No. 119

PROCEEDINGS

May 24, 25, 26, 1976

ACCIDENT LIMITATIONS FOR RETROSPECTIVE RATING

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The need for changes in retrospective rating plan accident limitation charges has been apparent for some time.

This paper describes recently adopted recommendations of the National Council on Compensation Insurance for developing such charges. The charges for accident limitations are familiarly known as Excess Loss Premium Factors or ELPF's. They are percentages of standard earned premium which are paid by the policyholder in lieu of his being charged for losses above a selected limit per accident. These charges also vary by industry grouping (hazard groups) to reflect the differences in expected frequency density and size of claim.

About 25 years ago, a system was developed for calculating ELPF's¹. To Dunbar Uhthoff's great credit, this system has withstood the test of time for most of the 25 years. However, the accelerating impetus of inflation has brought about many qualitative and quantitative changes in insurance. The basic forces at work are:

- a. Monetary inflation (the decreasing purchasing power of the accident limitation).
- b. Loss development (greater development on more severe injuries).
- c. Removal of benefit limitations.
- d. Relatively higher medical cost inflation versus indemnity benefit inflation, increasing the spread of the claim size distribution.

¹ D. Uhthoff, "Excess Loss Ratios via Loss Distributions," PCAS, Vol. XXXVII, (1950), p. 82ff.

RETROSPECTIVE RATING

Both frequency of claims and average claim costs have been seriously affected. In particular, claim costs have risen significantly with the dramatic rise in average weekly wages, medical costs and benefits afforded by workers' compensation laws. As an illustration, countrywide average weekly wages during the first six months of 1950 were \$52.51 compared with \$175.34 for the same period in 1975². Average claim costs for death cases are \$97,024 (Illinois) on 1975 benefit levels compared to \$3,967 (Illinois) which was used in the 1950 paper.

Since that time, many states which had previously limited the maximum dollar amount payable for such claims have enacted laws which provide lifetime benefits with significantly higher costs. Changes of such magnitude are bound to affect distributions of extreme values. Because charges for accident limitations represent costs which are intended to cover (on the average) amounts in excess of selected limitations, it follows that inflation will shift larger percentages of the total cost over to the higher end of the distribution.

The shift, wherein greater percentages of total cost have been transferred to the higher end of the scale, has been feared and known for some time. Newer tables which reflect the shift were needed. Documentation of the changes in distribution of cost was accomplished by digging into the customary reports used by the National Council on Compensation Insurance for ratemaking. The information was not in readily usable form³ and revisions of developed individual reports were required for purposes of this study. The need for mature reports is apparent in light of the substantial development of average cost per claim at successive reports. For example, in the state of Connecticut, permanent total average cost per claim for policy year 1969-70⁴ was \$87,348 at first report, \$95.047 at second report and \$121,432 at third report.

The program for updating distributions by size of claim called for the use of fourth reports for each of the serious loss categories of fatal, permanent total and major permanent partial injuries. Serious loss categories were used because these are the ones which are likely to result in individual claim costs in excess of the accident limit selected. Distributions as a ratio

² NCCI "Call for Wage Data for Injured Employees."

³ Because normal ratemaking requires aggregate data for developments, such aggregates were captured without taking the time to guarantee that individual claim reports were included in the data base at developed amounts.

⁴ Policies issued between August 1, 1969 through July 31, 1970.

of average cost were obtained for the medium or high benefit jurisdictions of Arkansas, Connecticut, District of Columbia, Maryland and Nebraska. By observing each jurisdiction in terms of that portion of cost which represented excess cost per case according to the intervals as a ratio to average, the problem of recognizing different benefit levels and different average costs per case in each of the jurisdictions was minimized. It then became possible to combine the excess cost per case for particular ratios to average. This combination was made based upon the total number of cases for the particular injury type in each of the jurisdictions considered (see Exhibits I-1 and II-1).

