(x)$
$S^{*}(x)=1-F^{*}(x)$ for the transformed probability distribution function, $F^{*}(x)$
$\Phi(x)=$ the standard normal probability distribution function
$\Phi^{-1}(x)=$ the inverse function of $\Phi(x)$
$\lambda=$ transform parameter for risk preference adjustment (market value of risk)
$b=$ transform parameter for parameter risk adjustment

Wang describes the $b$ parameter of the Wang Transform as a means for including parameter uncertainty in the measurement of risk. This may be useful in applying the approach presented in this paper to situations where an insurer's data or processes have significantly changed or where there is insufficient data available and the use of assumptions based on industry sources would certainly introduce parameter risk. The selection of the $b$ parameter would seem to be dependent on judgment. For this paper, we have used $b=1$ for the analyses of individual company data.

### 7.2 Market Value of Risk Parameter

By applying the Wang Transform (parameters $\lambda>0$ and $b=1$ ) to the profit probability distribution discussed in Section 5, it is possible to calibrate the market value of risk parameter ( $\lambda$ ) to the average market profit level based on industry data. The calibration is accomplished by using the transformed probability distribution, which includes the value of risk in the transformed probabilities. The transformed probabilities incorporate the average profit related to the average risk. Consequently, the expected value of profit using the transformed probability distribution would be equal to zero.

Wang shows that when the Wang transform is applied to the lognormal, the resultant expected value has the form,

$$
\begin{equation*}
E^{*}[x]=e^{\mu+1 / 2 \sigma^{2}+\lambda \cdot \sigma} \tag{7}
\end{equation*}
$$

Several of the authors referenced in this paper have selected a lognormal distribution. RehmanKlugman and Underwood-Zhu have reported good fits to actual insurance data. The industry data used for the results presented in this paper also produced good fits to the lines of insurance studied.

Hence, by using the lognormal distribution, the market value of risk parameter ( $\lambda$ ) can be obtained by solving the following equation for $\lambda$, assuming a lognormal distribution for the loss ratio (LR),

$$
\begin{gather*}
E^{*}[\text { Profit }]=0=\frac{(1-E R)}{(1+U L A E)}-P V \cdot E^{*}[L R]  \tag{8}\\
\frac{(1-E R)}{(1+U L A E)}=P V \cdot e^{\left(\mu+1 / 2 \sigma^{2}+\lambda \cdot \sigma\right)}  \tag{9}\\
\lambda=\frac{\left\{\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu-1 / 2 \cdot \sigma^{2}\right\}}{\sigma} \tag{10}
\end{gather*}
$$

where,
Profit ER, ULAE, PV, $\mu$, and $\sigma$ are defined in Section 5
$E^{*}[$ Profit $]=$ probability weighted expected value of the profit using a transformed probability distribution function

The application of this formula to the U.S. industry data, including the input data, is provided in the Exhibits included in this paper for each line of insurance.

### 7.3 Summary

This section has provided the framework and a function for computing a value of risk parameter. Using this approach, the probability distribution of the outcomes from a portfolio of insurance contracts can be used to derive the risk parameter. The next section shows the possible application of the risk transform function to determine risk margins for insurance liabilities associated with a portfolio of unpaid claims.

## 8. APPLICATION OF A RISK TRANSFORM FOR RISK MARGINS

The major advantage of using a risk transform function, such as the Wang Transform, in the valuation of risk is that it provides a means for consideration of the entire probability distribution, i.e., reflecting the range of outcomes. Additionally, when used to determine risk margins, a risk transform can be described as a risk preference function which implicitly reflects the cost of capital. The economic capital component of cost of capital is considered because the transform uses the full probability distribution and therefore the moments of the distribution, VaR, and similar measures are reflected. The rate of return on the capital component of cost of capital is also considered by the market value of risk parameter. This approach essentially aggregates these two components of cost of capital, without the need to separately develop each component (the capital amount and the rate of return). Consequently, the risk transform can be expressed in terms of various levels of capital (including the corresponding VaR and other measures) and the implied rates of return.

Wang suggests that the cost of capital is proportional to the "systematic" risk of the underlying business, and in theory, market insurance prices already reflect the probability of insolvency. This leads to the conclusion that the capital underlying market prices would be much lower than regulators and rating agencies typically require. However, to the extent the capital is required by regulators and rating agencies, the costs associated with holding higher levels of capital is a cost of doing business. If there is a higher cost of doing business due to regulatory or rating agency requirements and if the market pricing does not reflect that higher cost, then the insurers' expected rates of return on capital would be lower than other industries with similar risk profiles. However, market prices should reflect the regulatory cost or the cost of meeting rating agency requirements in a market where such costs for insurers are similar.

### 8.1 Risk Transform Considerations

In order to apply this risk transform approach to the problem of estimating risk margins for insurance liabilities, there are a few important considerations. First, the risk and uncertainty in the insurance liabilities should be expressed in terms of a probability distribution. Section 4 of this paper describes one method for estimating a probability distribution for the insurance liabilities associated with unpaid claim obligations from insurance contracts.

The type of probability distribution can be selected by fitting a distribution to a set of data, by simulation, or by assumption. Since the liabilities discussed in this paper are primarily related to unpaid claims, or other amounts that are a function of unpaid claims, an aggregate probability distribution may be needed to estimate the risk margins using a risk transform. In practice, creating
such an aggregate probability distribution might involve some component variables, such as frequency and severity, individual accident years or policy years, and other divisions that might be used to better represent the underlying random processes. In such cases, other techniques could be used to develop the aggregate distribution, such as convolutions, simulations, copulas or other numerical techniques.

Second, the market value of risk parameter, $\lambda$, should be adjusted to reflect the average duration of the outcomes, such as the duration of the cash flows associated with the payment of the unpaid claims. Wang provides a solution for the duration adjustment that can be used for the Wang Transform. The applicable formula for duration, $D$, is:

$$
\begin{equation*}
D=\int_{0}^{T} R(t) d t \tag{11}
\end{equation*}
$$

where
$R(t)=$ portion of losses that remain unpaid at time $t$
$T=$ length of time until unpaid losses equal zero.

From the method described in Section 7, the selected current market value of risk parameter, $\lambda_{\mathrm{AY}}$, for a single accident year is estimated. This accident year parameter is adjusted for duration to produce the one year duration parameter, $\lambda_{1}$. The adjustment suggested by Wang is:

$$
\begin{equation*}
\lambda_{1}=\frac{\lambda_{\mathrm{AY}}}{\sqrt{\mathrm{D}}} \tag{12}
\end{equation*}
$$

This adjustment is based on Wang's assumption of geometric Brownian motion to derive the relationship of the volatility and the length of time associated with the volatility. This assumption reflects an expected increase in volatility for longer periods of time between when the estimate is made and when the results can be observed. Hence, unpaid claims with longer payment duration will have higher volatility. The approach suggested by Wang is to compute an average adjustment to the market value of risk parameter, $\lambda$, which is proportional to the square root of the duration. Wang suggests that further refinement of this relationship may be appropriate if the underlying process exhibits volatility over time that is higher than the square root of the duration.

Third, the market value of risk parameter, $\boldsymbol{\lambda}_{1}$, which is estimated from the recent or projected levels of industry profitability, is suggested as being representative of the current market value of risk for a portfolio of unpaid claims from previous transactions. In other words, if the level of profit for a certain level of risk is estimated based on current industry data (a large portfolio of recent insurance transactions), then the relationship between profit and risk derived from that data can be applied to the level of risk measured on a portfolio of claims which are currently unpaid.

The relationship between risk and profit is contained in the market value of risk parameter, $\lambda_{1}$, and the value equation is given by the Wang Transform applied to the probability distribution
estimated for the unpaid claims. The duration adjustment reflects the difference in the duration of the claims payment used for the market profitability analysis (expected cash flows from claims for a single accident year as the beginning of that accident year) and the duration of the portfolio of unpaid claims (claims from multiple accident years each with different expected cash flows related to the unpaid amounts).

### 8.2 Estimate of Risk Margins

The risk margin is estimated as the difference between the probability weighted expected value of the unpaid claims using the original probability distribution and using the transformed probability distribution, as expressed by the following equation:

$$
\begin{equation*}
\text { Risk Margin }=E^{*}[\text { unpaid claims }]-E[\text { unpaid claims }] \tag{13}
\end{equation*}
$$

where,
$E^{*}[$ unpaid claims $]=$ probability weighted expected value of the unpaid claims using the transformed probability distribution function for the unpaid claims
$E[$ unpaid claims $]=$ probability weighted expected value of the unpaid claims using the estimated probability distribution function for the unpaid claims

### 8.3 Summary

By using the relationships described in each section, the proposed approach to estimating risk margins is summarized in the following table:

| Summary of Proposed Approach by Section | Parameters <br> Estimated |
| :---: | :---: |
| Section 4 |  |
| Reserve Risk Distributions <br> The estimation of a probability distribution of the unpaid claims by applying the Rehman-Klugman methodology. | by line of insurance by insurer |
|  | $\mu$ $\sigma$ D (duration) |
| Section 5 |  |
| Insurance Market Inputs and Risk Distributions <br> The analysis of industry data to estimate the level of profitability associated with recent market transactions for new and renewal policies. The analysis of industry loss development data to derive a risk distribution for the probability distribution of the most recent accident year loss ratio. This was accomplished by applying the Rehman-Klugman methodology to the industry aggregate loss development history. | industry aggregate by line of insurance by accident year |
|  | Expense Ratio ULAE Factor Loss Ratio PV Factor Average Profit $\mu$ $\sigma$ $D$ (duration) |
| Section 7 |  |
| Valuation of Insurance Market Risk using a Risk Transform | industry aggregate by line of insurance |
| The estimation of a market value of risk parameter, $\lambda$, for the industry by line which reflects the current value of risk, calibrated to the level of industry profitability associated with recent market transactions. The Wang Transform approach was applied to the risk distribution and the industry profit level estimated in Section 5. | $\lambda$ |
| Section 10 |  |
| Estimated Risk Margins <br> Risk margins were estimated by insurer for each of the five selected | Largest 100 insurers by insurer <br> by line of insurance |
| lines of insurance for unpaid claims as of December 2008. The market value of risk parameter, $\lambda$, was applied to the $F(x: \mu, \sigma)$ after adjustment for the $D$ associated with each insurer's reserves. | $\begin{gathered} \text { Risk Margins } \\ \text { as of } \\ \text { December } 2008 \end{gathered}$ |

## 9. TESTING OF APPROACH ON DATA FROM LARGEST 100 U.S. INSURERS

A validation of any model or method requires thorough testing of the results of using the model or method with actual data. Some of the methods used in this paper are relatively new and have not been in common usage by actuaries or others in estimating risk distributions for unpaid claims or for the pricing of risk in insurance. Consequently, the research for this paper included testing the methodology with a very large dataset of publicly available insurer data.

### 9.1 Data Used for Testing

The underlying data was taken from annual statutory financial reports filed with U.S. regulators, known as the Annual Statement. Each insurance company that has a license to write non-life insurance in one or more states is required to file its Annual Statement in March of each year. The detailed schedules and exhibits required for these reports include extensive data that is useful for testing this methodology. In addition, consolidated data from the reports are available on a combined basis for all subsidiaries and affiliated insurance companies within an insurance group. This data permitted the testing to be done at the group level. The final IFRS 4 guidelines will address the level of aggregation that is acceptable for purposes of estimating risk margins.

The data consisted of reported values from 1996 to 2008 for individual accident years 1987 through 2008 by insurer by line of insurance. The following schedules from U.S. Annual Statements were used:

$$
\begin{aligned}
& \text { Schedule P, Part 1B, 1C, 1D, 1E, 1H-1 } \\
& \text { Schedule P, Part 2B, 2C, 2D, 2E, 2H-1 } \\
& \text { Schedule P, Part 3B, 3C, 3D, 3E, 3H-1 }
\end{aligned}
$$

In addition, aggregate industry expense ratios by line of insurance were used from the figures published by the AM Best Company in their book (AM Best Company, 2008), Aggregates and Averages, 2008 edition.

Data values were excluded where abnormalities were suspected (such as negative claim amounts) or where the values were not relevant to the analysis. In general, the reported data was used without testing or validation since this data comes directly from regulatory reports. Consequently, there may be some results for individual insurers that are outliers due to additional data abnormalities.

The largest 100 insurers for each of the selected lines of insurance were chosen based on recent premium volume. For a few insurers the historical data might not be relevant for that particular insurer due to mergers and acquisitions, significant expansion or contraction of volume in a particular line of insurance, or other changes which were not discernable from the data. Such insurers could not be readily identified for exclusion from the study. Since this research was principally used to test the methodology for reasonableness of the approach, the results do not represent an assessment of the reserve levels, reserve risk or risk margins of the individual insurers used in the study. Therefore, the results for a specific individual insurer may not be indicative of appropriate risk margins for that insurer. Consequently, the names of the insurers were not included in the summaries of the results.

### 9.2 Steps in Testing Process

In order to estimate risk margins for the largest 100 insurers for each of the five lines of insurance included in the dataset, the following process was performed for each line of insurance:

1. The aggregate industry data was used to develop a market value of risk parameter $(\lambda)$, adjusted for a period of duration of one year;
2. An aggregate industry loss payout pattern was developed to estimate cash flows for each insurer based on each insurer's distribution of unpaid claims according to the maturity of the unpaid claim estimates for each accident year;
3. For each insurer in the database, the development pattern of estimated ultimate losses was run through the R-K methodology to estimate the parameters of the risk distribution of each insurer's portfolio of unpaid claims as of December 31, 2008;
4. The duration of each insurer's portfolio of unpaid claims as of December 31, 2008 was determined;
5. The present value factors for each insurer's portfolio of unpaid claims by accident year as of December 31, 2008 were determined;
6. Using the lognormal probability risk distribution with each insurer's parameters, $\mu$ and $\sigma$, developed from the R-K methodology through 120 months maturity, ultimate losses were simulated for each accident year and the unpaid losses \& ALAE were calculated by subtracting the paid losses \& ALAE as of December 31, 2008;
7. From the 500 simulations of each insurer's value of unpaid claims for each accident year, 1997 through 2008, the results were compiled and totaled for the unpaid losses \& ALAE for all accident years;
8. The sample mean ( $\hat{\mu}$ ) and sample standard deviation ( $\hat{\sigma}$ ) from the 500 simulations were computed, for the logarithm of the total (all accident years) of the simulated unpaid losses \& ALAE;
9. Using the simulated sample mean $(\hat{\mu})$ and sample standard deviation $(\hat{\sigma})$ for each insurer, from step (8), the expected value of the unpaid losses \& ALAE was computed using the formula for the mean of the lognormal distribution, $e^{\widehat{\mu}+1 / 2 \cdot \hat{\sigma}^{2}}$;
10. The risk adjusted expected value of the unpaid losses \& ALAE was computed using the industry market value of risk parameter $\left(\lambda_{1}\right)$ and the formula for the mean of the lognormal distribution after application of the Wang Transform, $e^{\hat{\mu}+1 / 2 \cdot \hat{\sigma}^{2}+\lambda_{1} \cdot \hat{\sigma} \cdot \sqrt{ } D}$;
11. The risk margin for each insurer was computed as the difference between the risk adjusted expected value from step (10) and the unadjusted expected value of the unpaid losses \& ALAE from step (9); and
12. The risks margins for the largest 100 insurers were totaled for all 100 insurers and expressed as a ratio of the total risk margins to the total unadjusted expected value of unpaid losses and ALAE for those insurers. The risk margins ratios were also computed individually for each of the 100 insurers.
The results are summarized in a series of exhibits which provide insights into the range of results and the levels of the risk margins by line of insurance.

## 10. RESULTS, CONCLUSIONS AND AREAS FOR FUTURE STUDY

The application of the approach discussed in this paper to real insurer data produces some very interesting results. Also, there are several areas where this research has indicated the need for further testing and live applications.

### 10.1 Results

The results of the methodology described in this paper are shown in Table 4 below:
TABLE 4
RISK MARGINS RESULTS FROM APPLICATION OF METHODOLOGY

| Largest 100 U.S. Insurance Groups <br> Accident Years 1997-2008 as of December 31, 2008 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Line of Insurance | Booked Unpaid Loss \& ALAE | Expected Unpaid Loss \& ALAE (R-K Method) | Average <br> Indicated <br> Risk <br> Margins* | Present <br> Value <br> Discount** | Net Impact of Risk Margins and Discount vs. Booked*** |
| Commercial Auto Liability | \$22.2 billion | \$21.8 billion | 10.1\% | (1.7\%) | 6.3\% |
| Commercial <br> Multiple Peril | \$32.3 billion | \$32.0 billion | 13.3\% | (3.0\%) | 8.8\% |
| Personal Auto Liability | \$75.2 billion | \$66.8 billion | 9.2\% | (1.4\%) | (4.3)\% |
| Workers <br> Compensation | \$83.1 billion | \$87.0 billion | 7.7\% | (8.9\%) | 2.7\% |
| Other Liability | \$60.7 billion | \$61.0 billion | 13.6\% | (3.8\%) | 9.8\% |

* Percent of the estimated unpaid loss \& ALAE (Exhibit 13 of each section $A-E$ ) (Total of 100 Insurers)
** Total present value of the estimated unpaid loss \& ALAE minus Total estimated unpaid loss \& ALAE (percent of total estimated unpaid loss \& ALAE) (Total of 100 Insurers)
**** Total estimated unpaid loss \& ALAE x (Average Risk Margin + Present Value Discount) (percent of booked estimated unpaid loss \& ALAE) (Total of 100 Insurers)
Source: Exhibit 16 for each line of insurance
These results were compiled with only minor adjustment to the data where needed to eliminate invalid computations. These results were also tested for the sensitivity of the inputs. There was
significant sensitivity to the values used for the industry profitability of the line of insurance for the current estimates. The profitability level has a significant impact on the indicated risk margins. This illustrates the potential for inconsistencies between the market value of risk for different lines of insurance, due to differences in the market profitability levels for each line. For purposes of this research, the profitability indicators were based on long term historical loss ratios after adjustment to normalize the historical series of loss ratios for major differences in the ratio levels over long time periods. Table 5 below illustrates the difference in the 2008 accident year loss ratios versus the long term averages by line of insurance. Note that the market value of risk parameter is quite sensitive to the differences in loss ratios, as well as to the target loss ratio by line of insurance.

TABLE 5

## SENSITIVITY OF RISK MARGINS RESULTS

|  | $\begin{array}{c}\text { Booked } \\ 2008\end{array}$ | $\begin{array}{c}\text { Adjusted } \\ \text { Long Term } \\ \text { Accident Year } \\ \text { Net Ultimate } \\ \text { Loss Ratio }\end{array}$ | $\begin{array}{c}\text { Net Ultimate } \\ \text { Loss Ratio }\end{array}$ | $\begin{array}{c}\text { Target } \\ \text { Loss } \\ \text { Ratio } *\end{array}$ | $\begin{array}{c}2008 \\ \text { Market } \\ \text { Value of } \\ \text { Risk } \lambda_{1} \\ \text { Risk Margin }]\end{array}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | \(\left.\begin{array}{c}Long Term <br>

Market <br>
Value of <br>
Risk \lambda_{1} <br>
[Risk Margin]\end{array}\right]\)

* Target Loss Ratio $=\frac{\frac{(1-\text { Expense Ratio })}{(1+U L A E)}}{} /_{\text {Present Value Factor }}$
** The industry average estimated ultimate loss ratio for accident year 2008 is much higher than the long term average loss ratio and even higher than the target loss ratio. This result indicates that market prices are expected to produce an operating loss on the business (underwriting results adjusted for discounted present value of the losses). Consequently, the market value of risk parameter would not be negative, but rather some minimum level. No basis for a minimum value was determined or selected.

Source: 11, 12A, 12B, 13A, 13B for each line of insurance
The two key variables that drive the profitability are as follows:

1. The portion of the premiums that are expected to be needed to pay the expenses of the insurer, and
2. The current estimate of the ultimate loss ratio for the recent accident year(s).

These two input variables were estimated from industry average loss ratios and expense ratios for all insurers reporting results in the U.S. and were used as a proxy for the level of profitability that the holder of the insurance liabilities would rationally pay (maximum value) to be relieved of the obligations underlying those liabilities. This implicitly assumes that the holder of the liabilities would not accept a lower level of profitability than the industry average, and conversely that the holder would not be able to obtain a higher level of profitability than the industry average. The industry average is used as an indication of the level of profitability that is generally available for new contracts (policies) in the marketplace.

The methodology adjusts the market value of risk parameter $(\lambda)$ for the difference in the risk distribution of the unpaid claim liabilities as compared to the risk distribution of a portfolio of new insurance contracts. Also, the adjustment reflects the difference in the duration of the liabilities from unpaid claims as compared to the duration of liabilities from new contracts. The profit levels indicated by the industry averages for the key variables can, however, vary from year to year. Such variations in expected profits can result in significant differences in the market value of risk parameter, and therefore there can be sensitivity in the risk margins produced from that parameter.

The results in Table 6 illustrate the differences in risk margins resulting from using the profit indicators for the total of the largest 25 or 50 largest companies versus the industry average in the Commercial Auto Liability line of insurance:

TABLE 6
COMPARISON OF RISK MARGIN RESULTS

| Sensitivity Analysis: Profit vs. Risk Margins |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Line of Insurance: Commercial Auto Liability |  |  |  |  |
|  | Adjusted <br> Long Term <br> Accident Year <br> Ultimate <br> Loss Ratio | Breakeven <br> Loss Ratio * | Profit** | Risk Margins*** |
| Industry Average | $58.3 \%$ | $62.8 \%$ | $6.2 \%$ | $10.1 \%$ |
| Largest 25 Insurers | $60.2 \%$ | $64.5 \%$ | $5.9 \%$ | $8.5 \%$ |
| Largest 50 Insurers | $59.3 \%$ | $63.4 \%$ | $5.8 \%$ | $9.1 \%$ |

*Breakeven Loss Ratio $=\frac{(1-\text { Expense Ratio })}{(1+U L A E)}$
** Profit $=$ Breakeven Loss Ratio - Present Value Factor $\cdot$ Ultimate Loss Ratio
*** Industry Average equal to Largest 100 Insurers

The small differences in these risk margins results from the small differences in the estimated profit level. To the extent that the risk margins reflect the value of being relieved of the obligations, an insurer who expects to earn higher profits from new contracts should rationally pay a higher
amount that is consistent with what that insurer can earn on new contracts with similar risk characteristics of existing contracts. Consequently, the risk margins could vary by insurer, even with similar risk distribution and duration.

### 10.2 Conclusions

The IASB and FASB had extensive discussions from July 2009 through January 2010 concerning liability measurement; the IASB released the IAS 37 Exposure Draft in January 2010; and there were further discussions concerning Phase II of the insurance contracts project during this period. These developments resulted in a description of the measurement of the amount that the entity would rationally pay to be relieved of the present obligation as equal to the lowest of:
a) The present value of the resources required to fulfill the obligation;
b) The amount the entity would have to pay to cancel the obligation; and
c) The amount the entity would have to pay to transfer the obligation to a third party.

The methodology described in this paper could be applied to the above liability measurement principles by estimating the key input variables (risk distribution, payment duration, etc.) and selecting a profit factor that reflects the market value of risk (market prices and the cost of capital implied by those prices) appropriate to (a) and (c). For example, item (c) above could be addressed by considering a third party market participant who would theoretically accept a profit level that is in line with industry averages. Since item (b) would be specific to particular counterparties individually and would be subject to applicable regulatory constraints, this methodology does not seem to apply to the determination of such values.

By using the methodology described in this paper, one can quantify the impact on estimated risk margins according to the values described based on a selected profit level, or the corresponding selected rate of return from other cost of capital calculations. This paper does not provide specific criteria for selecting a profit level that meets the requirements of (a) and (c) described above. Such criteria would need to meet the final guidance under IFRS. However, this methodology can provide a useful technical approach to the actuary in meeting the objectives of the IFRS guidance on risk margins.

### 10.3 Areas for Additional Research

There are several areas where the methodology described in this paper can be further refined to address specific implementation issues. The following list provides suggestions for further study.

- Underwriting Cycles: The profit levels in several competitive market situations have historically followed a pattern of hard markets (higher profits) followed by soft markets (lower profits) of a series of years. The use of time series analysis, such as described by Underwood and Zhu (Underwood, et al., 2009), can be studied further to assist in the selection of appropriate profit levels for determining risk margins.
- Market Profit Level Input to Risk Margins: The use of risk margins in the financial reporting of insurance liabilities has raised some issues about how to consider current profit levels that are driven by underwriting cycles. In particular, what are the implications of periods of very high or very low profit levels? What is the appropriate current market input assumption when markets are not in equilibrium and market prices produce very low or negative levels of profit? A study of historical market profit levels by line of insurance may
provide some useful insights, particularly with respect to the relationship of profit levels to risk margins. Also, it may be very useful to further explore the impact of market cycles on financial reporting values which use market inputs, including comparisons to risk margins that would have been reported based on historical underwriting cycles.
- Cash Flow Risk: The variability of the cash flows associated with the insurance liabilities can be improved by including a model that reflects the probabilities of different cash flows by year. The methodology as described in this paper only reflects the variability in the total cash flows, and therefore implicitly assumes that there is no significant additional variability in the cash flows by year. Since there can be correlations between the cash flows and the estimate of ultimate value of unpaid claims, it may be useful to expand the approach to incorporate the paid loss development history and the correlations to the estimates of ultimate values.
- Risk Distributions: The R-K methodology is a new methodology that has not been in general use as practical method for determining the probability distributions for unpaid claims. Further research would be quite valuable to understand how this method performs in various situations and in comparison to other approaches to estimating such distributions. Also, the further study of correlation within loss development patterns by accident year and by calendar year may prove useful, particularly as they may impact the estimation of risk margins. Additionally, since the R-K methodology is applied to estimates of ultimate losses including losses that have been paid, which are fixed (except for recoveries, such as from salvage and subrogation), there may be some concern that the R-K method may understate the risk in the unpaid claims. Further research into the application of the R-K methodology may be useful in better understanding this method of estimating risk distributions.
- Insufficient Data: Applying the R-K method to actual company data depends on the number of years and volume of relevant data available for the computation of risk margins for that company. Where a company has a limited history to analyze, or has made material changes to its business or it reserving process, such situations need practical solutions. Further study is needed to test the credibility of historical data and evaluate different approaches to selecting benchmark data for purposes of developing risk distributions for estimating risk margins.
- Low Frequency, Extreme Severity Risk and Reinsurance: For those lines of insurance that are significantly exposed to very low frequency or extreme severity claims, the approach described in this paper would need to be expanded. Also, further study is needed to address incoming (assumed) or outgoing (ceded) reinsurance which is material to an entity's insurance liabilities (or reinsurance assets), particularly for non-proportional (excess of loss) reinsurance. The risk distributions would need to be developed based on the specific types of claims and structure of the reinsurance cover. The R-K methodology is not well suited for such claims. The Wang Transform parameter would need to be calibrated to market data that is more specific to the insurance or reinsurance liabilities (or reinsurance assets), rather than to aggregate market profit levels. Further research is needed to adapt the key elements of the risk margin methodology developed in this paper to more difficult risks measurement problems associated with low frequency or extreme severity product types and reinsurance.
- Interest Rate Risk: It appears that interest rate risk, that is the rate used to discount the cash flows to produce a present value, is not included in the risk margins under IRFS. Consequently, changes in interest rates between financial reporting periods can result in
changes in reported financial results, simply due to the change in interest rates. The sensitivity of reported financial values due to interest rate changes would be a meaningful area for further study.
- Inflation Risk: The reflection of risk due to unanticipated inflationary changes to the cost of claims is limited to the period of time included in the historical data. Since the use of the R-K methodology only includes risks that have been reflected in the past history (or in the recalculated estimation based on improved calculations of ultimate values applied retroactively), the measurement of risk may need to be modified where the inflationary environment is changing. Also, some lines of insurance are more susceptible to inflation risk, or certain components of inflation such as medical costs. Further research of risk measurement techniques to address changing inflationary situations would be very useful.
- Correlation between Inflation and Interest Rates: Inflation and interest rates are typically highly correlated. Consequently, it may be important to consider the mitigation of inflation risk due to coincident changes in interest rates. Further research into the relationship between inflation risk and interest rate risk could be important to the consideration of these risks.
- Historical Back-Testing: The method described in this paper was applied to a large dataset of historical data. Further testing of the method by applying it to past periods and estimating what the historical risk margins would have been could provide some valuable insights such as quantifying the variation in risk margins over time and identifying refinements of the method.
- Field Testing: Additional research that applies this method to actual internal data from individual companies can be useful in refining the method and in devising a guide for its use in practice.
- Economic Capital, Return on Capital and Cost of Capital: While the concepts of economic capital, return on capital, and cost of capital are addressed in this paper in so far as risk margins are concerned, the analysis of the individual components and their relationship to regulatory capital are not fully addressed. Also, the allocation of capital based on risk has been a significant area of interest (Bodoff, 2009). Since the method developed in this paper is a function of the measurement of risk and the market level of profit, there is not a dependency on specific cost of capital assumptions involving a model of economic capital or the selection of a target return on capital. Further research on the relationships between the risk margins and the cost of capital would be a valuable addition to the literature.


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#### Abstract

APPENDIX

In Section 4 of the paper, the issue of changes in variables between accident years, and other changes over time is mentioned. The research for this paper included a few tests of changes in the underlying processes that may impact risk margins over time. Based on the dataset compiled for this paper, there were some interesting results produce by analyzing the adequacy of the estimates of ultimate losses across the largest 100 insurers. The graphs below show the results of analyzing the underestimation or overestimation of ultimate losses for Commercial Auto Liability by accident year. Graph A charts the average adequacy of ultimate loss estimates (log of development from 12 months to current) using the R-K methodology. Graph B charts the standard deviation of adequacy of ultimate loss estimates (log of development) among the 100 insurers.

These graphs provide some insight about the adequacy of the estimated ultimate losses, which seems to follow a predictable cycle. By using the times series analysis, it would be possible to forecast the cycle for one or two years. The standard deviation results indicate that the differences in adequacy among insurers do not change appreciably over time.


## GRAPH A



## GRAPH B



In addition, the approach used by Underwood and Zhu was applied to the Commercial Auto Liability dataset and the results shown in Graph C are quite similar to what those researchers found for a different line of insurance (Other Liability) over a longer time period.

## GRAPH C



## EXHIBITS

The following exhibits for each line of insurance are provided at the end of this paper:
Exhibit 1 Industry Net Booked Ultimate Loss \& ALAE
Exhibit 2 Industry Net Booked Ultimate Loss \& ALAE - Link Ratios
Exhibit 3 Cumulative Development in Ultimate Loss Estimates Based on Log of Link Ratios
Exhibit $4 \quad$ Variance-Covariance Matrix of Log of Incremental Link Ratios
Exhibit 5 Selection of Loss \& ALAE Ratio, ULAE Factor, and Loss \& LAE Ratio
Exhibit $6 \quad$ Industry Payout Pattern (Paid Loss \& ALAE)
Exhibit $7 \quad$ U.S. Treasury Yield Curves
Exhibit 8 Present Value Factors
Exhibit 9 Duration of Payout of Accident Year Losses
Exhibit 10 Developed Industry Ultimate Loss \& ALAE
Exhibit 11 Industry Historical Ultimate Loss \& ALAE Ratios
Exhibit 12A Derivation of Industry Market Value of Risk Parameter (2008 $\lambda$ )
Exhibit 12B Derivation of Industry Market Value of Risk Parameter (Long Term $\lambda$ )
Exhibit 13A Risk Margin Results for Industry and Largest 100 U.S. Insurers (2008 $\lambda$ )
Exhibit 13B Risk Margin Results for Industry and Largest 100 U.S. Insurers (Long Term $\lambda$ )
Exhibit 14 Payout of Expected Unpaid Loss \& ALAE for Largest 100 U.S. Insurers
Exhibit 15 Discounted Payout of Expected Unpaid Loss \& ALAE for Largest 100 U.S. Insurers
Exhibit 16 Net Impact of Margins and Discount for Largest 100 U.S. Insurers (Long Term $\lambda$ )

## SECTIONS

The Exhibits are organized by following Sections for each line of insurance:
Section A Commercial Auto Liability
Section B Commercial Multiple Peril
Section C Personal Auto Liability
Section D Workers Compensation
Section E Other Liability

COMMERCIAL AUTO LIABILITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Months of Maturity |  |  |  |  |  |  |  |  |  | Latest |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12 | $\underline{24}$ | 36 | 48 | 60 | $\underline{72}$ | 84 | $\underline{96}$ | 108 | 120 | Evaluation |
| 1987 | 8,195,868 | 8,093,702 | 8,083,907 | 8,104,034 | 8,091,634 | 8,078,034 | 8,092,658 | 8,068,131 | 8,042,289 | 8,034,872 | 8,034,872 |
| 1988 | 8,546,503 | 8,526,611 | 8,704,877 | 8,640,221 | 8,604,829 | 8,640,454 | 8,615,483 | 8,585,459 | 8,569,110 | 8,543,928 | 8,543,928 |
| 1989 | 9,420,085 | 9,246,724 | 9,279,795 | 9,287,502 | 9,281,584 | 9,229,632 | 9,176,851 | 9,148,599 | 9,120,928 | 9,101,236 | 9,101,236 |
| 1990 | 9,479,650 | 9,309,099 | 9,157,573 | 9,091,177 | 9,048,280 | 8,968,213 | 8,928,567 | 8,880,305 | 8,848,278 | 8,818,434 | 8,818,434 |
| 1991 | 9,031,017 | 8,853,171 | 8,575,945 | 8,381,188 | 8,289,001 | 8,216,473 | 8,154,828 | 8,123,474 | 8,060,272 | 8,016,358 | 8,016,358 |
| 1992 | 8,961,355 | 8,611,372 | 8,452,185 | 8,287,988 | 8,214,002 | 8,115,928 | 8,044,178 | 7,995,733 | 7,933,280 | 7,956,577 | 7,956,577 |
| 1993 | 8,747,317 | 8,633,221 | 8,606,389 | 8,523,034 | 8,455,054 | 8,390,747 | 8,334,471 | 8,285,543 | 8,269,077 | 8,284,094 | 8,284,094 |
| 1994 | 8,916,700 | 8,989,530 | 9,043,590 | 8,996,625 | 8,999,628 | 8,963,009 | 8,918,034 | 8,903,041 | 8,907,712 | 8,904,679 | 8,904,679 |
| 1995 | 9,057,286 | 9,029,922 | 9,028,225 | 9,086,186 | 9,082,557 | 9,084,951 | 9,057,872 | 9,044,750 | 9,040,049 | 9,031,717 | 9,031,717 |
| 1996 | 9,237,853 | 9,301,506 | 9,526,504 | 9,640,014 | 9,704,147 | 9,739,643 | 9,739,177 | 9,719,047 | 9,726,167 | 9,743,683 | 9,743,683 |
| 1997 | 9,485,776 | 9,537,708 | 9,741,479 | 9,974,342 | 10,180,228 | 10,225,662 | 10,221,048 | 10,198,180 | 10,214,647 | 10,205,685 | 10,205,685 |
| 1998 | 9,314,608 | 9,515,038 | 9,893,894 | 10,301,757 | 10,454,597 | 10,500,268 | 10,459,277 | 10,448,868 | 10,414,728 | 10,418,275 | 10,418,275 |
| 1999 | 9,408,335 | 10,043,371 | 10,549,185 | 10,945,497 | 11,101,670 | 11,091,395 | 11,123,348 | 11,099,762 | 11,078,047 | 11,075,835 | 11,075,835 |
| 2000 | 9,937,589 | 10,371,444 | 10,806,917 | 11,113,678 | 11,291,016 | 11,406,325 | 11,376,726 | 11,359,384 | 11,362,381 |  | 11,362,381 |
| 2001 | 10,290,153 | 10,277,719 | 10,632,589 | 10,891,786 | 11,051,340 | 10,993,292 | 10,953,987 | 10,943,423 |  |  | 10,943,423 |
| 2002 | 10,561,049 | 10,267,872 | 10,529,484 | 10,607,142 | 10,615,790 | 10,598,778 | 10,555,623 |  |  |  | 10,555,623 |
| 2003 | 11,210,956 | 10,801,169 | 10,753,873 | 10,779,804 | 10,708,701 | 10,659,927 |  |  |  |  | 10,659,927 |
| 2004 | 11,556,476 | 11,009,047 | 10,947,095 | 10,882,503 | 10,786,513 |  |  |  |  |  | 10,786,513 |
| 2005 | 11,717,674 | 11,407,000 | 11,258,547 | 11,239,808 |  |  |  |  |  |  | 11,239,808 |
| 2006 | 11,908,448 | 11,531,946 | 11,419,000 |  |  |  |  |  |  |  | 11,419,000 |
| 2007 | 11,944,741 | 11,819,461 |  |  |  |  |  |  |  |  | 11,819,461 |
| 2008 | 11,444,660 |  |  |  |  |  |  |  |  |  | 11,444,660 |

## Notes

Data from SNL Financial LC
1996-2008 Annual Statements
Industry Total Commercial Auto Liability Schedule P, Part 2C

COMMERCIAL AUTO LIABILITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | 0.988 | 0.999 | 1.002 | 0.998 | 0.998 | 1.002 | 0.997 | 0.997 | 0.999 |
| 1988 | 0.998 | 1.021 | 0.993 | 0.996 | 1.004 | 0.997 | 0.997 | 0.998 | 0.997 |
| 1989 | 0.982 | 1.004 | 1.001 | 0.999 | 0.994 | 0.994 | 0.997 | 0.997 | 0.998 |
| 1990 | 0.982 | 0.984 | 0.993 | 0.995 | 0.991 | 0.996 | 0.995 | 0.996 | 0.997 |
| 1991 | 0.980 | 0.969 | 0.977 | 0.989 | 0.991 | 0.992 | 0.996 | 0.992 | 0.995 |
| 1992 | 0.961 | 0.982 | 0.981 | 0.991 | 0.988 | 0.991 | 0.994 | 0.992 | 1.003 |
| 1993 | 0.987 | 0.997 | 0.990 | 0.992 | 0.992 | 0.993 | 0.994 | 0.998 | 1.002 |
| 1994 | 1.008 | 1.006 | 0.995 | 1.000 | 0.996 | 0.995 | 0.998 | 1.001 | 1.000 |
| 1995 | 0.997 | 1.000 | 1.006 | 1.000 | 1.000 | 0.997 | 0.999 | 0.999 | 0.999 |
| 1996 | 1.007 | 1.024 | 1.012 | 1.007 | 1.004 | 1.000 | 0.998 | 1.001 | 1.002 |
| 1997 | 1.005 | 1.021 | 1.024 | 1.021 | 1.004 | 1.000 | 0.998 | 1.002 | 0.999 |
| 1998 | 1.022 | 1.040 | 1.041 | 1.015 | 1.004 | 0.996 | 0.999 | 0.997 | 1.000 |
| 1999 | 1.067 | 1.050 | 1.038 | 1.014 | 0.999 | 1.003 | 0.998 | 0.998 | 1.000 |
| 2000 | 1.044 | 1.042 | 1.028 | 1.016 | 1.010 | 0.997 | 0.998 | 1.000 |  |
| 2001 | 0.999 | 1.035 | 1.024 | 1.015 | 0.995 | 0.996 | 0.999 |  |  |
| 2002 | 0.972 | 1.025 | 1.007 | 1.001 | 0.998 | 0.996 |  |  |  |
| 2003 | 0.963 | 0.996 | 1.002 | 0.993 | 0.995 |  |  |  |  |
| 2004 | 0.953 | 0.994 | 0.994 | 0.991 |  |  |  |  |  |
| 2005 | 0.973 | 0.987 | 0.998 |  |  |  |  |  |  |
| 2006 | 0.968 | 0.990 |  |  |  |  |  |  |  |
| 2007 | 0.990 |  |  |  |  |  |  |  |  |

COMMERCIAL AUTO LIABILITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
CUMULATIVE DEVELOPMENT IN ULTIMATE LOSS ESTIMATES BASED ON LOG OF LINK RATIOS

## SECTION A

EXHIBIT 3

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | -1.254\% | -0.121\% | 0.249\% | -0.153\% | -0.168\% | 0.181\% | -0.304\% | -0.321\% | -0.092\% |
| 1988 | -0.233\% | 2.069\% | -0.746\% | -0.410\% | 0.413\% | -0.289\% | -0.349\% | -0.191\% | -0.294\% |
| 1989 | -1.857\% | 0.357\% | 0.083\% | -0.064\% | -0.561\% | -0.574\% | -0.308\% | -0.303\% | -0.216\% |
| 1990 | -1.816\% | -1.641\% | -0.728\% | -0.473\% | -0.889\% | -0.443\% | -0.542\% | -0.361\% | -0.338\% |
| 1991 | -1.989\% | -3.181\% | -2.297\% | -1.106\% | -0.879\% | -0.753\% | -0.385\% | -0.781\% | -0.546\% |
| 1992 | -3.984\% | -1.866\% | -1.962\% | -0.897\% | -1.201\% | -0.888\% | -0.604\% | -0.784\% | 0.293\% |
| 1993 | -1.313\% | -0.311\% | -0.973\% | -0.801\% | -0.763\% | -0.673\% | -0.589\% | -0.199\% | 0.181\% |
| 1994 | 0.813\% | 0.600\% | -0.521\% | 0.033\% | -0.408\% | -0.503\% | -0.168\% | 0.052\% | -0.034\% |
| 1995 | -0.303\% | -0.019\% | 0.640\% | -0.040\% | 0.026\% | -0.299\% | -0.145\% | -0.052\% | -0.092\% |
| 1996 | 0.687\% | 2.390\% | 1.184\% | 0.663\% | 0.365\% | -0.005\% | -0.207\% | 0.073\% | 0.180\% |
| 1997 | 0.546\% | 2.114\% | 2.362\% | 2.043\% | 0.445\% | -0.045\% | -0.224\% | 0.161\% | -0.088\% |
| 1998 | 2.129\% | 3.904\% | 4.040\% | 1.473\% | 0.436\% | -0.391\% | -0.100\% | -0.327\% | 0.034\% |
| 1999 | 6.532\% | 4.914\% | 3.688\% | 1.417\% | -0.093\% | 0.288\% | -0.212\% | -0.196\% | -0.020\% |
| 2000 | 4.273\% | 4.113\% | 2.799\% | 1.583\% | 1.016\% | -0.260\% | -0.153\% | 0.026\% |  |
| 2001 | -0.121\% | 3.395\% | 2.409\% | 1.454\% | -0.527\% | -0.358\% | -0.096\% |  |  |
| 2002 | -2.815\% | 2.516\% | 0.735\% | 0.081\% | -0.160\% | -0.408\% |  |  |  |
| 2003 | -3.724\% | -0.439\% | 0.241\% | -0.662\% | -0.457\% |  |  |  |  |
| 2004 | -4.853\% | -0.564\% | -0.592\% | -0.886\% |  |  |  |  |  |
| 2005 | -2.687\% | -1.310\% | -0.167\% |  |  |  |  |  |  |
| 2006 | -3.213\% | -0.984\% |  |  |  |  |  |  |  |
| 2007 | -1.054\% |  |  |  |  |  |  |  |  |
| Average | -0.773\% | 0.797\% | 0.550\% | 0.181\% | -0.200\% | -0.339\% | -0.292\% | -0.229\% | -0.079\% |
|  | 12-108 | 24-108 | 36-108 | 48-108 | 60-108 | 72-108 | 84-108 | 96-108 | 108-108 |
| Cumulative Average | -0.385\% | 0.388\% | -0.409\% | -0.959\% | -1.139\% | -0.939\% | -0.600\% | -0.308\% | -0.079\% |

From Exhibit 2, natural log of ratio of successive ultimate loss estimates by accident year

## COMMERCIAL AUTO LIABILITY

SECTION A
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE

## VARIANCE-COVARIANCE MATRIX OF LOG OF INCREMENTAL LINK RATIOS

| Months of Maturity | 12-108 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 | 120-Ultimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12-108 | 0.071\% | 0.047\% | 0.036\% | 0.020\% | 0.010\% | 0.005\% | 0.003\% | 0.004\% | 0.001\% | 0.000\% |
| 24-36 | 0.047\% | 0.048\% | 0.034\% | 0.018\% | 0.010\% | 0.004\% | 0.003\% | 0.004\% | 0.002\% | 0.000\% |
| 36-48 | 0.036\% | 0.034\% | 0.030\% | 0.016\% | 0.007\% | 0.004\% | 0.002\% | 0.003\% | 0.001\% | 0.000\% |
| 48-60 | 0.020\% | 0.018\% | 0.016\% | 0.010\% | 0.004\% | 0.002\% | 0.001\% | 0.002\% | 0.000\% | 0.000\% |
| 60-72 | 0.010\% | 0.010\% | 0.007\% | 0.004\% | 0.003\% | 0.001\% | 0.001\% | 0.001\% | 0.000\% | 0.000\% |
| 72-84 | 0.005\% | 0.004\% | 0.004\% | 0.002\% | 0.001\% | 0.001\% | 0.000\% | 0.001\% | 0.000\% | 0.000\% |
| 84-96 | 0.003\% | 0.003\% | 0.002\% | 0.001\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 96-108 | 0.004\% | 0.004\% | 0.003\% | 0.002\% | 0.001\% | 0.001\% | 0.000\% | 0.001\% | 0.000\% | 0.000\% |
| 108-120 | 0.001\% | 0.002\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 120-Ultimate | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| Variance ( $\sigma^{\mathbf{2}}$ ) | 0.656\% | 0.336\% | 0.139\% | 0.042\% | 0.014\% | 0.005\% | 0.002\% | 0.002\% | 0.000\% | 0.000\% |