EXHIBIT I-1

FATAL—LIMITED

Ratio	Excess Ratios						
to Avg.	Maryland	Nebraska	Arkansas	Average*			
.00	1.000	1.000	1.000	1.000			
.25	.775	.776	.778	.776			
.50	.591	.597	.607	.597			
.75	.430	.439	.454	.440			
1.00	.289	.300	.339	.308			
1.25	.171	.181	.242	.196			
1.50	.143	.131	.164	.147			
1.75	.123	.124	.102	.116			
2.00	.105	.117	.052	.090			
2.25	.091	.110	.026	.073			
2.50	.078	.103	.017	.063			
2.75	.067	.096	.009	.054			
3.00	.058	.089	.002	.046			
3.25	.047	.082	.000	.039			
3.50	.041	.075	.000	.034			
Total Number							
of Claims	85	36	59	XXX			

*Average excess ratios weighted by state's total number of claims

The combined results were plotted on semi-logarithmic graph paper and compared with the tables known as "Uhthoff's Tables" (see Exhibits I-3 and II-3). It immediately became apparent that the latter have become seriously out of date at the high end of the scale. The graphic representation of data for permanent total cases showed a remarkable coincidence with the data for fatal limited cases. For this reason, it was decided to use the fatal limited tables for permanent total as well.

Unlimited fatal cases indicated much lower charges than did the table for limited fatal cases. Due to the paucity of unlimited fatal claims, and in the light of actual results, it was decided to apply the new table for limited fatal cases to the unlimited as well.

Since the values obtained by the averaging method described above were only calculated at each 25% of the average cost per claim, a method was needed to produce a complete table. The method of least squares was used in fitting various equations to the combined results (see Exhibits 1-2 and II-2). Each fitted equation was required to produce a value of 1.000 for a zero ratio to average cost. For those selected equations which did not lend themselves to a true least squares analysis, both an approximate least squares method (utilizing logarithms) and a method of collocation were tried. Collocation involves the algebraic solution of the general equation such that the collocation equation thus obtained passes through selected values of the actual data⁵. This is an iterative technique; it was continued until the observed deviations were evenly spread over the entire distribution. The equations, which exhibited the minimum sum of squared differences, were then used to generate complete tables of excess ratios. Exhibits I-4 and II-4 contain the new values developed by the collocation method.

A committee of actuaries reviewed and approved the use of the newly developed tables. The tables will be utilized in conjunction with the current excess loss premium factor calculations⁶ until such time as fourth reports of losses by type of injury become available. (See Appendix A for an example of these calculations). At this point, the calculation shall be modified to incorporate the use of estimated actual development by type of injury in lieu of the 1.6 factor which Uhthoff's procedure uses⁷. Detailed comparisons of results under Uhthoff's methods and the new method are described in Appendix A.

⁵ For a general description of collocation, see Stephen G. Kellison, *Fundamentals of Numerical Analysis*, Richard D. Irwin, Inc., (1975), p. 20ff.

⁶ These are based upon an average of first and second reports, updated by law amendments.

⁷ The factor is low in comparison with excess reinsurers' development factors based on actual experience:

EXHIBIT I-2 FATAL—LIMITED

EXCESS RATIOS

		CURVES FIT BY LEAST SQUARES CRITERION					
(x) Ratio to Avg.	(y) Actual*	$y' = (.342)^{x}$	$y' = .151x^2$	$\begin{array}{c} .127x^2 - \\ 1.417x \\ \underline{y' = e} \end{array}$	$y' = \frac{1}{1 + .185x + 2.310x^2}$	$y' = \frac{1}{\frac{1 - x + 3.883x^2406x^3}{2}}$	
.00	1.000	1.000	1.000	1.000	1.000	1.000	
.25	.776	.765	.815	.707	.840	1.014	
.50	.597	.585	.648	.508	.599	.704	
.75	.440	.447	.501	.371	.410	.442	
1.00	.308	.342	.372	.275	.286	.288	
1.25	.196	.262	.262	.207	.207	.199	
1.50	.147	.200	.171	.159	.154	.146	
1.75	.116	.153	.099	.124	.119	.112	
2.00	.090	.117	.046	.098	.094	.089	
2.25	.073	.089	.012	.078	.076	.073	
2.50	.063	.068	004	.064	.063	.061	
2.75	.054	.052	.000	.053	.053	.052	
3.00	.046	.040	.022	.045	.045	.045	
3.25	.039	.031	.063	.038	.038	.040	
3.50	.034	.023	.123	.033	.033	.036	
$\frac{\sum \mathbf{y} - \mathbf{y'} }{n}$	xx	.020	.046	.021	.010	.026	
$\frac{\sum (y-y')^2}{n}$	xx	.00749	.002620	.001264	.000379	.004569	

EXHIBIT I-3

FATAL - LIMITED



EXHIBIT I-4

FATAL CASES (LIMITED AMOUNT)*

Ratio	Excess	Ratio	Excess	Ra	tio Excess
10 Aver	Per Case	10 Aver	Per Case		o Per er Case
0%	1.000	33	762		<u>6 470</u>
1	008	34	752	6	7 463
2	005	35	742	6	7 .405 8 456
3	002	36	732	6	0 110
4	989	37	722	7	0 442
5	985	38	712	7	1 436
6	081	30	702	, 7	2 429
7	976	40	693	7	3 423
8	971	40	683	7	4 416
9	966	42	673	7	5 410
10	960	43	.664	7	6 404
11	954	44	.654	, 7	7 398
12	947	45	.645	7	8 .392
13	.941	46	.635	7	9.386
14	.934	47	.626	8	0.381
15	.926	48	.617	8	1 .375
16	.918	49	.608	8	2 .370
17	.911	50	.599	8	3.364
18	.902	51	.590	8	4 .359
19	.894	52	.581	8	5 .354
20	.885	53	.572	8	6.349
21	.877	54	.564	8	7.344
22	.868	55	.555	8	8.339
23	.859	56	.547	8	9.334
24	.849	57	.539	9	0.329
25	.840	58	.531	9	1.325
26	.830	59	.523	9	2.320
27	.821	60	.515	9	3.315
28	.811	61	.507	9	4 .311
29	.801	62	.499	9	5.307
30	.792	63	.492	9	6 .302
31	.782	64	.484	9	7.298
32	.772	65	.477	9	8.294
*Excess p	$er case = \frac{1}{1+1}$.185 (Ratio to	1 Average) +	- 2.310 (Ratio to A	verage) ²

Ratio To	Excess Per		Ratio To	Excess Per	 Ratio To	Excess Per
Aver.	Case		Aver.	Case	Aver.	Case
99	.290	-	134	.185	169	.126
100	.286		135	.183	170	.125
101	.282		136	.181	171	.124
102	.278		137	.179	172	.123
103	.275		138	.177	173	.121
104	.271		139	.175	174	.120
105	.267		140	.173	175	.119
106	.264		141	.171	176	.118
107	.260		142	.169	177	.117
108	.257		143	.167	178	.116
109	.253		144	.165	179	.115
110	.250		145	.163	180	.113
111	.247		146	.161	181	.112
112	.244		147	.160	182	.111
113	.240		148	.158	183	.110
114	.237		149	.156	184	.109
115	.234		150	.154	185	.108
116	.231		151	.153	186	.107
117	.228		152	.151	187	.106
118	.225		153	.149	188	.105
119	.223		154	.148	189	.104
120	.220		155	.146	190	.103
121	.217		156	.145	191	.102
122	.214		157	.143	192	.101
123	.212		158	.142	193	.100
124	.209		159	.140	194	.099
125	.207		160	.139	195	.099
126	.204		161	.137	196	.098
127	.202		162	.136	197	.097
128	.199		163	.134	198	.096
129	.197		164	.133	199	.095
130	.194		165	.132	200	.094
131	.192		166	.130	201	.093
132	.190		167	.129	202	.093
133	.188		168	.128	203	.092