Notes
From Exhibit 3, covariance of errors at given maturity with errors at all other maturities
Covariances above diagonal are symmetric with those below
Variance is sum of matrix for all maturities greater than or equal to maturity shown in column

Selection of loss \& alae ratio, ulae factor, and loss \& lae ratio
Dollars in Thousands

|  | Net <br> Earned Premium | Net Ultimate Loss \& LAE | Net <br> Ultimate Loss \& ALAE | $\begin{gathered} \text { Net } \\ \text { Paid } \\ \text { Loss \& ALAE } \\ \hline \end{gathered}$ | Net <br> Unpaid Loss \& ALAE | Net Ultimate Loss \& LAE Ratio | Net <br> Ultimate Loss \& ALAE Ratio | ULAE <br> Factor | Underwriting <br> Expense Ratio |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) |
| 1987 | 11,303,497 | 8,421,138 | 8,034,872 | 7,798,508 | 236,364 | 74.5\% | 71.1\% | 1.048 | 26.3\% | 73.7\% |
| 1988 | 11,137,272 | 8,925,276 | 8,543,928 | 8,270,462 | 273,466 | 80.1\% | 76.7\% | 1.045 | 28.1\% | 71.9\% |
| 1989 | 11,640,663 | 9,601,129 | 9,101,236 | 8,914,519 | 186,717 | 82.5\% | 78.2\% | 1.055 | 29.0\% | 71.0\% |
| 1990 | 11,885,710 | 9,359,215 | 8,818,434 | 8,673,421 | 145,013 | 78.7\% | 74.2\% | 1.061 | 29.5\% | 70.5\% |
| 1991 | 11,400,334 | 8,552,810 | 8,016,358 | 7,917,278 | 99,080 | 75.0\% | 70.3\% | 1.067 | 30.0\% | 70.0\% |
| 1992 | 11,487,315 | 8,522,527 | 7,956,577 | 7,823,914 | 132,663 | 74.2\% | 69.3\% | 1.071 | 30.6\% | 69.4\% |
| 1993 | 11,349,838 | 8,872,940 | 8,284,094 | 8,194,228 | 89,866 | 78.2\% | 73.0\% | 1.071 | 30.5\% | 69.5\% |
| 1994 | 11,391,025 | 9,556,415 | 8,904,679 | 8,813,471 | 91,208 | 83.9\% | 78.2\% | 1.073 | 30.7\% | 69.3\% |
| 1995 | 11,545,377 | 9,712,995 | 9,031,717 | 8,950,911 | 80,806 | 84.1\% | 78.2\% | 1.075 | 30.5\% | 69.5\% |
| 1996 | 12,038,793 | 10,484,408 | 9,743,683 | 9,630,426 | 113,257 | 87.1\% | 80.9\% | 1.076 | 30.6\% | 69.4\% |
| 1997 | 12,188,203 | 11,031,192 | 10,205,685 | 10,097,558 | 108,127 | 90.5\% | 83.7\% | 1.081 | 30.2\% | 69.8\% |
| 1998 | 12,093,751 | 11,329,093 | 10,418,275 | 10,300,393 | 117,882 | 93.7\% | 86.1\% | 1.087 | 30.1\% | 69.9\% |
| 1999 | 11,992,416 | 12,003,662 | 11,075,835 | 10,943,805 | 132,030 | 100.1\% | 92.4\% | 1.084 | 31.7\% | 68.3\% |
| 2000 | 12,844,883 | 12,325,072 | 11,362,381 | 11,176,545 | 185,836 | 96.0\% | 88.5\% | 1.085 | 30.2\% | 69.8\% |
| 2001 | 14,023,859 | 11,892,234 | 10,943,423 | 10,673,375 | 270,048 | 84.8\% | 78.0\% | 1.087 | 29.6\% | 70.4\% |
| 2002 | 15,846,301 | 11,590,418 | 10,555,623 | 10,191,909 | 363,714 | 73.1\% | 66.6\% | 1.098 | 28.2\% | 71.8\% |
| 2003 | 17,595,042 | 11,723,903 | 10,659,927 | 10,039,271 | 620,656 | 66.6\% | 60.6\% | 1.100 | 26.6\% | 73.4\% |
| 2004 | 18,772,204 | 11,909,100 | 10,786,513 | 9,682,114 | 1,104,399 | 63.4\% | 57.5\% | 1.104 | 27.7\% | 72.3\% |
| 2005 | 19,257,834 | 12,385,157 | 11,239,808 | 9,057,583 | 2,182,225 | 64.3\% | 58.4\% | 1.102 | 27.4\% | 72.6\% |
| 2006 | 19,338,884 | 12,647,829 | 11,419,000 | 7,543,503 | 3,875,497 | 65.4\% | 59.0\% | 1.108 | 28.5\% | 71.5\% |
| 2007 | 19,171,676 | 13,090,247 | 11,819,461 | 5,487,654 | 6,331,807 | 68.3\% | 61.7\% | 1.108 | 30.6\% | 69.4\% |
| 2008 | 18,367,084 | 12,820,906 | 11,444,660 | 2,553,063 | 8,891,597 | 69.8\% | 62.3\% | 1.120 | 30.5\% | 69.5\% |
| Selected |  |  |  |  | 25,632,258 |  | 62.3\% | 1.106 |  | 69.5\% |

Notes
(1), (2) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1C
(3) Exhibit 1, Latest Evaluation
(4) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1C
$(5)=(3)-(4)$
(6) $=(2) /(1)$
$(7)=(3) /(1)$; Selected from 2008
(8) $=(6) /(7)$; Selected from 2005-2007 Average
(9) From AM Best Aggregates and Averages, includes policyholder dividends
(10) $=1$ - (9); Selected from 2008

COMMERCIAL AUTO LIABILITY
NDUSTRY PAYOUT PATTERN (PAID LOSS \& ALAE)
Dollars in Thousands

## $\frac{\text { Accident Year }}{1987}$

 19871988
1989 1988
1989
1991
1991 1991
1992
1993 1992
1993
1994 19996
1997 1997
1998 1998
1999 1999
2000
2001

2005
2007
2007

| 12 | $\underline{24}$ | 36 |
| :---: | :---: | :---: |
| 1,447,237 | 3,489,508 | 5,084,540 |
| 1,609,269 | 3,773,198 | 5,522,054 |
| 1,827,370 | 4,184,777 | 6,065,400 |
| 2,491,964 | 4,092,486 | 5,953,821 |
| 1,814,961 | 3,799,444 | 5,523,652 |
| 1,669,374 | 3,716,814 | 5,396,263 |
| 1,740,569 | 3,931,270 | 5,688,755 |
| 1,991,344 | 4,313,471 | 6,088,493 |
| 2,109,110 | 4,464,486 | 6,274,090 |
| 2,310,732 | 4,689,420 | 6,676,411 |
| 2,332,509 | 4,846,563 | 6,952,542 |
| 2,325,407 | 4,926,252 | 7,049,841 |
| 2,473,596 | 5,302,486 | 7,634,504 |
| 2,626,282 | 5,502,154 | 7,807,475 |
| 2,555,847 | 5,267,400 | 7,505,311 |
| 2,246,248 | 4,687,722 | 6,956,645 |
| 2,235,298 | 4,764,047 | 6,942,024 |
| 2,385,037 | 4,863,666 | 7,019,567 |
| 2,394,118 | 5,133,485 | 7,390,225 |
| 2,545,051 | 5,237,326 | 7,543,503 |
| 2,608,213 | 5,487,654 |  |
| 2,553,063 |  |  |


| Age-to-Age Paid Loss Development |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | 2.411 | 1.457 | 1.233 | 1.111 | 1.057 | 1.030 | 1.016 | 1.008 | 1.004 |
| 1988 | 2.345 | 1.463 | 1.220 | 1.109 | 1.053 | 1.029 | 1.013 | 1.005 | 1.003 |
| 1989 | 2.290 | 1.449 | 1.211 | 1.105 | 1.051 | 1.025 | 1.011 | 1.005 | 1.003 |
| 1990 | 1.642 | 1.455 | 1.209 | 1.100 | 1.047 | 1.023 | 1.011 | 1.006 | 1.004 |
| 1991 | 2.093 | 1.454 | 1.194 | 1.099 | 1.047 | 1.024 | 1.011 | 1.006 | 1.002 |
| 1992 | 2.226 | 1.452 | 1.206 | 1.103 | 1.047 | 1.020 | 1.013 | 1.004 | 1.005 |
| 1993 | 2.259 | 1.447 | 1.202 | 1.096 | 1.046 | 1.025 | 1.010 | 1.006 | 1.004 |
| 1994 | 2.166 | 1.412 | 1.207 | 1.095 | 1.050 | 1.021 | 1.010 | 1.006 | 1.004 |
| 1995 | 2.117 | 1.405 | 1.196 | 1.093 | 1.047 | 1.023 | 1.010 | 1.006 | 1.003 |
| 1996 | 2.029 | 1.424 | 1.199 | 1.106 | 1.046 | 1.023 | 1.007 | 1.006 | 1.004 |
| 1997 | 2.078 | 1.435 | 1.209 | 1.102 | 1.049 | 1.020 | 1.009 | 1.008 | 1.002 |
| 1998 | 2.118 | 1.431 | 1.217 | 1.105 | 1.047 | 1.020 | 1.010 | 1.004 | 1.004 |
| 1999 | 2.144 | 1.440 | 1.216 | 1.097 | 1.032 | 1.023 | 1.007 | 1.006 | 1.004 |
| 2000 | 2.095 | 1.419 | 1.199 | 1.097 | 1.050 | 1.019 | 1.011 | 1.007 |  |
| 2001 | 2.061 | 1.425 | 1.203 | 1.096 | 1.045 | 1.021 | 1.011 |  |  |
| 2002 | 2.087 | 1.484 | 1.227 | 1.111 | 1.052 | 1.023 |  |  |  |
| 2003 | 2.131 | 1.457 | 1.233 | 1.117 | 1.050 |  |  |  |  |
| 2004 | 2.039 | 1.443 | 1.237 | 1.115 |  |  |  |  |  |
| 2005 | 2.144 | 1.440 | 1.226 |  |  |  |  |  |  |
| 2006 | 2.058 | 1.440 |  |  |  |  |  |  |  |
| 2007 | 2.104 |  |  |  |  |  |  |  |  |
| Averages |  |  |  |  |  |  |  |  |  |
| 10-Yr Weighted | 2.098 | 1.441 | 1.216 | 1.104 | 1.047 | 1.022 | 1.010 | 1.006 | 1.004 |
| 10-Yr Straight | 2.098 | 1.441 | 1.217 | 1.104 | 1.047 | 1.022 | 1.010 | 1.006 | 1.004 |
| Selected | 2.098 | 1.441 | 1.216 | 1.104 | 1.047 | 1.022 | 1.010 | 1.006 | 1.004 |


| Fitted Age-to-Ultimate |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Curve Fits: | R-squared | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| Weibull | 99.6\% | 1.004 | 1.002 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Power Curve | 99.7\% | 1.003 | 1.002 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Inverse Power Curve | 93.6\% | 1.028 | 1.023 | 1.019 | 1.016 | 1.014 | 1.012 | 1.010 | 1.009 | 1.008 | 1.007 | 1.006 | 1.005 | 1.005 |


| Selected Pattern | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age-to-Age | 2.098 | 1.441 | 1.216 | 1.104 | 1.047 | 1.022 | 1.010 | 1.006 | 1.004 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |  |
| Age-to-Ultimate | 4.436 | 2.115 | 1.468 | 1.207 | 1.093 | 1.045 | 1.022 | 1.013 | 1.007 | 1.003 | 1.002 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Cumulative \% Paid | 22.5\% | 47.3\% | 68.1\% | 82.9\% | 91.5\% | 95.7\% | 97.8\% | 98.8\% | 99.3\% | 99.7\% | 99.8\% | 99.9\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% |
| Incremental \% Paid | 22.5\% | 24.7\% | 20.8\% | 14.7\% | 8.6\% | 4.3\% | 2.1\% | 0.9\% | 0.6\% | 0.4\% | 0.1\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |

[^0]|  | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Duration | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) |
| 1 month | 0.11\% | 2.76\% | 4.75\% | 4.01\% | 1.89\% | 0.90\% | 1.20\% | 1.68\% | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |
| 3 months | 0.11\% | 3.36\% | 5.02\% | 4.08\% | 2.22\% | 0.95\% | 1.22\% | 1.74\% | 5.89\% | 5.33\% | 4.48\% | 5.36\% | 5.21\% | 5.10\% | 5.68\% | 3.07\% | 3.15\% | 3.96\% | 6.63\% |
| 6 months | 0.27\% | 3.49\% | 5.09\% | 4.37\% | 2.59\% | 1.02\% | 1.23\% | 1.83\% | 5.70\% | 5.74\% | 4.55\% | 5.45\% | 5.33\% | 5.17\% | 6.51\% | 3.30\% | 3.38\% | 4.00\% | 6.73\% |
| 1 year | 0.37\% | 3.34\% | 5.00\% | 4.38\% | 2.75\% | 1.26\% | 1.32\% | 2.17\% | 5.32\% | 5.98\% | 4.53\% | 5.51\% | 5.51\% | 5.18\% | 7.20\% | 3.63\% | 3.61\% | 4.12\% | 6.82\% |
| 2 years | 0.76\% | 3.05\% | 4.82\% | 4.41\% | 3.08\% | 1.84\% | 1.61\% | 3.07\% | 5.11\% | 6.24\% | 4.54\% | 5.66\% | 5.88\% | 5.18\% | 7.69\% | 4.25\% | 4.56\% | 4.77\% | 7.15\% |
| 3 years | 1.00\% | 3.07\% | 4.74\% | 4.37\% | 3.25\% | 2.37\% | 1.99\% | 3.59\% | 5.06\% | 6.29\% | 4.55\% | 5.68\% | 6.04\% | 5.25\% | 7.80\% | 4.58\% | 5.12\% | 5.11\% | 7.40\% |
| 5 years | 1.55\% | 3.45\% | 4.70\% | 4.35\% | 3.63\% | 3.25\% | 2.78\% | 4.38\% | 4.99\% | 6.36\% | 4.56\% | 5.71\% | 6.21\% | 5.38\% | 7.83\% | 5.21\% | 6.04\% | 5.93\% | 7.68\% |
| 7 years | 1.87\% | 3.70\% | 4.70\% | 4.36\% | 3.94\% | 3.77\% | 3.36\% | 4.84\% | 5.16\% | 6.55\% | 4.73\% | 5.77\% | 6.34\% | 5.49\% | 7.84\% | 5.53\% | 6.43\% | 6.38\% | 8.00\% |
| 10 years | 2.25\% | 4.04\% | 4.71\% | 4.39\% | 4.24\% | 4.27\% | 3.83\% | 5.07\% | 5.12\% | 6.45\% | 4.65\% | 5.75\% | 6.43\% | 5.58\% | 7.84\% | 5.83\% | 6.70\% | 6.71\% | 8.08\% |
| 20 years | 3.05\% | 4.50\% | 4.91\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.74\% | 5.59\% | 6.83\% | 5.39\% | 6.02\% | 6.73\% | 6.01\% | 8.02\% | 6.48\% | 7.05\% | 7.06\% | 8.17\% |
| 30 years | 2.69\% | 4.45\% | 4.81\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.48\% | 5.46\% | 6.48\% | 5.09\% | 5.93\% | 6.65\% | 5.96\% | 7.89\% | 6.35\% | 7.40\% | 7.41\% | 8.26\% |


| Discount Factor | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (months) | (20) | (21) | (22) | (23) | (24) | (25) | (26) | (27) | (28) | (29) | (30) | (31) | (32) | (33) | (34) | (35) | (36) | (37) | (38) |
| 6 | 0.999 | 0.983 | 0.975 | 0.979 | 0.987 | 0.995 | 0.994 | 0.991 | 0.973 | 0.972 | 0.978 | 0.974 | 0.974 | 0.975 | 0.969 | 0.984 | 0.984 | 0.981 | 0.968 |
| 18 | 0.992 | 0.954 | 0.931 | 0.938 | 0.958 | 0.977 | 0.978 | 0.962 | 0.927 | 0.915 | 0.936 | 0.922 | 0.920 | 0.927 | 0.898 | 0.944 | 0.942 | 0.937 | 0.904 |
| 30 | 0.978 | 0.927 | 0.890 | 0.898 | 0.925 | 0.949 | 0.956 | 0.921 | 0.883 | 0.859 | 0.895 | 0.871 | 0.865 | 0.881 | 0.830 | 0.898 | 0.889 | 0.886 | 0.839 |
| 42 | 0.961 | 0.897 | 0.851 | 0.861 | 0.891 | 0.914 | 0.927 | 0.878 | 0.842 | 0.807 | 0.856 | 0.824 | 0.813 | 0.835 | 0.769 | 0.850 | 0.833 | 0.834 | 0.777 |
| 54 | 0.939 | 0.862 | 0.813 | 0.825 | 0.855 | 0.874 | 0.892 | 0.832 | 0.803 | 0.758 | 0.818 | 0.779 | 0.764 | 0.791 | 0.713 | 0.801 | 0.776 | 0.778 | 0.719 |
| 66 | 0.915 | 0.827 | 0.777 | 0.791 | 0.819 | 0.833 | 0.853 | 0.785 | 0.763 | 0.711 | 0.781 | 0.736 | 0.717 | 0.749 | 0.661 | 0.753 | 0.721 | 0.724 | 0.663 |
| 78 | 0.891 | 0.793 | 0.742 | 0.758 | 0.782 | 0.793 | 0.814 | 0.741 | 0.723 | 0.664 | 0.742 | 0.695 | 0.672 | 0.708 | 0.612 | 0.708 | 0.671 | 0.674 | 0.609 |
| 90 | 0.866 | 0.758 | 0.709 | 0.726 | 0.746 | 0.753 | 0.776 | 0.700 | 0.686 | 0.622 | 0.708 | 0.657 | 0.630 | 0.669 | 0.568 | 0.665 | 0.625 | 0.626 | 0.561 |
| 102 | 0.841 | 0.724 | 0.677 | 0.695 | 0.711 | 0.715 | 0.741 | 0.663 | 0.653 | 0.586 | 0.677 | 0.621 | 0.591 | 0.633 | 0.526 | 0.625 | 0.582 | 0.583 | 0.518 |
| 114 | 0.814 | 0.690 | 0.646 | 0.665 | 0.677 | 0.677 | 0.705 | 0.627 | 0.622 | 0.551 | 0.649 | 0.588 | 0.554 | 0.598 | 0.488 | 0.586 | 0.542 | 0.542 | 0.479 |
| 126 | 0.788 | 0.658 | 0.616 | 0.636 | 0.645 | 0.642 | 0.671 | 0.593 | 0.591 | 0.518 | 0.618 | 0.555 | 0.519 | 0.564 | 0.452 | 0.550 | 0.505 | 0.505 | 0.442 |
| 138 | 0.764 | 0.629 | 0.587 | 0.608 | 0.614 | 0.610 | 0.638 | 0.560 | 0.559 | 0.484 | 0.586 | 0.523 | 0.486 | 0.532 | 0.419 | 0.516 | 0.472 | 0.471 | 0.409 |
| 150 | 0.739 | 0.601 | 0.559 | 0.581 | 0.584 | 0.578 | 0.607 | 0.528 | 0.528 | 0.453 | 0.554 | 0.493 | 0.455 | 0.501 | 0.387 | 0.483 | 0.440 | 0.440 | 0.378 |
| 162 | 0.714 | 0.574 | 0.532 | 0.554 | 0.555 | 0.548 | 0.575 | 0.498 | 0.499 | 0.423 | 0.524 | 0.464 | 0.425 | 0.471 | 0.358 | 0.452 | 0.410 | 0.410 | 0.349 |
| 174 | 0.688 | 0.547 | 0.507 | 0.529 | 0.527 | 0.518 | 0.545 | 0.468 | 0.471 | 0.395 | 0.494 | 0.437 | 0.398 | 0.443 | 0.331 | 0.422 | 0.382 | 0.382 | 0.322 |
| 186 | 0.663 | 0.521 | 0.482 | 0.505 | 0.500 | 0.489 | 0.515 | 0.440 | 0.444 | 0.368 | 0.465 | 0.411 | 0.372 | 0.416 | 0.306 | 0.394 | 0.356 | 0.355 | 0.298 |
| 198 | 0.637 | 0.496 | 0.458 | 0.481 | 0.473 | 0.461 | 0.485 | 0.413 | 0.418 | 0.343 | 0.438 | 0.387 | 0.347 | 0.391 | 0.283 | 0.368 | 0.331 | 0.331 | 0.275 |
| 210 | 0.612 | 0.472 | 0.436 | 0.459 | 0.448 | 0.433 | 0.457 | 0.387 | 0.394 | 0.320 | 0.411 | 0.364 | 0.324 | 0.367 | 0.261 | 0.342 | 0.308 | 0.307 | 0.254 |
| 222 | 0.586 | 0.448 | 0.414 | 0.437 | 0.423 | 0.407 | 0.429 | 0.362 | 0.370 | 0.297 | 0.386 | 0.342 | 0.302 | 0.344 | 0.241 | 0.318 | 0.286 | 0.286 | 0.234 |
| 234 | 0.561 | 0.426 | 0.393 | 0.416 | 0.399 | 0.382 | 0.402 | 0.339 | 0.348 | 0.277 | 0.362 | 0.321 | 0.282 | 0.322 | 0.223 | 0.296 | 0.266 | 0.265 | 0.216 |
| 246 | 0.542 | 0.406 | 0.375 | 0.397 | 0.379 | 0.361 | 0.380 | 0.319 | 0.328 | 0.259 | 0.342 | 0.302 | 0.263 | 0.302 | 0.206 | 0.276 | 0.247 | 0.246 | 0.200 |
| 258 | 0.530 | 0.389 | 0.358 | 0.379 | 0.361 | 0.343 | 0.363 | 0.304 | 0.312 | 0.244 | 0.326 | 0.285 | 0.247 | 0.286 | 0.191 | 0.260 | 0.229 | 0.228 | 0.184 |

## Notes

(1)-(19) Data from U.S. Treasury
ttp://www.treasury.gov/offices/domestic-finance/debt-management/interest-rate/yield_historical_main.shtml
20)-(38) Computed from (1)-(19), by interpolation of rates, compounded for number of months indicated

| Accident Year | Cumulative | Cumulative | Incremental |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age | Development | Percent | Percent |  |  |  |  |  |  |  |  | DISCO | UNT FACT |  |  |  |  |  |  |  |  |  |
| (Months) | Factor | Paid | Paid | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) | (20) | (21) | (22) |
| 12 | 4.436 | 22.5\% | 22.5\% | 22.5\% | 22.2\% | 22.0\% | 22.1\% | 22.3\% | 22.4\% | 22.4\% | 22.3\% | 21.9\% | 21.9\% | 22.0\% | 22.0\% | 22.0\% | 22.0\% | 21.8\% | 22.2\% | 22.2\% | 22.1\% | 21.8\% |
| 24 | 2.115 | 47.3\% | 24.7\% | 24.5\% | 23.6\% | 23.0\% | 23.2\% | 23.7\% | 24.2\% | 24.2\% | 23.8\% | 22.9\% | 22.6\% | 23.2\% | 22.8\% | 22.8\% | 22.9\% | 22.2\% | 23.4\% | 23.3\% | 23.2\% | 22.4\% |
| 36 | 1.468 | 68.1\% | 20.8\% | 20.4\% | 19.3\% | 18.5\% | 18.7\% | 19.3\% | 19.8\% | 19.9\% | 19.2\% | 18.4\% | 17.9\% | 18.7\% | 18.2\% | 18.0\% | 18.4\% | 17.3\% | 18.7\% | 18.5\% | 18.5\% | 17.5\% |
| 48 | 1.207 | 82.9\% | 14.7\% | 14.2\% | 13.2\% | 12.5\% | 12.7\% | 13.1\% | 13.5\% | 13.7\% | 12.9\% | 12.4\% | 11.9\% | 12.6\% | 12.1\% | 12.0\% | 12.3\% | 11.3\% | 12.5\% | 12.3\% | 12.3\% | 11.5\% |
| 60 | 1.093 | 91.5\% | 8.6\% | 8.1\% | 7.4\% | 7.0\% | 7.1\% | 7.4\% | 7.5\% | 7.7\% | 7.1\% | 6.9\% | 6.5\% | 7.0\% | 6.7\% | 6.6\% | 6.8\% | 6.1\% | 6.9\% | 6.7\% | 6.7\% | 6.2\% |
| 72 | 1.045 | 95.7\% | 4.3\% | 3.9\% | 3.5\% | 3.3\% | 3.4\% | 3.5\% | 3.6\% | 3.6\% | 3.3\% | 3.3\% | 3.0\% | 3.3\% | 3.1\% | 3.1\% | 3.2\% | 2.8\% | 3.2\% | 3.1\% | 3.1\% | 2.8\% |
| 84 | 1.022 | 97.8\% | 2.1\% | 1.9\% | 1.6\% | 1.5\% | 1.6\% | 1.6\% | 1.6\% | 1.7\% | 1.5\% | 1.5\% | 1.4\% | 1.5\% | 1.4\% | 1.4\% | 1.5\% | 1.3\% | 1.5\% | 1.4\% | 1.4\% | 1.3\% |
| 96 | 1.013 | 98.8\% | 0.9\% | 0.8\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.6\% | 0.6\% | 0.7\% | 0.6\% | 0.6\% | 0.6\% | 0.5\% | 0.6\% | 0.6\% | 0.6\% | 0.5\% |
| 108 | 1.007 | 99.3\% | 0.6\% | 0.5\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.3\% | 0.4\% | 0.4\% | 0.3\% | 0.4\% | 0.3\% | 0.4\% | 0.3\% | 0.3\% | 0.3\% |
| 120 | 1.003 | 99.7\% | 0.4\% | 0.3\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% |
| 132 | 1.002 | 99.8\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% |
| 144 | 1.001 | 99.9\% | 0.1\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 156 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 168 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 180 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 192 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 204 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 216 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 228 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 240 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 252 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 264 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| Total |  |  | 100.0\% | 97.3\% | 92.5\% | 89.4\% | 90.2\% | 92.4\% | 94.1\% | 94.8\% | 91.8\% | 88.8\% | 86.6\% | 89.8\% | 87.7\% | 87.1\% | 88.4\% | 84.1\% | 89.7\% | 88.7\% | 88.5\% | 84.5\% |
| Present Value Factor |  |  |  | 0.973 | 0.925 | 0.894 | 0.902 | 0.924 | 0.941 | 0.948 | 0.918 | 0.888 | 0.866 | 0.898 | 0.877 | 0.871 | 0.884 | 0.841 | 0.897 | 0.887 | 0.885 | 0.845 |
| Notes |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (1) From Exhibit 6 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (2) $=1 /(1)$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (3) From (2) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (4) - (22) Product of (3) and Exhibit 7, Columns (20) - (38) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

COMMERCIAL AUTO LIABILITY
INDUSTRY NET RESULTS
SECTION A

DURATION OF PAYOUT OF ACCIDENT YEAR LOSSES

| Accident Year <br> Age <br> (Months) | Cumulative <br> Paid <br> Development <br> Factor | Cumulative <br> Percent <br> Paid | Incremental <br> Percent <br> Paid | Duration |
| :---: | :---: | :---: | :---: | :---: |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
| 12 | 4.436 | $22.5 \%$ | $22.5 \%$ | 0.11 |
| 24 | 2.115 | $47.3 \%$ | $24.7 \%$ | 0.37 |
| 36 | 1.468 | $68.1 \%$ | $20.8 \%$ | 0.52 |
| 48 | 1.207 | $82.9 \%$ | $14.7 \%$ | 0.52 |
| 60 | 1.093 | $91.5 \%$ | $8.6 \%$ | 0.39 |
| 72 | 1.045 | $95.7 \%$ | $4.3 \%$ | 0.23 |
| 84 | 1.022 | $97.8 \%$ | $2.1 \%$ | 0.14 |
| 96 | 1.013 | $98.8 \%$ | $0.9 \%$ | 0.07 |
| 108 | 1.007 | $99.3 \%$ | $0.6 \%$ | 0.05 |
| 120 | 1.003 | $99.7 \%$ | $0.4 \%$ | 0.03 |
| 132 | 1.002 | $99.8 \%$ | $0.1 \%$ | 0.02 |
| 144 | 1.001 | $99.9 \%$ | $0.1 \%$ | 0.01 |
| 156 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 168 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 180 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 192 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 204 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 216 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 228 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 240 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 252 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 264 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
|  |  |  |  |  |
| Total |  |  |  |  |
|  |  |  |  |  |
| Duration (years) |  |  |  |  |

Notes
(2) From Exhibit 6
(3) $=1 /$ (2)
(4) From (2)
(5) $=(4) *[(1) / 12-0.5]$

## COMMERCIAL AUTO LIABILITY

INDUSTRY NET RESULTS
SECTION A

DEVELOPED INDUSTRY ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Net <br> Booked Ultimate Loss \& ALAE | Average Development Parameter <br> $\mu$ | Variance Development Parameter $\sigma^{2}$ | Net <br> Developed Ultimate Loss \& ALAE | Developed vs Booked Ultimate Loss \& ALAE | Paid Loss \& ALAE | Developed Unpaid Loss \& ALAE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1987 | 8,034,872 | 0.000\% | 0.000\% | 8,034,872 | - | 7,798,508 | 236,364 |
| 1988 | 8,543,928 | 0.000\% | 0.000\% | 8,543,928 | - | 8,270,462 | 273,466 |
| 1989 | 9,101,236 | 0.000\% | 0.000\% | 9,101,236 | - | 8,914,519 | 186,717 |
| 1990 | 8,818,434 | 0.000\% | 0.000\% | 8,818,434 | - | 8,673,421 | 145,013 |
| 1991 | 8,016,358 | 0.000\% | 0.000\% | 8,016,358 | - | 7,917,278 | 99,080 |
| 1992 | 7,956,577 | 0.000\% | 0.000\% | 7,956,577 | - | 7,823,914 | 132,663 |
| 1993 | 8,284,094 | 0.000\% | 0.000\% | 8,284,094 | - | 8,194,228 | 89,866 |
| 1994 | 8,904,679 | 0.000\% | 0.000\% | 8,904,679 | - | 8,813,471 | 91,208 |
| 1995 | 9,031,717 | 0.000\% | 0.000\% | 9,031,717 | - | 8,950,911 | 80,806 |
| 1996 | 9,743,683 | 0.000\% | 0.000\% | 9,743,683 | - | 9,630,426 | 113,257 |
| 1997 | 10,205,685 | 0.000\% | 0.000\% | 10,205,685 | - | 10,097,558 | 108,127 |
| 1998 | 10,418,275 | 0.000\% | 0.000\% | 10,418,275 | - | 10,300,393 | 117,882 |
| 1999 | 11,075,835 | 0.000\% | 0.000\% | 11,075,835 | - | 10,943,805 | 132,030 |
| 2000 | 11,362,381 | -0.079\% | 0.000\% | 11,353,391 | $(8,990)$ | 11,176,545 | 176,846 |
| 2001 | 10,943,423 | -0.308\% | 0.002\% | 10,909,844 | $(33,579)$ | 10,673,375 | 236,469 |
| 2002 | 10,555,623 | -0.600\% | 0.002\% | 10,492,550 | $(63,073)$ | 10,191,909 | 300,641 |
| 2003 | 10,659,927 | -0.939\% | 0.005\% | 10,560,536 | $(99,391)$ | 10,039,271 | 521,265 |
| 2004 | 10,786,513 | -1.139\% | 0.014\% | 10,665,074 | $(121,439)$ | 9,682,114 | 982,960 |
| 2005 | 11,239,808 | -0.959\% | 0.042\% | 11,134,937 | $(104,871)$ | 9,057,583 | 2,077,354 |
| 2006 | 11,419,000 | -0.409\% | 0.139\% | 11,380,317 | $(38,683)$ | 7,543,503 | 3,836,814 |
| 2007 | 11,819,461 | 0.388\% | 0.336\% | 11,885,368 | 65,907 | 5,487,654 | 6,397,714 |
| 2008 | 11,444,660 | -0.385\% | 0.656\% | 11,438,105 | $(6,555)$ | 2,553,063 | 8,885,042 |
| Total | 218,366,169 |  |  | 217,955,495 | $(410,674)$ | 192,733,911 | 25,221,584 |

Notes
(1) From Exhibit 5, Column 3
(2) From Exhibit 3, Cumulative Average
(3) From Exhibit 4, Variance
(4) $=(1) * \exp [(2)+(3) / 2]$
(5) $=(4)-(1)$
(6) From Exhibit 5, Column 4
(7) $=(4)-(6)$

|  | 12 month Booked Ultimate Loss \& ALAE Ratio | PV Factor | 1 - Exp Ratio | Loss Ratio Prior to Adjustment | Loss Ratio Adjustment | Adjusted <br> Loss Ratio | Log of Adjusted Loss Ratio | 12 Month <br> Booked <br> Ultimate <br> Loss | Latest <br> Evaluation Ultimate Loss | Ratio <br> Latest to <br> 12 Month <br> Booked | $\begin{gathered} \text { Log of } \\ \text { Ratio } \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) |
| 1987 | 72.5\% | 0.845 | 73.7\% | 59.4\% | 0.846 | 50.3\% | -68.8\% | 8,195,868 | 8,034,872 | 0.980 | -0.020 |
| 1988 | 76.7\% | 0.845 | 71.9\% | 64.5\% | 0.846 | 54.5\% | -60.6\% | 8,546,503 | 8,543,928 | 1.000 | 0.000 |
| 1989 | 80.9\% | 0.845 | 71.0\% | 68.8\% | 0.846 | 58.2\% | -54.0\% | 9,420,085 | 9,101,236 | 0.966 | -0.034 |
| 1990 | 79.8\% | 0.845 | 70.5\% | 68.3\% | 0.846 | 57.8\% | -54.8\% | 9,479,650 | 8,818,434 | 0.930 | -0.072 |
| 1991 | 79.2\% | 0.885 | 70.0\% | 71.6\% | 0.846 | 60.6\% | -50.2\% | 9,031,017 | 8,016,358 | 0.888 | -0.119 |
| 1992 | 78.0\% | 0.887 | 69.4\% | 71.2\% | 0.846 | 60.3\% | -50.6\% | 8,961,355 | 7,956,577 | 0.888 | -0.119 |
| 1993 | 77.1\% | 0.897 | 69.5\% | 71.1\% | 0.846 | 60.1\% | -50.8\% | 8,747,317 | 8,284,094 | 0.947 | -0.054 |
| 1994 | 78.3\% | 0.841 | 69.3\% | 67.8\% | 0.846 | 57.4\% | -55.5\% | 8,916,700 | 8,904,679 | 0.999 | -0.001 |
| 1995 | 78.4\% | 0.884 | 69.5\% | 71.3\% | 0.846 | 60.3\% | -50.5\% | 9,057,286 | 9,031,717 | 0.997 | -0.003 |
| 1996 | 76.7\% | 0.871 | 69.4\% | 68.8\% | 0.846 | 58.2\% | -54.1\% | 9,237,853 | 9,743,683 | 1.055 | 0.053 |
| 1997 | 77.8\% | 0.877 | 69.8\% | 69.9\% | 0.846 | 59.1\% | -52.5\% | 9,485,776 | 10,205,685 | 1.076 | 0.073 |
| 1998 | 77.0\% | 0.898 | 69.9\% | 70.8\% | 0.846 | 59.9\% | -51.3\% | 9,314,608 | 10,418,275 | 1.118 | 0.112 |
| 1999 | 78.5\% | 0.866 | 68.3\% | 71.1\% | 0.846 | 60.1\% | -50.8\% | 9,408,335 | 11,075,835 | 1.177 | 0.163 |
| 2000 | 77.4\% | 0.888 | 69.8\% | 70.3\% | 0.846 | 59.5\% | -51.9\% | 9,937,589 | 11,362,381 | 1.143 | 0.133 |
| 2001 | 73.4\% | 0.918 | 70.4\% | 68.3\% | 0.846 | 57.8\% | -54.8\% | 10,290,153 | 10,943,423 | 1.063 | 0.058 |
| 2002 | 66.6\% | 0.948 | 71.8\% | 62.9\% | 1.000 | 62.9\% | -46.4\% | 10,561,049 | 10,555,623 | 0.999 | -0.007 |
| 2003 | 63.7\% | 0.941 | 73.4\% | 58.4\% | 1.000 | 58.4\% | -53.9\% | 11,210,956 | 10,659,927 | 0.951 | -0.060 |
| 2004 | 61.6\% | 0.924 | 72.3\% | 56.2\% | 1.000 | 56.2\% | -57.7\% | 11,556,476 | 10,786,513 | 0.933 | -0.080 |
| 2005 | 60.8\% | 0.902 | 72.6\% | 54.0\% | 1.000 | 54.0\% | -61.6\% | 11,717,674 | 11,239,808 | 0.959 | -0.051 |
| 2006 | 61.6\% | 0.894 | 71.5\% | 55.0\% | 1.000 | 55.0\% | -59.8\% | 11,908,448 | 11,419,000 | 0.959 | -0.045 |
| 2007 | 62.3\% | 0.925 | 69.4\% | 59.3\% | 1.000 | 59.3\% | -52.3\% | 11,944,741 | 11,819,461 | 0.990 | -0.005 |
| 2008 | 62.3\% | 0.973 | 69.5\% | 62.3\% | 1.000 | 62.3\% | -47.3\% | 11,444,660 | 11,444,660 | 1.000 | -0.001 |
| (12) Average |  |  |  |  |  | 58.3\% | -54.1\% |  |  |  |  |
| (13) Variance |  |  |  |  |  |  | 0.261\% |  |  |  | 0.577\% |
| (14) Covariance (lo | of Adjusted Loss Ratio | og of Ratio of | est to 12 month | oked) |  |  | 0.061\% |  |  |  |  |
| (15) Total Variance | of Adjusted Loss Ratio | g) and Ratio of | atest to 12 month | ooked (log) |  |  | 0.960\% |  |  |  |  |

## Notes

(1) Exhibit 1 @ 12 Months / Exhibit 5, Column
(2) 1995-2008 from Exhibit 8, Columns 4-17; 1994 and prior selectec
(3) $=100 \%$ - Exhibit 5, Column 9
(4) $=(1) *(2)_{\text {AYXXXX }} /(2)_{\text {AY2008 }} *(3)_{\text {AY2008 }} /(3)_{\text {AYXXXX }}$
(5) Adjustment of historical loss ratios to normalize for major differences in levels across multi-year periods AY 1987-2001: AY 2002-2008 Average / AY 1987-2001 Average; 1.000 for AY 2002-2008
(6) $=(4) *(5)$
(7) $=\operatorname{LN}(6)$
(8) Exhibit 1 @ 12 Months
(9) Exhibit 1 @ 12 Current Evaluation
$(10)=(9) /(8$
(11) $=\mathrm{LN}(10)+$ Exhibit 10, Column $2+($ Exhibit 10, Column 3)/2
12) Average of Column 7
13) Variance of Column 7 and Column 11
(14) Covariance( Column 7, Column 11)
(15) = Row 13, Column 7 + Row 13, Column 7 + 2 * Row 14

DERIVATION OF INDUSTRY 2008 MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\lambda$ )

| 1 - ER | $69.5 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.106 |
| PV | 0.973 |
| Target Loss Ratio | $64.6 \%$ |
| ULR12 | $62.3 \%$ |
| $\mu$ | $-0.385 \%$ |
| $\sigma^{2}$ | $0.656 \%$ |
| $\sigma$ | $8.099 \%$ |
| D | 2.466 |
| $\lambda$ | 0.290 |
|  | $-47.3 \%$ |
| $\mu_{\text {AY ULR }}$ | $-47.7 \%$ |
| Combined $\mu$ | $0.261 \%$ |
| $\sigma^{2}{ }_{\text {AY ULR }}$ | $0.577 \%$ |
| $\sigma^{2}{ }_{12 \text {-ult }}$ | $0.061 \%$ |
| Cov(AY ULR, 12 -ult) | $0.960 \%$ |
| Combined $\sigma^{2}$ |  |
| $\lambda$ adj for pricing risk | 0.230 |
| $(2008$ market value of risk) |  |

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE $) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$

Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12 -ult)
$=\left[\ln (1-\mathrm{ER})-\ln (1+\mathrm{ULAE})-\ln (\mathrm{PV})-\mu_{\mathrm{AY} \text { ULR }}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, 2008 Accident Year

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

DERIVATION OF INDUSTRY LONG-TERM MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\lambda$ )

| 1 - ER | $69.5 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.106 |
| PV | 0.973 |
| Target Loss Ratio | $64.6 \%$ |
| ULR12 | $62.3 \%$ |
| $\mu$ | $-0.385 \%$ |
| $\sigma^{2}$ | $0.656 \%$ |
| $\sigma$ | $8.099 \%$ |
| $D$ | 2.466 |
| $\lambda$ | 0.290 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-54.1 \%$ |
| Combined $\mu$ | $-54.5 \%$ |
| $\sigma_{\text {AY ULR }}^{2}$ | $0.261 \%$ |
| $\sigma_{12 \text {-ult }}^{2}$ | $0.577 \%$ |
| Cov(AY ULR, 12 -ult) | $0.061 \%$ |
| Combined $\sigma^{2}$ | $0.960 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.671 |

(long-term market value of risk)

## Notes

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE $) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$

Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12-ult)
$=\left[\ln (1-\mathrm{ER})-\ln (1+\mathrm{ULAE})-\ln (\mathrm{PV})-\mu_{\mathrm{AY} \text { ULR }}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma \cdot \mathrm{V}(\mathrm{D})$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, Average

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

COMMERCIAL AUTO LIABILITY
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON 2008 MARKET VALUE OF RISK
Dollars in Thousands

## Simulated 1997-2008 Unpaid Claims

(1) 25th Percentile
(2) 50th Percentile
(3) 75th Percentile
(4) Average
(5) Standard Deviation
(6) Simulated Sample $\mu$
= Average[log(simulated unpaid claims)]
(7) Simulated Sample $\sigma$
= Standard Deviation[log(simulated unpaid claims)]
(8) Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}\right)$
(9) Industry Market Value of Risk $\left(\lambda_{1}\right)$
(10) Duration of Unpaid Claims (D)
(11) Risk Adjusted Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}+\lambda_{1} \cdot \sigma \cdot V D\right)$
(12) Risk Margin $=(11)-(8)$
(13) Risk Margin \% of Expected Unpaid Claims $=(11) /(8)$

| Industry | Company | Company | Company | Company | Total Largest 100 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Aggregate | A | B | C | D | Companies |
| 22,907,649 | 2,011,722 | 1,711,198 | 772,647 | 196,974 |  |
| 23,681,474 | 2,094,278 | 1,853,721 | 844,922 | 206,468 |  |
| 24,574,559 | 2,169,446 | 1,984,969 | 919,666 | 216,956 |  |
| 23,749,611 | 2,097,979 | 1,860,372 | 849,217 | 206,773 |  |
| 1,308,386 | 117,066 | 206,560 | 105,276 | 14,753 |  |
| 16.982 | 14.555 | 14.431 | 13.645 | 12.237 |  |
| 0.0546 | 0.055 | 0.110 | 0.124 | 0.071 |  |
| 23,757,283 | 2,098,698 | 1,861,442 | 850,040 | 206,870 | 21,802,469 |
| 0.230 | 0.230 | 0.230 | 0.230 | 0.230 |  |
| 1.793 | 1.785 | 1.818 | 1.846 | 1.807 |  |
| 24,159,174 | 2,134,490 | 1,925,892 | 883,459 | 211,422 | 22,521,456 |
| 401,891 | 35,792 | 64,451 | 33,419 | 4,552 | 718,987 |
| 1.7\% | 1.7\% | 3.5\% | 3.9\% | 2.2\% | 3.3\% |

COMMERCIAL AUTO LIABILITY
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands
Simulated 1997-2008 Unpaid Claims
(1) 25th Percentile
(2) 50th Percentile
(3) 75th Percentile
(4) Average
(5) Standard Deviation
(6) Simulated Sample $\mu$
= Average[log(simulated unpaid claims)]
(7) Simulated Sample $\sigma$
= Standard Deviation[log(simulated unpaid claims)]
(8) Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}\right)$
(9) Industry Market Value of Risk $\left(\lambda_{1}\right)$
(10) Duration of Unpaid Claims (D)
(11) Risk Adjusted Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}+\lambda_{1} \cdot \sigma \cdot V D\right)$
(12) Risk Margin $=(11)-(8)$
(13) Risk Margin \% of Expected Unpaid Claims $=(11) /(8)$

| Industry | Company | Company | Company | Company | Total Largest 100 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Aggregate | A | B | C | D | Companies |
| 22,907,649 | 2,011,722 | 1,711,198 | 772,647 | 196,974 |  |
| 23,681,474 | 2,094,278 | 1,853,721 | 844,922 | 206,468 |  |
| 24,574,559 | 2,169,446 | 1,984,969 | 919,666 | 216,956 |  |
| 23,749,611 | 2,097,979 | 1,860,372 | 849,217 | 206,773 |  |
| 1,308,386 | 117,066 | 206,560 | 105,276 | 14,753 |  |
| 16.982 | 14.555 | 14.431 | 13.645 | 12.237 |  |
| 0.0546 | 0.055 | 0.110 | 0.124 | 0.071 |  |
| 23,757,283 | 2,098,698 | 1,861,442 | 850,040 | 206,870 | 21,802,469 |
| 0.671 | 0.671 | 0.671 | 0.671 | 0.671 |  |
| 1.793 | 1.785 | 1.818 | 1.846 | 1.807 |  |
| 24,951,314 | 2,205,051 | 2,056,186 | 951,469 | 220,460 | 23,997,086 |
| 1,194,031 | 106,353 | 194,744 | 101,430 | 13,590 | 2,194,617 |
| 5.0\% | 5.1\% | 10.5\% | 11.9\% | 6.6\% | 10.1\% |