RETROSPECTIVE RATING

Ratio	Excess	Ratio	Excess	R	atio	Excess
То	Pcr	То	Per		То	Per
Aver.	Case	Aver.	Case	A	ver.	Case
204	.091	239	.068	2	274	.053
205	.090	240	.068	2	275	.053
206	.089	241	.067	2	.76	.052
207	.089	242	.067	2	277	.052
208	.088	243	.066	2	278	.052
209	.087	244	.066	2	279	.051
210	.086	245	.065	2	280	.051
211	.086	246	.065	2	281	.051
212	.085	247	.064	2	282	.050
213	.084	248	.064	2	283	.050
214	.084	249	.063	2	284	.050
215	.083	250	.063	2	285	.049
216	.082	251	.062	2	286	.049
217	.081	252	.062	2	287	.049
218	.081	253	.062	2	288	.048
219	.080	254	.061	2	289	.048
220	.079	255	.061	2	290	.048
221	.079	256	.060	2	291	.047
222	.078	257	.060	2	292	.047
223	.078	258	.059	2	293	.047
224	.077	259	.059	2	294	.046
225	.076	260	.058	2	295	.046
226	.076	261	.058	2	296	.046
227	.075	262	.058		297	.046
228	.074	263	.057	2	298	.045
229	.074	264	.057		299	.045
230	.073	265	.056		300	.045
231	.073	266	.056		301	.044
232	.072	267	.056	3	302	.044
233	.072	268	.055		303	.044
234	.071	269	.055		304	.044
235	.070	270	.055		305	.043
236	.070	271	.054		306	.043
237	.069	272	.054		307	.043
238	.069	273	.053	3	308	.043

Ratio To Aver.	Excess Per Case		Ratio To Aver.	Excess Per Case	Ratio To Aver.	Excess Per Case
309	.042	_	323	.039	337	.036
310	.042		324	.039	338	.036
311	.042		325	.038	339	.035
312	.042		326	.038	340	.035
313	.041		327	.038	341	.035
314	.041		328	.038	342	.035
315	.041		329	.038	343	.035
316	.041		330	.037	344	.035
317	.040		331	.037	345	.034
318	.040		332	.037	346	.034
319	.040		333	.037	347	.034
320	.040		334	.037	348	.034
321	.039		335	.036	349	.034
322	.039		336	.036	350 &	.033
					Over	

EXHIBIT I-4 (CONT'D)

A study of experience by hazard group is also under review. The indicated hazard group differentials to average are based upon a review of the experience indications of high, medium and low benefit states as well as the experience of the totals of the three groups of states. The experience is shown in Appendix B (Exhibits B-1 through B-4).

These procedures and tables reflect the situation known today. It is hoped that they may survive periodic review and serve the insurance industry's requirements as long as "Uhthoff's Tables" have.

Accident Years	Range of Factors
1968-1974 (1st Report to Ultimate)	3.10-3.51
1968-1973 (2nd Report to Ultimate)	1.68-2.13
1968-1972 (3rd Report to Ultimate)	1.41-1.67
1968-1971 (4th Report to Ultimate)	1.37-1.46

Reported in March, 1976 issue of Best's Property/Casualty Review, pp. 14-18.

EXHIBIT II-1

MAJOR PERMANENT PARTIAL

Ratio			Excess	Ratios		
to Avg.	Ark.	Conn.	D.C.	Md.	Neb.	Avg.*
.00	1.000	1.000	1.000	1.000	1.000	1.000
.25	.750	.751	.751	.751	.751	.751
.50	.509	.528	.518	.526	.504	.519
.75	.343	.281	.361	.383	.339	.344
1.00	.248	.194	.253	.285	.242	.249
1.25	.178	.140	.174	.216	.181	.182
1.50	.129	.105	.118	.165	.141	.136
1.75	.096	.082	.081	.127	.113	.103
2.00	.073	.065	.059	.098	.094	.080
2.25	.058	.055	.050	.077	.082	.065
2.50	.046	.045	.042	.063	.075	.053
2.75	.040	.037	.036	.052	.067	.045
3.00	.030	.033	.031	.044	.058	.038
3.25	.025	.029	.028	.038	.052	.033
3.50	.021	.024	.022	.029	.051	.027
3.75	.020	.021	.021	.025	.050	.024
4.00	.017	.018	.018	.021	.049	.021
4.25	.015	.015	.016	.018	.048	.019
4.50	.013	.015	.013	.016	.047	.017
4.75	.012	.012	.010	.013	.046	.015
5.00	.010	.011	.008	.012	.045	.013
5.25	.009	.010	.006	.011	.044	.012
5.50	.008	.009	.005	.010	.043	.011
5.75	.007	.007	.003	.010	.042	.010
6.00	.006	.006	.001	.009	.041	.009
Total Number of Claims	794	666	290	1,022	233	xxx

*Average excess ratios weighted by state's total number of claims

EXHIBIT II-2

MAJOR PERMANENT PARTIAL

EXCESS RATIOS

CURVES FIT BY LEAST SQUARES CRITERION

(x) Ratio	(y)		$v' = .072x^2 =$	$.113x^2 - 1.435x$	$y' = \frac{1}{1 + .555x +}$	$y' = \frac{1}{1 + .805x +}$
to Avg.	Actual*	$y' = (.267)^{x}$	$\frac{.565x + 1}{.565x + 1}$	y' = e	2.655x ²	$2.044x^2 + .167x^3$
.00	1.000	1.000	1.000	1.000	1.000	1.000
.25	.751	.719	.863	.703	.766	.751
.50	.519	.517	.736	.502	.515	.517
.75	.344	.371	.617	.363	.344	.354
1.00	.249	.267	.507	.267	.238	.249
1.25	.182	.192	.406	.198	.171	.181
1.50	.136	.138	.315	.150	.128	.136
1.75	.103	.099	.232	.115	.099	.105
2.00	.080	.071	.158	.089	.079	.082
2.25	.065	.051	.093	.070	.064	.066
2.50	.053	.037	.038	.056	.053	.054
2.75	.045	.026	009	.045	.044	.045
3.00	.038	.019		.037	.038	.038
3.25	.033	.014	076	.031	.032	.032
3.50	.027	.010	096	.026	.028	.028
3.75	.024	.007	106	.023	.025	.024
4.00	.021	.005	108	.020	.022	.021

*See Exhibit II-1 for derivation

EXHIBIT II-2 (CONT'D)

MAJOR PERMANENT PARTIAL

EXCESS RATIOS

CURVES FIT BY LEAST SQUARES CRITERION

(x)	(v)			$.113x^{2} -$	$v' = \frac{1}{1}$	$l' = \frac{1}{1}$
Ratio	Actual*	$v' - (267)^{*}$	$y' = .072x^2 - 565x + 1$	1.435x	$1 + .555x + \frac{1}{2} + \frac{555x^2}{655x^2}$	$1 + .805x + 2.044x^{2} + 167x^{3}$
to Avg.	Actual	<u>y - (.207)</u>		<u>y = c</u>	2.000X	2.044 1.107
4.25	.019	.004	101	.017	.019	.018
4.50	.017	.003	085	.015	.017	.016
4.75	.015	.002	059	.014	.016	.015
5.00	.013	.001	025	.013	.014	.013
5.25	.012	.001	.018	.012	.013	.012
5.50	.011	.001	.071	.011	.012	.011
5.75	.010	.001	.132	.011	.011	.010
6.00	.009	.000	.202	.011	.010	.009
$\frac{\Sigma \mid \mathbf{y} - \mathbf{y}' \mid}{n}$	xx	.013	.114	.007	.003	.001
$\frac{\sum (y - y')^2}{n}$	xx	.000231	.018594	.000160	.000023	.000005