COMMERCIAL AUTO LIABILITY
SECTION A
INDUSTRY NET RESULTS
EXHIBIT 14
PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands

Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Total <br> Accident Years 1997-2008 | Accident <br> Year <br> 2008 | Accident <br> Year <br> 2007 | Accident <br> Year <br> 2006 | Accident <br> Year <br> 2005 | Accident <br> Year <br> 2004 | Accident <br> Year <br> 2003 | Accident <br> Year <br> 2002 | Accident <br> Year <br> 2001 | Accident <br> Year <br> 2000 | Accident <br> Year <br> 1999 | Accident <br> Year <br> 1998 | Accident <br> Year <br> 1997 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| Year 1 | 8,643,182 | 2,630,986 | 2,343,308 | 1,616,590 | 938,012 | 443,807 | 223,326 | 119,825 | 92,202 | 77,970 | 60,258 | 51,417 | 45,482 |
| Year 2 | 5,840,959 | 2,215,956 | 1,657,295 | 942,462 | 465,494 | 216,133 | 101,834 | 74,299 | 55,533 | 32,900 | 30,324 | 25,860 | 22,869 |
| Year 3 | 3,514,004 | 1,567,226 | 966,193 | 467,703 | 226,695 | 98,554 | 63,143 | 44,750 | 23,432 | 16,556 | 15,251 | 13,003 | 11,497 |
| Year 4 | 1,882,431 | 913,683 | 479,479 | 227,771 | 103,370 | 61,109 | 38,031 | 18,882 | 11,792 | 8,327 | 7,669 | 6,537 | 5,780 |
| Year 5 | 937,403 | 453,421 | 233,506 | 103,861 | 64,096 | 36,806 | 16,047 | 9,502 | 5,931 | 4,187 | 3,855 | 3,286 | 2,905 |
| Year 6 | 468,819 | 220,815 | 106,476 | 64,400 | 38,605 | 15,530 | 8,076 | 4,779 | 2,982 | 2,105 | 1,938 | 1,652 | 1,460 |
| Year 7 | 241,164 | 100,689 | 66,021 | 38,788 | 16,289 | 7,815 | 4,062 | 2,403 | 1,499 | 1,058 | 974 | 830 | 734 |
| Year 8 | 136,505 | 62,433 | 39,764 | 16,367 | 8,197 | 3,931 | 2,042 | 1,208 | 754 | 532 | 490 | 417 | 369 |
| Year 9 | 71,639 | 37,603 | 16,779 | 8,236 | 4,123 | 1,976 | 1,027 | 607 | 379 | 267 | 246 | 210 | 185 |
| Year 10 | 33,083 | 15,867 | 8,444 | 4,142 | 2,073 | 994 | 516 | 305 | 190 | 134 | 124 | 105 | 187 |
| Year 11 | 16,601 | 7,985 | 4,247 | 2,083 | 1,042 | 500 | 259 | 153 | 96 | 68 | 62 | 107 | - |
| Year 12 | 8,326 | 4,016 | 2,135 | 1,047 | 524 | 251 | 130 | 77 | 48 | 34 | 63 | - | - |
| Year 13 | 4,172 | 2,019 | 1,074 | 526 | 263 | 126 | 66 | 39 | 24 | 34 | - | - | - |
| Year 14 | 2,092 | 1,015 | 540 | 265 | 132 | 63 | 33 | 19 | 24 | - | - | - | - |
| Year 15 | 1,049 | 510 | 271 | 133 | 67 | 32 | 17 | 20 | - | - | - | - | - |
| Year 16 | 526 | 257 | 136 | 67 | 33 | 16 | 17 | - | - | - | - | - | - |
| Year 17 | 264 | 129 | 69 | 34 | 17 | 16 | - | - | - | - | - | - | - |
| Year 18 | 133 | 65 | 34 | 17 | 17 | - | - | - | - | - | - | - | - |
| Year 19 | 67 | 33 | 17 | 17 | - | - | - | - | - | - | - | - | - |
| Year 20 | 34 | 16 | 18 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 17 | 17 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total | 21,802,469 | 8,234,742 | 5,925,807 | 3,494,508 | 1,869,050 | 887,661 | 458,625 | 276,870 | 194,887 | 144,173 | 121,254 | 103,424 | 91,469 |

[^1](2) - (13) Based on expected unpaid by accident year and payout pattern from Exhibit 8

COMMERCIAL AUTO LIABILITY
SECTION A
INDUSTRY NET RESULTS
DISCOUNTED PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands

Discounted Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Discount Factor | $\begin{gathered} \text { Total } \\ \text { Accident Years } \\ \text { 1997-2008 } \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2008 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2007 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2006 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2005 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2004 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2003 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2002 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2001 \\ \hline \end{gathered}$ | Accident <br> Year <br> 2000 | Accident <br> Year <br> 1999 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1998 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1997 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| Year 1 | 0.999 | 8,631,538 | 2,627,442 | 2,340,151 | 1,614,412 | 936,748 | 443,209 | 223,025 | 119,664 | 92,078 | 77,865 | 60,177 | 51,347 | 45,421 |
| Year 2 | 0.992 | 5,791,804 | 2,197,307 | 1,643,348 | 934,531 | 461,577 | 214,314 | 100,977 | 73,673 | 55,066 | 32,623 | 30,069 | 25,642 | 22,676 |
| Year 3 | 0.978 | 3,437,871 | 1,533,271 | 945,260 | 457,570 | 221,784 | 96,419 | 61,775 | 43,780 | 22,925 | 16,198 | 14,921 | 12,721 | 11,248 |
| Year 4 | 0.961 | 1,809,365 | 878,219 | 460,869 | 218,930 | 99,358 | 58,738 | 36,555 | 18,149 | 11,334 | 8,004 | 7,371 | 6,283 | 5,555 |
| Year 5 | 0.939 | 880,065 | 425,686 | 219,223 | 97,508 | 60,175 | 34,555 | 15,066 | 8,921 | 5,568 | 3,931 | 3,619 | 3,085 | 2,728 |
| Year 6 | 0.915 | 428,928 | 202,027 | 97,416 | 58,920 | 35,320 | 14,209 | 7,388 | 4,373 | 2,728 | 1,926 | 1,773 | 1,511 | 1,336 |
| Year 7 | 0.891 | 214,897 | 89,722 | 58,830 | 34,563 | 14,515 | 6,964 | 3,619 | 2,141 | 1,336 | 943 | 868 | 740 | 654 |
| Year 8 | 0.866 | 118,243 | 54,081 | 34,445 | 14,177 | 7,101 | 3,405 | 1,769 | 1,046 | 653 | 461 | 424 | 362 | 320 |
| Year 9 | 0.841 | 60,239 | 31,619 | 14,109 | 6,926 | 3,467 | 1,662 | 863 | 511 | 319 | 225 | 207 | 176 | 156 |
| Year 10 | 0.814 | 26,937 | 12,920 | 6,875 | 3,373 | 1,688 | 809 | 420 | 249 | 155 | 109 | 101 | 86 | 153 |
| Year 11 | 0.788 | 13,088 | 6,295 | 3,348 | 1,642 | 822 | 394 | 205 | 121 | 75 | 53 | 49 | 84 | - |
| Year 12 | 0.764 | 6,360 | 3,068 | 1,631 | 800 | 400 | 192 | 100 | 59 | 37 | 26 | 48 | - | - |
| Year 13 | 0.739 | 3,082 | 1,492 | 793 | 389 | 195 | 93 | 48 | 29 | 18 | 25 | - | - | - |
| Year 14 | 0.714 | 1,493 | 725 | 385 | 189 | 94 | 45 | 24 | 14 | 17 | - | - | - | - |
| Year 15 | 0.688 | 722 | 351 | 187 | 92 | 46 | 22 | 11 | 14 | - | - | - | - | - |
| Year 16 | 0.663 | 349 | 170 | 90 | 44 | 22 | 11 | 11 | - | - | - | - | - | - |
| Year 17 | 0.637 | 168 | 82 | 44 | 21 | 11 | 10 | - | - | - | - | - | - | - |
| Year 18 | 0.612 | 81 | 40 | 21 | 10 | 10 | - | - | - | - | - | - | - | - |
| Year 19 | 0.586 | 39 | 19 | 10 | 10 | - | - | - | - | - | - | - | - | - |
| Year 20 | 0.561 | 19 | 9 | 10 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 0.542 | 9 | 9 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | 0.530 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total |  | 21,425,299 | 8,064,554 | 5,827,046 | 3,444,107 | 1,843,333 | 875,051 | 451,856 | 272,743 | 192,309 | 142,388 | 119,627 | 102,038 | 90,246 |

Notes
(1) From Exhibit 7, Column 20
(2) Sum of Columns 3-14
(3) - (14) Product of Column 1 and Exhibit 14, Columns 2-13

COMMERCIAL AUTO LIABILITY
SECTION A
INDUSTRY NET RESULTS
EXHIBIT 16
NET IMPACT OF RISK MARGINS AND DISCOUNT FOR LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands

|  | $\begin{gathered} \text { 31-Dec-08 } \\ \text { Booked } \\ \text { Unpaid } \\ \text { Loss \& ALAE } \end{gathered}$ | 31-Dec-08 <br> Expected <br> Unpaid <br> Loss \& ALAE | Average Indicated Risk Margin | Present <br> Value <br> Expected Unpaid Loss \& ALAE | Present <br> Value <br> Discount | Risk-Adjusted <br> Discounted <br> Expected Unpaid Loss \& ALAE | Net Impact of Risk Margins and Discount vs. Booked |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1997 | 91,469 | 91,469 | N/A | 90,246 | -1.3\% | N/A | N/A |
| 1998 | 103,424 | 103,424 | N/A | 102,038 | -1.3\% | N/A | N/A |
| 1999 | 121,254 | 121,254 | N/A | 119,627 | -1.3\% | N/A | N/A |
| 2000 | 149,144 | 144,173 | N/A | 142,388 | -1.2\% | N/A | N/A |
| 2001 | 208,650 | 194,887 | N/A | 192,309 | -1.3\% | N/A | N/A |
| 2002 | 297,171 | 276,870 | N/A | 272,743 | -1.5\% | N/A | N/A |
| 2003 | 527,014 | 458,625 | N/A | 451,856 | -1.5\% | N/A | N/A |
| 2004 | 992,002 | 887,661 | N/A | 875,051 | -1.4\% | N/A | N/A |
| 2005 | 1,979,038 | 1,869,050 | N/A | 1,843,333 | -1.4\% | N/A | N/A |
| 2006 | 3,581,827 | 3,494,508 | N/A | 3,444,107 | -1.4\% | N/A | N/A |
| 2007 | 5,893,242 | 5,925,807 | N/A | 5,827,046 | -1.7\% | N/A | N/A |
| 2008 | 8,242,349 | 8,234,742 | N/A | 8,064,554 | -2.1\% | N/A | N/A |
| Total 1997-2008 | 22,186,584 | 21,802,469 | 10.1\% | 21,425,299 | -1.7\% | 23,581,950 | 6.3\% |

Notes
(3) From Exhibit 13B, Row 13, Total Largest 100 U.S. Insurers
(4) From Exhibit 15, Total by Accident Year
(5) $=(4) /(2)-1$
(6) $=(2)$ Total $*[1+(3)$ Total $]$ [ $1+(5)$ Total $]$
(7) $=$ (6) Total $/$ (1) Total -1

COMMERCIAL MULTIPLE PERIL
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Months of Maturity |  |  |  |  |  |  |  |  |  | Latest |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12 | $\underline{24}$ | 36 | 48 | $\underline{60}$ | 72 | 84 | $\underline{96}$ | 108 | 120 | Evaluation |
| 1987 | 8,277,207 | 7,966,088 | 7,955,398 | 7,950,411 | 7,954,522 | 7,952,914 | 7,934,667 | 7,922,340 | 7,893,492 | 7,935,340 | 7,935,340 |
| 1988 | 9,170,947 | 8,816,998 | 8,840,651 | 8,881,708 | 8,878,454 | 8,893,565 | 8,864,653 | 8,804,488 | 8,842,985 | 8,842,450 | 8,842,450 |
| 1989 | 10,830,290 | 10,951,877 | 10,978,664 | 11,003,974 | 11,013,922 | 10,986,587 | 10,932,566 | 10,962,659 | 10,956,062 | 10,950,486 | 10,950,486 |
| 1990 | 11,042,654 | 10,942,906 | 10,978,026 | 10,963,756 | 10,922,899 | 10,807,135 | 10,786,184 | 10,749,109 | 10,727,156 | 10,715,386 | 10,715,386 |
| 1991 | 11,224,333 | 11,045,534 | 11,006,969 | 10,903,018 | 10,823,456 | 10,722,686 | 10,701,751 | 10,681,624 | 10,644,493 | 10,654,254 | 10,654,254 |
| 1992 | 13,195,825 | 13,061,701 | 12,976,357 | 12,956,151 | 12,876,174 | 12,825,097 | 12,816,166 | 12,813,238 | 12,779,024 | 12,803,656 | 12,803,656 |
| 1993 | 11,859,305 | 11,649,773 | 11,687,180 | 11,662,260 | 11,602,493 | 11,599,115 | 11,562,504 | 11,517,046 | 11,551,976 | 11,605,537 | 11,605,537 |
| 1994 | 13,033,952 | 13,038,143 | 13,060,351 | 13,146,901 | 13,144,914 | 13,227,673 | 13,132,537 | 13,161,275 | 13,219,929 | 13,318,381 | 13,318,381 |
| 1995 | 12,388,985 | 12,281,447 | 12,183,409 | 12,259,760 | 12,229,157 | 12,247,747 | 12,239,631 | 12,322,719 | 12,439,427 | 12,477,097 | 12,477,097 |
| 1996 | 13,439,227 | 13,487,621 | 13,611,916 | 13,608,753 | 13,659,735 | 13,663,365 | 13,711,531 | 13,850,156 | 13,914,964 | 13,915,552 | 13,915,552 |
| 1997 | 12,491,912 | 12,440,590 | 12,397,181 | 12,484,893 | 12,537,096 | 12,578,605 | 12,760,841 | 12,841,478 | 12,844,775 | 12,898,050 | 12,898,050 |
| 1998 | 13,523,977 | 13,659,337 | 13,818,464 | 14,070,552 | 14,173,893 | 14,414,330 | 14,625,848 | 14,665,238 | 14,695,169 | 14,716,147 | 14,716,147 |
| 1999 | 13,769,366 | 13,971,979 | 14,155,966 | 14,509,802 | 14,867,336 | 15,042,732 | 15,053,224 | 15,165,656 | 15,130,562 | 15,128,644 | 15,128,644 |
| 2000 | 13,628,215 | 13,956,176 | 14,559,989 | 14,929,935 | 15,230,576 | 15,347,279 | 15,329,530 | 15,388,151 | 15,399,096 |  | 15,399,096 |
| 2001 | 15,615,731 | 15,552,860 | 15,700,111 | 15,943,122 | 15,779,052 | 15,900,765 | 15,992,656 | 15,992,975 |  |  | 15,992,975 |
| 2002 | 14,137,617 | 13,474,713 | 13,704,491 | 13,792,532 | 13,760,812 | 13,758,620 | 13,711,005 |  |  |  | 13,711,005 |
| 2003 | 14,751,482 | 14,005,959 | 13,806,266 | 13,776,230 | 13,664,366 | 13,590,079 |  |  |  |  | 13,590,079 |
| 2004 | 16,675,054 | 15,817,215 | 15,688,563 | 15,393,921 | 15,090,905 |  |  |  |  |  | 15,090,905 |
| 2005 | 17,761,767 | 17,510,282 | 17,080,086 | 16,643,679 |  |  |  |  |  |  | 16,643,679 |
| 2006 | 16,299,833 | 15,774,766 | 15,264,573 |  |  |  |  |  |  |  | 15,264,573 |
| 2007 | 17,306,437 | 16,828,126 |  |  |  |  |  |  |  |  | 16,828,126 |
| 2008 | 21,309,040 |  |  |  |  |  |  |  |  |  | 21,309,040 |

## Notes

Data from SNL Financial LC
1996-2008 Annual Statements
Industry Total Commercial Multiple Peril
Schedule P, Part 2E

COMMERCIAL MULTIPLE PERIL
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | 0.962 | 0.999 | 0.999 | 1.001 | 1.000 | 0.998 | 0.998 | 0.996 | 1.005 |
| 1988 | 0.961 | 1.003 | 1.005 | 1.000 | 1.002 | 0.997 | 0.993 | 1.004 | 1.000 |
| 1989 | 1.011 | 1.002 | 1.002 | 1.001 | 0.998 | 0.995 | 1.003 | 0.999 | 0.999 |
| 1990 | 0.991 | 1.003 | 0.999 | 0.996 | 0.989 | 0.998 | 0.997 | 0.998 | 0.999 |
| 1991 | 0.984 | 0.997 | 0.991 | 0.993 | 0.991 | 0.998 | 0.998 | 0.997 | 1.001 |
| 1992 | 0.990 | 0.993 | 0.998 | 0.994 | 0.996 | 0.999 | 1.000 | 0.997 | 1.002 |
| 1993 | 0.982 | 1.003 | 0.998 | 0.995 | 1.000 | 0.997 | 0.996 | 1.003 | 1.005 |
| 1994 | 1.000 | 1.002 | 1.007 | 1.000 | 1.006 | 0.993 | 1.002 | 1.004 | 1.007 |
| 1995 | 0.991 | 0.992 | 1.006 | 0.998 | 1.002 | 0.999 | 1.007 | 1.009 | 1.003 |
| 1996 | 1.004 | 1.009 | 1.000 | 1.004 | 1.000 | 1.004 | 1.010 | 1.005 | 1.000 |
| 1997 | 0.996 | 0.997 | 1.007 | 1.004 | 1.003 | 1.014 | 1.006 | 1.000 | 1.004 |
| 1998 | 1.010 | 1.012 | 1.018 | 1.007 | 1.017 | 1.015 | 1.003 | 1.002 | 1.001 |
| 1999 | 1.015 | 1.013 | 1.025 | 1.025 | 1.012 | 1.001 | 1.007 | 0.998 | 1.000 |
| 2000 | 1.024 | 1.043 | 1.025 | 1.020 | 1.008 | 0.999 | 1.004 | 1.001 |  |
| 2001 | 0.996 | 1.009 | 1.015 | 0.990 | 1.008 | 1.006 | 1.000 |  |  |
| 2002 | 0.953 | 1.017 | 1.006 | 0.998 | 1.000 | 0.997 |  |  |  |
| 2003 | 0.949 | 0.986 | 0.998 | 0.992 | 0.995 |  |  |  |  |
| 2004 | 0.949 | 0.992 | 0.981 | 0.980 |  |  |  |  |  |
| 2005 | 0.986 | 0.975 | 0.974 |  |  |  |  |  |  |
| 2006 | 0.968 | 0.968 |  |  |  |  |  |  |  |
| 2007 | 0.972 |  |  |  |  |  |  |  |  |

From Exhibit 1, ratio of successive ultimate loss estimates by accident year

COMMERCIAL MULTIPLE PERIL
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
CUMULATIVE DEVELOPMENT IN ULTIMATE LOSS ESTIMATES BASED ON LOG OF LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | -3.831\% | -0.134\% | -0.063\% | 0.052\% | -0.020\% | -0.230\% | -0.155\% | -0.365\% | 0.529\% |
| 1988 | -3.936\% | 0.268\% | 0.463\% | -0.037\% | 0.170\% | -0.326\% | -0.681\% | 0.436\% | -0.006\% |
| 1989 | 1.116\% | 0.244\% | 0.230\% | 0.090\% | -0.248\% | -0.493\% | 0.275\% | -0.060\% | -0.051\% |
| 1990 | -0.907\% | 0.320\% | -0.130\% | -0.373\% | -1.065\% | -0.194\% | -0.344\% | -0.204\% | -0.110\% |
| 1991 | -1.606\% | -0.350\% | -0.949\% | -0.732\% | -0.935\% | -0.195\% | -0.188\% | -0.348\% | 0.092\% |
| 1992 | -1.022\% | -0.656\% | -0.156\% | -0.619\% | -0.397\% | -0.070\% | -0.023\% | -0.267\% | 0.193\% |
| 1993 | -1.783\% | 0.321\% | -0.213\% | -0.514\% | -0.029\% | -0.316\% | -0.394\% | 0.303\% | 0.463\% |
| 1994 | 0.032\% | 0.170\% | 0.661\% | -0.015\% | 0.628\% | -0.722\% | 0.219\% | 0.445\% | 0.742\% |
| 1995 | -0.872\% | -0.801\% | 0.625\% | -0.250\% | 0.152\% | -0.066\% | 0.677\% | 0.943\% | 0.302\% |
| 1996 | 0.359\% | 0.917\% | -0.023\% | 0.374\% | 0.027\% | 0.352\% | 1.006\% | 0.467\% | 0.004\% |
| 1997 | -0.412\% | -0.350\% | 0.705\% | 0.417\% | 0.331\% | 1.438\% | 0.630\% | 0.026\% | 0.414\% |
| 1998 | 0.996\% | 1.158\% | 1.808\% | 0.732\% | 1.682\% | 1.457\% | 0.269\% | 0.204\% | 0.143\% |
| 1999 | 1.461\% | 1.308\% | 2.469\% | 2.434\% | 1.173\% | 0.070\% | 0.744\% | -0.232\% | -0.013\% |
| 2000 | 2.378\% | 4.236\% | 2.509\% | 1.994\% | 0.763\% | -0.116\% | 0.382\% | 0.071\% |  |
| 2001 | -0.403\% | 0.942\% | 1.536\% | -1.034\% | 0.768\% | 0.576\% | 0.002\% |  |  |
| 2002 | -4.802\% | 1.691\% | 0.640\% | -0.230\% | -0.016\% | -0.347\% |  |  |  |
| 2003 | -5.186\% | -1.436\% | -0.218\% | -0.815\% | -0.545\% |  |  |  |  |
| 2004 | -5.281\% | -0.817\% | -1.896\% | -1.988\% |  |  |  |  |  |
| 2005 | -1.426\% | -2.488\% | -2.588\% |  |  |  |  |  |  |
| 2006 | -3.274\% | -3.288\% |  |  |  |  |  |  |  |
| 2007 | -2.803\% |  |  |  |  |  |  |  |  |
| Average | -1.486\% | 0.063\% | 0.285\% | -0.029\% | 0.143\% | 0.051\% | 0.161\% | 0.101\% | 0.208\% |
|  | 12-108 | 24-108 | 36-108 | 48-108 | 60-108 | 72-108 | 84-108 | 96-108 | 108-108 |
| Cumulative Average | -0.502\% | 0.984\% | 0.921\% | 0.636\% | 0.665\% | 0.521\% | 0.470\% | 0.309\% | 0.208\% |

From Exhibit 2, natural log of ratio of successive ultimate loss estimates by accident year

COMMERCIAL MULTIPLE PERIL
SECTION B
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE

## VARIANCE-COVARIANCE MATRIX OF LOG OF INCREMENTAL LINK RATIOS

| Months of Maturity | 12-108 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 | 120-Ultimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12-108 | 0.048\% | 0.017\% | 0.016\% | 0.015\% | 0.007\% | 0.004\% | 0.005\% | 0.000\% | -0.001\% | 0.000\% |
| 24-36 | 0.017\% | 0.023\% | 0.013\% | 0.008\% | 0.004\% | 0.000\% | 0.001\% | 0.000\% | -0.001\% | 0.000\% |
| 36-48 | 0.016\% | 0.013\% | 0.016\% | 0.009\% | 0.006\% | 0.002\% | 0.002\% | 0.000\% | 0.000\% | 0.000\% |
| 48-60 | 0.015\% | 0.008\% | 0.009\% | 0.010\% | 0.004\% | 0.001\% | 0.002\% | 0.000\% | 0.000\% | 0.000\% |
| 60-72 | 0.007\% | 0.004\% | 0.006\% | 0.004\% | 0.005\% | 0.002\% | 0.001\% | 0.001\% | 0.000\% | 0.000\% |
| 72-84 | 0.004\% | 0.000\% | 0.002\% | 0.001\% | 0.002\% | 0.004\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% |
| 84-96 | 0.005\% | 0.001\% | 0.002\% | 0.002\% | 0.001\% | 0.001\% | 0.002\% | 0.000\% | 0.000\% | 0.000\% |
| 96-108 | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.001\% | 0.000\% | 0.000\% | 0.001\% | 0.000\% | 0.000\% |
| 108-120 | -0.001\% | -0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.001\% | 0.000\% |
| 120-Ultimate | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| Variance ( $\mathbf{\sigma}^{\mathbf{2}}$ ) | 0.352\% | 0.177\% | 0.100\% | 0.047\% | 0.025\% | 0.011\% | 0.005\% | 0.002\% | 0.001\% | 0.000\% |

Notes
From Exhibit 3, covariance of errors at given maturity with errors at all other maturities
Covariances above diagonal are symmetric with those below
Variance is sum of matrix for all maturities greater than or equal to maturity shown in column
selection of loss \& alae ratio, ulae factor, and loss \& lae ratio
Dollars in Thousands

|  | Net <br> Earned Premium | Net Ultimate Loss \& LAE | Net <br> Ultimate Loss \& ALAE | $\begin{gathered} \text { Net } \\ \text { Paid } \\ \text { Loss \& ALAE } \\ \hline \end{gathered}$ | Net <br> Unpaid Loss \& ALAE | Net Ultimate Loss \& LAE Ratio | Net <br> Ultimate Loss \& ALAE Ratio | ULAE <br> Factor | Underwriting <br> Expense Ratio |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) |
| 1987 | 16,409,943 | 8,420,937 | 7,935,340 | 7,640,931 | 294,409 | 51.3\% | 48.4\% | 1.061 | 34.1\% | 65.9\% |
| 1988 | 16,923,216 | 9,392,633 | 8,842,450 | 8,514,284 | 328,166 | 55.5\% | 52.3\% | 1.062 | 35.8\% | 64.2\% |
| 1989 | 16,827,295 | 11,586,017 | 10,950,486 | 10,574,151 | 376,335 | 68.9\% | 65.1\% | 1.058 | 36.7\% | 63.3\% |
| 1990 | 17,034,141 | 11,372,467 | 10,715,386 | 10,361,568 | 353,818 | 66.8\% | 62.9\% | 1.061 | 36.5\% | 63.5\% |
| 1991 | 16,515,610 | 11,357,259 | 10,654,254 | 10,297,937 | 356,317 | 68.8\% | 64.5\% | 1.066 | 37.6\% | 62.4\% |
| 1992 | 16,070,527 | 13,682,164 | 12,803,656 | 12,491,828 | 311,828 | 85.1\% | 79.7\% | 1.069 | 37.3\% | 62.7\% |
| 1993 | 16,273,849 | 12,422,779 | 11,605,537 | 11,235,210 | 370,327 | 76.3\% | 71.3\% | 1.070 | 36.5\% | 63.5\% |
| 1994 | 16,710,429 | 14,211,317 | 13,318,381 | 12,896,222 | 422,159 | 85.0\% | 79.7\% | 1.067 | 36.4\% | 63.6\% |
| 1995 | 17,558,782 | 13,447,154 | 12,477,097 | 12,082,205 | 394,892 | 76.6\% | 71.1\% | 1.078 | 35.7\% | 64.3\% |
| 1996 | 18,091,013 | 14,998,085 | 13,915,552 | 13,482,635 | 432,917 | 82.9\% | 76.9\% | 1.078 | 35.9\% | 64.1\% |
| 1997 | 18,371,092 | 14,028,079 | 12,898,050 | 12,422,696 | 475,354 | 76.4\% | 70.2\% | 1.088 | 36.5\% | 63.5\% |
| 1998 | 18,322,956 | 16,086,971 | 14,716,147 | 14,206,482 | 509,665 | 87.8\% | 80.3\% | 1.093 | 36.4\% | 63.6\% |
| 1999 | 18,699,440 | 16,434,336 | 15,128,644 | 14,593,734 | 534,910 | 87.9\% | 80.9\% | 1.086 | 36.7\% | 63.3\% |
| 2000 | 19,125,249 | 16,690,877 | 15,399,096 | 14,723,792 | 675,304 | 87.3\% | 80.5\% | 1.084 | 35.2\% | 64.8\% |
| 2001 | 20,904,316 | 17,439,196 | 15,992,975 | 15,193,486 | 799,489 | 83.4\% | 76.5\% | 1.090 | 33.1\% | 66.9\% |
| 2002 | 23,449,876 | 14,975,652 | 13,711,005 | 12,711,446 | 999,559 | 63.9\% | 58.5\% | 1.092 | 32.9\% | 67.1\% |
| 2003 | 26,301,855 | 14,918,540 | 13,590,079 | 12,255,864 | 1,334,215 | 56.7\% | 51.7\% | 1.098 | 32.7\% | 67.3\% |
| 2004 | 28,383,051 | 16,530,949 | 15,090,905 | 13,264,033 | 1,826,872 | 58.2\% | 53.2\% | 1.095 | 32.9\% | 67.1\% |
| 2005 | 28,945,274 | 18,244,278 | 16,643,679 | 13,524,309 | 3,119,370 | 63.0\% | 57.5\% | 1.096 | 33.0\% | 67.0\% |
| 2006 | 30,895,464 | 16,772,299 | 15,264,573 | 10,468,406 | 4,796,167 | 54.3\% | 49.4\% | 1.099 | 33.9\% | 66.1\% |
| 2007 | 31,551,713 | 18,398,731 | 16,828,126 | 9,851,336 | 6,976,790 | 58.3\% | 53.3\% | 1.093 | 35.4\% | 64.6\% |
| 2008 | 30,825,227 | 23,172,939 | 21,309,040 | 8,553,203 | 12,755,837 | 75.2\% | 69.1\% | 1.087 | 34.7\% | 65.3\% |
| Selected |  |  |  |  | 38,444,700 |  | 69.1\% | 1.096 |  | 65.3\% |

Notes
(1), (2) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1E
(3) Exhibit 1, Latest Evaluation
(4) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1E
(5) $=(3)-(4)$
(6) $=(2) /(1)$
$(7)=(3) /(1)$; Selected from 2008
(8) $=(6) /(7)$; Selected from 2005-2007 Average
(9) From AM Best Aggregates and Averages, includes policyholder dividends
(10) $=1$ - (9); Selected from 2008

COMMERCIAL MULTIPLE PERIL
INDUSTRY PAYOUT PATTERN (PAID LOSS \& ALAE)
Dollars in Thousands

| Months of Maturity |  |  | 36 | 48 | $\underline{60}$ | 72 | 84 | $\underline{96}$ | 108 | 120 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12 | 24 |  |  |  |  |  |  |  |  |
| 1987 | 2,494,978 | 4,290,176 | 5,197,518 | 5,973,622 | 6,589,871 | 7,016,429 | 7,287,059 | 7,458,807 | 7,563,284 | 7,640,931 |
| 1988 | 2,943,493 | 4,879,269 | 5,901,903 | 6,746,263 | 7,385,911 | 7,834,460 | 8,154,885 | 8,335,295 | 8,446,706 | 8,514,284 |
| 1989 | 3,614,761 | 6,421,141 | 7,603,112 | 8,579,066 | 9,307,370 | 9,803,762 | 10,151,943 | 10,366,266 | 10,476,119 | 10,574,151 |
| 1990 | 4,102,163 | 5,990,842 | 7,217,096 | 8,257,259 | 9,011,159 | 9,538,637 | 9,890,261 | 10,100,301 | 10,228,847 | 10,361,568 |
| 1991 | 3,935,305 | 6,013,629 | 7,268,247 | 8,319,251 | 9,040,993 | 9,528,242 | 9,845,680 | 10,057,435 | 10,200,199 | 10,297,937 |
| 1992 | 4,949,919 | 7,918,499 | 9,305,971 | 10,401,238 | 11,166,620 | 11,646,319 | 11,999,589 | 12,217,028 | 12,368,013 | 12,491,828 |
| 1993 | 4,043,394 | 6,610,710 | 8,015,057 | 9,096,561 | 9,879,357 | 10,387,363 | 10,714,538 | 10,920,173 | 11,103,079 | 11,235,210 |
| 1994 | 4,908,047 | 7,860,072 | 9,482,885 | 10,746,234 | 11,374,283 | 11,959,814 | 12,331,058 | 12,571,504 | 12,768,418 | 12,896,222 |
| 1995 | 4,427,743 | 7,170,671 | 8,626,682 | 9,782,412 | 10,547,571 | 11,150,901 | 11,533,886 | 11,781,313 | 11,945,778 | 12,082,205 |
| 1996 | 5,215,826 | 8,359,044 | 9,814,405 | 11,086,306 | 11,930,321 | 12,590,957 | 12,990,855 | 13,194,499 | 13,385,407 | 13,482,635 |
| 1997 | 4,525,879 | 7,240,188 | 8,708,830 | 9,994,201 | 10,939,689 | 11,543,345 | 11,875,463 | 12,132,509 | 12,293,297 | 12,422,696 |
| 1998 | 5,383,265 | 8,572,830 | 10,267,432 | 11,494,768 | 12,505,288 | 13,162,617 | 13,620,149 | 13,873,593 | 14,068,363 | 14,206,482 |
| 1999 | 5,650,566 | 9,006,646 | 10,767,906 | 12,187,259 | 13,089,107 | 13,693,876 | 13,998,073 | 14,267,636 | 14,467,661 | 14,593,734 |
| 2000 | 5,562,885 | 9,096,042 | 10,956,951 | 12,352,732 | 13,422,483 | 13,812,295 | 14,252,312 | 14,527,532 | 14,723,792 |  |
| 2001 | 6,137,525 | 9,467,177 | 11,455,361 | 12,975,959 | 13,740,021 | 14,471,400 | 14,899,288 | 15,193,486 |  |  |
| 2002 | 4,829,016 | 7,843,613 | 9,501,275 | 10,777,738 | 11,716,263 | 12,331,548 | 12,711,446 |  |  |  |
| 2003 | 5,082,670 | 7,989,483 | 9,373,040 | 10,691,325 | 11,624,205 | 12,255,864 |  |  |  |  |
| 2004 | 5,873,536 | 9,407,503 | 10,963,767 | 12,283,675 | 13,264,033 |  |  |  |  |  |
| 2005 | 5,651,168 | 10,513,108 | 12,041,288 | 13,524,309 |  |  |  |  |  |  |
| 2006 | 5,508,085 | 8,892,225 | 10,468,406 |  |  |  |  |  |  |  |
| 2007 | 6,236,478 | 9,851,336 |  |  |  |  |  |  |  |  |
| 2008 | 8,553,203 |  |  |  |  |  |  |  |  |  |
|  |  |  |  | Age-to-Age | Paid Loss Dev | elopment |  |  |  |  |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |  |
| 1987 | 1.720 | 1.211 | 1.149 | 1.103 | 1.065 | 1.039 | 1.024 | 1.014 | 1.010 |  |
| 1988 | 1.658 | 1.210 | 1.143 | 1.095 | 1.061 | 1.041 | 1.022 | 1.013 | 1.008 |  |
| 1989 | 1.776 | 1.184 | 1.128 | 1.085 | 1.053 | 1.036 | 1.021 | 1.011 | 1.009 |  |
| 1990 | 1.460 | 1.205 | 1.144 | 1.091 | 1.059 | 1.037 | 1.021 | 1.013 | 1.013 |  |
| 1991 | 1.528 | 1.209 | 1.145 | 1.087 | 1.054 | 1.033 | 1.022 | 1.014 | 1.010 |  |
| 1992 | 1.600 | 1.175 | 1.118 | 1.074 | 1.043 | 1.030 | 1.018 | 1.012 | 1.010 |  |
| 1993 | 1.635 | 1.212 | 1.135 | 1.086 | 1.051 | 1.031 | 1.019 | 1.017 | 1.012 |  |
| 1994 | 1.601 | 1.206 | 1.133 | 1.058 | 1.051 | 1.031 | 1.019 | 1.016 | 1.010 |  |
| 1995 | 1.619 | 1.203 | 1.134 | 1.078 | 1.057 | 1.034 | 1.021 | 1.014 | 1.011 |  |
| 1996 | 1.603 | 1.174 | 1.130 | 1.076 | 1.055 | 1.032 | 1.016 | 1.014 | 1.007 |  |
| 1997 | 1.600 | 1.203 | 1.148 | 1.095 | 1.055 | 1.029 | 1.022 | 1.013 | 1.011 |  |
| 1998 | 1.592 | 1.198 | 1.120 | 1.088 | 1.053 | 1.035 | 1.019 | 1.014 | 1.010 |  |
| 1999 | 1.594 | 1.196 | 1.132 | 1.074 | 1.046 | 1.022 | 1.019 | 1.014 | 1.009 |  |
| 2000 | 1.635 | 1.205 | 1.127 | 1.087 | 1.029 | 1.032 | 1.019 | 1.014 |  |  |
| 2001 | 1.543 | 1.210 | 1.133 | 1.059 | 1.053 | 1.030 | 1.020 |  |  |  |
| 2002 | 1.624 | 1.211 | 1.134 | 1.087 | 1.053 | 1.031 |  |  |  |  |
| 2003 | 1.572 | 1.173 | 1.141 | 1.087 | 1.054 |  |  |  |  |  |
| 2004 | 1.602 | 1.165 | 1.120 | 1.080 |  |  |  |  |  |  |
| 2005 | 1.860 | 1.145 | 1.123 |  |  |  |  |  |  |  |
| 2006 | 1.614 | 1.177 |  |  |  |  |  |  |  |  |
| 2007 | 1.580 |  |  |  |  |  |  |  |  |  |
| Averages |  |  |  |  |  |  |  |  |  |  |
| $10-\mathrm{Yr}$ Weighted | 1.621 | 1.187 | 1.130 | 1.081 | 1.050 | 1.031 | 1.019 | 1.014 | 1.010 |  |
| 10-Yr Straight | 1.622 | 1.188 | 1.131 | 1.081 | 1.051 | 1.031 | 1.019 | 1.014 | 1.010 |  |
| Selected | 1.621 | 1.187 | 1.130 | 1.081 | 1.050 | 1.031 | 1.019 | 1.014 | 1.010 |  |


| Fitted Age-to-Ultimate |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Curve Fits: | R-squared | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| Weibull | 99.1\% | 1.025 | 1.018 | 1.013 | 1.010 | 1.007 | 1.005 | 1.004 | 1.003 | 1.002 | 1.002 | 1.001 | 1.001 | 1.001 |
| Power Curve | 98.0\% | 1.014 | 1.009 | 1.006 | 1.004 | 1.002 | 1.001 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Inverse Power Curve | 97.3\% | 1.096 | 1.084 | 1.074 | 1.066 | 1.059 | 1.052 | 1.047 | 1.042 | 1.038 | 1.034 | 1.030 | 1.027 | 1.024 |


| Selected Pattern | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age-to-Age | 1.621 | 1.187 | 1.130 | 1.081 | 1.050 | 1.031 | 1.019 | 1.014 | 1.010 | 1.005 | 1.003 | 1.002 | 1.001 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |  |
| Age-to-Ultimate | 2.694 | 1.662 | 1.400 | 1.239 | 1.146 | 1.091 | 1.059 | 1.039 | 1.025 | 1.014 | 1.009 | 1.006 | 1.004 | 1.002 | 1.001 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.00 |
| Cumulative \% Paid | 37.1\% | 60.2\% | 71.4\% | 80.7\% | 87.2\% | 91.6\% | 94.4\% | 96.2\% | 97.6\% | 98.6\% | 99.1\% | 99.4\% | 99.6\% | 99.8\% | 99.9\% | 99.9\% | 99.9\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% |
| Incremental \% Paid | 37.1\% | 23.1\% | 11.3\% | 9.3\% | 6.5\% | 4.4\% | 2.8\% | 1.8\% | 1.4\% | 1.0\% | 0.5\% | 0.3\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |

[^2]|  | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Duration | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) |
| 1 month | 0.11\% | 2.76\% | 4.75\% | 4.01\% | 1.89\% | 0.90\% | 1.20\% | 1.68\% | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |
| 3 months | 0.11\% | 3.36\% | 5.02\% | 4.08\% | 2.22\% | 0.95\% | 1.22\% | 1.74\% | 5.89\% | 5.33\% | 4.48\% | 5.36\% | 5.21\% | 5.10\% | 5.68\% | 3.07\% | 3.15\% | 3.96\% | 6.63\% |
| 6 months | 0.27\% | 3.49\% | 5.09\% | 4.37\% | 2.59\% | 1.02\% | 1.23\% | 1.83\% | 5.70\% | 5.74\% | 4.55\% | 5.45\% | 5.33\% | 5.17\% | 6.51\% | 3.30\% | 3.38\% | 4.00\% | 6.73\% |
| 1 year | 0.37\% | 3.34\% | 5.00\% | 4.38\% | 2.75\% | 1.26\% | 1.32\% | 2.17\% | 5.32\% | 5.98\% | 4.53\% | 5.51\% | 5.51\% | 5.18\% | 7.20\% | 3.63\% | 3.61\% | 4.12\% | 6.82\% |
| 2 years | 0.76\% | 3.05\% | 4.82\% | 4.41\% | 3.08\% | 1.84\% | 1.61\% | 3.07\% | 5.11\% | 6.24\% | 4.54\% | 5.66\% | 5.88\% | 5.18\% | 7.69\% | 4.25\% | 4.56\% | 4.77\% | 7.15\% |
| 3 years | 1.00\% | 3.07\% | 4.74\% | 4.37\% | 3.25\% | 2.37\% | 1.99\% | 3.59\% | 5.06\% | 6.29\% | 4.55\% | 5.68\% | 6.04\% | 5.25\% | 7.80\% | 4.58\% | 5.12\% | 5.11\% | 7.40\% |
| 5 years | 1.55\% | 3.45\% | 4.70\% | 4.35\% | 3.63\% | 3.25\% | 2.78\% | 4.38\% | 4.99\% | 6.36\% | 4.56\% | 5.71\% | 6.21\% | 5.38\% | 7.83\% | 5.21\% | 6.04\% | 5.93\% | 7.68\% |
| 7 years | 1.87\% | 3.70\% | 4.70\% | 4.36\% | 3.94\% | 3.77\% | 3.36\% | 4.84\% | 5.16\% | 6.55\% | 4.73\% | 5.77\% | 6.34\% | 5.49\% | 7.84\% | 5.53\% | 6.43\% | 6.38\% | 8.00\% |
| 10 years | 2.25\% | 4.04\% | 4.71\% | 4.39\% | 4.24\% | 4.27\% | 3.83\% | 5.07\% | 5.12\% | 6.45\% | 4.65\% | 5.75\% | 6.43\% | 5.58\% | 7.84\% | 5.83\% | 6.70\% | 6.71\% | 8.08\% |
| 20 years | 3.05\% | 4.50\% | 4.91\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.74\% | 5.59\% | 6.83\% | 5.39\% | 6.02\% | 6.73\% | 6.01\% | 8.02\% | 6.48\% | 7.05\% | 7.06\% | 8.17\% |
| 30 years | 2.69\% | 4.45\% | 4.81\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.48\% | 5.46\% | 6.48\% | 5.09\% | 5.93\% | 6.65\% | 5.96\% | 7.89\% | 6.35\% | 7.40\% | 7.41\% | 8.26\% |


| Discount Factor | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (months) | (20) | (21) | (22) | (23) | (24) | (25) | (26) | (27) | (28) | (29) | (30) | (31) | (32) | (33) | (34) | (35) | (36) | (37) | (38) |
| 6 | 0.999 | 0.983 | 0.975 | 0.979 | 0.987 | 0.995 | 0.994 | 0.991 | 0.973 | 0.972 | 0.978 | 0.974 | 0.974 | 0.975 | 0.969 | 0.984 | 0.984 | 0.981 | 0.968 |
| 18 | 0.992 | 0.954 | 0.931 | 0.938 | 0.958 | 0.977 | 0.978 | 0.962 | 0.927 | 0.915 | 0.936 | 0.922 | 0.920 | 0.927 | 0.898 | 0.944 | 0.942 | 0.937 | 0.904 |
| 30 | 0.978 | 0.927 | 0.890 | 0.898 | 0.925 | 0.949 | 0.956 | 0.921 | 0.883 | 0.859 | 0.895 | 0.871 | 0.865 | 0.881 | 0.830 | 0.898 | 0.889 | 0.886 | 0.839 |
| 42 | 0.961 | 0.897 | 0.851 | 0.861 | 0.891 | 0.914 | 0.927 | 0.878 | 0.842 | 0.807 | 0.856 | 0.824 | 0.813 | 0.835 | 0.769 | 0.850 | 0.833 | 0.834 | 0.777 |
| 54 | 0.939 | 0.862 | 0.813 | 0.825 | 0.855 | 0.874 | 0.892 | 0.832 | 0.803 | 0.758 | 0.818 | 0.779 | 0.764 | 0.791 | 0.713 | 0.801 | 0.776 | 0.778 | 0.719 |
| 66 | 0.915 | 0.827 | 0.777 | 0.791 | 0.819 | 0.833 | 0.853 | 0.785 | 0.763 | 0.711 | 0.781 | 0.736 | 0.717 | 0.749 | 0.661 | 0.753 | 0.721 | 0.724 | 0.663 |
| 78 | 0.891 | 0.793 | 0.742 | 0.758 | 0.782 | 0.793 | 0.814 | 0.741 | 0.723 | 0.664 | 0.742 | 0.695 | 0.672 | 0.708 | 0.612 | 0.708 | 0.671 | 0.674 | 0.609 |
| 90 | 0.866 | 0.758 | 0.709 | 0.726 | 0.746 | 0.753 | 0.776 | 0.700 | 0.686 | 0.622 | 0.708 | 0.657 | 0.630 | 0.669 | 0.568 | 0.665 | 0.625 | 0.626 | 0.561 |
| 102 | 0.841 | 0.724 | 0.677 | 0.695 | 0.711 | 0.715 | 0.741 | 0.663 | 0.653 | 0.586 | 0.677 | 0.621 | 0.591 | 0.633 | 0.526 | 0.625 | 0.582 | 0.583 | 0.518 |
| 114 | 0.814 | 0.690 | 0.646 | 0.665 | 0.677 | 0.677 | 0.705 | 0.627 | 0.622 | 0.551 | 0.649 | 0.588 | 0.554 | 0.598 | 0.488 | 0.586 | 0.542 | 0.542 | 0.479 |
| 126 | 0.788 | 0.658 | 0.616 | 0.636 | 0.645 | 0.642 | 0.671 | 0.593 | 0.591 | 0.518 | 0.618 | 0.555 | 0.519 | 0.564 | 0.452 | 0.550 | 0.505 | 0.505 | 0.442 |
| 138 | 0.764 | 0.629 | 0.587 | 0.608 | 0.614 | 0.610 | 0.638 | 0.560 | 0.559 | 0.484 | 0.586 | 0.523 | 0.486 | 0.532 | 0.419 | 0.516 | 0.472 | 0.471 | 0.409 |
| 150 | 0.739 | 0.601 | 0.559 | 0.581 | 0.584 | 0.578 | 0.607 | 0.528 | 0.528 | 0.453 | 0.554 | 0.493 | 0.455 | 0.501 | 0.387 | 0.483 | 0.440 | 0.440 | 0.378 |
| 162 | 0.714 | 0.574 | 0.532 | 0.554 | 0.555 | 0.548 | 0.575 | 0.498 | 0.499 | 0.423 | 0.524 | 0.464 | 0.425 | 0.471 | 0.358 | 0.452 | 0.410 | 0.410 | 0.349 |
| 174 | 0.688 | 0.547 | 0.507 | 0.529 | 0.527 | 0.518 | 0.545 | 0.468 | 0.471 | 0.395 | 0.494 | 0.437 | 0.398 | 0.443 | 0.331 | 0.422 | 0.382 | 0.382 | 0.322 |
| 186 | 0.663 | 0.521 | 0.482 | 0.505 | 0.500 | 0.489 | 0.515 | 0.440 | 0.444 | 0.368 | 0.465 | 0.411 | 0.372 | 0.416 | 0.306 | 0.394 | 0.356 | 0.355 | 0.298 |
| 198 | 0.637 | 0.496 | 0.458 | 0.481 | 0.473 | 0.461 | 0.485 | 0.413 | 0.418 | 0.343 | 0.438 | 0.387 | 0.347 | 0.391 | 0.283 | 0.368 | 0.331 | 0.331 | 0.275 |
| 210 | 0.612 | 0.472 | 0.436 | 0.459 | 0.448 | 0.433 | 0.457 | 0.387 | 0.394 | 0.320 | 0.411 | 0.364 | 0.324 | 0.367 | 0.261 | 0.342 | 0.308 | 0.307 | 0.254 |
| 222 | 0.586 | 0.448 | 0.414 | 0.437 | 0.423 | 0.407 | 0.429 | 0.362 | 0.370 | 0.297 | 0.386 | 0.342 | 0.302 | 0.344 | 0.241 | 0.318 | 0.286 | 0.286 | 0.234 |
| 234 | 0.561 | 0.426 | 0.393 | 0.416 | 0.399 | 0.382 | 0.402 | 0.339 | 0.348 | 0.277 | 0.362 | 0.321 | 0.282 | 0.322 | 0.223 | 0.296 | 0.266 | 0.265 | 0.216 |
| 246 | 0.542 | 0.406 | 0.375 | 0.397 | 0.379 | 0.361 | 0.380 | 0.319 | 0.328 | 0.259 | 0.342 | 0.302 | 0.263 | 0.302 | 0.206 | 0.276 | 0.247 | 0.246 | 0.200 |
| 258 | 0.530 | 0.389 | 0.358 | 0.379 | 0.361 | 0.343 | 0.363 | 0.304 | 0.312 | 0.244 | 0.326 | 0.285 | 0.247 | 0.286 | 0.191 | 0.260 | 0.229 | 0.228 | 0.184 |

## Notes

(1)-(19) Data from U.S. Treasury
http://www.treasury.gov/offices/domestic-finance/debt-management/interest-rate/yield_historical_main.shtml
(20)-(38) Computed from (1)-(19), by interpolation of rates, compounded for number of months indicated

| Accident Year <br> Age (Months) | Cumulative Paid Development Factor | Cumulative <br> Percent <br> Paid | Incremental <br> Percent <br> Paid |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | DISCOUNT FACTORS |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) | (20) | (21) | (22) |
| 12 | 2.694 | 37.1\% | 37.1\% | 37.1\% | 36.5\% | 36.2\% | 36.3\% | 36.6\% | 36.9\% | 36.9\% | 36.8\% | 36.1\% | 36.1\% | 36.3\% | 36.1\% | 36.2\% | 36.2\% | 36.0\% | 36.5\% | 36.5\% | 36.4\% | 35.9\% |
| 24 | 1.662 | 60.2\% | 23.1\% | 22.9\% | 22.0\% | 21.5\% | 21.6\% | 22.1\% | 22.5\% | 22.6\% | 22.2\% | 21.4\% | 21.1\% | 21.6\% | 21.2\% | 21.2\% | 21.4\% | 20.7\% | 21.8\% | 21.7\% | 21.6\% | 20.8\% |
| 36 | 1.400 | 71.4\% | 11.3\% | 11.0\% | 10.4\% | 10.0\% | 10.1\% | 10.4\% | 10.7\% | 10.8\% | 10.4\% | 9.9\% | 9.7\% | 10.1\% | 9.8\% | 9.7\% | 9.9\% | 9.3\% | 10.1\% | 10.0\% | 10.0\% | 9.4\% |
| 48 | 1.239 | 80.7\% | 9.3\% | 8.9\% | 8.3\% | 7.9\% | 8.0\% | 8.3\% | 8.5\% | 8.6\% | 8.2\% | 7.8\% | 7.5\% | 8.0\% | 7.7\% | 7.6\% | 7.8\% | 7.1\% | 7.9\% | 7.7\% | 7.8\% | 7.2\% |
| 60 | 1.146 | 87.2\% | 6.5\% | 6.1\% | 5.6\% | 5.3\% | 5.4\% | 5.6\% | 5.7\% | 5.8\% | 5.4\% | 5.2\% | 4.9\% | 5.3\% | 5.1\% | 5.0\% | 5.1\% | 4.6\% | 5.2\% | 5.0\% | 5.1\% | 4.7\% |
| 72 | 1.091 | 91.6\% | 4.4\% | 4.0\% | 3.6\% | 3.4\% | 3.5\% | 3.6\% | 3.7\% | 3.7\% | 3.4\% | 3.4\% | 3.1\% | 3.4\% | 3.2\% | 3.1\% | 3.3\% | 2.9\% | 3.3\% | 3.2\% | 3.2\% | 2.9\% |
| 84 | 1.059 | 94.4\% | 2.8\% | 2.5\% | 2.2\% | 2.1\% | 2.1\% | 2.2\% | 2.2\% | 2.3\% | 2.1\% | 2.0\% | 1.9\% | 2.1\% | 1.9\% | 1.9\% | 2.0\% | 1.7\% | 2.0\% | 1.9\% | 1.9\% | 1.7\% |
| 96 | 1.039 | 96.2\% | 1.8\% | 1.6\% | 1.4\% | 1.3\% | 1.3\% | 1.4\% | 1.4\% | 1.4\% | 1.3\% | 1.2\% | 1.1\% | 1.3\% | 1.2\% | 1.1\% | 1.2\% | 1.0\% | 1.2\% | 1.1\% | 1.1\% | 1.0\% |
| 108 | 1.025 | 97.6\% | 1.4\% | 1.1\% | 1.0\% | 0.9\% | 0.9\% | 1.0\% | 1.0\% | 1.0\% | 0.9\% | 0.9\% | 0.8\% | 0.9\% | 0.8\% | 0.8\% | 0.9\% | 0.7\% | 0.9\% | 0.8\% | 0.8\% | 0.7\% |
| 120 | 1.014 | 98.6\% | 1.0\% | 0.8\% | 0.7\% | 0.6\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.6\% | 0.6\% | 0.5\% | 0.6\% | 0.6\% | 0.5\% | 0.6\% | 0.5\% | 0.6\% | 0.5\% | 0.5\% | 0.5\% |
| 132 | 1.009 | 99.1\% | 0.5\% | 0.4\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.2\% | 0.3\% | 0.3\% | 0.3\% | 0.2\% |
| 144 | 1.006 | 99.4\% | 0.3\% | 0.3\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.1\% | 0.2\% | 0.2\% | 0.2\% | 0.1\% |
| 156 | 1.004 | 99.6\% | 0.2\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% |
| 168 | 1.002 | 99.8\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.0\% | 0.1\% | 0.1\% | 0.1\% | 0.0\% |
| 180 | 1.001 | 99.9\% | 0.1\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 192 | 1.001 | 99.9\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 204 | 1.001 | 99.9\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 216 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 228 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 240 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 252 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| 264 | 1.000 | 100.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% |
| Total |  |  | 100.0\% | 97.1\% | 92.6\% | 90.0\% | 90.8\% | 92.6\% | 94.1\% | 94.6\% | 92.0\% | 89.3\% | 87.4\% | 90.4\% | 88.4\% | 87.8\% | 89.0\% | 85.2\% | 90.1\% | 89.2\% | 89.0\% | 85.5\% |
| Present Value Factor |  |  |  | 0.971 | 0.926 | 0.900 | 0.908 | 0.926 | 0.941 | 0.946 | 0.920 | 0.893 | 0.874 | 0.904 | 0.884 | 0.878 | 0.890 | 0.852 | 0.901 | 0.892 | 0.890 | 0.855 |
| Notes |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (1) From Exhibit 6 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (2) $=1 /$ (1) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (3) From (2) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (4) - (22) | Product of (3) and | d Exhibit 7, Co | olumns (20) - (38) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

COMMERCIAL MULTIPLE PERIL
INDUSTRY NET RESULTS
SECTION B

DURATION OF PAYOUT OF ACCIDENT YEAR LOSSES

| Accident Year <br> Age <br> (Months) | Cumulative <br> Paid <br> Development <br> Factor | Cumulative <br> Percent <br> Paid | Incremental <br> Percent <br> Paid | Duration |
| :---: | :---: | :---: | :---: | :---: |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
| 12 | 2.694 | $37.1 \%$ | $37.1 \%$ | 0.19 |
| 24 | 1.662 | $60.2 \%$ | $23.1 \%$ | 0.35 |
| 36 | 1.400 | $71.4 \%$ | $11.3 \%$ | 0.28 |
| 48 | 1.239 | $80.7 \%$ | $9.3 \%$ | 0.33 |
| 60 | 1.146 | $87.2 \%$ | $6.5 \%$ | 0.29 |
| 72 | 1.091 | $91.6 \%$ | $4.4 \%$ | 0.24 |
| 84 | 1.059 | $94.4 \%$ | $2.8 \%$ | 0.18 |
| 96 | 1.039 | $96.2 \%$ | $1.8 \%$ | 0.14 |
| 108 | 1.025 | $97.6 \%$ | $1.4 \%$ | 0.12 |
| 120 | 1.014 | $98.6 \%$ | $1.0 \%$ | 0.09 |
| 132 | 1.009 | $99.1 \%$ | $0.5 \%$ | 0.05 |
| 144 | 1.006 | $99.4 \%$ | $0.3 \%$ | 0.04 |
| 156 | 1.004 | $99.6 \%$ | $0.2 \%$ | 0.03 |
| 168 | 1.002 | $99.8 \%$ | $0.1 \%$ | 0.02 |
| 180 | 1.001 | $99.9 \%$ | $0.1 \%$ | 0.01 |
| 192 | 1.001 | $99.9 \%$ | $0.1 \%$ | 0.01 |
| 204 | 1.001 | $99.9 \%$ | $0.0 \%$ | 0.01 |
| 216 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 228 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 240 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 252 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 264 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
|  |  |  |  |  |
| Total |  |  |  |  |
|  |  |  |  |  |
| Duration (years) |  |  |  |  |

Notes
(2) From Exhibit 6
(3) $=1 /$ (2)
(4) From (2)
(5) $=(4) *[(1) / 12-0.5]$

COMMERCIAL MULTIPLE PERIL
INDUSTRY NET RESULTS
SECTION B
DEVELOPED INDUSTRY ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Net <br> Booked Ultimate Loss \& ALAE | Average Development Parameter <br> $\mu$ | Variance Development <br> Parameter $\sigma^{2}$ | Net <br> Developed Ultimate Loss \& ALAE | Developed vs Booked Ultimate Loss \& ALAE | Paid Loss \& ALAE | Developed Unpaid Loss \& ALAE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1987 | 7,935,340 | 0.000\% | 0.000\% | 7,935,340 | - | 7,640,931 | 294,409 |
| 1988 | 8,842,450 | 0.000\% | 0.000\% | 8,842,450 | - | 8,514,284 | 328,166 |
| 1989 | 10,950,486 | 0.000\% | 0.000\% | 10,950,486 | - | 10,574,151 | 376,335 |
| 1990 | 10,715,386 | 0.000\% | 0.000\% | 10,715,386 | - | 10,361,568 | 353,818 |
| 1991 | 10,654,254 | 0.000\% | 0.000\% | 10,654,254 | - | 10,297,937 | 356,317 |
| 1992 | 12,803,656 | 0.000\% | 0.000\% | 12,803,656 | - | 12,491,828 | 311,828 |
| 1993 | 11,605,537 | 0.000\% | 0.000\% | 11,605,537 | - | 11,235,210 | 370,327 |
| 1994 | 13,318,381 | 0.000\% | 0.000\% | 13,318,381 | - | 12,896,222 | 422,159 |
| 1995 | 12,477,097 | 0.000\% | 0.000\% | 12,477,097 | - | 12,082,205 | 394,892 |
| 1996 | 13,915,552 | 0.000\% | 0.000\% | 13,915,552 | - | 13,482,635 | 432,917 |
| 1997 | 12,898,050 | 0.000\% | 0.000\% | 12,898,050 | - | 12,422,696 | 475,354 |
| 1998 | 14,716,147 | 0.000\% | 0.000\% | 14,716,147 | - | 14,206,482 | 509,665 |
| 1999 | 15,128,644 | 0.000\% | 0.000\% | 15,128,644 | - | 14,593,734 | 534,910 |
| 2000 | 15,399,096 | 0.208\% | 0.001\% | 15,431,176 | 32,080 | 14,723,792 | 707,384 |
| 2001 | 15,992,975 | 0.309\% | 0.002\% | 16,042,666 | 49,691 | 15,193,486 | 849,180 |
| 2002 | 13,711,005 | 0.470\% | 0.005\% | 13,775,991 | 64,986 | 12,711,446 | 1,064,545 |
| 2003 | 13,590,079 | 0.521\% | 0.011\% | 13,661,868 | 71,789 | 12,255,864 | 1,406,004 |
| 2004 | 15,090,905 | 0.665\% | 0.025\% | 15,193,428 | 102,523 | 13,264,033 | 1,929,395 |
| 2005 | 16,643,679 | 0.636\% | 0.047\% | 16,753,839 | 110,160 | 13,524,309 | 3,229,530 |
| 2006 | 15,264,573 | 0.921\% | 0.100\% | 15,413,494 | 148,921 | 10,468,406 | 4,945,088 |
| 2007 | 16,828,126 | 0.984\% | 0.177\% | 17,009,468 | 181,342 | 9,851,336 | 7,158,132 |
| 2008 | 21,309,040 | -0.502\% | 0.352\% | 21,239,585 | $(69,455)$ | 8,553,203 | 12,686,382 |
| Total | 299,790,458 |  |  | 300,482,497 | 692,039 | 261,345,758 | 39,136,739 |

Notes
(1) From Exhibit 5, Column 3
(2) From Exhibit 3, Cumulative Average
(3) From Exhibit 4, Variance
(4) $=(1) * \exp [(2)+(3) / 2]$
(5) $=(4)-(1)$
(6) From Exhibit 5, Column 4
(7) $=(4)-(6)$

## INDUSTRY HISTORICAL ULTIMATE LOSS \& ALAE RATIO

Dollars in Thousands

|  | 12 month Booked Ultimate Loss \& ALAE Ratio | PV Factor | 1 - Exp Ratio | Loss Ratio <br> Prior to Adjustment | Loss Ratio Adjustment | Adjusted <br> Loss Ratio | Log of Adjusted Loss Ratio | 12 Month Booked Ultimate Loss | Latest Evaluation Ultimate Loss | Ratio Latest to 12 Month Booked | Log of Ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) |
| 1987 | 50.4\% | 0.855 | 65.9\% | 44.0\% | 1.000 | 44.0\% | -82.1\% | 8,277,207 | 7,935,340 | 0.959 | -0.042 |
| 1988 | 54.2\% | 0.855 | 64.2\% | 48.5\% | 1.000 | 48.5\% | -72.3\% | 9,170,947 | 8,842,450 | 0.964 | -0.036 |
| 1989 | 64.4\% | 0.855 | 63.3\% | 58.4\% | 1.000 | 58.4\% | -53.7\% | 10,830,290 | 10,950,486 | 1.011 | 0.011 |
| 1990 | 64.8\% | 0.855 | 63.5\% | 58.7\% | 1.000 | 58.7\% | -53.3\% | 11,042,654 | 10,715,386 | 0.970 | -0.030 |
| 1991 | 68.0\% | 0.890 | 62.4\% | 65.1\% | 0.813 | 53.0\% | -63.5\% | 11,224,333 | 10,654,254 | 0.949 | -0.052 |
| 1992 | 82.1\% | 0.892 | 62.7\% | 78.5\% | 0.813 | 63.8\% | -44.9\% | 13,195,825 | 12,803,656 | 0.970 | -0.030 |
| 1993 | 72.9\% | 0.901 | 63.5\% | 69.5\% | 0.813 | 56.5\% | -57.0\% | 11,859,305 | 11,605,537 | 0.979 | -0.022 |
| 1994 | 78.0\% | 0.852 | 63.6\% | 70.2\% | 0.813 | 57.1\% | -56.0\% | 13,033,952 | 13,318,381 | 1.022 | 0.022 |
| 1995 | 70.6\% | 0.890 | 64.3\% | 65.7\% | 0.813 | 53.4\% | -62.7\% | 12,388,985 | 12,477,097 | 1.007 | 0.007 |
| 1996 | 74.3\% | 0.878 | 64.1\% | 68.4\% | 0.813 | 55.6\% | -58.7\% | 13,439,227 | 13,915,552 | 1.035 | 0.035 |
| 1997 | 68.0\% | 0.884 | 63.5\% | 63.6\% | 0.813 | 51.8\% | -65.9\% | 12,491,912 | 12,898,050 | 1.033 | 0.032 |
| 1998 | 73.8\% | 0.904 | 63.6\% | 70.5\% | 0.813 | 57.3\% | -55.7\% | 13,523,977 | 14,716,147 | 1.088 | 0.084 |
| 1999 | 73.6\% | 0.874 | 63.3\% | 68.4\% | 0.813 | 55.6\% | -58.7\% | 13,769,366 | 15,128,644 | 1.099 | 0.094 |
| 2000 | 71.3\% | 0.893 | 64.8\% | 66.0\% | 0.813 | 53.7\% | -62.2\% | 13,628,215 | 15,399,096 | 1.130 | 0.124 |
| 2001 | 74.7\% | 0.920 | 66.9\% | 69.1\% | 0.813 | 56.2\% | -57.7\% | 15,615,731 | 15,992,975 | 1.024 | 0.027 |
| 2002 | 60.3\% | 0.946 | 67.1\% | 57.2\% | 1.000 | 57.2\% | -55.9\% | 14,137,617 | 13,711,005 | 0.970 | -0.026 |
| 2003 | 56.1\% | 0.941 | 67.3\% | 52.7\% | 1.000 | 52.7\% | -64.1\% | 14,751,482 | 13,590,079 | 0.921 | -0.077 |
| 2004 | 58.8\% | 0.926 | 67.1\% | 54.6\% | 1.000 | 54.6\% | -60.6\% | 16,675,054 | 15,090,905 | 0.905 | -0.093 |
| 2005 | 61.4\% | 0.908 | 67.0\% | 55.9\% | 1.000 | 55.9\% | -58.1\% | 17,761,767 | 16,643,679 | 0.937 | -0.058 |
| 2006 | 52.8\% | 0.900 | 66.1\% | 48.3\% | 1.000 | 48.3\% | -72.7\% | 16,299,833 | 15,264,573 | 0.936 | -0.056 |
| 2007 | 54.9\% | 0.926 | 64.6\% | 52.9\% | 1.000 | 52.9\% | -63.7\% | 17,306,437 | 16,828,126 | 0.972 | -0.017 |
| 2008 | 69.1\% | 0.971 | 65.3\% | 69.1\% | 1.000 | 69.1\% | -36.9\% | 21,309,040 | 21,309,040 | 1.000 | -0.003 |
| (12) Average |  |  |  |  |  | 55.2\% | -59.8\% |  |  |  |  |
| (13) Variance |  |  |  |  |  |  | 0.862\% |  |  |  | 0.308\% |
| (14) Covariance (log of Adjusted Loss Ratio, log of Ratio of Latest to 12 month Booked) |  |  |  |  |  |  | 0.090\% |  |  |  |  |
| (15) Total Variance of Adjusted Loss Ratio (log) and Ratio of Latest to 12 month Booked (log) |  |  |  |  |  |  | 1.351\% |  |  |  |  |

## Notes

(1) Exhibit 1 @ 12 Months / Exhibit 5, Column
(2) 1995-2008 from Exhibit 8, Columns 4-17; 1994 and prior selectec
(3) $=100 \%$ - Exhibit 5, Column 9
(4) $=(1) *(2)_{\text {AYXXXX }} /(2)_{\text {AY2008 }} *(3)_{\text {AY2008 }} /(3)_{\text {AYXXXX }}$
(5) Adjustment of historical loss ratios to normalize for major differences in levels across multi-year periods

AY 1991-2001: AY 2002-2008 Average / AY 1991-2001 Average; 1.000 for AY 1987-1990 and AY 2002-2008
(6) $=(4) *(5)$
(7) $=\operatorname{LN}(6)$
(8) Exhibit 1 @ 12 Months
(9) Exhibit 1 @ 12 Current Evaluation
$(10)=(9) /(8$
11) $=\mathrm{LN}(10)+$ Exhibit 10, Column $2+($ Exhibit 10, Column 3)/2
12) Average of Column 7
(13) Variance of Column 7 and Column 11
14) Covariance( Column 7, Column 11)
(15) = Row 13, Column 7 + Row 13, Column 7 + 2 * Row 14

DERIVATION OF INDUSTRY 2008 MARKET VALUE OF RISK PARAMETER ( $\boldsymbol{\lambda}$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\boldsymbol{\lambda}$ )

| 1 - ER | $65.3 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.096 |
| PV | 0.971 |
| Target Loss Ratio | $61.3 \%$ |
| ULR12 | $69.1 \%$ |
| $\mu$ | $-0.502 \%$ |
| $\sigma^{2}$ | $0.352 \%$ |
| $\sigma$ | $5.929 \%$ |
| D | 2.373 |
| $\lambda$ | -1.274 |
| $\lambda$ | $-36.9 \%$ |
| $\mu_{\text {AY uLR }}$ | $-37.4 \%$ |
| Combined $\mu$ | $0.862 \%$ |
| $\sigma^{2}{ }_{\text {AY uLR }}$ | $0.308 \%$ |
| $\sigma^{2}{ }_{12 \text {-ult }}$ | $0.090 \%$ |
| Cov(AY ULR, 12-ult) | $1.351 \%$ |
| Combined $\sigma^{2}$ |  |
| $\lambda$ adj for pricing risk | -0.678 |
| (2008 market value of risk) |  |

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+U L A E) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$
Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12 -ult)
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu_{A Y U L R}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma$.

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, 2008 Accident Year

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

DERIVATION OF INDUSTRY LONG-TERM MARKET VALUE OF RISK PARAMETER ( $\boldsymbol{\lambda}$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\boldsymbol{\lambda}$ )

| 1 - ER | $65.3 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.096 |
| PV | 0.971 |
| Target Loss Ratio | $61.3 \%$ |
| ULR12 | $69.1 \%$ |
| $\mu$ | $-0.502 \%$ |
| $\sigma^{2}$ | $0.352 \%$ |
| $\sigma$ | $5.929 \%$ |
| D | 2.373 |
| $\lambda$ | -1.274 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-59.8 \%$ |
| Combined $\mu$ | $-60.3 \%$ |
| $\sigma_{\text {AY ULR }}^{2}$ | $0.862 \%$ |
| $\sigma_{12 \text {-ult }}^{2}$ | $0.308 \%$ |
| Cov(AY ULR, 12 -ult) | $0.090 \%$ |
| Combined $\sigma^{2}$ | $1.351 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.603 |

(long-term market value of risk)

## Notes

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE) / PV
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$
Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12-ult)
$=\left[\ln (1-\mathrm{ER})-\ln (1+\mathrm{ULAE})-\ln (\mathrm{PV})-\mu_{\mathrm{AY}} \operatorname{LLR}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma \cdot \mathrm{v}(\mathrm{D})$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, Average

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

COMMERCIAL MULTIPLE PERIL
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON 2008 MARKET VALUE OF RISK
Dollars in Thousands


COMMERCIAL MULTIPLE PERIL
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands

|  |  | Industry | Company | Company | Company | Company | Total Largest 100 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Simulated 1997-2008 Unpaid Claims | Aggregate | A | B | C | D | Companies |
| (1) | 25th Percentile | 34,389,881 | 2,349,275 | 1,154,756 | 1,015,512 | 314,395 |  |
| (2) | 50th Percentile | 35,356,510 | 2,497,183 | 1,267,359 | 1,126,345 | 395,619 |  |
| (3) | 75th Percentile | 36,542,121 | 2,634,274 | 1,366,300 | 1,230,940 | 474,338 |  |
| (4) | Average | 35,465,626 | 2,504,659 | 1,263,990 | 1,131,559 | 400,216 |  |
| (5) | Standard Deviation | 1,654,241 | 213,345 | 154,390 | 169,931 | 117,777 |  |
| (6) | Simulated Sample $\mu$ <br> = Average[ $\log ($ simulated unpaid claims)] | 17.383 | 14.731 | 14.043 | 13.929 | 12.855 |  |
| (7) | Simulated Sample $\sigma$ <br> = Standard Deviation[log(simulated unpaid claims)] | 0.046 | 0.084 | 0.123 | 0.148 | 0.313 |  |
| (8) | Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}\right)$ | 35,474,978 | 2,505,925 | 1,265,066 | 1,132,475 | 402,061 | 32,002,837 |
| (9) | Industry Market Value of Risk ( $\lambda_{1}$ ) | 0.603 | 0.603 | 0.603 | 0.603 | 0.603 |  |
| (10) | Duration of Unpaid Claims (D) | 2.457 | 2.438 | 2.469 | 2.435 | 2.496 |  |
| (11) | Risk Adjusted Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}+\lambda_{1} \cdot \sigma \cdot V D\right)$ | 37,057,519 | 2,712,920 | 1,421,079 | 1,302,002 | 541,641 | 36,261,741 |
| (12) | Risk Margin = (11) - (8) | 1,582,540 | 206,996 | 156,014 | 169,527 | 139,580 | 4,258,904 |
| (13) | Risk Margin \% of Expected Unpaid Claims = (11) / (8) | 4.5\% | 8.3\% | 12.3\% | 15.0\% | 34.7\% | 13.3\% |

PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands

## Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Total <br> Accident Years 1997-2008 | Accident <br> Year <br> 2008 | Accident <br> Year <br> 2007 | Accident <br> Year <br> 2006 | Accident <br> Year <br> 2005 | Accident <br> Year <br> 2004 | Accident <br> Year <br> 2003 | Accident <br> Year <br> 2002 | Accident <br> Year <br> 2001 | Accident <br> Year <br> 2000 | Accident <br> Year <br> 1999 | Accident <br> Year <br> 1998 | Accident <br> Year <br> 1997 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| Year 1 | 10,830,207 | 4,208,051 | 1,817,162 | 1,433,073 | 942,364 | 581,066 | 510,671 | 308,829 | 266,947 | 265,595 | 182,276 | 160,655 | 153,518 |
| Year 2 | 6,775,343 | 2,055,765 | 1,500,362 | 1,002,240 | 636,145 | 370,610 | 330,978 | 232,322 | 192,910 | 139,960 | 115,458 | 101,602 | 96,991 |
| Year 3 | 4,874,805 | 1,697,368 | 1,049,299 | 676,564 | 405,740 | 240,201 | 248,984 | 167,888 | 101,657 | 88,654 | 73,019 | 64,192 | 61,240 |
| Year 4 | 3,284,768 | 1,187,078 | 708,331 | 431,520 | 262,969 | 180,696 | 179,929 | 88,472 | 64,392 | 56,067 | 46,133 | 40,530 | 38,651 |
| Year 5 | 2,167,302 | 801,339 | 451,781 | 279,678 | 197,824 | 130,580 | 94,817 | 56,040 | 40,723 | 35,423 | 29,128 | 25,580 | 24,388 |
| Year 6 | 1,419,581 | 511,103 | 292,810 | 210,393 | 142,958 | 68,812 | 60,059 | 35,441 | 25,729 | 22,366 | 18,384 | 16,141 | 15,386 |
| Year 7 | 944,716 | 331,257 | 220,272 | 152,041 | 75,334 | 43,587 | 37,983 | 22,391 | 16,245 | 14,116 | 11,600 | 10,183 | 9,706 |
| Year 8 | 640,939 | 249,195 | 159,180 | 80,121 | 47,719 | 27,565 | 23,997 | 14,138 | 10,253 | 8,907 | 7,318 | 6,424 | 6,122 |
| Year 9 | 411,002 | 180,081 | 83,883 | 50,751 | 30,178 | 17,416 | 15,152 | 8,923 | 6,469 | 5,619 | 4,617 | 4,052 | 3,862 |
| Year 10 | 245,067 | 94,897 | 53,133 | 32,096 | 19,066 | 10,996 | 9,563 | 5,630 | 4,081 | 3,545 | 2,912 | 2,556 | 6,591 |
| Year 11 | 153,565 | 60,110 | 33,603 | 20,278 | 12,038 | 6,940 | 6,034 | 3,552 | 2,575 | 2,236 | 1,837 | 4,362 | - |
| Year 12 | 96,243 | 38,015 | 21,230 | 12,803 | 7,598 | 4,379 | 3,807 | 2,241 | 1,624 | 1,410 | 3,135 | - | - |
| Year 13 | 60,306 | 24,018 | 13,405 | 8,081 | 4,794 | 2,763 | 2,401 | 1,413 | 1,024 | 2,407 | - | - | - |
| Year 14 | 37,646 | 15,165 | 8,460 | 5,099 | 3,025 | 1,743 | 1,515 | 892 | 1,748 | - | - | - | - |
| Year 15 | 23,610 | 9,571 | 5,338 | 3,217 | 1,908 | 1,099 | 955 | 1,522 | - | - | - | - | - |
| Year 16 | 14,964 | 6,039 | 3,368 | 2,029 | 1,204 | 693 | 1,631 | - | - | - | - | - | - |
| Year 17 | 9,157 | 3,810 | 2,125 | 1,280 | 759 | 1,183 | - | - | - | - | - | - | - |
| Year 18 | 5,847 | 2,403 | 1,340 | 807 | 1,296 | - | - | - | - | - | - | - | - |
| Year 19 | 3,739 | 1,516 | 845 | 1,378 | - | - | - | - | - | - | - | - | - |
| Year 20 | 2,399 | 956 | 1,443 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 1,632 | 1,632 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total | 32,002,837 | 11,479,369 | 6,427,369 | 4,403,447 | 2,792,918 | 1,690,329 | 1,528,476 | 949,695 | 736,379 | 646,305 | 495,816 | 436,277 | 416,456 |

[^3]DISCOUNTED PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands
Discounted Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Discount Factor | Total Accident Years 1997-2008 | Accident Year 2008 | Accident <br> Year <br> 2007 | Accident Year 2006 | Accident <br> Year <br> 2005 | Accident Year 2004 | Accident Year 2003 | Accident <br> Year <br> 2002 | Accident <br> Year <br> 2001 | Accident Year 2000 | Accident <br> Year <br> 1999 | Accident Year 1998 | Accident Year 1997 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| Year 1 | 0.999 | 10,815,616 | 4,202,382 | 1,814,714 | 1,431,142 | 941,095 | 580,283 | 509,983 | 308,413 | 266,588 | 265,237 | 182,031 | 160,439 | 153,311 |
| Year 2 | 0.992 | 6,718,325 | 2,038,465 | 1,487,735 | 993,805 | 630,791 | 367,491 | 328,192 | 230,367 | 191,286 | 138,782 | 114,487 | 100,747 | 96,175 |
| Year 3 | 0.978 | 4,769,190 | 1,660,593 | 1,026,565 | 661,905 | 396,949 | 234,997 | 243,590 | 164,251 | 99,455 | 86,734 | 71,437 | 62,801 | 59,913 |
| Year 4 | 0.961 | 3,157,272 | 1,141,002 | 680,838 | 414,770 | 252,762 | 173,682 | 172,945 | 85,038 | 61,893 | 53,891 | 44,342 | 38,957 | 37,151 |
| Year 5 | 0.939 | 2,034,734 | 752,323 | 424,147 | 262,571 | 185,723 | 122,593 | 89,017 | 52,612 | 38,232 | 33,256 | 27,346 | 24,016 | 22,897 |
| Year 6 | 0.915 | 1,298,792 | 467,614 | 267,895 | 192,491 | 130,794 | 62,957 | 54,949 | 32,426 | 23,539 | 20,463 | 16,820 | 14,767 | 14,077 |
| Year 7 | 0.891 | 841,817 | 295,177 | 196,280 | 135,480 | 67,129 | 38,840 | 33,846 | 19,953 | 14,476 | 12,578 | 10,337 | 9,074 | 8,649 |
| Year 8 | 0.866 | 555,194 | 215,857 | 137,885 | 69,402 | 41,335 | 23,878 | 20,787 | 12,247 | 8,881 | 7,715 | 6,339 | 5,564 | 5,303 |
| Year 9 | 0.841 | 345,598 | 151,424 | 70,534 | 42,674 | 25,376 | 14,644 | 12,741 | 7,503 | 5,440 | 4,725 | 3,882 | 3,407 | 3,247 |
| Year 10 | 0.814 | 199,545 | 77,269 | 43,264 | 26,134 | 15,525 | 8,954 | 7,787 | 4,584 | 3,323 | 2,886 | 2,371 | 2,081 | 5,367 |
| Year 11 | 0.788 | 121,072 | 47,391 | 26,493 | 15,987 | 9,491 | 5,472 | 4,757 | 2,800 | 2,030 | 1,763 | 1,448 | 3,439 | - |
| Year 12 | 0.764 | 73,516 | 29,038 | 16,217 | 9,780 | 5,804 | 3,345 | 2,908 | 1,712 | 1,241 | 1,077 | 2,395 | - | - |
| Year 13 | 0.739 | 44,562 | 17,747 | 9,905 | 5,971 | 3,543 | 2,041 | 1,774 | 1,044 | 757 | 1,779 | - | - | - |
| Year 14 | 0.714 | 26,868 | 10,823 | 6,038 | 3,639 | 2,159 | 1,244 | 1,081 | 636 | 1,248 | - | - | - | - |
| Year 15 | 0.688 | 16,250 | 6,587 | 3,674 | 2,214 | 1,313 | 757 | 658 | 1,047 | - | - | - | - | - |
| Year 16 | 0.663 | 9,916 | 4,002 | 2,232 | 1,345 | 798 | 460 | 1,081 | - | - | - | - | - | - |
| Year 17 | 0.637 | 5,834 | 2,427 | 1,354 | 815 | 484 | 754 | - | - | - | - | - | - | - |
| Year 18 | 0.612 | 3,575 | 1,470 | 820 | 494 | 792 | - | - | - | - | - | - | - | - |
| Year 19 | 0.586 | 2,192 | 889 | 495 | 808 | - | - | - | - | - | - | - | - | - |
| Year 20 | 0.561 | 1,345 | 536 | 809 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 0.542 | 885 | 885 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | 0.530 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total |  | 31,042,097 | 11,123,904 | 6,217,893 | 4,271,429 | 2,711,862 | 1,642,389 | 1,486,095 | 924,633 | 718,389 | 630,886 | 483,233 | 425,293 | 406,090 |

Notes
(1) From Exhibit 7, Column 20
(2) Sum of Columns 3-14
(3) - (14) Product of Column 1 and Exhibit 14, Columns 2-13

COMMERCIAL MULTIPLE PERIL
SECTION B
INDUSTRY NET RESULTS
EXHIBIT 16
NET IMPACT OF RISK MARGINS AND DISCOUNT FOR LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands


Notes
(3) From Exhibit 13B, Row 13, Total Largest 100 U.S. Insurers
(4) From Exhibit 15, Total by Accident Year
(5) $=(4) /(2)-1$
(6) $=(2)$ Total $*[1+(3)$ Total $]$ [ $1+(5)$ Total $]$
(7) $=(6)$ Total $/(1)$ Total -1

PRIVATE PASSENGER AUTO LIABLLITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Months of Maturity |  |  |  |  |  |  |  |  |  | Latest |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12 | $\underline{24}$ | $\underline{36}$ | 48 | 60 | 72 | 84 | 96 | 108 | $\underline{120}$ | Evaluation |
| 1987 | 30,073,940 | 30,014,097 | 29,916,731 | 29,869,664 | 29,837,370 | 29,776,950 | 29,739,293 | 29,711,894 | 29,666,018 | 29,639,489 | 29,639,489 |
| 1988 | 33,876,530 | 33,607,912 | 33,388,007 | 33,240,654 | 33,026,121 | 32,917,166 | 32,801,787 | 32,715,383 | 32,685,033 | 32,654,526 | 32,654,526 |
| 1989 | 37,233,839 | 37,032,098 | 36,850,477 | 36,511,610 | 36,361,849 | 36,191,650 | 36,035,671 | 35,952,437 | 35,908,659 | 35,904,083 | 35,904,083 |
| 1990 | 40,624,863 | 40,002,856 | 39,272,320 | 38,929,128 | 38,578,887 | 38,309,133 | 38,122,001 | 38,061,930 | 38,036,542 | 38,001,440 | 38,001,440 |
| 1991 | 41,349,440 | 40,070,087 | 39,181,888 | 38,439,672 | 38,000,435 | 37,641,671 | 37,464,409 | 37,417,385 | 37,367,059 | 37,358,272 | 37,358,272 |
| 1992 | 44,368,312 | 42,559,695 | 41,335,520 | 40,481,851 | 39,870,465 | 39,558,371 | 39,401,256 | 39,342,494 | 39,311,949 | 39,284,461 | 39,284,461 |
| 1993 | 46,768,470 | 44,955,497 | 43,828,900 | 42,796,950 | 42,267,365 | 42,017,981 | 41,909,422 | 41,821,767 | 41,802,336 | 41,791,971 | 41,791,971 |
| 1994 | 48,881,084 | 47,227,469 | 45,876,145 | 45,184,300 | 44,786,877 | 44,569,087 | 44,433,838 | 44,376,155 | 44,367,434 | 44,368,818 | 44,368,818 |
| 1995 | 49,635,063 | 47,910,101 | 46,766,699 | 46,265,087 | 45,904,532 | 45,737,876 | 45,684,266 | 45,647,254 | 45,649,510 | 45,677,291 | 45,677,291 |
| 1996 | 50,317,796 | 48,397,933 | 47,597,839 | 47,106,148 | 46,980,288 | 46,942,173 | 46,941,775 | 46,932,367 | 46,961,724 | 46,968,387 | 46,968,387 |
| 1997 | 49,765,419 | 48,076,614 | 47,429,358 | 47,173,733 | 47,029,570 | 46,981,100 | 46,964,622 | 46,961,281 | 46,964,675 | 46,961,444 | 46,961,444 |
| 1998 | 49,240,853 | 48,443,399 | 48,273,854 | 48,125,090 | 48,130,877 | 48,079,675 | 48,096,070 | 48,060,546 | 48,076,015 | 48,069,447 | 48,069,447 |
| 1999 | 51,632,511 | 51,529,797 | 51,474,323 | 51,573,936 | 51,482,579 | 51,491,473 | 51,526,727 | 51,548,383 | 51,520,753 | 51,518,156 | 51,518,156 |
| 2000 | 54,557,893 | 54,876,830 | 55,032,600 | 55,109,558 | 55,123,996 | 55,163,934 | 55,198,693 | 55,204,511 | 55,254,295 |  | 55,254,295 |
| 2001 | 56,991,221 | 56,747,179 | 56,645,139 | 56,684,994 | 56,817,224 | 56,782,670 | 56,747,660 | 56,734,057 |  |  | 56,734,057 |
| 2002 | 60,398,169 | 59,687,868 | 59,417,844 | 59,436,712 | 59,369,961 | 59,282,630 | 59,256,413 |  |  |  | 59,256,413 |
| 2003 | 61,633,969 | 59,698,968 | 58,946,020 | 58,740,482 | 58,568,183 | 58,526,059 |  |  |  |  | 58,526,059 |
| 2004 | 62,276,716 | 59,981,303 | 59,128,221 | 58,732,132 | 58,523,896 |  |  |  |  |  | 58,523,896 |
| 2005 | 63,227,347 | 61,118,622 | 60,420,357 | 60,144,772 |  |  |  |  |  |  | 60,144,772 |
| 2006 | 62,825,209 | 62,008,666 | 61,588,607 |  |  |  |  |  |  |  | 61,588,607 |
| 2007 | 65,552,945 | 65,218,021 |  |  |  |  |  |  |  |  | 65,218,021 |
| 2008 | 65,469,504 |  |  |  |  |  |  |  |  |  | 65,469,504 |

## Notes

Data from SNL Financial LC
1996-2008 Annual Statements
Industry Total Private Passenger Auto Liability Schedule P, Part 2B

Latest valuation 32,654,526 35,904,083 38,001,440 39,284,461 41,791,971 45,677,291 46,968,387 48,069,447 51,518,156 56,734,057 5,256,413 58,523,896 61,588,607 $65,218,021$
$65,469,504$

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
LINK RATIOS


From Exhibit 1, ratio of successive ultimate loss estimates by accident year

Notes
From Exhibit 2, natural log of ratio of successive ultimate loss estimates by accident year

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
CUMULATIVE DEVELOPMENT IN ULTIMATE LOSS ESTIMATES BASED ON LOG OF LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | -0.199\% | -0.325\% | -0.157\% | -0.108\% | -0.203\% | -0.127\% | -0.092\% | -0.155\% | -0.089\% |
| 1988 | -0.796\% | -0.656\% | -0.442\% | -0.647\% | -0.330\% | -0.351\% | -0.264\% | -0.093\% | -0.093\% |
| 1989 | -0.543\% | -0.492\% | -0.924\% | -0.411\% | -0.469\% | -0.432\% | -0.231\% | -0.122\% | -0.013\% |
| 1990 | -1.543\% | -1.843\% | -0.878\% | -0.904\% | -0.702\% | -0.490\% | -0.158\% | -0.067\% | -0.092\% |
| 1991 | -3.143\% | -2.242\% | -1.912\% | -1.149\% | -0.949\% | -0.472\% | -0.126\% | -0.135\% | -0.024\% |
| 1992 | -4.162\% | -2.919\% | -2.087\% | -1.522\% | -0.786\% | -0.398\% | -0.149\% | -0.078\% | -0.070\% |
| 1993 | -3.954\% | -2.538\% | -2.383\% | -1.245\% | -0.592\% | -0.259\% | -0.209\% | -0.046\% | -0.025\% |
| 1994 | -3.441\% | -2.903\% | -1.520\% | -0.883\% | -0.487\% | -0.304\% | -0.130\% | -0.020\% | 0.003\% |
| 1995 | -3.537\% | -2.415\% | -1.078\% | -0.782\% | -0.364\% | -0.117\% | -0.081\% | 0.005\% | 0.061\% |
| 1996 | -3.890\% | -1.667\% | -1.038\% | -0.268\% | -0.081\% | -0.001\% | -0.020\% | 0.063\% | 0.014\% |
| 1997 | -3.452\% | -1.355\% | -0.540\% | -0.306\% | -0.103\% | -0.035\% | -0.007\% | 0.007\% | -0.007\% |
| 1998 | -1.633\% | -0.351\% | -0.309\% | 0.012\% | -0.106\% | 0.034\% | -0.074\% | 0.032\% | -0.014\% |
| 1999 | -0.199\% | -0.108\% | 0.193\% | -0.177\% | 0.017\% | 0.068\% | 0.042\% | -0.054\% | -0.005\% |
| 2000 | 0.583\% | 0.283\% | 0.140\% | 0.026\% | 0.072\% | 0.063\% | 0.011\% | 0.090\% |  |
| 2001 | -0.429\% | -0.180\% | 0.070\% | 0.233\% | -0.061\% | -0.062\% | -0.024\% |  |  |
| 2002 | -1.183\% | -0.453\% | 0.032\% | -0.112\% | -0.147\% | -0.044\% |  |  |  |
| 2003 | -3.190\% | -1.269\% | -0.349\% | -0.294\% | -0.072\% |  |  |  |  |
| 2004 | -3.755\% | -1.432\% | -0.672\% | -0.355\% |  |  |  |  |  |
| 2005 | -3.392\% | -1.149\% | -0.457\% |  |  |  |  |  |  |
| 2006 | -1.308\% | -0.680\% |  |  |  |  |  |  |  |
| 2007 | -0.512\% |  |  |  |  |  |  |  |  |
| Average | -2.080\% | -1.235\% | -0.753\% | -0.494\% | -0.315\% | -0.183\% | -0.101\% | -0.041\% | -0.027\% |
|  | 12-108 | 24-108 | 36-108 | 48-108 | 60-108 | 72-108 | 84-108 | 96-108 | 108-108 |
| Cumulative Average | -5.229\% | -3.149\% | -1.914\% | -1.161\% | -0.667\% | -0.352\% | -0.169\% | -0.068\% | -0.027\% |