*See Exhibit II-1 for derivation

RETROSPECTIVE RATING

EXHIBIT 11-3





EXHIBIT II-4

MAJOR PERMANENT PARTIAL CASES*

Ratio	Excess	Ratio	Excess	Ratio	Excess
To	Per	To	Per	To	Per
Aver.	Case	Aver.	Case	Aver.	Case
0%	6 1.000	33	.669	66	.405
1	.992	34	.659	67	.399
2	.983	35	.650	68	.393
3	.975	36	.640	69	.387
4	.966	37	.630	70	.381
5	.957	38	.621	71	.376
6	.947	39	.612	72	.370
7	.938	40	.603	73	.365
8	.928	41	.593	74	.359
9	.918	42	.584	75	.354
10	.908	43	.576	76	.349
11	.898	44	.567	77	.344
12	.888	45	.558	78	.339
13	.878	46	.550	79	.334
14	.867	47	.541	80	.329
15	.857	48	.533	81	.324
16	.846	49	.525	82	.320
17	.836	50	.517	83	.315
18	.825	51	.509	84	.311
19	.814	52	.501	85	.306
20	.804	53	.494	86	.302
21	.793	54	.486	87	.298
22	.783	55	.479	88	.294
23	.772	56	.471	89	.290
24	.761	57	.464	90	.286
25	.751	58	.457	91	.282
26	.741	59	.450	92	.278
27	.730	60	.443	93	.274
28	.720	61	.437	94	.270
29	.710	62	.430	95	.266
30	.699	63	.424	96	.263
31	.689	64	.417	97	.259
32	.679	65	.411	98	.256
*Excess	per case =	Å	I		
		4	r		

1 + .805 (Ratio to Avg.) + 2.044 (Ratio to Avg.) 2 + .167 (Ratio to Avg.) 3

RETROSPECTIVE RATING

EXHIBIT II-4 (CONT'D)

Ratio To	Excess Per	Ratio To	Excess Per	Ratio To	D Excess Per
Aver.	Case	Aver	. Case	Aver	. Case
99	.252	134	.163	169	.111
100	.249	135	.161	170	.110
101	.246	136	.159	171	.109
102	.242	137	.157	172	.108
103	.239	138	.155	173	.107
104	.236	139	.153	174	.106
105	.233	140	.152	175	.105
106	.230	141	.150	176	.104
107	.227	142	.148	177	.103
108	.224	143	.147	178	.102
109	.221	144	.145	179	.101
110	.218	145	.143	180	.100
111	.216	146	.142	181	.099
112	.213	147	.140	182	.098
113	.210	148	.139	183	.097
114	.207	149	.137	184	.096
115	.205	150	.136	185	.095
116	.202	151	.134	186	.094
117	.200	152	.133	187	.093
118	.197	153	.131	188	.092
119	.195	154	.130	189	.091
120	.192	155	.129	190	.090
121	.190	156	.127	191	.090
122	.188	157	.126	192	.089
123	.185	158	.124	193	.088
124	.183	159	.123	194	.087
125	.181	160	.122	195	.086
126	.179	161	.121	196	.086
127	.177	162	.119	197	.085
128	.175	163	.118	198	.084
129	.172	164	.117	199	.083
130	.170	165	.116	200	.082
131	.168	166	.115	201	.082
132	.166	167	.113	202	.081
133	.164	168	.112	203	.080

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Ratio	Excess	Ratio	Excess	Ratio	Excess
	Per	LO Aver	Per Case	IO Aver	Case
		220	. Case	274	045
204	.080	239	.039	274	.045
205	.079	240	.039	275	.045
206	.078	241	.038	270	.045
207	.077	242	.058	277	.045
208	.077	243	.057	270	.044
209	.076	244	.057	279	.044
210	.075	245	.057	280	.044
211	.075	240	.030	201	.043
212	.074	247	.030	202	.043
213	.074	248	.055	283	.043
214	.073	249	.055	204	.042
215	.072	250	.054	283	.042
216	.072	251	.054	280	.042
217	.071	252	.054	287	.042
218	.070	253	.053	200	.041
219	.070	254	.053	289	.041
220	.069	255	.052	290	.041
221	.069	250	.052	291	.040
222	.068	257	.054	292	.040
223	.068	258	.051	293	.040
224	.007	259	.051	294	.040
225	.000	260	.050	293	.039
226	.066	261	.050	290	.039
227	.005	202	.050	297	.039
228	.005	203	.049	298	.039
229	.064	204	.049	299	.038
230	.004	203	.049	300	.030
231	.063	200	.048	301	.038
232	.003	267	.048	302	.037
233	.062	208	.047	303	.037
234	.062	269	.047	304	.037
233	.001	270	.047	305	.037
230	.001	271	.040	300	.03/
231	.060	272	.046	307	,030
238	.060	273	.046	308	.036

RETROSPECTIVE RATING

Ratio To	Excess Per	Rati To	o Excess	R	latio	Excess
Aver.	Case	Ave	r. Case	А	ver.	Case
309	.036		.029	3	79	.024
310	.036	345	.029	3	80	.023
311	.035	346	.028	3	81	.023
312	.035	347	.028	3	82	.023
313	.035	348	.028	3	83	.023
314	.035	349	.028	3	84	.023
315	.034	350	.028	3	85	.023
316	.034	351	.028	3	86	.023
317	.034	352	.027	3	87	.023
318	.034	353	.027	3	88	.022
319	.034	354	.027	3	89	.022
320	.033	355	.027	3	90	.022
321	.033	356	.027	3	91	.022
322	.033	357	.027	3	92	.022
323	.033	358	.026	3	93	.022
324	.033	359	.026	3	94	.022
325	.032	360	.026	3	95	.022
326	.032	361	.026	3	96	.021
327	.032	362	.026	3	97	.021
328	.032	363	.026	3	98	.021
329	.032	364	.026	3	99	.021
330	.031	365	.025	4	00	.021
331	.031	366	.025	4	01	.021
332	.031	367	.025	4	02	.021
333	.031	368	.025	4	103	.021
334	.031	369	.025	4	104	.021
335	.030	370	.025	4	105	.020
336	.030	371	.025	4	106	.020
337	.030	372	.024	4	107	.020
338	.030	373	.024	4	108	.020
339	.030	374	.024	4	09	.020
340	.029	375	.024	4	10	.020
341	.029	376	.024	4	11	.020
342	.029	377	.024	4	12	.020
343	.029	378	.024	4	13	.020

Ratio	Excess	Rati	o Excess	Ratio	Excess
10 Aver	Per Case	I O Avei	· Case		Case
<u></u>	020		016	404	014
414	.020	449	.010	484	.014
415	.019	430	.010	485	.014
410	.019	431	.010	480	.014
417	.019	432	.010	40/	.014
410	.019	433	.010	400	.014
419	.019	434	.010	489	.014
420	.019	433	.010	490	.014
421	.019	450	.010	491	.014
422	.019	437	.010	492	.013
425	.019	438	.010	493	.013
424	.019	439	.010	494	.013
425	.010	460	.010	495	.013
420	.018	461	.016	496	.013
427	.018	462	.015	497	.013
428	,018	463	.015	498	.013
429	.018	464	.015	499	.013
430	.018	465	.015	500	.013
431	.018	466	.015	501	.013
432	.018	467	.015	502	.013
433	.018	468	.015	503	.013
434	.018	469	.015	504	.013
435	.018	470	.015	505	.013
436	.017	471	.015	506	.013
437	.017	472	.015	507	.013
438	.017	473	.015	508	.013
439	.017	474	.015	509	.012
440	.017	475	.015	510	.012
441	.017	476	.014	511	.012
442	.017	477	.014	512	.012
443	.017	478	.014	513	.012
444	.017	479	.014	514	.012
445	.017	480	.014	515	.012
446	.017	481	.014	516	.012
447	.017	482	.014	517	.012
448	.016	483	.014	518	.012

	Ratio To Aver.	Excess Per Case		Ratio To Aver.	Excess Per Case	Ratio To Aver.	Excess Per Case
-	519	.012	-	547	.011	575	010
	520	.012		548	.011	576	.009
	521	.012		549	.011	577	.009
	522	.012		550	.011	578	.009
	523	.012		551	.010	579	.009
	524	.012		552	.010	580	.009
	525	.012		553	.010	581	.009
	526	.012		554	.010	582	.009
	527	.012		555	.010	583	.009
	528	.012		556	.010	584	.009
	529	.011		557	.010	585	.009
	530	.011		558	.010	586	.009
	531	.011		559	.010	587	.009
	532	.011		560	.010	588	.009
	533	.011		561	.010	589	.009
	534	.011		562	.010	590	.009
	535	.011		563	.010	591	.009
	536	.011		564	.010	592	.009
	537	.011		565	.010	593	.009
	538	.011		566	.010	594	.009
	539	.011		567	.010	595	.009
	540	.011		568	.010	596	.009
	541	.011		569	.010	597	.009
	542	.011		570	.010	598	.009
	543	.011		571	.010	599	.009
	544	.011		572	.010	600 &	.009
	545	.011		573	.010	Over	
	546	.011		574	.010		