SECTION C
EXHIBIT 3

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE

## VARIANCE-COVARIANCE MATRIX OF LOG OF INCREMENTAL LINK RATIOS

| Months of Maturity | 12-108 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 | 120-Ultimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12-108 | 0.023\% | 0.012\% | 0.008\% | 0.005\% | 0.002\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 24-36 | 0.012\% | 0.009\% | 0.006\% | 0.004\% | 0.002\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 36-48 | 0.008\% | 0.006\% | 0.006\% | 0.003\% | 0.002\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 48-60 | 0.005\% | 0.004\% | 0.003\% | 0.002\% | 0.001\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 60-72 | 0.002\% | 0.002\% | 0.002\% | 0.001\% | 0.001\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 72-84 | 0.001\% | 0.001\% | 0.001\% | 0.001\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 84-96 | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 96-108 | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 108-120 | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| 120-Ultimate | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| Variance ( $\boldsymbol{\sigma}^{\mathbf{2}}$ ) | 0.147\% | 0.068\% | 0.030\% | 0.011\% | 0.004\% | 0.001\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |

Notes
From Exhibit 3, covariance of errors at given maturity with errors at all other maturities
Covariances above diagonal are symmetric with those below
Variance is sum of matrix for all maturities greater than or equal to maturity shown in column

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET RESULTS
SELECTION OF LOSS \& ALAE RATIO, ULAE FACTOR, AND LOSS \& LAE RATIO
Dollars in Thousands

|  | Net <br> Earned Premium | Net Ultimate Loss \& LAE | Net <br> Ultimate Loss \& ALAE | Net Paid Loss \& ALAE | Net <br> Unpaid Loss \& ALAE | Net Ultimate Loss \& LAE Ratio | Net <br> Ultimate Loss \& ALAE Ratio | ULAE <br> Factor | Underwriting Expense Ratio |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) |
| 1987 | 35,637,196 | 32,232,745 | 29,639,489 | 29,467,912 | 171,577 | 90.4\% | 83.2\% | 1.087 | 23.8\% | 76.2\% |
| 1988 | 39,418,843 | 35,605,154 | 32,654,526 | 32,484,806 | 169,720 | 90.3\% | 82.8\% | 1.090 | 23.5\% | 76.5\% |
| 1989 | 42,875,769 | 39,220,045 | 35,904,083 | 35,725,452 | 178,631 | 91.5\% | 83.7\% | 1.092 | 23.4\% | 76.6\% |
| 1990 | 46,362,866 | 41,664,283 | 38,001,440 | 37,836,187 | 165,253 | 89.9\% | 82.0\% | 1.096 | 23.4\% | 76.6\% |
| 1991 | 49,395,069 | 41,213,658 | 37,358,272 | 37,202,829 | 155,443 | 83.4\% | 75.6\% | 1.103 | 24.1\% | 75.9\% |
| 1992 | 53,365,666 | 43,469,020 | 39,284,461 | 39,159,559 | 124,902 | 81.5\% | 73.6\% | 1.107 | 23.7\% | 76.3\% |
| 1993 | 56,764,444 | 46,298,123 | 41,791,971 | 41,635,331 | 156,640 | 81.6\% | 73.6\% | 1.108 | 23.3\% | 76.7\% |
| 1994 | 59,548,633 | 49,282,166 | 44,368,818 | 44,215,159 | 153,659 | 82.8\% | 74.5\% | 1.111 | 22.6\% | 77.4\% |
| 1995 | 63,098,900 | 50,983,872 | 45,677,291 | 45,494,007 | 183,284 | 80.8\% | 72.4\% | 1.116 | 23.2\% | 76.8\% |
| 1996 | 65,880,165 | 52,841,192 | 46,968,387 | 46,793,738 | 174,649 | 80.2\% | 71.3\% | 1.125 | 22.8\% | 77.2\% |
| 1997 | 68,245,961 | 53,304,349 | 46,961,444 | 46,777,820 | 183,624 | 78.1\% | 68.8\% | 1.135 | 24.9\% | 75.1\% |
| 1998 | 68,908,363 | 54,576,482 | 48,069,447 | 47,895,384 | 174,063 | 79.2\% | 69.8\% | 1.135 | 25.6\% | 74.4\% |
| 1999 | 68,840,314 | 58,218,992 | 51,518,156 | 51,324,356 | 193,800 | 84.6\% | 74.8\% | 1.130 | 25.3\% | 74.7\% |
| 2000 | 69,161,761 | 62,307,261 | 55,254,295 | 54,907,512 | 346,783 | 90.1\% | 79.9\% | 1.128 | 25.6\% | 74.4\% |
| 2001 | 72,739,653 | 64,002,047 | 56,734,057 | 56,329,466 | 404,591 | 88.0\% | 78.0\% | 1.128 | 23.9\% | 76.1\% |
| 2002 | 79,500,987 | 67,054,498 | 59,256,413 | 58,516,357 | 740,056 | 84.3\% | 74.5\% | 1.132 | 24.0\% | 76.0\% |
| 2003 | 86,900,392 | 66,568,042 | 58,526,059 | 57,213,665 | 1,312,394 | 76.6\% | 67.3\% | 1.137 | 23.6\% | 76.4\% |
| 2004 | 91,955,540 | 66,831,479 | 58,523,896 | 56,213,701 | 2,310,195 | 72.7\% | 63.6\% | 1.142 | 24.2\% | 75.8\% |
| 2005 | 94,297,862 | 68,778,198 | 60,144,772 | 55,278,660 | 4,866,112 | 72.9\% | 63.8\% | 1.144 | 24.0\% | 76.0\% |
| 2006 | 95,452,865 | 70,777,290 | 61,588,607 | 51,754,053 | 9,834,554 | 74.1\% | 64.5\% | 1.149 | 26.1\% | 73.9\% |
| 2007 | 95,291,384 | 74,453,427 | 65,218,021 | 46,324,452 | 18,893,569 | 78.1\% | 68.4\% | 1.142 | 25.5\% | 74.5\% |
| 2008 | 94,407,183 | 75,626,083 | 65,469,504 | 26,975,954 | 38,493,550 | 80.1\% | 69.3\% | 1.155 | 25.6\% | 74.4\% |
| Selected |  |  |  |  | 79,387,049 |  | 69.3\% | 1.145 |  | 74.4\% |

Notes
(1), (2) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1B
(3) Exhibit 1, Latest Evaluation
(4) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1B
(5) $=(3)-(4)$
(6) $=(2) /(1)$
$(7)=(3) /(1)$; Selected from 2008
(8) $=(6) /(7)$; Selected from 2005-2007 Average
(9) From AM Best Aggregates and Averages, includes policyholder dividends
(10) $=1$ - (9); Selected from 2008


| Fitted Age-to-Ultimate |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Curve Fits: | R-squared | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| Weibull | 99.8\% | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Power Curve | 99.5\% | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Inverse Power Curve | 95.7\% | 1.010 | 1.008 | 1.007 | 1.006 | 1.005 | 1.004 | 1.004 | 1.003 | 1.003 | 1.002 | 1.002 | 1.002 | 1.002 |


| Selected Pattern | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age-to-Age | 1.730 | 1.192 | 1.092 | 1.044 | 1.020 | 1.009 | 1.005 | 1.003 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |  |
| Age-to-Ultimate | 2.443 | 1.413 | 1.185 | 1.086 | 1.039 | 1.019 | 1.010 | 1.005 | 1.002 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.00 |
| Cumulative \% Paid | 40.9\% | 70.8\% | 84.4\% | 92.1\% | 96.2\% | 98.1\% | 99.0\% | 99.5\% | 99.8\% | 99.9\% | 99.9\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% |
| Incremental \% Paid | 40.9\% | 29.9\% | 13.6\% | 7.7\% | 4.1\% | 1.9\% | 0.9\% | 0.5\% | 0.3\% | 0.1\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0\% | 0.0 |

[^4]|  | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Duration | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) |
| 1 month | 0.11\% | 2.76\% | 4.75\% | 4.01\% | 1.89\% | 0.90\% | 1.20\% | 1.68\% | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |
| 3 months | 0.11\% | 3.36\% | 5.02\% | 4.08\% | 2.22\% | 0.95\% | 1.22\% | 1.74\% | 5.89\% | 5.33\% | 4.48\% | 5.36\% | 5.21\% | 5.10\% | 5.68\% | 3.07\% | 3.15\% | 3.96\% | 6.63\% |
| 6 months | 0.27\% | 3.49\% | 5.09\% | 4.37\% | 2.59\% | 1.02\% | 1.23\% | 1.83\% | 5.70\% | 5.74\% | 4.55\% | 5.45\% | 5.33\% | 5.17\% | 6.51\% | 3.30\% | 3.38\% | 4.00\% | 6.73\% |
| 1 year | 0.37\% | 3.34\% | 5.00\% | 4.38\% | 2.75\% | 1.26\% | 1.32\% | 2.17\% | 5.32\% | 5.98\% | 4.53\% | 5.51\% | 5.51\% | 5.18\% | 7.20\% | 3.63\% | 3.61\% | 4.12\% | 6.82\% |
| 2 years | 0.76\% | 3.05\% | 4.82\% | 4.41\% | 3.08\% | 1.84\% | 1.61\% | 3.07\% | 5.11\% | 6.24\% | 4.54\% | 5.66\% | 5.88\% | 5.18\% | 7.69\% | 4.25\% | 4.56\% | 4.77\% | 7.15\% |
| 3 years | 1.00\% | 3.07\% | 4.74\% | 4.37\% | 3.25\% | 2.37\% | 1.99\% | 3.59\% | 5.06\% | 6.29\% | 4.55\% | 5.68\% | 6.04\% | 5.25\% | 7.80\% | 4.58\% | 5.12\% | 5.11\% | 7.40\% |
| 5 years | 1.55\% | 3.45\% | 4.70\% | 4.35\% | 3.63\% | 3.25\% | 2.78\% | 4.38\% | 4.99\% | 6.36\% | 4.56\% | 5.71\% | 6.21\% | 5.38\% | 7.83\% | 5.21\% | 6.04\% | 5.93\% | 7.68\% |
| 7 years | 1.87\% | 3.70\% | 4.70\% | 4.36\% | 3.94\% | 3.77\% | 3.36\% | 4.84\% | 5.16\% | 6.55\% | 4.73\% | 5.77\% | 6.34\% | 5.49\% | 7.84\% | 5.53\% | 6.43\% | 6.38\% | 8.00\% |
| 10 years | 2.25\% | 4.04\% | 4.71\% | 4.39\% | 4.24\% | 4.27\% | 3.83\% | 5.07\% | 5.12\% | 6.45\% | 4.65\% | 5.75\% | 6.43\% | 5.58\% | 7.84\% | 5.83\% | 6.70\% | 6.71\% | 8.08\% |
| 20 years | 3.05\% | 4.50\% | 4.91\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.74\% | 5.59\% | 6.83\% | 5.39\% | 6.02\% | 6.73\% | 6.01\% | 8.02\% | 6.48\% | 7.05\% | 7.06\% | 8.17\% |
| 30 years | 2.69\% | 4.45\% | 4.81\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.48\% | 5.46\% | 6.48\% | 5.09\% | 5.93\% | 6.65\% | 5.96\% | 7.89\% | 6.35\% | 7.40\% | 7.41\% | 8.26\% |


| Discount Factor | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (months) | (20) | (21) | (22) | (23) | (24) | (25) | (26) | (27) | (28) | (29) | (30) | (31) | (32) | (33) | (34) | (35) | (36) | (37) | (38) |
| 6 | 0.999 | 0.983 | 0.975 | 0.979 | 0.987 | 0.995 | 0.994 | 0.991 | 0.973 | 0.972 | 0.978 | 0.974 | 0.974 | 0.975 | 0.969 | 0.984 | 0.984 | 0.981 | 0.968 |
| 18 | 0.992 | 0.954 | 0.931 | 0.938 | 0.958 | 0.977 | 0.978 | 0.962 | 0.927 | 0.915 | 0.936 | 0.922 | 0.920 | 0.927 | 0.898 | 0.944 | 0.942 | 0.937 | 0.904 |
| 30 | 0.978 | 0.927 | 0.890 | 0.898 | 0.925 | 0.949 | 0.956 | 0.921 | 0.883 | 0.859 | 0.895 | 0.871 | 0.865 | 0.881 | 0.830 | 0.898 | 0.889 | 0.886 | 0.839 |
| 42 | 0.961 | 0.897 | 0.851 | 0.861 | 0.891 | 0.914 | 0.927 | 0.878 | 0.842 | 0.807 | 0.856 | 0.824 | 0.813 | 0.835 | 0.769 | 0.850 | 0.833 | 0.834 | 0.777 |
| 54 | 0.939 | 0.862 | 0.813 | 0.825 | 0.855 | 0.874 | 0.892 | 0.832 | 0.803 | 0.758 | 0.818 | 0.779 | 0.764 | 0.791 | 0.713 | 0.801 | 0.776 | 0.778 | 0.719 |
| 66 | 0.915 | 0.827 | 0.777 | 0.791 | 0.819 | 0.833 | 0.853 | 0.785 | 0.763 | 0.711 | 0.781 | 0.736 | 0.717 | 0.749 | 0.661 | 0.753 | 0.721 | 0.724 | 0.663 |
| 78 | 0.891 | 0.793 | 0.742 | 0.758 | 0.782 | 0.793 | 0.814 | 0.741 | 0.723 | 0.664 | 0.742 | 0.695 | 0.672 | 0.708 | 0.612 | 0.708 | 0.671 | 0.674 | 0.609 |
| 90 | 0.866 | 0.758 | 0.709 | 0.726 | 0.746 | 0.753 | 0.776 | 0.700 | 0.686 | 0.622 | 0.708 | 0.657 | 0.630 | 0.669 | 0.568 | 0.665 | 0.625 | 0.626 | 0.561 |
| 102 | 0.841 | 0.724 | 0.677 | 0.695 | 0.711 | 0.715 | 0.741 | 0.663 | 0.653 | 0.586 | 0.677 | 0.621 | 0.591 | 0.633 | 0.526 | 0.625 | 0.582 | 0.583 | 0.518 |
| 114 | 0.814 | 0.690 | 0.646 | 0.665 | 0.677 | 0.677 | 0.705 | 0.627 | 0.622 | 0.551 | 0.649 | 0.588 | 0.554 | 0.598 | 0.488 | 0.586 | 0.542 | 0.542 | 0.479 |
| 126 | 0.788 | 0.658 | 0.616 | 0.636 | 0.645 | 0.642 | 0.671 | 0.593 | 0.591 | 0.518 | 0.618 | 0.555 | 0.519 | 0.564 | 0.452 | 0.550 | 0.505 | 0.505 | 0.442 |
| 138 | 0.764 | 0.629 | 0.587 | 0.608 | 0.614 | 0.610 | 0.638 | 0.560 | 0.559 | 0.484 | 0.586 | 0.523 | 0.486 | 0.532 | 0.419 | 0.516 | 0.472 | 0.471 | 0.409 |
| 150 | 0.739 | 0.601 | 0.559 | 0.581 | 0.584 | 0.578 | 0.607 | 0.528 | 0.528 | 0.453 | 0.554 | 0.493 | 0.455 | 0.501 | 0.387 | 0.483 | 0.440 | 0.440 | 0.378 |
| 162 | 0.714 | 0.574 | 0.532 | 0.554 | 0.555 | 0.548 | 0.575 | 0.498 | 0.499 | 0.423 | 0.524 | 0.464 | 0.425 | 0.471 | 0.358 | 0.452 | 0.410 | 0.410 | 0.349 |
| 174 | 0.688 | 0.547 | 0.507 | 0.529 | 0.527 | 0.518 | 0.545 | 0.468 | 0.471 | 0.395 | 0.494 | 0.437 | 0.398 | 0.443 | 0.331 | 0.422 | 0.382 | 0.382 | 0.322 |
| 186 | 0.663 | 0.521 | 0.482 | 0.505 | 0.500 | 0.489 | 0.515 | 0.440 | 0.444 | 0.368 | 0.465 | 0.411 | 0.372 | 0.416 | 0.306 | 0.394 | 0.356 | 0.355 | 0.298 |
| 198 | 0.637 | 0.496 | 0.458 | 0.481 | 0.473 | 0.461 | 0.485 | 0.413 | 0.418 | 0.343 | 0.438 | 0.387 | 0.347 | 0.391 | 0.283 | 0.368 | 0.331 | 0.331 | 0.275 |
| 210 | 0.612 | 0.472 | 0.436 | 0.459 | 0.448 | 0.433 | 0.457 | 0.387 | 0.394 | 0.320 | 0.411 | 0.364 | 0.324 | 0.367 | 0.261 | 0.342 | 0.308 | 0.307 | 0.254 |
| 222 | 0.586 | 0.448 | 0.414 | 0.437 | 0.423 | 0.407 | 0.429 | 0.362 | 0.370 | 0.297 | 0.386 | 0.342 | 0.302 | 0.344 | 0.241 | 0.318 | 0.286 | 0.286 | 0.234 |
| 234 | 0.561 | 0.426 | 0.393 | 0.416 | 0.399 | 0.382 | 0.402 | 0.339 | 0.348 | 0.277 | 0.362 | 0.321 | 0.282 | 0.322 | 0.223 | 0.296 | 0.266 | 0.265 | 0.216 |
| 246 | 0.542 | 0.406 | 0.375 | 0.397 | 0.379 | 0.361 | 0.380 | 0.319 | 0.328 | 0.259 | 0.342 | 0.302 | 0.263 | 0.302 | 0.206 | 0.276 | 0.247 | 0.246 | 0.200 |
| 258 | 0.530 | 0.389 | 0.358 | 0.379 | 0.361 | 0.343 | 0.363 | 0.304 | 0.312 | 0.244 | 0.326 | 0.285 | 0.247 | 0.286 | 0.191 | 0.260 | 0.229 | 0.228 | 0.184 |

$\frac{\text { Notes }}{(1)-(19)}$ Data from U.S. Treasury
ittp://www.treasury.gov/offices/domestic-finance/debt-management/interest-rate/yield_historical_main.shtml
20)-(38) Computed from (1)-(19), by interpolation of rates, compounded for number of months indicated


PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET RESULTS
SECTION C
duration of payout of accident year losses

| Accident Year <br> Age <br> (Months) | Cumulative <br> Paid <br> Development <br> Factor | Cumulative <br> Percent <br> Paid | Incremental <br> Percent <br> Paid | Duration |
| :---: | ---: | :---: | ---: | ---: |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
| 12 | 2.443 | $40.9 \%$ | $40.9 \%$ | 0.20 |
| 24 | 1.413 | $70.8 \%$ | $29.9 \%$ | 0.45 |
| 36 | 1.185 | $84.4 \%$ | $13.6 \%$ | 0.34 |
| 48 | 1.086 | $92.1 \%$ | $7.7 \%$ | 0.27 |
| 60 | 1.039 | $96.2 \%$ | $4.1 \%$ | 0.18 |
| 72 | 1.019 | $98.1 \%$ | $1.9 \%$ | 0.10 |
| 84 | 1.010 | $99.0 \%$ | $0.9 \%$ | 0.06 |
| 96 | 1.005 | $99.5 \%$ | $0.5 \%$ | 0.04 |
| 108 | 1.002 | $99.8 \%$ | $0.3 \%$ | 0.02 |
| 120 | 1.001 | $99.9 \%$ | $0.1 \%$ | 0.01 |
| 132 | 1.001 | $99.9 \%$ | $0.1 \%$ | 0.01 |
| 144 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 156 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 168 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 180 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 192 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 204 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 216 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 228 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 240 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 252 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 264 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
|  |  |  |  |  |
| Total |  |  | $100.0 \%$ | $169.4 \%$ |
|  |  |  |  |  |

Duration (years)
1.6941

Notes
(2) From Exhibit 6
(3) $=1 /(2)$
(4) From (2)
(5) $=(4) *[(1) / 12-0.5]$

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET RESULTS
SECTION C

DEVELOPED INDUSTRY ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Net <br> Booked Ultimate Loss \& ALAE | Average Development Parameter <br> $\mu$ | Variance Development Parameter $\sigma^{2}$ | Net <br> Developed Ultimate Loss \& ALAE | Developed vs Booked Ultimate Loss \& ALAE | Paid Loss \& ALAE | Developed Unpaid Loss \& ALAE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1987 | 29,639,489 | 0.000\% | 0.000\% | 29,639,489 | - | 29,467,912 | 171,577 |
| 1988 | 32,654,526 | 0.000\% | 0.000\% | 32,654,526 | - | 32,484,806 | 169,720 |
| 1989 | 35,904,083 | 0.000\% | 0.000\% | 35,904,083 | - | 35,725,452 | 178,631 |
| 1990 | 38,001,440 | 0.000\% | 0.000\% | 38,001,440 | - | 37,836,187 | 165,253 |
| 1991 | 37,358,272 | 0.000\% | 0.000\% | 37,358,272 | - | 37,202,829 | 155,443 |
| 1992 | 39,284,461 | 0.000\% | 0.000\% | 39,284,461 | - | 39,159,559 | 124,902 |
| 1993 | 41,791,971 | 0.000\% | 0.000\% | 41,791,971 | - | 41,635,331 | 156,640 |
| 1994 | 44,368,818 | 0.000\% | 0.000\% | 44,368,818 | - | 44,215,159 | 153,659 |
| 1995 | 45,677,291 | 0.000\% | 0.000\% | 45,677,291 | - | 45,494,007 | 183,284 |
| 1996 | 46,968,387 | 0.000\% | 0.000\% | 46,968,387 | - | 46,793,738 | 174,649 |
| 1997 | 46,961,444 | 0.000\% | 0.000\% | 46,961,444 | - | 46,777,820 | 183,624 |
| 1998 | 48,069,447 | 0.000\% | 0.000\% | 48,069,447 | - | 47,895,384 | 174,063 |
| 1999 | 51,518,156 | 0.000\% | 0.000\% | 51,518,156 | - | 51,324,356 | 193,800 |
| 2000 | 55,254,295 | -0.027\% | 0.000\% | 55,239,273 | $(15,022)$ | 54,907,512 | 331,761 |
| 2001 | 56,734,057 | -0.068\% | 0.000\% | 56,695,533 | $(38,524)$ | 56,329,466 | 366,067 |
| 2002 | 59,256,413 | -0.169\% | 0.000\% | 59,156,553 | $(99,860)$ | 58,516,357 | 640,196 |
| 2003 | 58,526,059 | -0.352\% | 0.001\% | 58,320,972 | $(205,087)$ | 57,213,665 | 1,107,307 |
| 2004 | 58,523,896 | -0.667\% | 0.004\% | 58,135,908 | $(387,988)$ | 56,213,701 | 1,922,207 |
| 2005 | 60,144,772 | -1.161\% | 0.011\% | 59,453,704 | $(691,068)$ | 55,278,660 | 4,175,044 |
| 2006 | 61,588,607 | -1.914\% | 0.030\% | 60,429,809 | $(1,158,798)$ | 51,754,053 | 8,675,756 |
| 2007 | 65,218,021 | -3.149\% | 0.068\% | 63,217,625 | $(2,000,396)$ | 46,324,452 | 16,893,173 |
| 2008 | 65,469,504 | -5.229\% | 0.147\% | 62,179,641 | $(3,289,863)$ | 26,975,954 | 35,203,687 |
| Total | 1,078,913,409 |  |  | 1,071,026,802 | $(7,886,607)$ | 999,526,360 | 71,500,442 |

Notes
(1) From Exhibit 5, Column 3
(2) From Exhibit 3, Cumulative Average
(3) From Exhibit 4, Variance
(4) $=(1) * \exp [(2)+(3) / 2]$
(5) $=(4)-(1)$
(6) From Exhibit 5, Column 4
(7) $=(4)-(6)$

## INDUSTRY HISTORICAL ULTIMATE LOSS \& ALAE RATIO

Dollars in Thousands

|  | 12 month <br> Booked Ultimate <br> Loss \& ALAE Ratio | PV Factor | 1 - Exp Ratio | Loss Ratio Prior to Adjustment | Loss Ratio Adjustment | Adjusted Loss Ratio | Log of <br> Adjusted Loss Ratio | 12 Month Booked Ultimate Loss | Latest <br> Evaluation Ultimate Loss | Ratio Latest to 12 Month Booked | $\begin{aligned} & \text { Log of } \\ & \text { Ratio } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) |
| 1987 | 84.4\% | 0.893 | 76.2\% | 74.8\% | 0.894 | 66.9\% | -40.3\% | 30,073,940 | 29,639,489 | 0.986 | -0.015 |
| 1988 | 85.9\% | 0.893 | 76.5\% | 75.8\% | 0.894 | 67.8\% | -38.8\% | 33,876,530 | 32,654,526 | 0.964 | -0.037 |
| 1989 | 86.8\% | 0.893 | 76.6\% | 76.5\% | 0.894 | 68.4\% | -37.9\% | 37,233,839 | 35,904,083 | 0.964 | -0.036 |
| 1990 | 87.6\% | 0.893 | 76.6\% | 77.2\% | 0.894 | 69.1\% | -37.0\% | 40,624,863 | 38,001,440 | 0.935 | -0.067 |
| 1991 | 83.7\% | 0.924 | 75.9\% | 77.0\% | 0.894 | 68.9\% | -37.3\% | 41,349,440 | 37,358,272 | 0.903 | -0.102 |
| 1992 | 83.1\% | 0.926 | 76.3\% | 76.3\% | 0.894 | 68.2\% | -38.2\% | 44,368,312 | 39,284,461 | 0.885 | -0.122 |
| 1993 | 82.4\% | 0.932 | 76.7\% | 75.7\% | 0.894 | 67.7\% | -39.0\% | 46,768,470 | 41,791,971 | 0.894 | -0.113 |
| 1994 | 82.1\% | 0.889 | 77.4\% | 71.3\% | 0.894 | 63.8\% | -45.0\% | 48,881,084 | 44,368,818 | 0.908 | -0.097 |
| 1995 | 78.7\% | 0.919 | 76.8\% | 71.2\% | 0.894 | 63.7\% | -45.1\% | 49,635,063 | 45,677,291 | 0.920 | -0.083 |
| 1996 | 76.4\% | 0.911 | 77.2\% | 68.2\% | 0.894 | 61.0\% | -49.5\% | 50,317,796 | 46,968,387 | 0.933 | -0.069 |
| 1997 | 72.9\% | 0.914 | 75.1\% | 67.1\% | 0.894 | 60.0\% | -51.1\% | 49,765,419 | 46,961,444 | 0.944 | -0.058 |
| 1998 | 71.5\% | 0.929 | 74.4\% | 67.5\% | 0.894 | 60.3\% | -50.5\% | 49,240,853 | 48,069,447 | 0.976 | -0.024 |
| 1999 | 75.0\% | 0.907 | 74.7\% | 68.8\% | 0.894 | 61.6\% | -48.5\% | 51,632,511 | 51,518,156 | 0.998 | -0.002 |
| 2000 | 78.9\% | 0.920 | 74.4\% | 73.7\% | 0.894 | 65.9\% | -41.6\% | 54,557,893 | 55,254,295 | 1.013 | 0.012 |
| 2001 | 78.3\% | 0.948 | 76.1\% | 73.8\% | 0.894 | 66.0\% | -41.6\% | 56,991,221 | 56,734,057 | 0.995 | -0.005 |
| 2002 | 76.0\% | 0.968 | 76.0\% | 73.2\% | 0.894 | 65.4\% | -42.4\% | 60,398,169 | 59,256,413 | 0.981 | -0.021 |
| 2003 | 70.9\% | 0.965 | 76.4\% | 67.7\% | 1.000 | 67.7\% | -39.0\% | 61,633,969 | 58,526,059 | 0.950 | -0.055 |
| 2004 | 67.7\% | 0.949 | 75.8\% | 64.1\% | 1.000 | 64.1\% | -44.5\% | 62,276,716 | 58,523,896 | 0.940 | -0.069 |
| 2005 | 67.1\% | 0.932 | 76.0\% | 62.1\% | 1.000 | 62.1\% | -47.6\% | 63,227,347 | 60,144,772 | 0.951 | -0.062 |
| 2006 | 65.8\% | 0.925 | 73.9\% | 62.3\% | 1.000 | 62.3\% | -47.3\% | 62,825,209 | 61,588,607 | 0.980 | -0.039 |
| 2007 | 68.8\% | 0.948 | 74.5\% | 66.2\% | 1.000 | 66.2\% | -41.3\% | 65,552,945 | 65,218,021 | 0.995 | -0.036 |
| 2008 | 69.3\% | 0.984 | 74.4\% | 69.3\% | 1.000 | 69.3\% | -36.6\% | 65,469,504 | 65,469,504 | 1.000 | -0.052 |
| (12) Average |  |  |  |  |  | 65.3\% | -42.7\% |  |  |  |  |
| (13) Variance |  |  |  |  |  |  | 0.221\% |  |  |  | 0.132\% |
| (14) Covariance (lo | of Adjusted Loss Ratio | log of Ratio of | est to 12 month B | oked) |  |  | -0.030\% |  |  |  |  |
| (15) Total Variance | of Adjusted Loss Rati | g) and Ratio of | atest to 12 month | ooked (log) |  |  | 0.292\% |  |  |  |  |

## Notes

(1) Exhibit 1 @ 12 Months / Exhibit 5, Column
(2) 1995-2008 from Exhibit 8, Columns 4-17; 1994 and prior selectec
(3) $=100 \%$ - Exhibit 5, Column 9
(4) $=(1) *(2)_{\text {AYXXXX }} /(2)_{\text {AY2008 }} *(3)_{\text {AY2008 }} /(3)_{\text {AYXXXX }}$
(5) Adjustment of historical loss ratios to normalize for major differences in levels across multi-year period AY 1987-2002: AY 2003-2008 Average / AY 1987-2002 Average; 1.000 for AY 2003-2008
(6) $=(4) *(5)$
(7) $=\operatorname{LN}(6)$
(8) Exhibit 1 @ 12 Months
(9) Exhibit 1 @ 12 Current Evaluation
$(10)=(9) /(8$
11) $=\mathrm{LN}(10)+$ Exhibit 10, Column $2+($ Exhibit 10, Column 3)/2
12) Average of Column 7
13) Variance of Column 7 and Column 11
14) Covariance( Column 7, Column 11)
15) = Row 13, Column 7 + Row 13, Column 7 + $2 \cdot$ Row 14

PRIVATE PASSENGER AUTO LIABILITY

DERIVATION OF INDUSTRY 2008 MARKET VALUE OF RISK PARAMETER ( $\boldsymbol{\lambda}$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\boldsymbol{\lambda}$ )

| 1 - ER | $74.4 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.145 |
| PV | 0.984 |
| Target Loss Ratio | $66.0 \%$ |
| ULR12 | $69.3 \%$ |
| $\mu$ | $-5.229 \%$ |
| $\sigma^{2}$ | $0.147 \%$ |
| $\sigma$ | $3.833 \%$ |
| $D$ | 1.694 |
| $\lambda$ | 0.054 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-36.6 \%$ |
| Combined $\mu$ | $-41.8 \%$ |
| $\sigma_{\text {AY ULR }}^{2}$ | $0.221 \%$ |
| $\sigma_{\text {12-ult }}^{2}$ | $0.132 \%$ |
| Cov(AY ULR, 12-ult) | $-0.030 \%$ |
| Combined $\sigma^{2}$ | $0.292 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.028 |
| (2008 market value of risk) |  |

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE $) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$
Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12 -ult)
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu_{A Y U L R}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma$.

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, 2008 Accident Year

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

PRIVATE PASSENGER AUTO LIABILITY

DERIVATION OF INDUSTRY LONG-TERM MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\lambda$ )

| 1 - ER | $74.4 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.145 |
| PV | 0.984 |
| Target Loss Ratio | $66.0 \%$ |
| ULR12 | $69.3 \%$ |
| $\mu$ | $-5.229 \%$ |
| $\sigma^{2}$ | $0.147 \%$ |
| $\sigma$ | $3.833 \%$ |
| D | 1.694 |
| $\lambda$ | 0.054 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-42.7 \%$ |
| Combined $\mu$ | $-48.0 \%$ |
| $\sigma^{2}{ }_{\text {AY ULR }}$ | $0.221 \%$ |
| $\sigma^{2}{ }_{\text {12-ult }}$ | $0.132 \%$ |
| Cov(AY ULR, 12 -ult) | $-0.030 \%$ |
| Combined $\sigma^{2}$ | $0.292 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.899 |

(long-term market value of risk)

## Notes

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+U L A E) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$

Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12-ult)
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu_{A Y ~ U L R}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma \cdot v(D)$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, Average

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON 2008 MARKET VALUE OF RISK
Dollars in Thousands

|  |  | Industry | Company | Company | Company | Company | Total Largest 100 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Simulated 1997-2008 Unpaid Claims | Aggregate | A | B | C | D | Companies |
| (1) | 25th Percentile | 67,752,753 | 5,054,184 | 3,215,080 | 2,760,737 | 1,415,485 |  |
| (2) | 50th Percentile | 69,656,233 | 5,181,725 | 3,441,110 | 2,969,409 | 1,471,962 |  |
| (3) | 75th Percentile | 71,950,777 | 5,320,588 | 3,642,303 | 3,185,073 | 1,527,469 |  |
| (4) | Average | 69,809,588 | 5,181,427 | 3,429,387 | 2,982,952 | 1,471,132 |  |
| (5) | Standard Deviation | 3,285,611 | 207,864 | 310,479 | 334,987 | 83,228 |  |
| (6) | Simulated Sample $\mu$ <br> = Average[ $\log ($ simulated unpaid claims)] | 18.060 | 15.460 | 15.044 | 14.903 | 14.200 |  |
| (7) | Simulated Sample $\sigma$ <br> = Standard Deviation[log(simulated unpaid claims)] | 0.047 | 0.040 | 0.091 | 0.112 | 0.056 |  |
| (8) | Expected Unpaid Claims $=\exp \left(\mu+1 / 2 \cdot \sigma^{2}\right)$ | 69,829,093 | 5,182,698 | 3,431,420 | 2,984,903 | 1,471,612 | 66,803,283 |
| (9) | Industry Market Value of Risk ( $\lambda_{1}$ ) | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 |  |
| (10) | Duration of Unpaid Claims (D) | 1.522 | 1.524 | 1.525 | 1.522 | 1.525 |  |
| (11) | Risk Adjusted Expected Unpaid Claims $=\exp \left(\mu+\frac{1}{2} \cdot \sigma^{2}+\lambda_{1} \cdot \sigma \cdot V D\right)$ | 69,940,418 | 5,189,794 | 3,442,081 | 2,996,308 | 1,474,448 | 66,980,222 |
| (12) | Risk Margin = (11) - (8) | 111,324 | 7,096 | 10,661 | 11,405 | 2,836 | 176,939 |
| (13) | Risk Margin \% of Expected Unpaid Claims = (11) / (8) | 0.2\% | 0.1\% | 0.3\% | 0.4\% | 0.2\% | 0.3\% |

## PRIVATE PASSENGER AUTO LIABILITY

RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands


PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands

## Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Total <br> Accident Years 1997-2008 | Accident <br> Year <br> 2008 | Accident <br> Year <br> 2007 | Accident Year 2006 | Accident <br> Year <br> 2005 | Accident Year 2004 | Accident Year 2003 | Accident Year 2002 | Accident Year 2001 | Accident Year 2000 | Accident Year 1999 | Accident <br> Year <br> 1998 | Accident Year 1997 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| Year 1 | 33,070,948 | 17,070,668 | 7,510,225 | 4,128,791 | 2,066,515 | 896,116 | 493,989 | 276,360 | 196,641 | 166,381 | 87,758 | 93,396 | 84,108 |
| Year 2 | 16,325,808 | 7,768,992 | 4,276,380 | 2,182,133 | 958,401 | 433,605 | 255,639 | 147,542 | 108,889 | 66,618 | 42,224 | 44,928 | 40,456 |
| Year 3 | 8,739,228 | 4,423,724 | 2,260,136 | 1,012,022 | 463,743 | 224,390 | 136,480 | 81,701 | 43,598 | 32,053 | 20,312 | 21,610 | 19,458 |
| Year 4 | 4,409,887 | 2,338,010 | 1,048,198 | 489,688 | 239,987 | 119,797 | 75,575 | 32,712 | 20,977 | 15,419 | 9,770 | 10,394 | 9,358 |
| Year 5 | 2,117,087 | 1,084,314 | 507,193 | 253,414 | 128,123 | 66,337 | 30,260 | 15,740 | 10,091 | 7,416 | 4,699 | 4,999 | 4,501 |
| Year 6 | 1,057,322 | 524,669 | 262,472 | 135,292 | 70,948 | 26,561 | 14,559 | 7,571 | 4,854 | 3,567 | 2,260 | 2,404 | 2,165 |
| Year 7 | 545,728 | 271,516 | 140,128 | 74,917 | 28,407 | 12,780 | 7,004 | 3,642 | 2,334 | 1,716 | 1,087 | 1,156 | 1,041 |
| Year 8 | 281,011 | 144,956 | 77,595 | 29,996 | 13,668 | 6,148 | 3,369 | 1,752 | 1,123 | 825 | 523 | 556 | 501 |
| Year 9 | 139,461 | 80,269 | 31,069 | 14,433 | 6,575 | 2,957 | 1,620 | 842 | 540 | 397 | 251 | 267 | 241 |
| Year 10 | 60,723 | 32,139 | 14,949 | 6,943 | 3,162 | 1,422 | 779 | 405 | 260 | 191 | 121 | 129 | 223 |
| Year 11 | 29,163 | 15,464 | 7,191 | 3,339 | 1,521 | 684 | 375 | 195 | 125 | 92 | 58 | 119 | - |
| Year 12 | 13,996 | 7,439 | 3,459 | 1,606 | 732 | 329 | 180 | 94 | 60 | 44 | 54 | - | - |
| Year 13 | 6,726 | 3,578 | 1,664 | 772 | 352 | 158 | 87 | 45 | 29 | 41 | - | - | - |
| Year 14 | 3,228 | 1,721 | 800 | 372 | 169 | 76 | 42 | 22 | 27 | - | - | - | - |
| Year 15 | 1,549 | 828 | 385 | 179 | 81 | 37 | 20 | 20 | - | - | - | - | - |
| Year 16 | 744 | 398 | 185 | 86 | 39 | 18 | 19 | - | - | - | - | - | - |
| Year 17 | 357 | 191 | 89 | 41 | 19 | 16 | - | - | - | - | - | - | - |
| Year 18 | 172 | 92 | 43 | 20 | 17 | - | - | - | - | - | - | - | - |
| Year 19 | 83 | 44 | 21 | 18 | - | - | - | - | - | - | - | - | - |
| Year 20 | 40 | 21 | 19 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 20 | 20 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total | 66,803,283 | 33,769,053 | 16,142,201 | 8,334,064 | 3,982,460 | 1,791,430 | 1,019,997 | 568,643 | 389,549 | 294,759 | 169,117 | 179,959 | 162,052 |

Notes
Total equals expected unpaid by accident year
(2) - (13) Based on expected unpaid by accident year and payout pattern from Exhibit 8

PRIVATE PASSENGER AUTO LIABILITY
INDUSTRY NET RESULTS
DISCOUNTED PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands
Discounted Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Discount Factor | Total Accident Years 1997-2008 |  | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2007 \\ \hline \end{gathered}$ | Accident Year 2006 |  | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2004 \\ \hline \end{gathered}$ | Accident Year 2003 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2002 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2001 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2000 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1999 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1998 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1997 \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| Year 1 | 0.999 | 33,026,393 | 17,047,669 | 7,500,107 | 4,123,229 | 2,063,731 | 894,908 | 493,324 | 275,988 | 196,376 | 166,157 | 87,639 | 93,271 | 83,995 |
| Year 2 | 0.992 | 16,188,417 | 7,703,612 | 4,240,392 | 2,163,769 | 950,336 | 429,956 | 253,488 | 146,301 | 107,973 | 66,057 | 41,869 | 44,550 | 40,115 |
| Year 3 | 0.978 | 8,549,888 | 4,327,882 | 2,211,169 | 990,096 | 453,695 | 219,529 | 133,523 | 79,931 | 42,654 | 31,358 | 19,872 | 21,142 | 19,036 |
| Year 4 | 0.961 | 4,238,720 | 2,247,262 | 1,007,513 | 470,682 | 230,672 | 115,147 | 72,642 | 31,443 | 20,163 | 14,820 | 9,391 | 9,990 | 8,995 |
| Year 5 | 0.939 | 1,987,591 | 1,017,990 | 476,170 | 237,913 | 120,287 | 62,279 | 28,409 | 14,777 | 9,474 | 6,963 | 4,412 | 4,693 | 4,226 |
| Year 6 | 0.915 | 967,357 | 480,026 | 240,139 | 123,780 | 64,911 | 24,301 | 13,321 | 6,927 | 4,441 | 3,264 | 2,068 | 2,200 | 1,981 |
| Year 7 | 0.891 | 486,287 | 241,943 | 124,865 | 66,757 | 25,313 | 11,388 | 6,241 | 3,245 | 2,080 | 1,529 | 969 | 1,030 | 928 |
| Year 8 | 0.866 | 243,418 | 125,564 | 67,215 | 25,983 | 11,839 | 5,325 | 2,918 | 1,517 | 973 | 715 | 453 | 482 | 434 |
| Year 9 | 0.841 | 117,268 | 67,495 | 26,125 | 12,136 | 5,529 | 2,486 | 1,362 | 708 | 454 | 334 | 211 | 225 | 203 |
| Year 10 | 0.814 | 49,443 | 26,169 | 12,172 | 5,653 | 2,575 | 1,158 | 635 | 330 | 211 | 155 | 98 | 105 | 182 |
| Year 11 | 0.788 | 22,992 | 12,192 | 5,669 | 2,633 | 1,199 | 539 | 295 | 154 | 98 | 72 | 46 | 94 | - |
| Year 12 | 0.764 | 10,691 | 5,682 | 2,642 | 1,227 | 559 | 251 | 138 | 72 | 46 | 34 | 41 | - | - |
| Year 13 | 0.739 | 4,970 | 2,644 | 1,229 | 571 | 260 | 117 | 64 | 33 | 21 | 30 | - | - | - |
| Year 14 | 0.714 | 2,304 | 1,228 | 571 | 265 | 121 | 54 | 30 | 15 | 19 | - | - | - | - |
| Year 15 | 0.688 | 1,066 | 570 | 265 | 123 | 56 | 25 | 14 | 14 | - | - | - | - | - |
| Year 16 | 0.663 | 493 | 264 | 123 | 57 | 26 | 12 | 12 | - | - | - | - | - | - |
| Year 17 | 0.637 | 227 | 122 | 57 | 26 | 12 | 10 | - | - | - | - | - | - | - |
| Year 18 | 0.612 | 105 | 56 | 26 | 12 | 11 | - | - | - | - | - | - | - | - |
| Year 19 | 0.586 | 49 | 26 | 12 | 11 | - | - | - | - | - | - | - | - | - |
| Year 20 | 0.561 | 23 | 12 | 11 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 0.542 | 11 | 11 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | 0.530 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total |  | 65,897,714 | 33,308,417 | 15,916,472 | 8,224,924 | 3,931,131 | 1,767,486 | 1,006,415 | 561,454 | 384,984 | 291,488 | 167,069 | 177,781 | 160,094 |

[^5](3) - (14) Product of Column 1 and Exhibit 14, Columns 2-13

PRIVATE PASSENGER AUTO LIABILITY
SECTION C
INDUSTRY NET RESULTS
NET IMPACT OF RISK MARGINS AND DISCOUNT FOR LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands


Notes
(3) From Exhibit 13B, Row 13, Total Largest 100 U.S. Insurers
(4) From Exhibit 15, Total by Accident Year
(5) $=(4) /(2)-1$
(6) $=(2)$ Total $*[1+(3)$ Total $]$ [ $1+(5)$ Total $]$
(7) $=(6)$ Total $/(1)$ Total -1


## Notes

Data from SNL Financial LC
1996-2008 Annual Statements
Industry Total Workers Compensation
Schedule P, Part 2D

WORKERS COMPENSATION
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
LINK RATIOS


From Exhibit 1, ratio of successive ultimate loss estimates by accident year

WORKERS COMPENSATION
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
CUMULATIVE DEVELOPMENT IN ULTIMATE LOSS ESTIMATES BASED ON LOG OF LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | 1.229\% | 1.260\% | 0.891\% | 1.477\% | 1.196\% | 0.509\% | 0.458\% | 0.303\% | 0.548\% |
| 1988 | 2.723\% | 1.831\% | 1.479\% | 1.430\% | 0.504\% | 0.307\% | 0.736\% | 0.380\% | -0.613\% |
| 1989 | 3.431\% | 2.414\% | 1.325\% | 0.669\% | -0.197\% | 0.588\% | 0.536\% | -0.201\% | -0.130\% |
| 1990 | 3.835\% | 1.443\% | 0.108\% | 0.130\% | -0.472\% | 0.417\% | -0.170\% | -0.086\% | -0.355\% |
| 1991 | 0.623\% | -1.770\% | -2.256\% | -0.709\% | -0.274\% | -0.250\% | -0.316\% | -0.267\% | -0.470\% |
| 1992 | -2.016\% | -5.822\% | -4.929\% | -1.787\% | -0.610\% | -0.547\% | -0.412\% | -0.500\% | -0.477\% |
| 1993 | -4.130\% | -4.203\% | -5.954\% | -1.730\% | -1.403\% | -1.610\% | -1.128\% | -0.425\% | -0.155\% |
| 1994 | -4.420\% | -4.130\% | -6.440\% | -2.659\% | -1.205\% | -1.552\% | -0.154\% | -0.546\% | 0.639\% |
| 1995 | -4.010\% | -3.342\% | -4.228\% | -0.717\% | -0.745\% | -0.463\% | -0.738\% | 0.347\% | 0.301\% |
| 1996 | -2.660\% | -0.431\% | -2.950\% | -0.776\% | -0.362\% | 0.423\% | 0.815\% | 0.390\% | 1.317\% |
| 1997 | 3.011\% | 0.808\% | -0.013\% | 0.421\% | 1.402\% | 0.409\% | 1.186\% | 1.409\% | 0.530\% |
| 1998 | 2.316\% | 2.814\% | 1.916\% | 2.230\% | 1.770\% | 1.345\% | 1.672\% | 0.869\% | 0.762\% |
| 1999 | 4.709\% | 4.299\% | 4.391\% | 2.150\% | 1.008\% | 2.690\% | 0.910\% | 1.368\% | -0.112\% |
| 2000 | 4.442\% | 4.297\% | 3.153\% | 2.736\% | 2.847\% | 1.359\% | 1.235\% | -0.098\% |  |
| 2001 | 1.879\% | 1.126\% | 1.094\% | 3.846\% | 0.935\% | 1.556\% | 0.683\% |  |  |
| 2002 | -0.055\% | 0.959\% | 1.352\% | 0.827\% | 0.463\% | 0.455\% |  |  |  |
| 2003 | -5.936\% | -1.989\% | 0.289\% | -0.109\% | 0.562\% |  |  |  |  |
| 2004 | -7.150\% | -3.713\% | -3.424\% | -1.073\% |  |  |  |  |  |
| 2005 | -7.019\% | -6.148\% | -2.445\% |  |  |  |  |  |  |
| 2006 | -5.975\% | -2.504\% |  |  |  |  |  |  |  |
| 2007 | -1.866\% |  |  |  |  |  |  |  |  |
| Average | -0.811\% | -0.640\% | -0.876\% | 0.353\% | 0.319\% | 0.352\% | 0.354\% | 0.210\% | 0.137\% |
|  | 12-108 | 24-108 | 36-108 | 48-108 | 60-108 | 72-108 | 84-108 | 96-108 | 108-108 |
| Cumulative Average | -0.601\% | 0.210\% | 0.850\% | 1.726\% | 1.373\% | 1.054\% | 0.702\% | 0.348\% | 0.137\% |

[^6]WORKERS COMPENSATION
SECTION D
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE

## VARIANCE-COVARIANCE MATRIX OF LOG OF INCREMENTAL LINK RATIOS

| Months of Maturity | 12-108 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 | 120-Ultimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12-108 | 0.153\% | 0.109\% | 0.089\% | 0.045\% | 0.023\% | 0.026\% | 0.017\% | 0.010\% | -0.005\% | 0.000\% |
| 24-36 | 0.109\% | 0.099\% | 0.087\% | 0.043\% | 0.025\% | 0.028\% | 0.019\% | 0.011\% | 0.001\% | 0.000\% |
| 36-48 | 0.089\% | 0.087\% | 0.093\% | 0.047\% | 0.028\% | 0.031\% | 0.020\% | 0.012\% | -0.002\% | 0.000\% |
| 48-60 | 0.045\% | 0.043\% | 0.047\% | 0.028\% | 0.015\% | 0.016\% | 0.010\% | 0.006\% | 0.000\% | 0.000\% |
| 60-72 | 0.023\% | 0.025\% | 0.028\% | 0.015\% | 0.012\% | 0.009\% | 0.008\% | 0.004\% | 0.001\% | 0.000\% |
| 72-84 | 0.026\% | 0.028\% | 0.031\% | 0.016\% | 0.009\% | 0.011\% | 0.007\% | 0.005\% | 0.000\% | 0.000\% |
| 84-96 | 0.017\% | 0.019\% | 0.020\% | 0.010\% | 0.008\% | 0.007\% | 0.006\% | 0.003\% | 0.002\% | 0.000\% |
| 96-108 | 0.010\% | 0.011\% | 0.012\% | 0.006\% | 0.004\% | 0.005\% | 0.003\% | 0.004\% | 0.001\% | 0.000\% |
| 108-120 | -0.005\% | 0.001\% | -0.002\% | 0.000\% | 0.001\% | 0.000\% | 0.002\% | 0.001\% | 0.003\% | 0.000\% |
| 120-Ultimate | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| Variance ( $\boldsymbol{\sigma}^{\mathbf{2}}$ ) | 1.912\% | 1.132\% | 0.605\% | 0.240\% | 0.116\% | 0.060\% | 0.025\% | 0.009\% | 0.003\% | 0.000\% |

Notes
From Exhibit 3, covariance of errors at given maturity with errors at all other maturities
Covariances above diagonal are symmetric with those below
Variance is sum of matrix for all maturities greater than or equal to maturity shown in column

WORKERS COMPENSATION
INDUSTRY NET RESULTS
SELECTION OF LOSS \& ALAE RATIO, ULAE FACTOR, AND LOSS \& LAE RATIO
Dollars in Thousands

|  | Net <br> Earned Premium | Net Ultimate Loss \& LAE | Net Ultimate Loss \& ALAE | $\begin{gathered} \text { Net } \\ \text { Paid } \\ \text { Loss \& ALAE } \end{gathered}$ | Net <br> Unpaid Loss \& ALAE | Net Ultimate Loss \& LAE Ratio | Net <br> Ultimate Loss \& ALAE Ratio | ULAE <br> Factor | Underwriting <br> Expense Ratio |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) |
| 1987 | 22,943,227 | 21,303,668 | 20,397,951 | 17,858,804 | 2,539,147 | 92.9\% | 88.9\% | 1.044 | 24.4\% | 75.6\% |
| 1988 | 26,609,598 | 25,433,972 | 24,381,050 | 21,756,428 | 2,624,622 | 95.6\% | 91.6\% | 1.043 | 24.2\% | 75.8\% |
| 1989 | 29,386,638 | 28,422,089 | 27,150,337 | 24,332,493 | 2,817,844 | 96.7\% | 92.4\% | 1.047 | 23.5\% | 76.5\% |
| 1990 | 33,394,865 | 31,296,427 | 29,864,671 | 26,902,429 | 2,962,242 | 93.7\% | 89.4\% | 1.048 | 22.7\% | 77.3\% |
| 1991 | 34,203,477 | 28,975,268 | 27,425,492 | 24,762,776 | 2,662,716 | 84.7\% | 80.2\% | 1.057 | 23.4\% | 76.6\% |
| 1992 | 33,052,386 | 24,090,547 | 22,585,089 | 20,204,109 | 2,380,980 | 72.9\% | 68.3\% | 1.067 | 24.4\% | 75.6\% |
| 1993 | 31,341,767 | 20,869,805 | 19,456,020 | 17,331,393 | 2,124,627 | 66.6\% | 62.1\% | 1.073 | 25.1\% | 74.9\% |
| 1994 | 28,101,444 | 18,560,558 | 17,193,950 | 15,148,767 | 2,045,183 | 66.0\% | 61.2\% | 1.079 | 28.0\% | 72.0\% |
| 1995 | 25,949,262 | 17,952,050 | 16,448,810 | 14,390,813 | 2,057,997 | 69.2\% | 63.4\% | 1.091 | 29.6\% | 70.4\% |
| 1996 | 25,443,406 | 18,880,422 | 17,219,810 | 14,983,956 | 2,235,854 | 74.2\% | 67.7\% | 1.096 | 30.0\% | 70.0\% |
| 1997 | 23,732,368 | 20,413,443 | 18,665,040 | 16,102,359 | 2,562,681 | 86.0\% | 78.6\% | 1.094 | 31.5\% | 68.5\% |
| 1998 | 22,961,874 | 22,396,051 | 20,543,308 | 17,570,425 | 2,972,883 | 97.5\% | 89.5\% | 1.090 | 33.0\% | 67.0\% |
| 1999 | 21,246,093 | 22,441,898 | 20,650,698 | 17,762,207 | 2,888,491 | 105.6\% | 97.2\% | 1.087 | 34.1\% | 65.9\% |
| 2000 | 23,150,128 | 23,717,866 | 21,784,432 | 18,528,864 | 3,255,568 | 102.5\% | 94.1\% | 1.089 | 31.5\% | 68.5\% |
| 2001 | 25,445,547 | 23,525,229 | 21,514,904 | 17,595,713 | 3,919,191 | 92.5\% | 84.6\% | 1.093 | 29.7\% | 70.3\% |
| 2002 | 28,612,523 | 22,375,942 | 20,513,706 | 16,314,355 | 4,199,351 | 78.2\% | 71.7\% | 1.091 | 26.1\% | 73.9\% |
| 2003 | 31,747,597 | 23,093,386 | 21,123,786 | 15,929,976 | 5,193,810 | 72.7\% | 66.5\% | 1.093 | 24.2\% | 75.8\% |
| 2004 | 35,768,867 | 23,242,992 | 21,318,142 | 15,081,378 | 6,236,764 | 65.0\% | 59.6\% | 1.090 | 23.6\% | 76.4\% |
| 2005 | 38,350,984 | 24,294,075 | 22,200,172 | 14,358,206 | 7,841,966 | 63.3\% | 57.9\% | 1.094 | 23.8\% | 76.2\% |
| 2006 | 41,244,380 | 27,900,594 | 25,554,253 | 13,950,057 | 11,604,196 | 67.6\% | 62.0\% | 1.092 | 22.4\% | 77.6\% |
| 2007 | 39,408,672 | 29,008,693 | 26,730,744 | 11,208,806 | 15,521,938 | 73.6\% | 67.8\% | 1.085 | 26.3\% | 73.7\% |
| 2008 | 37,234,381 | 28,574,906 | 26,279,616 | 5,279,866 | 20,999,750 | 76.7\% | 70.6\% | 1.087 | 26.8\% | 73.2\% |
| Selected |  |  |  |  | 111,647,801 |  | 70.6\% | 1.090 |  | 73.2\% |

Notes
1), (2) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1D
(3) Exhibit 1, Latest Evaluation
(4) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1D
$(5)=(3)-(4)$
(6) $=(2) /(1)$
$(7)=(3) /(1)$; Selected from 2008
(8) $=(6) /(7)$; Selected from 2005-2007 Average
(9) From AM Best Aggregates and Averages, includes policyholder dividends
(10) $=1$ - (9); Selected from 2008

WORKERS COMPENSATION
INDUSTRY PAYOUT PATTERN (PAID LOSS \& ALAE)
SECTION D EXHIBIT 6

## Dollars in Thousands

Months of Maturit
$\frac{\text { Accident Year }}{1987}$


1988
1989 1990 1991 1993 1996
1997 1997
2000

2004
2006
2007

## 2008

$3,865,9 \frac{12}{76} \quad 9,032,0 \frac{24}{11}$
6,406,012

6,086,295
4,898,291
$4,205,226$
4,
$4,205,226$
$3,812,136$
$3,708,840$ $3,708,840$
$3,840,629$
$3,965,710$
$4,595,612$
4,161,594
$4,463,586$
4,464,
$4,464,626$
4,161,055
$9,56,201$
$\begin{array}{ll}4,199,742 & 9,309,273\end{array}$
$\begin{array}{llll}4,534,769 & 9,642,587 & 12,278,263 \\ 4,770,668 & 9,74,815 & 12,950,057\end{array}$
$\begin{array}{lrr}4,770,668 & 9,746,848 & 12,562,596\end{array}$
$\begin{array}{lll}5,001,579 & 10,519,615 & 13,950,057\end{array}$
$5,109,809$
$5,279,866$
$11,208,806$

| Age-to-Age Paid Loss Development |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | 2.336 | 1.349 | 1.163 | 1.090 | 1.055 | 1.034 | 1.026 | 1.019 | 1.015 |
| 1988 | 2.359 | 1.356 | 1.158 | 1.086 | 1.047 | 1.034 | 1.024 | 1.017 | 1.012 |
| 1989 | 2.432 | 1.347 | 1.156 | 1.081 | 1.048 | 1.031 | 1.023 | 1.013 | 1.015 |
| 1990 | 2.230 | 1.353 | 1.146 | 1.077 | 1.044 | 1.029 | 1.020 | 1.017 | 1.012 |
| 1991 | 2.208 | 1.320 | 1.141 | 1.080 | 1.047 | 1.029 | 1.020 | 1.015 | 1.015 |
| 1992 | 2.221 | 1.309 | 1.151 | 1.080 | 1.045 | 1.035 | 1.021 | 1.021 | 1.012 |
| 1993 | 2.215 | 1.318 | 1.141 | 1.075 | 1.054 | 1.031 | 1.031 | 1.016 | 1.012 |
| 1994 | 2.201 | 1.299 | 1.128 | 1.083 | 1.045 | 1.034 | 1.024 | 1.015 | 1.014 |
| 1995 | 2.123 | 1.279 | 1.162 | 1.072 | 1.053 | 1.032 | 1.021 | 1.018 | 1.015 |
| 1996 | 2.100 | 1.325 | 1.133 | 1.085 | 1.044 | 1.034 | 1.020 | 1.018 | 1.017 |
| 1997 | 2.245 | 1.285 | 1.141 | 1.072 | 1.049 | 1.032 | 1.029 | 1.018 | 1.015 |
| 1998 | 2.055 | 1.317 | 1.121 | 1.084 | 1.052 | 1.037 | 1.026 | 1.020 | 1.018 |
| 1999 | 2.294 | 1.325 | 1.147 | 1.069 | 1.036 | 1.032 | 1.026 | 1.020 | 1.024 |
| 2000 | 2.292 | 1.325 | 1.134 | 1.073 | 1.038 | 1.034 | 1.025 | 1.021 |  |
| 2001 | 2.275 | 1.333 | 1.136 | 1.047 | 1.030 | 1.028 | 1.033 |  |  |
| 2002 | 2.255 | 1.317 | 1.132 | 1.079 | 1.039 | 1.041 |  |  |  |
| 2003 | 2.217 | 1.313 | 1.141 | 1.081 | 1.057 |  |  |  |  |
| 2004 | 2.126 | 1.273 | 1.134 | 1.083 |  |  |  |  |  |
| 2005 | 2.043 | 1.289 | 1.143 |  |  |  |  |  |  |
| 2006 | 2.103 | 1.326 |  |  |  |  |  |  |  |
| 2007 | 2.194 |  |  |  |  |  |  |  |  |
| Averages |  |  |  |  |  |  |  |  |  |
| $10-\mathrm{Yr}$ Weighted | 2.182 | 1.311 | 1.136 | 1.074 | 1.044 | 1.033 | 1.026 | 1.018 | 1.015 |
| $10-\mathrm{Yr}$ Straight | 2.185 | 1.310 | 1.136 | 1.074 | 1.044 | 1.033 | 1.026 | 1.018 | 1.015 |
| Selected | 2.182 | 1.311 | 1.136 | 1.074 | 1.044 | 1.033 | 1.026 | 1.018 | 1.015 |

Age-to-Age Paid Loss Development

| Fitted Age-to-Ultimate |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Curve Fits: | R-squared | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| Weibull | 96.8\% | 1.015 | 1.010 | 1.006 | 1.004 | 1.003 | 1.002 | 1.001 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 |
| Power Curve | 93.0\% | 1.017 | 1.011 | 1.007 | 1.004 | 1.003 | 1.002 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| Inverse Power Curve | 99.9\% | 1.097 | 1.084 | 1.073 | 1.064 | 1.057 | 1.050 | 1.045 | 1.040 | 1.036 | 1.032 | 1.028 | 1.025 | 1.023 |


| Selected Pattern | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age-to-Age | 2.182 | 1.311 | 1.136 | 1.074 | 1.044 | 1.033 | 1.026 | 1.018 | 1.015 | 1.012 | 1.010 | 1.008 | 1.007 | 1.006 | 1.005 | 1.005 | 1.004 | 1.004 | 1.003 | 1.003 | 1.025 |  |
| Age-to-Ultimate | 4.377 | 2.006 | 1.531 | 1.347 | 1.254 | 1.202 | 1.163 | 1.134 | 1.113 | 1.097 | 1.084 | 1.073 | 1.064 | 1.057 | 1.050 | 1.045 | 1.040 | 1.036 | 1.032 | 1.028 | 1.025 | 1.000 |
| Cumulative \% Paid | 22.8\% | 49.8\% | 65.3\% | 74.2\% | 79.7\% | 83.2\% | 86.0\% | 88.2\% | 89.8\% | 91.2\% | 92.3\% | 93.2\% | 94.0\% | 94.6\% | 95.2\% | 95.7\% | 96.2\% | 96.6\% | 96.9\% | 97.2\% | 97.5\% | 100.0\% |
| Incremental \% Paid | 22.8\% | 27.0\% | 15.5\% | 8.9\% | 5.5\% | 3.5\% | 2.8\% | 2.2\% | 1.6\% | 1.4\% | 1.1\% | 0.9\% | 0.8\% | 0.7\% | 0.6\% | 0.5\% | 0.4\% | 0.4\% | 0.4\% | 0.3\% | 0.3\% | 2.5 |

[^7]|  | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Duration | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) |
| 1 month | 0.11\% | 2.76\% | 4.75\% | 4.01\% | 1.89\% | 0.90\% | 1.20\% | 1.68\% | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |
| 3 months | 0.11\% | 3.36\% | 5.02\% | 4.08\% | 2.22\% | 0.95\% | 1.22\% | 1.74\% | 5.89\% | 5.33\% | 4.48\% | 5.36\% | 5.21\% | 5.10\% | 5.68\% | 3.07\% | 3.15\% | 3.96\% | 6.63\% |
| 6 months | 0.27\% | 3.49\% | 5.09\% | 4.37\% | 2.59\% | 1.02\% | 1.23\% | 1.83\% | 5.70\% | 5.74\% | 4.55\% | 5.45\% | 5.33\% | 5.17\% | 6.51\% | 3.30\% | 3.38\% | 4.00\% | 6.73\% |
| 1 year | 0.37\% | 3.34\% | 5.00\% | 4.38\% | 2.75\% | 1.26\% | 1.32\% | 2.17\% | 5.32\% | 5.98\% | 4.53\% | 5.51\% | 5.51\% | 5.18\% | 7.20\% | 3.63\% | 3.61\% | 4.12\% | 6.82\% |
| 2 years | 0.76\% | 3.05\% | 4.82\% | 4.41\% | 3.08\% | 1.84\% | 1.61\% | 3.07\% | 5.11\% | 6.24\% | 4.54\% | 5.66\% | 5.88\% | 5.18\% | 7.69\% | 4.25\% | 4.56\% | 4.77\% | 7.15\% |
| 3 years | 1.00\% | 3.07\% | 4.74\% | 4.37\% | 3.25\% | 2.37\% | 1.99\% | 3.59\% | 5.06\% | 6.29\% | 4.55\% | 5.68\% | 6.04\% | 5.25\% | 7.80\% | 4.58\% | 5.12\% | 5.11\% | 7.40\% |
| 5 years | 1.55\% | 3.45\% | 4.70\% | 4.35\% | 3.63\% | 3.25\% | 2.78\% | 4.38\% | 4.99\% | 6.36\% | 4.56\% | 5.71\% | 6.21\% | 5.38\% | 7.83\% | 5.21\% | 6.04\% | 5.93\% | 7.68\% |
| 7 years | 1.87\% | 3.70\% | 4.70\% | 4.36\% | 3.94\% | 3.77\% | 3.36\% | 4.84\% | 5.16\% | 6.55\% | 4.73\% | 5.77\% | 6.34\% | 5.49\% | 7.84\% | 5.53\% | 6.43\% | 6.38\% | 8.00\% |
| 10 years | 2.25\% | 4.04\% | 4.71\% | 4.39\% | 4.24\% | 4.27\% | 3.83\% | 5.07\% | 5.12\% | 6.45\% | 4.65\% | 5.75\% | 6.43\% | 5.58\% | 7.84\% | 5.83\% | 6.70\% | 6.71\% | 8.08\% |
| 20 years | 3.05\% | 4.50\% | 4.91\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.74\% | 5.59\% | 6.83\% | 5.39\% | 6.02\% | 6.73\% | 6.01\% | 8.02\% | 6.48\% | 7.05\% | 7.06\% | 8.17\% |
| 30 years | 2.69\% | 4.45\% | 4.81\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.48\% | 5.46\% | 6.48\% | 5.09\% | 5.93\% | 6.65\% | 5.96\% | 7.89\% | 6.35\% | 7.40\% | 7.41\% | 8.26\% |


| Discount Factor | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (months) | (20) | (21) | (22) | (23) | (24) | (25) | (26) | (27) | (28) | (29) | (30) | (31) | (32) | (33) | (34) | (35) | (36) | (37) | (38) |
| 6 | 0.999 | 0.983 | 0.975 | 0.979 | 0.987 | 0.995 | 0.994 | 0.991 | 0.973 | 0.972 | 0.978 | 0.974 | 0.974 | 0.975 | 0.969 | 0.984 | 0.984 | 0.981 | 0.968 |
| 18 | 0.992 | 0.954 | 0.931 | 0.938 | 0.958 | 0.977 | 0.978 | 0.962 | 0.927 | 0.915 | 0.936 | 0.922 | 0.920 | 0.927 | 0.898 | 0.944 | 0.942 | 0.937 | 0.904 |
| 30 | 0.978 | 0.927 | 0.890 | 0.898 | 0.925 | 0.949 | 0.956 | 0.921 | 0.883 | 0.859 | 0.895 | 0.871 | 0.865 | 0.881 | 0.830 | 0.898 | 0.889 | 0.886 | 0.839 |
| 42 | 0.961 | 0.897 | 0.851 | 0.861 | 0.891 | 0.914 | 0.927 | 0.878 | 0.842 | 0.807 | 0.856 | 0.824 | 0.813 | 0.835 | 0.769 | 0.850 | 0.833 | 0.834 | 0.777 |
| 54 | 0.939 | 0.862 | 0.813 | 0.825 | 0.855 | 0.874 | 0.892 | 0.832 | 0.803 | 0.758 | 0.818 | 0.779 | 0.764 | 0.791 | 0.713 | 0.801 | 0.776 | 0.778 | 0.719 |
| 66 | 0.915 | 0.827 | 0.777 | 0.791 | 0.819 | 0.833 | 0.853 | 0.785 | 0.763 | 0.711 | 0.781 | 0.736 | 0.717 | 0.749 | 0.661 | 0.753 | 0.721 | 0.724 | 0.663 |
| 78 | 0.891 | 0.793 | 0.742 | 0.758 | 0.782 | 0.793 | 0.814 | 0.741 | 0.723 | 0.664 | 0.742 | 0.695 | 0.672 | 0.708 | 0.612 | 0.708 | 0.671 | 0.674 | 0.609 |
| 90 | 0.866 | 0.758 | 0.709 | 0.726 | 0.746 | 0.753 | 0.776 | 0.700 | 0.686 | 0.622 | 0.708 | 0.657 | 0.630 | 0.669 | 0.568 | 0.665 | 0.625 | 0.626 | 0.561 |
| 102 | 0.841 | 0.724 | 0.677 | 0.695 | 0.711 | 0.715 | 0.741 | 0.663 | 0.653 | 0.586 | 0.677 | 0.621 | 0.591 | 0.633 | 0.526 | 0.625 | 0.582 | 0.583 | 0.518 |
| 114 | 0.814 | 0.690 | 0.646 | 0.665 | 0.677 | 0.677 | 0.705 | 0.627 | 0.622 | 0.551 | 0.649 | 0.588 | 0.554 | 0.598 | 0.488 | 0.586 | 0.542 | 0.542 | 0.479 |
| 126 | 0.788 | 0.658 | 0.616 | 0.636 | 0.645 | 0.642 | 0.671 | 0.593 | 0.591 | 0.518 | 0.618 | 0.555 | 0.519 | 0.564 | 0.452 | 0.550 | 0.505 | 0.505 | 0.442 |
| 138 | 0.764 | 0.629 | 0.587 | 0.608 | 0.614 | 0.610 | 0.638 | 0.560 | 0.559 | 0.484 | 0.586 | 0.523 | 0.486 | 0.532 | 0.419 | 0.516 | 0.472 | 0.471 | 0.409 |
| 150 | 0.739 | 0.601 | 0.559 | 0.581 | 0.584 | 0.578 | 0.607 | 0.528 | 0.528 | 0.453 | 0.554 | 0.493 | 0.455 | 0.501 | 0.387 | 0.483 | 0.440 | 0.440 | 0.378 |
| 162 | 0.714 | 0.574 | 0.532 | 0.554 | 0.555 | 0.548 | 0.575 | 0.498 | 0.499 | 0.423 | 0.524 | 0.464 | 0.425 | 0.471 | 0.358 | 0.452 | 0.410 | 0.410 | 0.349 |
| 174 | 0.688 | 0.547 | 0.507 | 0.529 | 0.527 | 0.518 | 0.545 | 0.468 | 0.471 | 0.395 | 0.494 | 0.437 | 0.398 | 0.443 | 0.331 | 0.422 | 0.382 | 0.382 | 0.322 |
| 186 | 0.663 | 0.521 | 0.482 | 0.505 | 0.500 | 0.489 | 0.515 | 0.440 | 0.444 | 0.368 | 0.465 | 0.411 | 0.372 | 0.416 | 0.306 | 0.394 | 0.356 | 0.355 | 0.298 |
| 198 | 0.637 | 0.496 | 0.458 | 0.481 | 0.473 | 0.461 | 0.485 | 0.413 | 0.418 | 0.343 | 0.438 | 0.387 | 0.347 | 0.391 | 0.283 | 0.368 | 0.331 | 0.331 | 0.275 |
| 210 | 0.612 | 0.472 | 0.436 | 0.459 | 0.448 | 0.433 | 0.457 | 0.387 | 0.394 | 0.320 | 0.411 | 0.364 | 0.324 | 0.367 | 0.261 | 0.342 | 0.308 | 0.307 | 0.254 |
| 222 | 0.586 | 0.448 | 0.414 | 0.437 | 0.423 | 0.407 | 0.429 | 0.362 | 0.370 | 0.297 | 0.386 | 0.342 | 0.302 | 0.344 | 0.241 | 0.318 | 0.286 | 0.286 | 0.234 |
| 234 | 0.561 | 0.426 | 0.393 | 0.416 | 0.399 | 0.382 | 0.402 | 0.339 | 0.348 | 0.277 | 0.362 | 0.321 | 0.282 | 0.322 | 0.223 | 0.296 | 0.266 | 0.265 | 0.216 |
| 246 | 0.542 | 0.406 | 0.375 | 0.397 | 0.379 | 0.361 | 0.380 | 0.319 | 0.328 | 0.259 | 0.342 | 0.302 | 0.263 | 0.302 | 0.206 | 0.276 | 0.247 | 0.246 | 0.200 |
| 258 | 0.530 | 0.389 | 0.358 | 0.379 | 0.361 | 0.343 | 0.363 | 0.304 | 0.312 | 0.244 | 0.326 | 0.285 | 0.247 | 0.286 | 0.191 | 0.260 | 0.229 | 0.228 | 0.184 |

## Notes

(1)-(19) Data from U.S. Treasury
http://www.treasury.gov/offices/domestic-finance/debt-management/interest-rate/yield_historical_main.shtml
(20)-(38) Computed from (1)-(19), by interpolation of rates, compounded for number of months indicated

| Accident Year | Cumulative Paid | Cumulative | Incremental |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age | Development | Percent | Percent |  |  |  |  |  |  |  |  | DISC | UNT FACTO |  |  |  |  |  |  |  |  |  |
| (Months) | Factor | Paid | Paid | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) | (20) | (21) | (22) |
| 12 | 4.377 | 22.8\% | 22.8\% | 22.8\% | 22.5\% | 22.3\% | 22.4\% | 22.6\% | 22.7\% | 22.7\% | 22.6\% | 22.2\% | 22.2\% | 22.3\% | 22.2\% | 22.3\% | 22.3\% | 22.1\% | 22.5\% | 22.5\% | 22.4\% | 22.1\% |
| 24 | 2.006 | 49.8\% | 27.0\% | 26.8\% | 25.8\% | 25.1\% | 25.3\% | 25.9\% | 26.4\% | 26.4\% | 26.0\% | 25.0\% | 24.7\% | 25.3\% | 24.9\% | 24.8\% | 25.0\% | 24.2\% | 25.5\% | 25.4\% | 25.3\% | 24.4\% |
| 36 | 1.531 | 65.3\% | 15.5\% | 15.2\% | 14.4\% | 13.8\% | 13.9\% | 14.3\% | 14.7\% | 14.8\% | 14.3\% | 13.7\% | 13.3\% | 13.9\% | 13.5\% | 13.4\% | 13.6\% | 12.9\% | 13.9\% | 13.8\% | 13.7\% | 13.0\% |
| 48 | 1.347 | 74.2\% | 8.9\% | 8.5\% | 8.0\% | 7.6\% | 7.7\% | 7.9\% | 8.1\% | 8.2\% | 7.8\% | 7.5\% | 7.2\% | 7.6\% | 7.3\% | 7.2\% | 7.4\% | 6.8\% | 7.6\% | 7.4\% | 7.4\% | 6.9\% |
| 60 | 1.254 | 79.7\% | 5.5\% | 5.2\% | 4.7\% | 4.5\% | 4.5\% | 4.7\% | 4.8\% | 4.9\% | 4.6\% | 4.4\% | 4.2\% | 4.5\% | 4.3\% | 4.2\% | 4.3\% | 3.9\% | 4.4\% | 4.3\% | 4.3\% | 3.9\% |
| 72 | 1.202 | 83.2\% | 3.5\% | 3.2\% | 2.9\% | 2.7\% | 2.8\% | 2.9\% | 2.9\% | 3.0\% | 2.8\% | 2.7\% | 2.5\% | 2.7\% | 2.6\% | 2.5\% | 2.6\% | 2.3\% | 2.6\% | 2.5\% | 2.5\% | 2.3\% |
| 84 | 1.163 | 86.0\% | 2.8\% | 2.5\% | 2.2\% | 2.1\% | 2.1\% | 2.2\% | 2.2\% | 2.3\% | 2.1\% | 2.0\% | 1.9\% | 2.1\% | 1.9\% | 1.9\% | 2.0\% | 1.7\% | 2.0\% | 1.9\% | 1.9\% | 1.7\% |
| 96 | 1.134 | 88.2\% | 2.2\% | 1.9\% | 1.7\% | 1.6\% | 1.6\% | 1.6\% | 1.7\% | 1.7\% | 1.5\% | 1.5\% | 1.4\% | 1.6\% | 1.4\% | 1.4\% | 1.5\% | 1.3\% | 1.5\% | 1.4\% | 1.4\% | 1.2\% |
| 108 | 1.113 | 89.8\% | 1.6\% | 1.3\% | 1.2\% | 1.1\% | 1.1\% | 1.1\% | 1.1\% | 1.2\% | 1.1\% | 1.0\% | 0.9\% | 1.1\% | 1.0\% | 0.9\% | 1.0\% | 0.8\% | 1.0\% | 0.9\% | 0.9\% | 0.8\% |
| 120 | 1.097 | 91.2\% | 1.4\% | 1.1\% | 0.9\% | 0.9\% | 0.9\% | 0.9\% | 0.9\% | 1.0\% | 0.9\% | 0.8\% | 0.8\% | 0.9\% | 0.8\% | 0.8\% | 0.8\% | 0.7\% | 0.8\% | 0.7\% | 0.7\% | 0.7\% |
| 132 | 1.084 | 92.3\% | 1.1\% | 0.9\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.7\% | 0.6\% | 0.6\% | 0.6\% | 0.7\% | 0.6\% | 0.6\% | 0.6\% | 0.5\% | 0.6\% | 0.6\% | 0.6\% | 0.5\% |
| 144 | 1.073 | 93.2\% | 0.9\% | 0.7\% | 0.6\% | 0.5\% | 0.6\% | 0.6\% | 0.6\% | 0.6\% | 0.5\% | 0.5\% | 0.4\% | 0.5\% | 0.5\% | 0.4\% | 0.5\% | 0.4\% | 0.5\% | 0.4\% | 0.4\% | 0.4\% |
| 156 | 1.064 | 94.0\% | 0.8\% | 0.6\% | 0.5\% | 0.4\% | 0.4\% | 0.5\% | 0.4\% | 0.5\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.3\% | 0.4\% | 0.3\% | 0.3\% | 0.3\% |
| 168 | 1.057 | 94.6\% | 0.7\% | 0.5\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.4\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.2\% | 0.3\% | 0.3\% | 0.3\% | 0.2\% |
| 180 | 1.050 | 95.2\% | 0.6\% | 0.4\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.3\% | 0.2\% | 0.3\% | 0.3\% | 0.2\% | 0.3\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% |
| 192 | 1.045 | 95.7\% | 0.5\% | 0.3\% | 0.3\% | 0.2\% | 0.3\% | 0.3\% | 0.2\% | 0.3\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% |
| 204 | 1.040 | 96.2\% | 0.4\% | 0.3\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.1\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% |
| 216 | 1.036 | 96.6\% | 0.4\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.2\% | 0.1\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% |
| 228 | 1.032 | 96.9\% | 0.4\% | 0.2\% | 0.2\% | 0.1\% | 0.2\% | 0.2\% | 0.1\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% |
| 240 | 1.028 | 97.2\% | 0.3\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% |
| 252 | 1.025 | 97.5\% | 0.3\% | 0.2\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% | 0.1\% |
| 264 | 1.000 | 100.0\% | 2.5\% | 1.3\% | 1.0\% | 0.9\% | 0.9\% | 0.9\% | 0.8\% | 0.9\% | 0.8\% | 0.8\% | 0.6\% | 0.8\% | 0.7\% | 0.6\% | 0.7\% | 0.5\% | 0.6\% | 0.6\% | 0.6\% | 0.5\% |
| Total |  |  | 100.0\% | 94.2\% | 88.7\% | 85.7\% | 86.7\% | 88.4\% | 89.8\% | 90.6\% | 87.3\% | 84.8\% | 82.2\% | 85.9\% | 83.6\% | 82.6\% | 84.2\% | 79.4\% | 85.1\% | 83.9\% | 83.7\% | 79.7\% |
| Present Value Factor |  |  |  | 0.942 | 0.887 | 0.857 | 0.867 | 0.884 | 0.898 | 0.906 | 0.873 | 0.848 | 0.822 | 0.859 | 0.836 | 0.826 | 0.842 | 0.794 | 0.851 | 0.839 | 0.837 | 0.797 |
| Notes |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (1) From Exhibit 6 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (2) $=1 /(1)$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (3) From (2) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (4) - (22) Product of (3) and Exhibit 7, Columns (20) - (38) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

WORKERS COMPENSATION
SECTION D
INDUSTRY NET RESULTS
EXHIBIT 9
DURATION OF PAYOUT OF ACCIDENT YEAR LOSSES

| Accident Year <br> Age <br> (Months) | Cumulative <br> Paid <br> Development <br> Factor | Cumulative <br> Percent <br> Paid | Incremental <br> Percent <br> Paid | Duration |
| :---: | :---: | :---: | :---: | ---: |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
| 12 | 4.377 | $22.8 \%$ | $22.8 \%$ | 0.11 |
| 24 | 2.006 | $49.8 \%$ | $27.0 \%$ | 0.40 |
| 36 | 1.531 | $65.3 \%$ | $15.5 \%$ | 0.39 |
| 48 | 1.347 | $74.2 \%$ | $8.9 \%$ | 0.31 |
| 60 | 1.254 | $79.7 \%$ | $5.5 \%$ | 0.25 |
| 72 | 1.202 | $83.2 \%$ | $3.5 \%$ | 0.19 |
| 84 | 1.163 | $86.0 \%$ | $2.8 \%$ | 0.18 |
| 96 | 1.134 | $88.2 \%$ | $2.2 \%$ | 0.17 |
| 108 | 1.113 | $89.8 \%$ | $1.6 \%$ | 0.14 |
| 120 | 1.097 | $91.2 \%$ | $1.4 \%$ | 0.13 |
| 132 | 1.084 | $92.3 \%$ | $1.1 \%$ | 0.11 |
| 144 | 1.073 | $93.2 \%$ | $0.9 \%$ | 0.10 |
| 156 | 1.064 | $94.0 \%$ | $0.8 \%$ | 0.10 |
| 168 | 1.057 | $94.6 \%$ | $0.7 \%$ | 0.09 |
| 180 | 1.050 | $95.2 \%$ | $0.6 \%$ | 0.08 |
| 192 | 1.045 | $95.7 \%$ | $0.5 \%$ | 0.08 |
| 204 | 1.040 | $96.2 \%$ | $0.4 \%$ | 0.07 |
| 216 | 1.036 | $96.6 \%$ | $0.4 \%$ | 0.07 |
| 228 | 1.032 | $96.9 \%$ | $0.4 \%$ | 0.07 |
| 240 | 1.028 | $97.2 \%$ | $0.3 \%$ | 0.06 |
| 252 | 1.025 | $97.5 \%$ | $0.3 \%$ | 0.06 |
| 264 | 1.000 | $100.0 \%$ | $2.5 \%$ | 0.53 |
|  |  |  |  |  |
| Total |  |  | $100.0 \%$ | $370.2 \%$ |
|  |  |  |  |  |
| Duration (years) |  |  |  |  |

Notes
(2) From Exhibit 6
(3) $=1 /$ (2)
(4) From (2)
(5) $=(4) *[(1) / 12-0.5]$

WORKERS COMPENSATION
SECTION D
INDUSTRY NET RESULTS
EXHIBIT 10
DEVELOPED INDUSTRY ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Net <br> Booked Ultimate Loss \& ALAE | Average Development Parameter <br> $\mu$ | Variance Development Parameter $\sigma^{2}$ | Net Developed Ultimate Loss \& ALAE | Developed vs Booked Ultimate Loss \& ALAE | Paid Loss \& ALAE | Developed Unpaid Loss \& ALAE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1987 | 20,397,951 | 0.000\% | 0.000\% | 20,397,951 | - | 17,858,804 | 2,539,147 |
| 1988 | 24,381,050 | 0.000\% | 0.000\% | 24,381,050 | - | 21,756,428 | 2,624,622 |
| 1989 | 27,150,337 | 0.000\% | 0.000\% | 27,150,337 | - | 24,332,493 | 2,817,844 |
| 1990 | 29,864,671 | 0.000\% | 0.000\% | 29,864,671 | - | 26,902,429 | 2,962,242 |
| 1991 | 27,425,492 | 0.000\% | 0.000\% | 27,425,492 | - | 24,762,776 | 2,662,716 |
| 1992 | 22,585,089 | 0.000\% | 0.000\% | 22,585,089 | - | 20,204,109 | 2,380,980 |
| 1993 | 19,456,020 | 0.000\% | 0.000\% | 19,456,020 | - | 17,331,393 | 2,124,627 |
| 1994 | 17,193,950 | 0.000\% | 0.000\% | 17,193,950 | - | 15,148,767 | 2,045,183 |
| 1995 | 16,448,810 | 0.000\% | 0.000\% | 16,448,810 | - | 14,390,813 | 2,057,997 |
| 1996 | 17,219,810 | 0.000\% | 0.000\% | 17,219,810 | - | 14,983,956 | 2,235,854 |
| 1997 | 18,665,040 | 0.000\% | 0.000\% | 18,665,040 | - | 16,102,359 | 2,562,681 |
| 1998 | 20,543,308 | 0.000\% | 0.000\% | 20,543,308 | - | 17,570,425 | 2,972,883 |
| 1999 | 20,650,698 | 0.000\% | 0.000\% | 20,650,698 | - | 17,762,207 | 2,888,491 |
| 2000 | 21,784,432 | 0.137\% | 0.003\% | 21,814,736 | 30,304 | 18,528,864 | 3,285,872 |
| 2001 | 21,514,904 | 0.348\% | 0.009\% | 21,590,821 | 75,917 | 17,595,713 | 3,995,108 |
| 2002 | 20,513,706 | 0.702\% | 0.025\% | 20,660,823 | 147,117 | 16,314,355 | 4,346,468 |
| 2003 | 21,123,786 | 1.054\% | 0.060\% | 21,354,051 | 230,265 | 15,929,976 | 5,424,075 |
| 2004 | 21,318,142 | 1.373\% | 0.116\% | 21,625,404 | 307,262 | 15,081,378 | 6,544,026 |
| 2005 | 22,200,172 | 1.726\% | 0.240\% | 22,613,757 | 413,585 | 14,358,206 | 8,255,551 |
| 2006 | 25,554,253 | 0.850\% | 0.605\% | 25,850,466 | 296,213 | 13,950,057 | 11,900,409 |
| 2007 | 26,730,744 | 0.210\% | 1.132\% | 26,938,968 | 208,224 | 11,208,806 | 15,730,162 |
| 2008 | 26,279,616 | -0.601\% | 1.912\% | 26,372,918 | 93,302 | 5,279,866 | 21,093,052 |
| Total | 489,001,981 |  |  | 490,804,172 | 1,802,191 | 377,354,180 | 113,449,992 |

Notes
(1) From Exhibit 5, Column 3
(2) From Exhibit 3, Cumulative Average
(3) From Exhibit 4, Variance
(4) $=(1) * \exp [(2)+(3) / 2]$
(5) $=(4)-(1)$
(6) From Exhibit 5, Column 4
(7) $=(4)-(6)$

## industry historical ultimate Loss \& ALAE RATIO

Dollars in Thousands

|  | 12 month Booked Ultimate Loss \& ALAE Ratio | PV Factor | 1 - Exp Ratio | Loss Ratio <br> Prior to Adjustment | Loss Ratio Adjustment | Adjusted <br> Loss Ratio | Log of <br> Adjusted <br> Loss Ratio | 12 Month Booked Ultimate Loss | Latest <br> Evaluation Ultimate Loss | Ratio Latest to 12 Month Booked | $\begin{aligned} & \text { Log of } \\ & \text { Ratio } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) |
| 1987 | 82.2\% | 0.797 | 75.6\% | 67.4\% | 0.940 | 63.3\% | -45.7\% | 18,853,888 | 20,397,951 | 1.082 | 0.079 |
| 1988 | 83.9\% | 0.797 | 75.8\% | 68.6\% | 0.940 | 64.5\% | -43.9\% | 22,332,320 | 24,381,050 | 1.092 | 0.088 |
| 1989 | 84.9\% | 0.797 | 76.5\% | 68.8\% | 0.940 | 64.7\% | -43.6\% | 24,953,996 | 27,150,337 | 1.088 | 0.084 |
| 1990 | 85.2\% | 0.797 | 77.3\% | 68.3\% | 0.940 | 64.2\% | -44.3\% | 28,450,870 | 29,864,671 | 1.050 | 0.048 |
| 1991 | 84.9\% | 0.837 | 76.6\% | 72.1\% | 0.940 | 67.8\% | -38.9\% | 29,031,028 | 27,425,492 | 0.945 | -0.057 |
| 1992 | 81.1\% | 0.839 | 75.6\% | 69.9\% | 0.940 | 65.7\% | -42.0\% | 26,796,917 | 22,585,089 | 0.843 | -0.171 |
| 1993 | 76.4\% | 0.851 | 74.9\% | 67.5\% | 0.940 | 63.4\% | -45.5\% | 23,939,453 | 19,456,020 | 0.813 | -0.207 |
| 1994 | 75.1\% | 0.794 | 72.0\% | 64.4\% | 0.940 | 60.5\% | -50.2\% | 21,099,133 | 17,193,950 | 0.815 | -0.205 |
| 1995 | 72.6\% | 0.842 | 70.4\% | 67.5\% | 0.940 | 63.5\% | -45.4\% | 18,843,899 | 16,448,810 | 0.873 | -0.136 |
| 1996 | 70.6\% | 0.826 | 70.0\% | 64.8\% | 0.940 | 60.9\% | -49.6\% | 17,964,604 | 17,219,810 | 0.959 | -0.042 |
| 1997 | 71.8\% | 0.836 | 68.5\% | 68.0\% | 0.940 | 63.9\% | -44.7\% | 17,030,758 | 18,665,040 | 1.096 | 0.092 |
| 1998 | 76.5\% | 0.859 | 67.0\% | 76.2\% | 0.853 | 65.0\% | -43.1\% | 17,559,397 | 20,543,308 | 1.170 | 0.157 |
| 1999 | 78.5\% | 0.822 | 65.9\% | 76.1\% | 0.853 | 64.9\% | -43.3\% | 16,670,037 | 20,650,698 | 1.239 | 0.214 |
| 2000 | 77.1\% | 0.848 | 68.5\% | 74.2\% | 0.853 | 63.3\% | -45.8\% | 17,840,887 | 21,784,432 | 1.221 | 0.201 |
| 2001 | 75.7\% | 0.873 | 70.3\% | 73.1\% | 0.853 | 62.3\% | -47.3\% | 19,250,955 | 21,514,904 | 1.118 | 0.115 |
| 2002 | 68.9\% | 0.906 | 73.9\% | 65.6\% | 1.000 | 65.6\% | -42.1\% | 19,709,488 | 20,513,706 | 1.041 | 0.047 |
| 2003 | 71.5\% | 0.898 | 75.8\% | 65.9\% | 1.000 | 65.9\% | -41.7\% | 22,696,915 | 21,123,786 | 0.931 | -0.061 |
| 2004 | 69.5\% | 0.884 | 76.4\% | 62.5\% | 1.000 | 62.5\% | -47.0\% | 24,857,632 | 21,318,142 | 0.858 | -0.139 |
| 2005 | 67.7\% | 0.867 | 76.2\% | 59.8\% | 1.000 | 59.8\% | -51.4\% | 25,951,454 | 22,200,172 | 0.855 | -0.138 |
| 2006 | 67.4\% | 0.857 | 77.6\% | 57.9\% | 1.000 | 57.9\% | -54.7\% | 27,815,601 | 25,554,253 | 0.919 | -0.073 |
| 2007 | 69.1\% | 0.887 | 73.7\% | 64.7\% | 1.000 | 64.7\% | -43.6\% | 27,234,231 | 26,730,744 | 0.982 | -0.011 |
| 2008 | 70.6\% | 0.942 | 73.2\% | 70.6\% | 1.000 | 70.6\% | -34.8\% | 26,279,616 | 26,279,616 | 1.000 | 0.004 |
| (12) Average |  |  |  |  |  | 63.9\% | -44.9\% |  |  |  |  |
| (13) Variance |  |  |  |  |  |  | 0.178\% |  |  |  | 1.632\% |
| (14) Covariance (lo | of Adjusted Loss Ratio | og of Ratio of | est to 12 month | oked) |  |  | 0.130\% |  |  |  |  |
| (15) Total Variance | of Adjusted Loss Rati | $\mathrm{g})$ and Ratio of | atest to 12 month | ooked (log) |  |  | 2.070\% |  |  |  |  |

## Notes

(1) Exhibit 1 @ 12 Months / Exhibit 5, Column
(2) 1995-2008 from Exhibit 8, Columns 4-17; 1994 and prior selectec
(3) $=100 \%$ - Exhibit 5, Column 9
(4) $=(1) *(2)_{\text {AYXXXX }} /(2)_{\text {AY2008 }} *(3)_{\text {AY2008 }} /(3)_{\text {AYXXXX }}$
(5) Adjustment of historical loss ratios to normalize for major differences in levels across multi-year period

AY 1987-1997: AY 2002-2008 Average / AY 1987-1997 Average; AY 1998-2001: AY 2002-2008 Average / AY 1998-2001 Average; 1.000 for AY 2002-200
(6) $=(4) *(5)$
(7) $=\operatorname{LN}(6)$
(8) Exhibit 1 @ 12 Months
(9) Exhibit 1 @ 12 Current Evaluation
$(10)=(9) /(8$
11) $=\mathrm{LN}(10)+$ Exhibit 10, Column $2+($ Exhibit 10, Column 3)/2
12) Average of Column 7
13) Variance of Column 7 and Column 11
14) Covariance( Column 7, Column 11)
(15) = Row 13, Column 7 + Row 13, Column 7 + 2 * Row 14

DERIVATION OF INDUSTRY 2008 MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\boldsymbol{\lambda}$ )

| 1 - ER | $73.2 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.090 |
| PV | 0.942 |
| Target Loss Ratio | $71.3 \%$ |
| ULR12 | $70.6 \%$ |
| $\mu$ | $-0.601 \%$ |
| $\sigma^{2}$ | $1.912 \%$ |
| $\sigma$ | $13.826 \%$ |
| D | 3.702 |
| $\lambda$ | 0.024 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-34.8 \%$ |
| Combined $\mu$ | $-35.4 \%$ |
| $\sigma^{2}{ }_{\text {AY ULR }}$ | $0.178 \%$ |
| $\sigma^{2}{ }_{12 \text {-ult }}$ | $1.632 \%$ |
| Cov(AY ULR, 12 -ult) | $0.130 \%$ |
| Combined $\sigma^{2}$ | $2.070 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.020 |
| $(2008$ market value of risk) |  |

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE $) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$

Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12 -ult)
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu_{A Y U L R}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma$.

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, 2008 Accident Year

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

DERIVATION OF INDUSTRY LONG-TERM MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\boldsymbol{\lambda}$ )

| 1 - ER | $73.2 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.090 |
| PV | 0.942 |
| Target Loss Ratio | $71.3 \%$ |
| ULR12 | $70.6 \%$ |
| $\mu$ | $-0.601 \%$ |
| $\sigma^{2}$ | $1.912 \%$ |
| $\sigma$ | $13.826 \%$ |
| D | 3.702 |
| $\lambda$ | 0.024 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-44.9 \%$ |
| Combined $\mu$ | $-45.5 \%$ |
| $\sigma_{\text {AY ULR }}^{2}$ | $0.178 \%$ |
| $\sigma_{12 \text {-ult }}^{2}$ | $1.632 \%$ |
| Cov(AY ULR, 12 -ult) | $0.130 \%$ |
| Combined $\sigma^{2}$ | $2.070 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.385 |

(long-term market value of risk)

## Notes

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+U L A E) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$
Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12-ult)
$=\left[\ln (1-\mathrm{ER})-\ln (1+\mathrm{ULAE})-\ln (\mathrm{PV})-\mu_{\mathrm{AY}} \operatorname{LLR}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma \cdot \mathrm{v}(\mathrm{D})$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, Average

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11
From Exhibit 11, Row 14, Covariance
From Exhibit 11, Row 15

WORKERS COMPENSATION
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON 2008 MARKET VALUE OF RISK
Dollars in Thousands


WORKERS COMPENSATION
INDUSTRY NET RESULTS
SECTION D
EXHIBIT 13B
RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands


WORKERS COMPENSATION
SECTION D
INDUSTRY NET RESULTS
EXHIBIT 14
PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands

|  | Total Accident Years 1997-2008 | Accident Year 2008 | Accident Year 2007 | Accident Year 2006 | Accident Year 2005 | Accident Year 2004 | Accident Year 2003 | Accident Year 2002 | Accident Year 2001 | Accident Year 2000 | Accident Year 1999 | Accident Year 1998 | Accident Year 1997 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| Year 1 | 21,351,338 | 7,172,177 | 4,817,354 | 3,079,430 | 1,767,089 | 1,141,922 | 872,274 | 656,942 | 506,783 | 412,921 | 337,870 | 325,082 | 261,494 |
| Year 2 | 13,530,766 | 4,115,410 | 2,765,587 | 1,901,976 | 1,127,804 | 907,833 | 690,378 | 476,823 | 431,261 | 330,663 | 282,548 | 275,838 | 224,646 |
| Year 3 | 9,100,266 | 2,362,609 | 1,708,134 | 1,213,892 | 896,609 | 718,522 | 501,092 | 405,766 | 345,349 | 276,521 | 239,747 | 236,968 | 195,057 |
| Year 4 | 6,603,072 | 1,459,239 | 1,090,177 | 965,050 | 709,639 | 521,519 | 426,418 | 324,933 | 288,802 | 234,633 | 205,963 | 205,757 | 170,943 |
| Year 5 | 5,090,711 | 931,326 | 866,696 | 763,807 | 515,071 | 443,801 | 341,471 | 271,729 | 245,054 | 201,570 | 178,836 | 180,319 | 151,032 |
| Year 6 | 4,126,580 | 740,408 | 685,963 | 554,388 | 438,314 | 355,391 | 285,559 | 230,567 | 210,522 | 175,021 | 156,726 | 159,317 | 134,404 |
| Year 7 | 3,381,045 | 586,010 | 497,887 | 471,772 | 350,997 | 297,200 | 242,302 | 198,077 | 182,794 | 153,383 | 138,472 | 141,776 | 120,375 |
| Year 8 | 2,807,018 | 425,339 | 423,691 | 377,790 | 293,525 | 252,179 | 208,158 | 171,988 | 160,196 | 135,518 | 123,226 | 126,978 | 108,430 |
| Year 9 | 2,399,399 | 361,954 | 339,287 | 315,931 | 249,062 | 216,644 | 180,741 | 150,725 | 141,537 | 120,598 | 110,364 | 114,378 | 98,178 |
| Year 10 | 2,808,464 | 289,849 | 283,733 | 268,073 | 213,965 | 188,109 | 158,397 | 133,170 | 125,954 | 108,010 | 99,413 | 103,563 | 836,229 |
| Year 11 | 2,504,744 | 242,390 | 240,752 | 230,298 | 185,784 | 164,854 | 139,947 | 118,508 | 112,807 | 97,292 | 90,013 | 882,099 | - |
| Year 12 | 2,108,001 | 205,672 | 206,827 | 199,965 | 162,816 | 145,652 | 124,539 | 106,138 | 101,613 | 88,093 | 766,685 | - | - |
| Year 13 | 1,854,469 | 176,690 | 179,586 | 175,244 | 143,852 | 129,616 | 111,540 | 95,606 | 92,006 | 750,330 | - | - | - |
| Year 14 | 1,680,429 | 153,418 | 157,384 | 154,832 | 128,014 | 116,087 | 100,472 | 86,566 | 783,656 | - | - | - | - |
| Year 15 | 1,458,809 | 134,451 | 139,052 | 137,786 | 114,652 | 104,568 | 90,972 | 737,328 | - | - | - | - | - |
| Year 16 | 1,338,749 | 118,791 | 123,743 | 123,403 | 103,275 | 94,681 | 774,855 | - | - | - | - | - | - |
| Year 17 | 1,227,650 | 105,712 | 110,827 | 111,159 | 93,510 | 806,442 | - | - | - | - | - | - | - |
| Year 18 | 1,091,628 | 94,678 | 99,830 | 100,648 | 796,472 | - | - | - | - | - | - | - | - |
| Year 19 | 1,032,943 | 85,283 | 90,391 | 857,269 | - | - | - | - | - | - | - | - | - |
| Year 20 | 847,119 | 77,220 | 769,900 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 657,717 | 657,717 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total | 87,000,919 | 20,496,344 | 15,596,799 | 12,002,714 | 8,290,450 | 6,605,020 | 5,249,116 | 4,164,866 | 3,728,333 | 3,084,552 | 2,729,864 | 2,752,075 | 2,300,787 |

Total equals expected unpaid by accident year
(2) - (13) Based on expected unpaid by accident year and payout pattern from Exhibit 8

DISCOUNTED PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS

## Dollars in Thousands

Discounted Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Discount Factor | Total Accident Years 1997-2008 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2008 \\ \hline \end{gathered}$ | Accident Year 2007 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2006 \end{gathered}$ | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2005 \\ \hline \end{gathered}$ | Accident Year 2004 | Accident Year 2003 | Accident Year 2002 | Accident Year 2001 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2000 \end{gathered}$ | Accident Year 1999 | Accident Year 1998 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1997 \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| Year 1 | 0.999 | 21,322,572 | 7,162,514 | 4,810,864 | 3,075,281 | 1,764,708 | 1,140,383 | 871,099 | 656,057 | 506,100 | 412,365 | 337,415 | 324,644 | 261,141 |
| Year 2 | 0.992 | 13,416,897 | 4,080,777 | 2,742,313 | 1,885,970 | 1,118,313 | 900,193 | 684,568 | 472,810 | 427,631 | 327,880 | 280,170 | 273,516 | 222,755 |
| Year 3 | 0.978 | 8,903,103 | 2,311,422 | 1,671,126 | 1,187,593 | 877,183 | 702,955 | 490,235 | 396,975 | 337,867 | 270,530 | 234,553 | 231,834 | 190,831 |
| Year 4 | 0.961 | 6,346,778 | 1,402,600 | 1,047,863 | 927,592 | 682,094 | 501,276 | 409,866 | 312,321 | 277,592 | 225,526 | 197,969 | 197,771 | 164,308 |
| Year 5 | 0.939 | 4,779,327 | 874,360 | 813,682 | 717,087 | 483,566 | 416,655 | 320,584 | 255,108 | 230,065 | 189,240 | 167,897 | 169,290 | 141,794 |
| Year 6 | 0.915 | 3,775,458 | 677,408 | 627,596 | 507,216 | 401,019 | 325,152 | 261,261 | 210,948 | 192,609 | 160,129 | 143,391 | 145,761 | 122,968 |
| Year 7 | 0.891 | 3,012,782 | 522,182 | 443,657 | 420,386 | 312,767 | 264,829 | 215,910 | 176,502 | 162,884 | 136,677 | 123,390 | 126,334 | 107,263 |
| Year 8 | 0.866 | 2,431,496 | 368,437 | 367,009 | 327,249 | 254,258 | 218,443 | 180,311 | 148,979 | 138,765 | 117,388 | 106,741 | 109,991 | 93,925 |
| Year 9 | 0.841 | 2,017,577 | 304,355 | 285,296 | 265,656 | 209,428 | 182,169 | 151,980 | 126,740 | 119,014 | 101,407 | 92,801 | 96,177 | 82,555 |
| Year 10 | 0.814 | 2,286,777 | 236,008 | 231,028 | 218,277 | 174,220 | 153,167 | 128,974 | 108,433 | 102,557 | 87,946 | 80,946 | 84,326 | 680,895 |
| Year 11 | 0.788 | 1,974,763 | 191,102 | 189,811 | 181,569 | 146,474 | 129,972 | 110,336 | 93,433 | 88,938 | 76,706 | 70,967 | 695,455 | - |
| Year 12 | 0.764 | 1,610,218 | 157,105 | 157,987 | 152,745 | 124,368 | 111,258 | 95,131 | 81,075 | 77,618 | 67,291 | 585,640 | - | - |
| Year 13 | 0.739 | 1,370,314 | 130,561 | 132,700 | 129,492 | 106,296 | 95,777 | 82,420 | 70,646 | 67,985 | 554,438 | - | - | - |
| Year 14 | 0.714 | 1,199,312 | 109,493 | 112,324 | 110,503 | 91,363 | 82,851 | 71,707 | 61,782 | 559,290 | - | - | - | - |
| Year 15 | 0.688 | 1,004,033 | 92,537 | 95,704 | 94,832 | 78,910 | 71,970 | 62,612 | 507,470 | - | - | - | - | - |
| Year 16 | 0.663 | 887,182 | 78,722 | 82,004 | 81,779 | 68,440 | 62,745 | 513,492 | - | - | - | - | - | - |
| Year 17 | 0.637 | 782,131 | 67,349 | 70,607 | 70,819 | 59,575 | 513,781 | - | - | - | - | - | - | - |
| Year 18 | 0.612 | 667,574 | 57,899 | 61,050 | 61,550 | 487,075 | - | - | - | - | - | - | - | - |
| Year 19 | 0.586 | 605,410 | 49,985 | 52,978 | 502,448 | - | - | - | - | - | - | - | - | - |
| Year 20 | 0.561 | 475,113 | 43,309 | 431,803 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 0.542 | 356,541 | 356,541 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | 0.530 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total |  | 79,225,360 | 19,274,667 | 14,427,403 | 10,918,045 | 7,440,056 | 5,873,574 | 4,650,486 | 3,679,279 | 3,288,917 | 2,727,522 | 2,421,881 | 2,455,098 | 2,068,434 |

[^8](1) From Exhibit 7, Column 20
(2) Sum of Columns 3-14
(3) - (14) Product of Column 1 and Exhibit 14, Columns 2-13

NET IMPACT OF RISK MARGINS AND DISCOUNT FOR LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands

|  | $\begin{gathered} \text { 31-Dec-08 } \\ \text { Booked } \\ \text { Unpaid } \\ \text { Loss \& ALAE } \\ \hline \end{gathered}$ | 31-Dec-08 <br> Expected Unpaid Loss \& ALAE | Average <br> Indicated <br> Risk <br> Margin | Present <br> Value <br> Expected <br> Unpaid <br> Loss \& ALAE | Present <br> Value <br> Discount | Risk-Adjusted <br> Discounted Expected Unpaid Loss \& ALAE | Net Impact of Risk Margins and Discount vs. Booked |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1997 | 2,300,787 | 2,300,787 | N/A | 2,068,434 | -10.1\% | N/A | N/A |
| 1998 | 2,752,075 | 2,752,075 | N/A | 2,455,098 | -10.8\% | N/A | N/A |
| 1999 | 2,729,864 | 2,729,864 | N/A | 2,421,881 | -11.3\% | N/A | N/A |
| 2000 | 3,064,481 | 3,084,552 | N/A | 2,727,522 | -11.6\% | N/A | N/A |
| 2001 | 3,638,616 | 3,728,333 | N/A | 3,288,917 | -11.8\% | N/A | N/A |
| 2002 | 3,938,110 | 4,164,866 | N/A | 3,679,279 | -11.7\% | N/A | N/A |
| 2003 | 4,963,490 | 5,249,116 | N/A | 4,650,486 | -11.4\% | N/A | N/A |
| 2004 | 6,045,419 | 6,605,020 | N/A | 5,873,574 | -11.1\% | N/A | N/A |
| 2005 | 7,603,741 | 8,290,450 | N/A | 7,440,056 | -10.3\% | N/A | N/A |
| 2006 | 11,221,393 | 12,002,714 | N/A | 10,918,045 | -9.0\% | N/A | N/A |
| 2007 | 14,901,020 | 15,596,799 | N/A | 14,427,403 | -7.5\% | N/A | N/A |
| 2008 | 19,981,328 | 20,496,344 | N/A | 19,274,667 | -6.0\% | N/A | N/A |
| Total 1997-2008 | 83,140,324 | 87,000,919 | 7.7\% | 79,225,360 | -8.9\% | 85,365,106 | 2.7\% |

Notes
(3) From Exhibit 13B, Row 13, Total Largest 100 U.S. Insurers
(4) From Exhibit 15, Total by Accident Year
(5) $=(4) /(2)-1$
(6) $=(2)$ Total $*[1+(3)$ Total $]$ [ $1+(5)$ Total $]$
(7) $=$ (6) Total $/$ (1) Total -1

OTHER LIABILITY OCCURRENCE
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Months of Maturity |  |  |  |  |  |  |  |  |  | Latest |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12 | $\underline{24}$ | 36 | 48 | 60 | 72 | 84 | $\underline{96}$ | 108 | 120 | Evaluation |
| 1987 | 10,715,088 | 10,524,540 | 9,837,162 | 9,196,223 | 8,815,916 | 8,384,500 | 8,110,195 | 8,090,341 | 7,848,168 | 7,803,623 | 7,803,623 |
| 1988 | 10,073,805 | 9,688,397 | 9,456,362 | 8,959,028 | 8,653,537 | 8,475,500 | 8,370,337 | 8,164,276 | 8,161,523 | 8,080,501 | 8,080,501 |
| 1989 | 9,643,663 | 9,422,893 | 9,075,254 | 8,860,896 | 8,635,586 | 8,586,319 | 8,463,208 | 8,415,211 | 8,397,764 | 8,283,756 | 8,283,756 |
| 1990 | 9,537,734 | 9,329,769 | 9,222,109 | 8,933,850 | 8,809,155 | 8,693,410 | 8,597,218 | 8,635,194 | 8,479,377 | 8,392,058 | 8,392,058 |
| 1991 | 8,805,106 | 8,701,279 | 8,774,605 | 8,601,465 | 8,430,468 | 8,272,286 | 8,219,507 | 8,060,161 | 8,017,665 | 7,902,927 | 7,902,927 |
| 1992 | 8,657,249 | 8,709,414 | 8,535,967 | 8,254,500 | 8,065,343 | 8,071,067 | 7,910,783 | 7,803,085 | 7,688,487 | 7,604,931 | 7,604,931 |
| 1993 | 8,711,506 | 8,701,406 | 8,729,189 | 8,529,414 | 8,483,222 | 8,264,345 | 8,031,116 | 7,911,150 | 7,770,920 | 7,670,083 | 7,670,083 |
| 1994 | 8,877,242 | 8,884,276 | 8,911,710 | 8,860,874 | 8,757,641 | 8,663,479 | 8,400,987 | 8,220,135 | 8,146,441 | 8,106,941 | 8,106,941 |
| 1995 | 9,042,828 | 8,963,182 | 9,035,420 | 8,920,113 | 8,948,289 | 8,758,129 | 8,682,010 | 8,587,648 | 8,587,501 | 8,604,084 | 8,604,084 |
| 1996 | 9,342,998 | 9,300,819 | 9,388,051 | 9,267,012 | 9,193,089 | 9,041,813 | 9,019,986 | 8,929,207 | 9,122,552 | 9,262,316 | 9,262,316 |
| 1997 | 10,028,801 | 10,105,779 | 10,224,417 | 10,060,443 | 10,166,764 | 10,385,293 | 10,326,095 | 10,506,716 | 10,700,450 | 10,843,992 | 10,843,992 |
| 1998 | 10,841,918 | 10,938,158 | 11,274,314 | 11,667,655 | 12,065,956 | 12,017,293 | 12,557,126 | 12,906,016 | 13,011,988 | 13,048,118 | 13,048,118 |
| 1999 | 9,714,700 | 9,938,708 | 10,164,081 | 10,926,011 | 11,258,512 | 11,721,408 | 12,256,819 | 12,511,231 | 12,504,492 | 12,936,281 | 12,936,281 |
| 2000 | 9,755,953 | 9,765,154 | 10,323,078 | 11,065,972 | 11,828,949 | 12,048,323 | 12,154,975 | 12,321,009 | 12,364,579 |  | 12,364,579 |
| 2001 | 11,666,056 | 11,886,716 | 12,000,451 | 12,400,605 | 12,920,644 | 13,217,208 | 13,408,643 | 13,325,195 |  |  | 13,325,195 |
| 2002 | 12,600,530 | 12,552,758 | 12,947,646 | 13,524,415 | 13,813,623 | 13,900,469 | 13,945,357 |  |  |  | 13,945,357 |
| 2003 | 15,247,263 | 14,569,640 | 14,533,990 | 14,384,767 | 14,065,082 | 13,937,881 |  |  |  |  | 13,937,881 |
| 2004 | 17,438,909 | 15,465,420 | 14,744,641 | 14,228,037 | 13,935,832 |  |  |  |  |  | 13,935,832 |
| 2005 | 16,690,750 | 15,641,990 | 15,137,033 | 14,378,626 |  |  |  |  |  |  | 14,378,626 |
| 2006 | 18,183,265 | 17,529,078 | 16,612,206 |  |  |  |  |  |  |  | 16,612,206 |
| 2007 | 18,735,570 | 18,021,362 |  |  |  |  |  |  |  |  | 18,021,362 |
| 2008 | 17,908,920 |  |  |  |  |  |  |  |  |  | 17,908,920 |

## Notes

Data from SNL Financial LC
1996-2008 Annual Statements
Industry Total Other Liability Occurrence
Schedule P, Part 2H-1

OTHER LIABILITY OCCURRENCE
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | 0.982 | 0.935 | 0.935 | 0.959 | 0.951 | 0.967 | 0.998 | 0.970 | 0.994 |
| 1988 | 0.962 | 0.976 | 0.947 | 0.966 | 0.979 | 0.988 | 0.975 | 1.000 | 0.990 |
| 1989 | 0.977 | 0.963 | 0.976 | 0.975 | 0.994 | 0.986 | 0.994 | 0.998 | 0.986 |
| 1990 | 0.978 | 0.988 | 0.969 | 0.986 | 0.987 | 0.989 | 1.004 | 0.982 | 0.990 |
| 1991 | 0.988 | 1.008 | 0.980 | 0.980 | 0.981 | 0.994 | 0.981 | 0.995 | 0.986 |
| 1992 | 1.006 | 0.980 | 0.967 | 0.977 | 1.001 | 0.980 | 0.986 | 0.985 | 0.989 |
| 1993 | 0.999 | 1.003 | 0.977 | 0.995 | 0.974 | 0.972 | 0.985 | 0.982 | 0.987 |
| 1994 | 1.001 | 1.003 | 0.994 | 0.988 | 0.989 | 0.970 | 0.978 | 0.991 | 0.995 |
| 1995 | 0.991 | 1.008 | 0.987 | 1.003 | 0.979 | 0.991 | 0.989 | 1.000 | 1.002 |
| 1996 | 0.995 | 1.009 | 0.987 | 0.992 | 0.984 | 0.998 | 0.990 | 1.022 | 1.015 |
| 1997 | 1.008 | 1.012 | 0.984 | 1.011 | 1.021 | 0.994 | 1.017 | 1.018 | 1.013 |
| 1998 | 1.009 | 1.031 | 1.035 | 1.034 | 0.996 | 1.045 | 1.028 | 1.008 | 1.003 |
| 1999 | 1.023 | 1.023 | 1.075 | 1.030 | 1.041 | 1.046 | 1.021 | 0.999 | 1.035 |
| 2000 | 1.001 | 1.057 | 1.072 | 1.069 | 1.019 | 1.009 | 1.014 | 1.004 |  |
| 2001 | 1.019 | 1.010 | 1.033 | 1.042 | 1.023 | 1.014 | 0.994 |  |  |
| 2002 | 0.996 | 1.031 | 1.045 | 1.021 | 1.006 | 1.003 |  |  |  |
| 2003 | 0.956 | 0.998 | 0.990 | 0.978 | 0.991 |  |  |  |  |
| 2004 | 0.887 | 0.953 | 0.965 | 0.979 |  |  |  |  |  |
| 2005 | 0.937 | 0.968 | 0.950 |  |  |  |  |  |  |
| 2006 | 0.964 | 0.948 |  |  |  |  |  |  |  |
| 2007 | 0.962 |  |  |  |  |  |  |  |  |

From Exhibit 1, ratio of successive ultimate loss estimates by accident year

OTHER LIABILITY OCCURRENCE
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE
CUMULATIVE DEVELOPMENT IN ULTIMATE LOSS ESTIMATES BASED ON LOG OF LINK RATIOS

| Months of Maturity |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |
| 1987 | -1.794\% | -6.754\% | -6.737\% | -4.223\% | -5.017\% | -3.326\% | -0.245\% | -3.039\% | -0.569\% |
| 1988 | -3.901\% | -2.424\% | -5.403\% | -3.469\% | -2.079\% | -1.249\% | -2.493\% | -0.034\% | -0.998\% |
| 1989 | -2.316\% | -3.759\% | -2.390\% | -2.576\% | -0.572\% | -1.444\% | -0.569\% | -0.208\% | -1.367\% |
| 1990 | -2.205\% | -1.161\% | -3.176\% | -1.406\% | -1.323\% | -1.113\% | 0.441\% | -1.821\% | -1.035\% |
| 1991 | -1.186\% | 0.839\% | -1.993\% | -2.008\% | -1.894\% | -0.640\% | -1.958\% | -0.529\% | -1.441\% |
| 1992 | 0.601\% | -2.012\% | -3.353\% | -2.318\% | 0.071\% | -2.006\% | -1.371\% | -1.480\% | -1.093\% |
| 1993 | -0.116\% | 0.319\% | -2.315\% | -0.543\% | -2.614\% | -2.863\% | -1.505\% | -1.788\% | -1.306\% |
| 1994 | 0.079\% | 0.308\% | -0.572\% | -1.172\% | -1.081\% | -3.077\% | -2.176\% | -0.901\% | -0.486\% |
| 1995 | -0.885\% | 0.803\% | -1.284\% | 0.315\% | -2.148\% | -0.873\% | -1.093\% | -0.002\% | 0.193\% |
| 1996 | -0.452\% | 0.934\% | -1.298\% | -0.801\% | -1.659\% | -0.242\% | -1.012\% | 2.142\% | 1.520\% |
| 1997 | 0.765\% | 1.167\% | -1.617\% | 1.051\% | 2.127\% | -0.572\% | 1.734\% | 1.827\% | 1.333\% |
| 1998 | 0.884\% | 3.027\% | 3.429\% | 3.357\% | -0.404\% | 4.394\% | 2.741\% | 0.818\% | 0.277\% |
| 1999 | 2.280\% | 2.242\% | 7.229\% | 2.998\% | 4.029\% | 4.467\% | 2.054\% | -0.054\% | 3.395\% |
| 2000 | 0.094\% | 5.556\% | 6.949\% | 6.668\% | 1.838\% | 0.881\% | 1.357\% | 0.353\% |  |
| 2001 | 1.874\% | 0.952\% | 3.280\% | 4.108\% | 2.269\% | 1.438\% | -0.624\% |  |  |
| 2002 | -0.380\% | 3.097\% | 4.358\% | 2.116\% | 0.627\% | 0.322\% |  |  |  |
| 2003 | -4.546\% | -0.245\% | -1.032\% | -2.247\% | -0.908\% |  |  |  |  |
| 2004 | -12.010\% | -4.773\% | -3.567\% | -2.075\% |  |  |  |  |  |
| 2005 | -6.490\% | -3.281\% | -5.140\% |  |  |  |  |  |  |
| 2006 | -3.664\% | -5.372\% |  |  |  |  |  |  |  |
| 2007 | -3.887\% |  |  |  |  |  |  |  |  |
| Average | -1.774\% | -0.527\% | -0.770\% | -0.124\% | -0.514\% | -0.369\% | -0.315\% | -0.337\% | -0.121\% |
|  | 12-108 | 24-108 | 36-108 | 48-108 | 60-108 | 72-108 | 84-108 | 96-108 | 108-108 |
| Cumulative Average | -4.850\% | -3.076\% | -2.549\% | -1.779\% | -1.655\% | -1.141\% | -0.773\% | -0.458\% | -0.121\% |

From Exhibit 2, natural log of ratio of successive ultimate loss estimates by accident year

OTHER LIABILITY OCCURRENCE
SECTION E
INDUSTRY NET BOOKED ULTIMATE LOSS \& ALAE

## VARIANCE-COVARIANCE MATRIX OF LOG OF INCREMENTAL LINK RATIOS

| Months of Maturity | 12-108 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 | 120-Ultimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12-108 | 0.101\% | 0.061\% | 0.068\% | 0.045\% | 0.023\% | 0.019\% | 0.013\% | 0.006\% | 0.014\% | 0.000\% |
| 24-36 | 0.061\% | 0.094\% | 0.096\% | 0.070\% | 0.037\% | 0.040\% | 0.020\% | 0.024\% | 0.018\% | 0.000\% |
| 36-48 | 0.068\% | 0.096\% | 0.152\% | 0.101\% | 0.065\% | 0.070\% | 0.038\% | 0.023\% | 0.034\% | 0.000\% |
| 48-60 | 0.045\% | 0.070\% | 0.101\% | 0.081\% | 0.045\% | 0.047\% | 0.030\% | 0.019\% | 0.021\% | 0.000\% |
| 60-72 | 0.023\% | 0.037\% | 0.065\% | 0.045\% | 0.045\% | 0.033\% | 0.020\% | 0.015\% | 0.020\% | 0.000\% |
| 72-84 | 0.019\% | 0.040\% | 0.070\% | 0.047\% | 0.033\% | 0.050\% | 0.026\% | 0.017\% | 0.022\% | 0.000\% |
| 84-96 | 0.013\% | 0.020\% | 0.038\% | 0.030\% | 0.020\% | 0.026\% | 0.025\% | 0.007\% | 0.014\% | 0.000\% |
| 96-108 | 0.006\% | 0.024\% | 0.023\% | 0.019\% | 0.015\% | 0.017\% | 0.007\% | 0.019\% | 0.011\% | 0.000\% |
| 108-120 | 0.014\% | 0.018\% | 0.034\% | 0.021\% | 0.020\% | 0.022\% | 0.014\% | 0.011\% | 0.019\% | 0.000\% |
| 120-Ultimate | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% | 0.000\% |
| Variance ( $\mathbf{\sigma}^{\mathbf{2}}$ ) | 3.050\% | 2.450\% | 1.746\% | 0.932\% | 0.526\% | 0.305\% | 0.127\% | 0.060\% | 0.019\% | 0.000\% |

Notes
From Exhibit 3, covariance of errors at given maturity with errors at all other maturities
Covariances above diagonal are symmetric with those below
Variance is sum of matrix for all maturities greater than or equal to maturity shown in column

Selection of loss \& alae ratio, ulae factor, and loss \& lae ratio
Dollars in Thousands

|  | Net <br> Earned Premium | Net Ultimate Loss \& LAE | Net <br> Ultimate Loss \& ALAE | $\begin{gathered} \text { Net } \\ \text { Paid } \\ \text { Loss \& ALAE } \\ \hline \end{gathered}$ | Net <br> Unpaid Loss \& ALAE | Net Ultimate Loss \& LAE Ratio | Net <br> Ultimate Loss \& ALAE Ratio | ULAE <br> Factor | Underwriting <br> Expense Ratio |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) |
| 1987 | 14,291,671 | 8,245,541 | 7,803,623 | 6,683,895 | 1,119,728 | 57.7\% | 54.6\% | 1.057 | 22.6\% | 77.4\% |
| 1988 | 13,564,797 | 8,520,718 | 8,080,501 | 7,137,308 | 943,193 | 62.8\% | 59.6\% | 1.054 | 24.5\% | 75.5\% |
| 1989 | 12,386,042 | 8,742,917 | 8,283,756 | 7,364,261 | 919,495 | 70.6\% | 66.9\% | 1.055 | 26.0\% | 74.0\% |
| 1990 | 12,411,178 | 8,938,207 | 8,392,058 | 7,478,012 | 914,046 | 72.0\% | 67.6\% | 1.065 | 26.7\% | 73.3\% |
| 1991 | 11,520,825 | 8,476,299 | 7,902,927 | 7,077,850 | 825,077 | 73.6\% | 68.6\% | 1.073 | 28.3\% | 71.7\% |
| 1992 | 11,344,293 | 8,177,522 | 7,604,931 | 6,904,651 | 700,280 | 72.1\% | 67.0\% | 1.075 | 27.9\% | 72.1\% |
| 1993 | 10,900,968 | 8,276,302 | 7,670,083 | 7,085,431 | 584,652 | 75.9\% | 70.4\% | 1.079 | 27.8\% | 72.2\% |
| 1994 | 11,080,131 | 8,734,738 | 8,106,941 | 7,595,110 | 511,831 | 78.8\% | 73.2\% | 1.077 | 27.0\% | 73.0\% |
| 1995 | 11,403,009 | 9,291,483 | 8,604,084 | 7,937,811 | 666,273 | 81.5\% | 75.5\% | 1.080 | 28.3\% | 71.7\% |
| 1996 | 11,680,096 | 10,016,969 | 9,262,316 | 8,410,530 | 851,786 | 85.8\% | 79.3\% | 1.081 | 26.6\% | 73.4\% |
| 1997 | 12,399,909 | 11,633,294 | 10,843,992 | 9,753,103 | 1,090,889 | 93.8\% | 87.5\% | 1.073 | 27.1\% | 72.9\% |
| 1998 | 13,177,772 | 13,955,806 | 13,048,118 | 11,305,671 | 1,742,447 | 105.9\% | 99.0\% | 1.070 | 29.5\% | 70.5\% |
| 1999 | 12,274,900 | 13,793,567 | 12,936,281 | 11,207,812 | 1,728,469 | 112.4\% | 105.4\% | 1.066 | 30.9\% | 69.1\% |
| 2000 | 12,328,944 | 13,221,613 | 12,364,579 | 10,817,577 | 1,547,002 | 107.2\% | 100.3\% | 1.069 | 29.5\% | 70.5\% |
| 2001 | 13,103,263 | 14,314,992 | 13,325,195 | 11,139,425 | 2,185,770 | 109.2\% | 101.7\% | 1.074 | 28.6\% | 71.4\% |
| 2002 | 17,548,879 | 14,786,490 | 13,945,357 | 11,253,888 | 2,691,469 | 84.3\% | 79.5\% | 1.060 | 25.4\% | 74.6\% |
| 2003 | 21,776,064 | 14,961,194 | 13,937,881 | 10,621,280 | 3,316,601 | 68.7\% | 64.0\% | 1.073 | 22.8\% | 77.2\% |
| 2004 | 25,499,752 | 14,900,390 | 13,935,832 | 9,206,140 | 4,729,692 | 58.4\% | 54.7\% | 1.069 | 25.4\% | 74.6\% |
| 2005 | 25,653,043 | 15,419,386 | 14,378,626 | 7,748,686 | 6,629,940 | 60.1\% | 56.1\% | 1.072 | 25.4\% | 74.6\% |
| 2006 | 28,520,199 | 17,768,275 | 16,612,206 | 6,469,418 | 10,142,788 | 62.3\% | 58.2\% | 1.070 | 25.5\% | 74.5\% |
| 2007 | 28,550,977 | 19,214,123 | 18,021,362 | 4,443,315 | 13,578,047 | 67.3\% | 63.1\% | 1.066 | 26.4\% | 73.6\% |
| 2008 | 26,731,149 | 19,128,358 | 17,908,920 | 1,678,871 | 16,230,049 | 71.6\% | 67.0\% | 1.068 | 27.9\% | 72.1\% |
| Selected |  |  |  |  | 73,649,524 |  | 67.0\% | 1.069 |  | 72.1\% |

Notes
(1), (2) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1H-1
(3) Exhibit 1, Latest Evaluation
(4) Data from SNL Financial LC, 1996-2008 Annual Statements, Industry Total, Schedule P, Part 1H-1
(5) $=(3)-(4)$
(6) $=(2) /(1)$
(7) $=(3) /(1)$; Selected from 2008
(8) $=(6) /(7)$; Selected from 2005-2007 Average
(9) From AM Best Aggregates and Averages, includes policyholder dividends
(10) $=1$ - (9); Selected from 2008

OTHER LIABILITY OCCURRENCE
INDUSTRY PAYOUT PATTERN (PAID LOSS \& ALAE)
Dollars in Thousands
Months of Maturity

| Months of Maturity |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | 12 | $\underline{24}$ | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 |
| 1987 | 539,328 | 1,556,961 | 2,673,397 | 3,800,613 | 4,800,405 | 5,517,892 | 6,053,023 | 6,405,363 | 6,570,948 | 6,683,895 |
| 1988 | 959,076 | 1,904,412 | 3,121,034 | 4,396,712 | 5,337,418 | 6,046,903 | 6,541,614 | 6,824,942 | 7,017,356 | 7,137,308 |
| 1989 | 999,938 | 2,043,505 | 3,329,789 | 4,594,674 | 5,542,622 | 6,319,100 | 6,770,714 | 7,077,793 | 7,281,415 | 7,364,261 |
| 1990 | 1,469,766 | 2,020,695 | 3,344,513 | 4,615,497 | 5,635,764 | 6,922,801 | 6,802,379 | 7,129,194 | 7,304,642 | 7,478,012 |
| 1991 | 981,915 | 1,881,997 | 3,246,969 | 4,486,006 | 5,388,761 | 5,970,889 | 6,426,686 | 6,676,421 | 6,895,646 | 7,077,850 |
| 1992 | 809,655 | 1,904,184 | 3,222,764 | 4,402,457 | 5,200,068 | 5,883,646 | 6,310,691 | 6,579,060 | 6,809,279 | 6,904,651 |
| 1993 | 832,294 | 2,034,096 | 3,314,309 | 4,604,116 | 5,469,513 | 5,986,369 | 6,373,138 | 6,657,735 | 6,880,548 | 7,085,431 |
| 1994 | 897,948 | 2,114,522 | 3,569,250 | 4,775,790 | 5,685,176 | 6,397,278 | 6,894,879 | 7,184,362 | 7,433,002 | 7,595,110 |
| 1995 | 998,874 | 2,306,297 | 3,761,851 | 4,897,240 | 5,771,311 | 6,535,177 | 7,115,873 | 7,482,085 | 7,743,799 | 7,937,811 |
| 1996 | 1,031,079 | 2,330,423 | 3,848,052 | 5,355,401 | 6,393,906 | 7,111,288 | 7,683,278 | 7,905,586 | 8,200,561 | 8,410,530 |
| 1997 | 1,107,399 | 2,581,997 | 4,492,981 | 6,104,803 | 7,480,770 | 8,399,171 | 8,845,383 | 9,252,423 | 9,446,321 | 9,753,103 |
| 1998 | 1,395,386 | 3,248,148 | 5,380,542 | 7,334,567 | 8,625,616 | 9,684,715 | 10,290,981 | 10,662,747 | 11,018,271 | 11,305,671 |
| 1999 | 1,571,650 | 3,426,380 | 5,808,632 | 7,515,166 | 8,806,146 | 9,500,278 | 10,203,329 | 10,623,155 | 10,922,828 | 11,207,812 |
| 2000 | 1,718,409 | 3,736,120 | 5,790,499 | 7,499,102 | 8,660,215 | 9,282,859 | 9,912,388 | 10,476,035 | 10,817,577 |  |
| 2001 | 1,863,360 | 3,901,104 | 6,069,016 | 7,647,345 | 8,784,261 | 9,826,543 | 10,665,878 | 11,139,425 |  |  |
| 2002 | 1,994,171 | 3,666,805 | 5,793,758 | 7,687,085 | 9,326,401 | 10,289,055 | 11,253,888 |  |  |  |
| 2003 | 1,793,072 | 3,695,577 | 5,805,277 | 7,679,899 | 9,197,443 | 10,621,280 |  |  |  |  |
| 2004 | 1,968,910 | 3,592,377 | 5,544,136 | 7,487,781 | 9,206,140 |  |  |  |  |  |
| 2005 | 2,111,707 | 3,782,031 | 5,643,607 | 7,748,686 |  |  |  |  |  |  |
| 2006 | 2,056,885 | 3,967,470 | 6,469,418 |  |  |  |  |  |  |  |
| 2007 | 2,162,645 | 4,443,315 |  |  |  |  |  |  |  |  |
| 2008 | 1,678,871 |  |  |  |  |  |  |  |  |  |
| Age-to-Age Paid Loss Development |  |  |  |  |  |  |  |  |  |  |
| Accident Year | 12-24 | 24-36 | 36-48 | 48-60 | 60-72 | 72-84 | 84-96 | 96-108 | 108-120 |  |
| 1987 | 2.887 | 1.717 | 1.422 | 1.263 | 1.149 | 1.097 | 1.058 | 1.026 | 1.017 |  |
| 1988 | 1.986 | 1.639 | 1.409 | 1.214 | 1.133 | 1.082 | 1.043 | 1.028 | 1.017 |  |
| 1989 | 2.044 | 1.629 | 1.380 | 1.206 | 1.140 | 1.071 | 1.045 | 1.029 | 1.011 |  |
| 1990 | 1.375 | 1.655 | 1.380 | 1.221 | 1.228 | 0.983 | 1.048 | 1.025 | 1.024 |  |
| 1991 | 1.917 | 1.725 | 1.382 | 1.201 | 1.108 | 1.076 | 1.039 | 1.033 | 1.026 |  |
| 1992 | 2.352 | 1.692 | 1.366 | 1.181 | 1.131 | 1.073 | 1.043 | 1.035 | 1.014 |  |
| 1993 | 2.444 | 1.629 | 1.389 | 1.188 | 1.094 | 1.065 | 1.045 | 1.033 | 1.030 |  |
| 1994 | 2.355 | 1.688 | 1.338 | 1.190 | 1.125 | 1.078 | 1.042 | 1.035 | 1.022 |  |
| 1995 | 2.309 | 1.631 | 1.302 | 1.178 | 1.132 | 1.089 | 1.051 | 1.035 | 1.025 |  |
| 1996 | 2.260 | 1.651 | 1.392 | 1.194 | 1.112 | 1.080 | 1.029 | 1.037 | 1.026 |  |
| 1997 | 2.332 | 1.740 | 1.359 | 1.225 | 1.123 | 1.053 | 1.046 | 1.021 | 1.032 |  |
| 1998 | 2.328 | 1.656 | 1.363 | 1.176 | 1.123 | 1.063 | 1.036 | 1.033 | 1.026 |  |
| 1999 | 2.180 | 1.695 | 1.294 | 1.172 | 1.079 | 1.074 | 1.041 | 1.028 | 1.026 |  |
| 2000 | 2.174 | 1.550 | 1.295 | 1.155 | 1.072 | 1.068 | 1.057 | 1.033 |  |  |
| 2001 | 2.094 | 1.556 | 1.260 | 1.149 | 1.119 | 1.085 | 1.044 |  |  |  |
| 2002 | 1.839 | 1.580 | 1.327 | 1.213 | 1.103 | 1.094 |  |  |  |  |
| 2003 | 2.061 | 1.571 | 1.323 | 1.198 | 1.155 |  |  |  |  |  |
| 2004 | 1.825 | 1.543 | 1.351 | 1.229 |  |  |  |  |  |  |
| 2005 | 1.791 | 1.492 | 1.373 |  |  |  |  |  |  |  |
| 2006 | 1.929 | 1.631 |  |  |  |  |  |  |  |  |
| 2007 | 2.055 |  |  |  |  |  |  |  |  |  |
| Averages |  |  |  |  |  |  |  |  |  |  |
| 10-Yr Weighted | 2.010 | 1.596 | 1.330 | 1.188 | 1.113 | 1.075 | 1.043 | 1.032 | 1.025 |  |
| 10-Yr Straight | 2.027 | 1.601 | 1.334 | 1.189 | 1.114 | 1.075 | 1.043 | 1.032 | 1.025 |  |
| Selected | 2.010 | 1.596 | 1.330 | 1.188 | 1.113 | 1.075 | 1.043 | 1.032 | 1.025 |  |


| Fitted Age-to-Ultimate |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Curve Fits: | R-squared | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| Weibull | 98.8\% | 1.070 | 1.051 | 1.037 | 1.027 | 1.020 | 1.015 | 1.011 | 1.008 | 1.006 | 1.005 | 1.004 | 1.003 | 1.002 |
| Power Curve | 99.3\% | 1.039 | 1.025 | 1.016 | 1.010 | 1.007 | 1.004 | 1.003 | 1.002 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 |
| Inverse Power Curve | 94.9\% | 1.267 | 1.233 | 1.205 | 1.181 | 1.161 | 1.144 | 1.129 | 1.115 | 1.104 | 1.093 | 1.083 | 1.075 | 1.067 |


| Selected Pattern | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 | 192 | 204 | 216 | 228 | 240 | 252 | 264 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age-to-Age | 2.010 | 1.596 | 1.330 | 1.188 | 1.113 | 1.075 | 1.043 | 1.032 | 1.025 | 1.013 | 1.009 | 1.006 | 1.004 | 1.002 | 1.002 | 1.001 | 1.001 | 1.000 | 1.000 | 1.000 | 1.000 |  |
| Age-to-Ultimate | 6.958 | 3.462 | 2.170 | 1.631 | 1.373 | 1.233 | 1.147 | 1.099 | 1.065 | 1.039 | 1.025 | 1.016 | 1.010 | 1.007 | 1.004 | 1.003 | 1.002 | 1.001 | 1.001 | 1.000 | 1.000 | 1.00 |
| Cumulative \% Paid | 14.4\% | 28.9\% | 46.1\% | 61.3\% | 72.9\% | 81.1\% | 87.2\% | 91.0\% | 93.9\% | 96.3\% | 97.6\% | 98.4\% | 99.0\% | 99.3\% | 99.6\% | 99.7\% | 99.8\% | 99.9\% | 99.9\% | 100.0\% | 100.0\% | 100.0\% |
| Incremental \% Paid | 14.4\% | 14.5\% | 17.2\% | 15.2\% | 11.6\% | 8.3\% | 6.1\% | 3.8\% | 2.9\% | 2.4\% | 1.3\% | 0.8\% | 0.6\% | 0.4\% | 0.2\% | 0.2\% | 0.1\% | 0.1\% | 0.0\% | 0.0\% | 0.0\% | $0.0 \%$ |

[^9]|  | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Duration | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) | (15) | (16) | (17) | (18) | (19) |
| 1 month | 0.11\% | 2.76\% | 4.75\% | 4.01\% | 1.89\% | 0.90\% | 1.20\% | 1.68\% | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |
| 3 months | 0.11\% | 3.36\% | 5.02\% | 4.08\% | 2.22\% | 0.95\% | 1.22\% | 1.74\% | 5.89\% | 5.33\% | 4.48\% | 5.36\% | 5.21\% | 5.10\% | 5.68\% | 3.07\% | 3.15\% | 3.96\% | 6.63\% |
| 6 months | 0.27\% | 3.49\% | 5.09\% | 4.37\% | 2.59\% | 1.02\% | 1.23\% | 1.83\% | 5.70\% | 5.74\% | 4.55\% | 5.45\% | 5.33\% | 5.17\% | 6.51\% | 3.30\% | 3.38\% | 4.00\% | 6.73\% |
| 1 year | 0.37\% | 3.34\% | 5.00\% | 4.38\% | 2.75\% | 1.26\% | 1.32\% | 2.17\% | 5.32\% | 5.98\% | 4.53\% | 5.51\% | 5.51\% | 5.18\% | 7.20\% | 3.63\% | 3.61\% | 4.12\% | 6.82\% |
| 2 years | 0.76\% | 3.05\% | 4.82\% | 4.41\% | 3.08\% | 1.84\% | 1.61\% | 3.07\% | 5.11\% | 6.24\% | 4.54\% | 5.66\% | 5.88\% | 5.18\% | 7.69\% | 4.25\% | 4.56\% | 4.77\% | 7.15\% |
| 3 years | 1.00\% | 3.07\% | 4.74\% | 4.37\% | 3.25\% | 2.37\% | 1.99\% | 3.59\% | 5.06\% | 6.29\% | 4.55\% | 5.68\% | 6.04\% | 5.25\% | 7.80\% | 4.58\% | 5.12\% | 5.11\% | 7.40\% |
| 5 years | 1.55\% | 3.45\% | 4.70\% | 4.35\% | 3.63\% | 3.25\% | 2.78\% | 4.38\% | 4.99\% | 6.36\% | 4.56\% | 5.71\% | 6.21\% | 5.38\% | 7.83\% | 5.21\% | 6.04\% | 5.93\% | 7.68\% |
| 7 years | 1.87\% | 3.70\% | 4.70\% | 4.36\% | 3.94\% | 3.77\% | 3.36\% | 4.84\% | 5.16\% | 6.55\% | 4.73\% | 5.77\% | 6.34\% | 5.49\% | 7.84\% | 5.53\% | 6.43\% | 6.38\% | 8.00\% |
| 10 years | 2.25\% | 4.04\% | 4.71\% | 4.39\% | 4.24\% | 4.27\% | 3.83\% | 5.07\% | 5.12\% | 6.45\% | 4.65\% | 5.75\% | 6.43\% | 5.58\% | 7.84\% | 5.83\% | 6.70\% | 6.71\% | 8.08\% |
| 20 years | 3.05\% | 4.50\% | 4.91\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.74\% | 5.59\% | 6.83\% | 5.39\% | 6.02\% | 6.73\% | 6.01\% | 8.02\% | 6.48\% | 7.05\% | 7.06\% | 8.17\% |
| 30 years | 2.69\% | 4.45\% | 4.81\% | 4.61\% | 4.85\% | 5.10\% | 4.83\% | 5.48\% | 5.46\% | 6.48\% | 5.09\% | 5.93\% | 6.65\% | 5.96\% | 7.89\% | 6.35\% | 7.40\% | 7.41\% | 8.26\% |


| Discount Factor | 12/31/2008 | 12/31/2007 | 12/29/2006 | 12/30/2005 | 12/31/2004 | 12/31/2003 | 12/31/2002 | 12/31/2001 | 12/29/2000 | 12/31/1999 | 12/31/1998 | 12/31/1997 | 12/31/1996 | 12/29/1995 | 12/30/1994 | 12/31/1993 | 12/31/1992 | 12/31/1991 | 12/31/1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (months) | (20) | (21) | (22) | (23) | (24) | (25) | (26) | (27) | (28) | (29) | (30) | (31) | (32) | (33) | (34) | (35) | (36) | (37) | (38) |
| 6 | 0.999 | 0.983 | 0.975 | 0.979 | 0.987 | 0.995 | 0.994 | 0.991 | 0.973 | 0.972 | 0.978 | 0.974 | 0.974 | 0.975 | 0.969 | 0.984 | 0.984 | 0.981 | 0.968 |
| 18 | 0.992 | 0.954 | 0.931 | 0.938 | 0.958 | 0.977 | 0.978 | 0.962 | 0.927 | 0.915 | 0.936 | 0.922 | 0.920 | 0.927 | 0.898 | 0.944 | 0.942 | 0.937 | 0.904 |
| 30 | 0.978 | 0.927 | 0.890 | 0.898 | 0.925 | 0.949 | 0.956 | 0.921 | 0.883 | 0.859 | 0.895 | 0.871 | 0.865 | 0.881 | 0.830 | 0.898 | 0.889 | 0.886 | 0.839 |
| 42 | 0.961 | 0.897 | 0.851 | 0.861 | 0.891 | 0.914 | 0.927 | 0.878 | 0.842 | 0.807 | 0.856 | 0.824 | 0.813 | 0.835 | 0.769 | 0.850 | 0.833 | 0.834 | 0.777 |
| 54 | 0.939 | 0.862 | 0.813 | 0.825 | 0.855 | 0.874 | 0.892 | 0.832 | 0.803 | 0.758 | 0.818 | 0.779 | 0.764 | 0.791 | 0.713 | 0.801 | 0.776 | 0.778 | 0.719 |
| 66 | 0.915 | 0.827 | 0.777 | 0.791 | 0.819 | 0.833 | 0.853 | 0.785 | 0.763 | 0.711 | 0.781 | 0.736 | 0.717 | 0.749 | 0.661 | 0.753 | 0.721 | 0.724 | 0.663 |
| 78 | 0.891 | 0.793 | 0.742 | 0.758 | 0.782 | 0.793 | 0.814 | 0.741 | 0.723 | 0.664 | 0.742 | 0.695 | 0.672 | 0.708 | 0.612 | 0.708 | 0.671 | 0.674 | 0.609 |
| 90 | 0.866 | 0.758 | 0.709 | 0.726 | 0.746 | 0.753 | 0.776 | 0.700 | 0.686 | 0.622 | 0.708 | 0.657 | 0.630 | 0.669 | 0.568 | 0.665 | 0.625 | 0.626 | 0.561 |
| 102 | 0.841 | 0.724 | 0.677 | 0.695 | 0.711 | 0.715 | 0.741 | 0.663 | 0.653 | 0.586 | 0.677 | 0.621 | 0.591 | 0.633 | 0.526 | 0.625 | 0.582 | 0.583 | 0.518 |
| 114 | 0.814 | 0.690 | 0.646 | 0.665 | 0.677 | 0.677 | 0.705 | 0.627 | 0.622 | 0.551 | 0.649 | 0.588 | 0.554 | 0.598 | 0.488 | 0.586 | 0.542 | 0.542 | 0.479 |
| 126 | 0.788 | 0.658 | 0.616 | 0.636 | 0.645 | 0.642 | 0.671 | 0.593 | 0.591 | 0.518 | 0.618 | 0.555 | 0.519 | 0.564 | 0.452 | 0.550 | 0.505 | 0.505 | 0.442 |
| 138 | 0.764 | 0.629 | 0.587 | 0.608 | 0.614 | 0.610 | 0.638 | 0.560 | 0.559 | 0.484 | 0.586 | 0.523 | 0.486 | 0.532 | 0.419 | 0.516 | 0.472 | 0.471 | 0.409 |
| 150 | 0.739 | 0.601 | 0.559 | 0.581 | 0.584 | 0.578 | 0.607 | 0.528 | 0.528 | 0.453 | 0.554 | 0.493 | 0.455 | 0.501 | 0.387 | 0.483 | 0.440 | 0.440 | 0.378 |
| 162 | 0.714 | 0.574 | 0.532 | 0.554 | 0.555 | 0.548 | 0.575 | 0.498 | 0.499 | 0.423 | 0.524 | 0.464 | 0.425 | 0.471 | 0.358 | 0.452 | 0.410 | 0.410 | 0.349 |
| 174 | 0.688 | 0.547 | 0.507 | 0.529 | 0.527 | 0.518 | 0.545 | 0.468 | 0.471 | 0.395 | 0.494 | 0.437 | 0.398 | 0.443 | 0.331 | 0.422 | 0.382 | 0.382 | 0.322 |
| 186 | 0.663 | 0.521 | 0.482 | 0.505 | 0.500 | 0.489 | 0.515 | 0.440 | 0.444 | 0.368 | 0.465 | 0.411 | 0.372 | 0.416 | 0.306 | 0.394 | 0.356 | 0.355 | 0.298 |
| 198 | 0.637 | 0.496 | 0.458 | 0.481 | 0.473 | 0.461 | 0.485 | 0.413 | 0.418 | 0.343 | 0.438 | 0.387 | 0.347 | 0.391 | 0.283 | 0.368 | 0.331 | 0.331 | 0.275 |
| 210 | 0.612 | 0.472 | 0.436 | 0.459 | 0.448 | 0.433 | 0.457 | 0.387 | 0.394 | 0.320 | 0.411 | 0.364 | 0.324 | 0.367 | 0.261 | 0.342 | 0.308 | 0.307 | 0.254 |
| 222 | 0.586 | 0.448 | 0.414 | 0.437 | 0.423 | 0.407 | 0.429 | 0.362 | 0.370 | 0.297 | 0.386 | 0.342 | 0.302 | 0.344 | 0.241 | 0.318 | 0.286 | 0.286 | 0.234 |
| 234 | 0.561 | 0.426 | 0.393 | 0.416 | 0.399 | 0.382 | 0.402 | 0.339 | 0.348 | 0.277 | 0.362 | 0.321 | 0.282 | 0.322 | 0.223 | 0.296 | 0.266 | 0.265 | 0.216 |
| 246 | 0.542 | 0.406 | 0.375 | 0.397 | 0.379 | 0.361 | 0.380 | 0.319 | 0.328 | 0.259 | 0.342 | 0.302 | 0.263 | 0.302 | 0.206 | 0.276 | 0.247 | 0.246 | 0.200 |
| 258 | 0.530 | 0.389 | 0.358 | 0.379 | 0.361 | 0.343 | 0.363 | 0.304 | 0.312 | 0.244 | 0.326 | 0.285 | 0.247 | 0.286 | 0.191 | 0.260 | 0.229 | 0.228 | 0.184 |

$\frac{\text { Notes }}{(1)-(19)}$ Data from U.S. Treasury
ittp://www.treasury.gov/offices/domestic-finance/debt-management/interest-rate/yield_historical_main.shtml
(20)-(38) Computed from (1)-(19), by interpolation of rates, compounded for number of months indicated


OTHER LIABILITY OCCURRENCE
INDUSTRY NET RESULTS
SECTION E

DURATION OF PAYOUT OF ACCIDENT YEAR LOSSES

| Accident Year <br> Age <br> (Months) | Cumulative <br> Paid <br> Development <br> Factor | Cumulative <br> Percent <br> Paid | Incremental <br> Percent <br> Paid | Duration |
| :---: | :---: | :---: | :---: | :---: |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
| 12 | 6.958 | $14.4 \%$ | $14.4 \%$ | 0.07 |
| 24 | 3.462 | $28.9 \%$ | $14.5 \%$ | 0.22 |
| 36 | 2.170 | $46.1 \%$ | $17.2 \%$ | 0.43 |
| 48 | 1.631 | $61.3 \%$ | $15.2 \%$ | 0.53 |
| 60 | 1.373 | $72.9 \%$ | $11.6 \%$ | 0.52 |
| 72 | 1.233 | $81.1 \%$ | $8.3 \%$ | 0.45 |
| 84 | 1.147 | $87.2 \%$ | $6.1 \%$ | 0.40 |
| 96 | 1.099 | $91.0 \%$ | $3.8 \%$ | 0.28 |
| 108 | 1.065 | $93.9 \%$ | $2.9 \%$ | 0.25 |
| 120 | 1.039 | $96.3 \%$ | $2.4 \%$ | 0.23 |
| 132 | 1.025 | $97.6 \%$ | $1.3 \%$ | 0.14 |
| 144 | 1.016 | $98.4 \%$ | $0.8 \%$ | 0.10 |
| 156 | 1.010 | $99.0 \%$ | $0.6 \%$ | 0.07 |
| 168 | 1.007 | $99.3 \%$ | $0.4 \%$ | 0.05 |
| 180 | 1.004 | $99.6 \%$ | $0.2 \%$ | 0.03 |
| 192 | 1.003 | $99.7 \%$ | $0.2 \%$ | 0.02 |
| 204 | 1.002 | $99.8 \%$ | $0.1 \%$ | 0.02 |
| 216 | 1.001 | $99.9 \%$ | $0.1 \%$ | 0.01 |
| 228 | 1.001 | $99.9 \%$ | $0.0 \%$ | 0.01 |
| 240 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.01 |
| 252 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.00 |
| 264 | 1.000 | $100.0 \%$ | $0.0 \%$ | 0.01 |
|  |  |  |  |  |
| Total |  |  |  |  |
|  |  |  |  |  |
| Duration (years) |  |  |  |  |

Notes
(2) From Exhibit 6
(3) $=1 /$ (2)
(4) From (2)
(5) $=(4) *[(1) / 12-0.5]$

OTHER LIABILITY OCCURRENCE
INDUSTRY NET RESULTS
SECTION E

DEVELOPED INDUSTRY ULTIMATE LOSS \& ALAE
Dollars in Thousands

|  | Net <br> Booked Ultimate Loss \& ALAE | Average Development Parameter <br> $\mu$ | Variance Development Parameter $\sigma^{2}$ | Net <br> Developed Ultimate Loss \& ALAE | Developed vs Booked Ultimate Loss \& ALAE | Paid Loss \& ALAE | Developed Unpaid Loss \& ALAE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1987 | 7,803,623 | 0.000\% | 0.000\% | 7,803,623 | - | 6,683,895 | 1,119,728 |
| 1988 | 8,080,501 | 0.000\% | 0.000\% | 8,080,501 | - | 7,137,308 | 943,193 |
| 1989 | 8,283,756 | 0.000\% | 0.000\% | 8,283,756 | - | 7,364,261 | 919,495 |
| 1990 | 8,392,058 | 0.000\% | 0.000\% | 8,392,058 | - | 7,478,012 | 914,046 |
| 1991 | 7,902,927 | 0.000\% | 0.000\% | 7,902,927 | - | 7,077,850 | 825,077 |
| 1992 | 7,604,931 | 0.000\% | 0.000\% | 7,604,931 | - | 6,904,651 | 700,280 |
| 1993 | 7,670,083 | 0.000\% | 0.000\% | 7,670,083 | - | 7,085,431 | 584,652 |
| 1994 | 8,106,941 | 0.000\% | 0.000\% | 8,106,941 | - | 7,595,110 | 511,831 |
| 1995 | 8,604,084 | 0.000\% | 0.000\% | 8,604,084 | - | 7,937,811 | 666,273 |
| 1996 | 9,262,316 | 0.000\% | 0.000\% | 9,262,316 | - | 8,410,530 | 851,786 |
| 1997 | 10,843,992 | 0.000\% | 0.000\% | 10,843,992 | - | 9,753,103 | 1,090,889 |
| 1998 | 13,048,118 | 0.000\% | 0.000\% | 13,048,118 | - | 11,305,671 | 1,742,447 |
| 1999 | 12,936,281 | 0.000\% | 0.000\% | 12,936,281 | - | 11,207,812 | 1,728,469 |
| 2000 | 12,364,579 | -0.121\% | 0.019\% | 12,350,775 | $(13,804)$ | 10,817,577 | 1,533,198 |
| 2001 | 13,325,195 | -0.458\% | 0.060\% | 13,268,268 | $(56,927)$ | 11,139,425 | 2,128,843 |
| 2002 | 13,945,357 | -0.773\% | 0.127\% | 13,846,795 | $(98,562)$ | 11,253,888 | 2,592,907 |
| 2003 | 13,937,881 | -1.141\% | 0.305\% | 13,800,757 | $(137,124)$ | 10,621,280 | 3,179,477 |
| 2004 | 13,935,832 | -1.655\% | 0.526\% | 13,743,091 | $(192,741)$ | 9,206,140 | 4,536,951 |
| 2005 | 14,378,626 | -1.779\% | 0.932\% | 14,191,014 | $(187,612)$ | 7,748,686 | 6,442,328 |
| 2006 | 16,612,206 | -2.549\% | 1.746\% | 16,336,113 | $(276,093)$ | 6,469,418 | 9,866,695 |
| 2007 | 18,021,362 | -3.076\% | 2.450\% | 17,690,879 | $(330,483)$ | 4,443,315 | 13,247,564 |
| 2008 | 17,908,920 | -4.850\% | 3.050\% | 17,323,213 | $(585,707)$ | 1,678,871 | 15,644,342 |
| Total | 252,969,569 |  |  | 251,090,515 | $(1,879,054)$ | 179,320,045 | 71,770,470 |

Notes
(1) From Exhibit 5, Column 3
(2) From Exhibit 3, Cumulative Average
(3) From Exhibit 4, Variance
(4) $=(1) * \exp [(2)+(3) / 2]$
(5) $=(4)-(1)$
(6) From Exhibit 5, Column 4
(7) $=(4)-(6)$

|  | 12 month Booked Ultimate Loss \& ALAE Ratio | PV Factor | 1 - Exp Ratio | Loss Ratio Prior to Adjustment | Loss Ratio Adjustment | Adjusted Loss Ratio | Log of <br> Adjusted <br> Loss Ratio | 12 Month <br> Booked <br> Ultimate <br> Loss | Latest Evaluation Ultimate Loss | Ratio Latest to 12 Month Booked | $\begin{aligned} & \text { Log of } \\ & \text { Ratio } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) |
| 1987 | 75.0\% | 0.770 | 77.4\% | 56.9\% | 0.946 | 53.9\% | -61.9\% | 10,715,088 | 7,803,623 | 0.728 | -0.317 |
| 1988 | 74.3\% | 0.770 | 75.5\% | 57.8\% | 0.946 | 54.7\% | -60.4\% | 10,073,805 | 8,080,501 | 0.802 | -0.220 |
| 1989 | 77.9\% | 0.770 | 74.0\% | 61.8\% | 0.946 | 58.5\% | -53.6\% | 9,643,663 | 8,283,756 | 0.859 | -0.152 |
| 1990 | 76.8\% | 0.770 | 73.3\% | 61.6\% | 0.946 | 58.3\% | -54.0\% | 9,537,734 | 8,392,058 | 0.880 | -0.128 |
| 1991 | 76.4\% | 0.817 | 71.7\% | 66.5\% | 0.946 | 62.9\% | -46.3\% | 8,805,106 | 7,902,927 | 0.898 | -0.108 |
| 1992 | 76.3\% | 0.818 | 72.1\% | 66.1\% | 0.946 | 62.5\% | -47.0\% | 8,657,249 | 7,604,931 | 0.878 | -0.130 |
| 1993 | 79.9\% | 0.836 | 72.2\% | 70.6\% | 0.946 | 66.8\% | -40.4\% | 8,711,506 | 7,670,083 | 0.880 | -0.127 |
| 1994 | 80.1\% | 0.767 | 73.0\% | 64.2\% | 0.946 | 60.8\% | -49.8\% | 8,877,242 | 8,106,941 | 0.913 | -0.091 |
| 1995 | 79.3\% | 0.826 | 71.7\% | 69.8\% | 0.946 | 66.0\% | -41.5\% | 9,042,828 | 8,604,084 | 0.951 | -0.050 |
| 1996 | 80.0\% | 0.806 | 73.4\% | 67.0\% | 0.946 | 63.4\% | -45.6\% | 9,342,998 | 9,262,316 | 0.991 | -0.009 |
| 1997 | 80.9\% | 0.818 | 72.9\% | 69.3\% | 0.946 | 65.5\% | -42.3\% | 10,028,801 | 10,843,992 | 1.081 | 0.078 |
| 1998 | 82.3\% | 0.848 | 70.5\% | 75.4\% | 0.819 | 61.8\% | -48.1\% | 10,841,918 | 13,048,118 | 1.203 | 0.185 |
| 1999 | 79.1\% | 0.801 | 69.1\% | 70.0\% | 0.819 | 57.3\% | -55.6\% | 9,714,700 | 12,936,281 | 1.332 | 0.286 |
| 2000 | 79.1\% | 0.834 | 70.5\% | 71.4\% | 0.819 | 58.5\% | -53.6\% | 9,755,953 | 12,364,579 | 1.267 | 0.236 |
| 2001 | 89.0\% | 0.861 | 71.4\% | 81.9\% | 0.819 | 67.1\% | -39.8\% | 11,666,056 | 13,325,195 | 1.142 | 0.129 |
| 2002 | 71.8\% | 0.904 | 74.6\% | 66.4\% | 1.000 | 66.4\% | -40.9\% | 12,600,530 | 13,945,357 | 1.107 | 0.094 |
| 2003 | 70.0\% | 0.893 | 77.2\% | 61.8\% | 1.000 | 61.8\% | -48.1\% | 15,247,263 | 13,937,881 | 0.914 | -0.100 |
| 2004 | 68.4\% | 0.877 | 74.6\% | 61.3\% | 1.000 | 61.3\% | -48.9\% | 17,438,909 | 13,935,832 | 0.799 | -0.238 |
| 2005 | 65.1\% | 0.854 | 74.6\% | 56.9\% | 1.000 | 56.9\% | -56.5\% | 16,690,750 | 14,378,626 | 0.861 | -0.162 |
| 2006 | 63.8\% | 0.844 | 74.5\% | 55.1\% | 1.000 | 55.1\% | -59.6\% | 18,183,265 | 16,612,206 | 0.914 | -0.107 |
| 2007 | 65.6\% | 0.881 | 73.6\% | 59.9\% | 1.000 | 59.9\% | -51.2\% | 18,735,570 | 18,021,362 | 0.962 | -0.057 |
| 2008 | 67.0\% | 0.945 | 72.1\% | 67.0\% | 1.000 | 67.0\% | -40.1\% | 17,908,920 | 17,908,920 | 1.000 | -0.033 |
| (12) Average |  |  |  |  |  | 61.2\% | -49.3\% |  |  |  |  |
| (13) Variance |  |  |  |  |  |  | 0.480\% |  |  |  | 2.424\% |
| (14) Covariance (log of Adjusted Loss Ratio, log of Ratio of Latest to 12 month Booked) |  |  |  |  |  |  | 0.335\% |  |  |  |  |
| (15) Total Variance of Adjusted Loss Ratio (log) and Ratio of Latest to 12 month Booked (log) |  |  |  |  |  |  | 3.573\% |  |  |  |  |

## Notes

(1) Exhibit 1 @ 12 Months / Exhibit 5, Column
(2) 1995-2008 from Exhibit 8, Columns 4-17; 1994 and prior selectec
(3) $=100 \%$ - Exhibit 5, Column 9
(4) $=(1) *(2)_{\text {AYXXXX }} /(2)_{\text {AY2008 }} *(3)_{\text {AY2008 }} /(3)_{\text {AYXXXX }}$
(5) Adjustment of historical loss ratios to normalize for major differences in levels across multi-year periods

AY 1987-1997: AY 2002-2008 Average / AY 1987-1997 Average; AY 1998-2001: AY 2002-2008 Average / AY 1998-2001 Average; 1.000 for AY 2002-200
(6) $=(4) *(5)$
(7) $=\operatorname{LN}(6)$
(8) Exhibit 1 @ 12 Months
(9) Exhibit 1 @ 12 Current Evaluation
$(10)=(9) /(8$
(11) $=\operatorname{LN}(10)+$ Exhibit 10, Column $2+($ Exhibit 10, Column 3)/2
12) Average of Column 7
13) Variance of Column 7 and Column 11
14) Covariance( Column 7, Column 11)
15) = Row 13, Column 7 + Row 13, Column 7 + 2 * Row 14

DERIVATION OF INDUSTRY 2008 MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\lambda$ )

| 1 - ER | $72.1 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.069 |
| PV | 0.945 |
| Target Loss Ratio | $71.4 \%$ |
| ULR12 | $67.0 \%$ |
| $\mu$ | $-4.850 \%$ |
| $\sigma^{2}$ | $3.050 \%$ |
| $\sigma$ | $17.464 \%$ |
| D | 3.839 |
| $\lambda$ | 0.282 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-40.1 \%$ |
| Combined $\mu$ | $-44.9 \%$ |
| $\sigma_{\text {AY ULR }}^{2}$ | $0.480 \%$ |
| $\sigma_{\text {12-ult }}^{2}$ | $2.424 \%$ |
| Cov(AY ULR, 12 -ult) | $0.335 \%$ |
| Combined $\sigma^{2}$ | $3.573 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.253 |
| (2008 market value of risk) |  |

## Notes

## 100\% - Expense Ratio

1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE $) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$

Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12 -ult)
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu_{\mathrm{AY}} \operatorname{ULR}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma \cdot \mathrm{v}(\mathrm{D})]$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, 2008 Accident Year

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11 From Exhibit 11, Row 14, Covariance From Exhibit 11, Row 15

DERIVATION OF INDUSTRY LONG-TERM MARKET VALUE OF RISK PARAMETER ( $\lambda$ )

## Dollars in Thousands

MARKET VALUE OF RISK ( $\boldsymbol{\lambda}$ )

| 1 - ER | $72.1 \%$ |
| :---: | :---: |
| $1+$ ULAE | 1.069 |
| PV | 0.945 |
| Target Loss Ratio | $71.4 \%$ |
| ULR12 | $67.0 \%$ |
| $\mu$ | $-4.850 \%$ |
| $\sigma^{2}$ | $3.050 \%$ |
| $\sigma$ | $17.464 \%$ |
| D | 3.839 |
| $\lambda$ | 0.282 |
|  |  |
| $\mu_{\text {AY ULR }}$ | $-49.3 \%$ |
| Combined $\mu$ | $-54.2 \%$ |
| $\sigma_{\text {AY ULR }}^{2}$ | $0.480 \%$ |
| $\sigma_{12 \text {-ult }}^{2}$ | $2.424 \%$ |
| Cov(AY ULR, 12 -ult) | $0.335 \%$ |
| Combined $\sigma^{2}$ | $3.573 \%$ |
|  |  |
| $\lambda$ adj for pricing risk | 0.503 |

(long-term market value of risk)

## Notes

100\% - Expense Ratio
1 + ULAE Factor
Present Value Factor
$=(1-E R) /(1+$ ULAE $) / P V$
Estimated Ultimate Loss Ratio (at 12 months) of Latest Accident Year Sample mean of development of estimated ultimate losses
Variance of development of estimated ultimate losses
Standard deviation of development of estimated ultimate losses Duration
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\ln (U L R 12)-\mu-1 / 2 \sigma^{2}\right] /[\sigma \cdot v(D)]$

Sample mean of logarithm of Accident Year Ultimate Loss Ratio
$=\mu+\mu_{\mathrm{AY} \text { ULR }}$
Sample variance of logarithm of Accident Year Ultimate Loss Ratio
Sample variance of logarithm of developed accident year ultimate Covariance of Accident Year Loss Ratio and Development $=\sigma_{\text {AY ULR }}^{2}+\sigma_{12-\mathrm{ult}}^{2}+2 \cdot \operatorname{Cov}(A Y$ ULR, 12-ult)
$=\left[\ln (1-E R)-\ln (1+U L A E)-\ln (P V)-\mu_{\text {AY ULR }}-1 / 2 \cdot\right.$ combined $\left.\sigma^{2}\right] /[$ combined $\sigma \cdot v(D)$

From Exhibit 5, Column 10 Selected From Exhibit 5, Column 8 Selected From Exhibit 8, Column 4 Total

From Exhibit 5, Column 7 Selected From Exhibit 10, Column 2, 2008
From Exhibit 10, Column 3, 2008
= square root of $\sigma^{2}$
From Exhibit 9, Total Duration

From Exhibit 11, Row 12, Average

From Exhibit 11, Row 13, Variance of Column 7
From Exhibit 11, Row 13, Variance of Column 11 From Exhibit 11, Row 14, Covariance From Exhibit 11, Row 15

OTHER LIABILITY OCCURRENCE
INDUSTRY NET RESULTS
SECTION E

NET IMPACT OF RISK MARGINS AND DISCOUNT FOR LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands


OTHER LIABILITY OCCURRENCE
INDUSTRY NET RESULTS
SECTION E

RISK MARGIN RESULTS FOR INDUSTRY AND LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands


OTHER LIABILITY OCCURRENCE
INDUSTRY NET RESULTS
PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS
Dollars in Thousands

|  | Total Accident Years 1997-2008 | Accident Year 2008 | Accident Year 2007 | Accident Year 2006 | Accident Year 2005 | Accident Year 2004 | Accident Year 2003 | Accident Year 2002 | Accident Year 2001 | Accident Year 2000 | Accident Year 1999 | Accident Year 1998 | Accident Year 1997 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| Year 1 | 15,849,476 | 2,563,265 | 3,113,260 | 2,695,196 | 1,834,516 | 1,295,767 | 972,108 | 702,895 | 618,680 | 546,304 | 576,884 | 579,763 | 350,835 |
| Year 2 | 13,036,552 | 3,037,868 | 2,753,291 | 2,046,827 | 1,310,107 | 955,348 | 606,068 | 538,815 | 507,883 | 296,264 | 377,709 | 378,127 | 228,244 |
| Year 3 | 9,817,739 | 2,686,615 | 2,090,946 | 1,461,727 | 965,921 | 595,619 | 464,591 | 442,321 | 275,429 | 193,976 | 246,345 | 246,000 | 148,248 |
| Year 4 | 7,014,390 | 2,040,311 | 1,493,235 | 1,077,708 | 602,210 | 456,581 | 381,389 | 239,874 | 180,334 | 126,513 | 160,266 | 159,781 | 96,189 |
| Year 5 | 4,900,305 | 1,457,073 | 1,100,938 | 671,905 | 461,633 | 374,814 | 206,830 | 157,055 | 117,616 | 82,306 | 104,096 | 103,671 | 62,368 |
| Year 6 | 3,400,960 | 1,074,277 | 686,388 | 515,059 | 378,962 | 203,264 | 135,420 | 102,433 | 76,518 | 53,459 | 67,541 | 67,220 | 40,421 |
| Year 7 | 2,310,240 | 669,766 | 526,161 | 422,819 | 205,513 | 133,085 | 88,322 | 66,640 | 49,700 | 34,686 | 43,793 | 43,565 | 26,190 |
| Year 8 | 1,625,063 | 513,419 | 431,933 | 229,298 | 134,558 | 86,799 | 57,460 | 43,284 | 32,247 | 22,490 | 28,382 | 28,227 | 16,966 |
| Year 9 | 1,098,627 | 421,473 | 234,240 | 150,131 | 87,760 | 56,469 | 37,321 | 28,084 | 20,909 | 14,576 | 18,390 | 18,285 | 10,989 |
| Year 10 | 682,973 | 228,568 | 153,367 | 97,916 | 57,094 | 36,678 | 24,215 | 18,209 | 13,551 | 9,444 | 11,913 | 11,844 | 20,173 |
| Year 11 | 446,122 | 149,653 | 100,027 | 63,702 | 37,084 | 23,798 | 15,701 | 11,802 | 8,780 | 6,118 | 7,716 | 21,742 | - |
| Year 12 | 285,185 | 97,605 | 65,075 | 41,376 | 24,061 | 15,430 | 10,176 | 7,647 | 5,688 | 3,963 | 14,165 | - | - |
| Year 13 | 180,719 | 63,499 | 42,267 | 26,846 | 15,601 | 10,000 | 6,593 | 4,953 | 3,684 | 7,275 | - | - | - |
| Year 14 | 116,908 | 41,244 | 27,425 | 17,407 | 10,111 | 6,480 | 4,271 | 3,208 | 6,763 | - | - | - | - |
| Year 15 | 75,229 | 26,760 | 17,782 | 11,281 | 6,551 | 4,197 | 2,766 | 5,890 | - | - | - | - | - |
| Year 16 | 48,226 | 17,351 | 11,525 | 7,309 | 4,244 | 2,719 | 5,079 | - | - | - | - | - | - |
| Year 17 | 31,187 | 11,245 | 7,467 | 4,735 | 2,749 | 4,991 | - | - | - | - | - | - | - |
| Year 18 | 20,236 | 7,286 | 4,837 | 3,067 | 5,046 | - | - | - | - | - | - | - | - |
| Year 19 | 13,483 | 4,720 | 3,133 | 5,630 | - | - | - | - | - | - | - | - | - |
| Year 20 | 8,809 | 3,057 | 5,752 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 5,612 | 5,612 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total | 60,968,044 | 15,120,668 | 12,869,048 | 9,549,940 | 6,143,722 | 4,262,040 | 3,018,311 | 2,373,111 | 1,917,780 | 1,397,376 | 1,657,200 | 1,658,226 | 1,000,622 |

Total equals expected unpaid by accident year
(2) - (13) Based on expected unpaid by accident year and payout pattern from Exhibit 8

DISCOUNTED PAYOUT OF EXPECTED UNPAID LOSS \& ALAE FOR LARGEST 100 U.S. INSURERS

## Dollars in Thousands

## Discounted Payout of 12/31/2008 Expected Unpaid Loss \& ALAE

|  | Discount Factor | Total Accident Years 1997-2008 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 2008 \\ \hline \end{gathered}$ | Accident Year 2007 | Accident Year <br> 2006 | Accident Year 2005 | Accident <br> Year <br> 2004 | Accident Year 2003 | Accident Year 2002 | Accident Year 2001 | Accident Year 2000 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1999 \\ \hline \end{gathered}$ | Accident Year 1998 | $\begin{gathered} \text { Accident } \\ \text { Year } \\ 1997 \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paid in | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| Year 1 | 0.999 | 15,828,122 | 2,559,812 | 3,109,066 | 2,691,565 | 1,832,045 | 1,294,021 | 970,799 | 701,948 | 617,847 | 545,568 | 576,107 | 578,982 | 350,362 |
| Year 2 | 0.992 | 12,926,843 | 3,012,302 | 2,730,120 | 2,029,602 | 1,299,082 | 947,309 | 600,967 | 534,281 | 503,609 | 293,771 | 374,531 | 374,945 | 226,323 |
| Year 3 | 0.978 | 9,605,032 | 2,628,408 | 2,045,645 | 1,430,058 | 944,994 | 582,714 | 454,525 | 432,738 | 269,461 | 189,774 | 241,008 | 240,670 | 145,037 |
| Year 4 | 0.961 | 6,742,131 | 1,961,117 | 1,435,276 | 1,035,878 | 578,836 | 438,859 | 366,586 | 230,563 | 173,335 | 121,603 | 154,045 | 153,579 | 92,455 |
| Year 5 | 0.939 | 4,600,568 | 1,367,949 | 1,033,597 | 630,806 | 433,397 | 351,887 | 194,179 | 147,449 | 110,421 | 77,272 | 97,728 | 97,330 | 58,553 |
| Year 6 | 0.915 | 3,111,580 | 982,869 | 627,984 | 471,234 | 346,717 | 185,969 | 123,897 | 93,717 | 70,007 | 48,911 | 61,794 | 61,500 | 36,982 |
| Year 7 | 0.891 | 2,058,609 | 596,815 | 468,852 | 376,766 | 183,129 | 118,590 | 78,702 | 59,382 | 44,286 | 30,908 | 39,023 | 38,820 | 23,337 |
| Year 8 | 0.866 | 1,407,663 | 444,734 | 374,149 | 198,622 | 116,557 | 75,187 | 49,773 | 37,493 | 27,933 | 19,482 | 24,585 | 24,451 | 14,696 |
| Year 9 | 0.841 | 923,800 | 354,403 | 196,965 | 126,240 | 73,794 | 47,483 | 31,382 | 23,615 | 17,581 | 12,257 | 15,463 | 15,376 | 9,240 |
| Year 10 | 0.814 | 556,107 | 186,110 | 124,878 | 79,728 | 46,489 | 29,865 | 19,717 | 14,827 | 11,034 | 7,690 | 9,700 | 9,644 | 16,426 |
| Year 11 | 0.788 | 351,727 | 117,987 | 78,862 | 50,223 | 29,237 | 18,762 | 12,379 | 9,305 | 6,922 | 4,823 | 6,084 | 17,142 | - |
| Year 12 | 0.764 | 217,841 | 74,556 | 49,708 | 31,605 | 18,379 | 11,787 | 7,773 | 5,841 | 4,345 | 3,027 | 10,820 | - | - |
| Year 13 | 0.739 | 133,538 | 46,921 | 31,232 | 19,837 | 11,528 | 7,390 | 4,872 | 3,660 | 2,722 | 5,375 | - | - | - |
| Year 14 | 0.714 | 83,437 | 29,435 | 19,573 | 12,423 | 7,216 | 4,624 | 3,048 | 2,290 | 4,827 | - | - | - | - |
| Year 15 | 0.688 | 51,776 | 18,418 | 12,238 | 7,764 | 4,509 | 2,889 | 1,904 | 4,054 | - | - | - | - | - |
| Year 16 | 0.663 | 31,959 | 11,499 | 7,637 | 4,844 | 2,812 | 1,802 | 3,366 | - | - | - | - | - | - |
| Year 17 | 0.637 | 19,869 | 7,164 | 4,757 | 3,017 | 1,751 | 3,180 | - | - | - | - | - | - | - |
| Year 18 | 0.612 | 12,375 | 4,456 | 2,958 | 1,876 | 3,086 | - | - | - | - | - | - | - | - |
| Year 19 | 0.586 | 7,903 | 2,766 | 1,836 | 3,300 | - | - | - | - | - | - | - | - | - |
| Year 20 | 0.561 | 4,940 | 1,715 | 3,226 | - | - | - | - | - | - | - | - | - | - |
| Year 21 | 0.542 | 3,042 | 3,042 | - | - | - | - | - | - | - | - | - | - | - |
| Year 22 | 0.530 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| Total |  | 58,678,863 | 14,412,480 | 12,358,560 | 9,205,388 | 5,933,557 | 4,122,318 | 2,923,869 | 2,301,162 | 1,864,330 | 1,360,460 | 1,610,888 | 1,612,439 | 973,411 |

Notes
(1) From Exhibit 7, Column 20
(2) Sum of Columns 3-14
(3) - (14) Product of Column 1 and Exhibit 14, Columns 2-13

OTHER LIABILITY OCCURRENCE
SECTION E
INDUSTRY NET RESULTS
RISK MARGIN RESULTS FOR LARGEST 100 U.S. INSURERS BASED ON LONG-TERM MARKET VALUE OF RISK
Dollars in Thousands

|  | $\begin{gathered} \text { 31-Dec-08 } \\ \text { Booked } \\ \text { Unpaid } \\ \text { Loss \& ALAE } \\ \hline \end{gathered}$ | 31-Dec-08 <br> Expected Unpaid Loss \& ALAE | Average Indicated Risk Margin | Present <br> Value <br> Expected Unpaid Loss \& ALAE | Present <br> Value <br> Discount | Risk-Adjusted <br> Discounted <br> Expected Unpaid Loss \& ALAE | Net Impact of Risk Margins and Discount vs. Booked |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accident Year | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| 1997 | 1,000,622 | 1,000,622 | N/A | 973,411 | -2.7\% | N/A | N/A |
| 1998 | 1,658,226 | 1,658,226 | N/A | 1,612,439 | -2.8\% | N/A | N/A |
| 1999 | 1,657,200 | 1,657,200 | N/A | 1,610,888 | -2.8\% | N/A | N/A |
| 2000 | 1,447,529 | 1,397,376 | N/A | 1,360,460 | -2.6\% | N/A | N/A |
| 2001 | 2,030,975 | 1,917,780 | N/A | 1,864,330 | -2.8\% | N/A | N/A |
| 2002 | 2,421,754 | 2,373,111 | N/A | 2,301,162 | -3.0\% | N/A | N/A |
| 2003 | 3,091,860 | 3,018,311 | N/A | 2,923,869 | -3.1\% | N/A | N/A |
| 2004 | 4,386,332 | 4,262,040 | N/A | 4,122,318 | -3.3\% | N/A | N/A |
| 2005 | 6,112,082 | 6,143,722 | N/A | 5,933,557 | -3.4\% | N/A | N/A |
| 2006 | 9,322,158 | 9,549,940 | N/A | 9,205,388 | -3.6\% | N/A | N/A |
| 2007 | 12,558,570 | 12,869,048 | N/A | 12,358,560 | -4.0\% | N/A | N/A |
| 2008 | 15,029,823 | 15,120,668 | N/A | 14,412,480 | -4.7\% | N/A | N/A |
| Total 1997-2008 | 60,717,131 | 60,968,044 | 13.6\% | 58,678,863 | -3.8\% | 66,667,708 | 9.8\% |

Notes
(3) From Exhibit 13B, Row 13, Total Largest 100 U.S. Insurers
(4) From Exhibit 15, Total by Accident Year
(5) $=(4) /(2)-1$
(6) $=(2)$ Total $*[1+(3)$ Total $]$ [ $1+(5)$ Total $]$
(7) $=(6)$ Total $/(1)$ Total -1


[^0]:    Notes
    Data from SNL Financial LC
    1996-2008 Annual Statements
    Industry Total Commercial Auto Liability
    Schedule P, Part 3C

[^1]:    Notes
    Total equals expected unpaid by accident year

[^2]:    Notes
    Data from SNL Financial LC
    1996-2008 Annual Statements
    Industry Total Commercial Multiple Peril
    Schedule P, Part 3E

[^3]:    Notes
    Total equals expected unpaid by accident year
    (2) - (13) Based on expected unpaid by accident year and payout pattern from Exhibit 8

[^4]:    Notes
    Data from SNL Financial LC
    1996-2008 Annual Statements
    Industry Total Private Passenger Auto Liability
    Schedule P, Part 3B

[^5]:    Notes
    (1) From Exhibit 7, Column 20
    (2) Sum of Columns 3-14

[^6]:    Notes
    From Exhibit 2, natural log of ratio of successive ultimate loss estimates by accident year

[^7]:    Notes
    Data from SNL Financial LC
    1996-2008 Annual Statements
    Industry Total Workers Compensation
    Schedule P, Part 3D

[^8]:    Notes

[^9]:    Notes
    Data from SNL Financial LC
    1996-2008 Annual Statements
    Industry Total Other Liability Occurrence
    Schedule P, Part 3H-1