RETROSPECTIVE RATING

APPENDIX A

Three exhibits which follow set forth the calculation of Excess Loss Premium Factors. The first (Appendix A-1) describes the present procedure based on Uhthoff's tables, the second (Appendix A-2) describes the present procedure based on revised tables and the third (Appendix A-3) describes the present procedure (modified) based on revised tables. For convenience, they will be referred to as A-1, A-2 and A-3, respectively

All three exhibits rest upon two policy years of experience; one at a first report and one at a second report. The average claim cost is determined by adjusting the reported incurred losses to reflect law amendment factors and then dividing the result by the number of cases. This is performed by type of injury and is shown in Column 12 of A-1 and A-2. With respect to A-3, not only are the incurred losses adjusted to reflect law amendment factors, they are also modified to reflect loss development by type of injury. The resulting average claim cost is shown in Column 16 of A-3.

The average claim costs are shown on lines 13 (death), 16 (permanent total), and 19 (major) for Exhibits A-1 and A-2. The corresponding lines for Exhibit A-3 are lines 17, 20 and 23. In all three exhibits, the bottom half shows the selected accident limit ranging from \$10,000 to \$250,000 arranged by columns lettered from (A) through (L). These amounts are expressed as ratios to the average cost for each serious type of claim. These ratios are then used to enter the appropriate table, namely, Uhthoff's or Revised in order to determine the excess ratio contribution by each type of claim. These excess ratios are then weighted in proportion to the contribution to total cost made by each type of claim. The proportion, which is shown on line 22, is derived from the data in Column 11 for A-1 and A-2. These proportions shown on line 26 of A-3 are different from those of A-1 and A-2 because loss development has been included; they are derived from Column 15. The average excess ratio is multiplied by the permissible loss ratio increased by 10% to reflect the conversion of data complied on a per claim basis to a "per accident" basis. It is then increased by flat loadings ranging from .005 to .001 as the accident limit increases. Finally, the indicated Excess Loss Premium Factors are modified by a factor of 1.6 to reflect loss development with respect to the procedures in A-1 and A-2. With respect to A-3, this factor is not necessary since development was included at the beginning; consequently the indicated Excess Loss Premium Factors are the proposed Excess Loss Premium Factors.

The present procedures based on the revised tables tend to produce lower charges for the lower accidents limits and higher charges for the higher accident limits than those based on Uhthoff's tables. This is also true for the present procedure (modified) based on the revised tables wherein loss development by type of injury is included in the calculation of the average claim cost.

It is believed that the revised tables and the modified procedures will effectively generate more appropriate charges since quite frequently the proposed Excess Loss Premium Factors at the lower limits may need to be arbitrarily reduced because they exceed the permissible loss ratio.

APPENDIX A-1

PRESENT PROCEDURE - BASED ON UHTHOFF'S TABLES

		Policy Pe	riod (70-	71) 2nd		Policy	Period (71-72) 1st				
(1) Type Of	(2) No. Of	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)		(12) Average
Injury	Cases	Indemnity	A.F.	Medical	A.F.	Indemnity	A.F.	Medica	1 A.F.	Tota	d ($(11) \div (2)$
Death	86	2.451,463	1.150	87,228	1.000	2,280,619	1.100	57,10	9 1.000	5,472.	200	63,630
P.T.	19	344,657	1.033	384.440	1.000	1,284,254	1.091	614.26	1 1.000	2.755.	853	145,045
Мајог	1,271	6,950,644	1.145	2,585,223	1.000	8,763,791	1.086	3,948.94	7 1.000	24.010.	134	18,891
Minor	xx	6,125,412	1.143	2,281,834	1.000	7,238,922	1.089	2,740,60	5 1.000	19.906,	971	xx
T.T.	xx	5,617.151	1.156	3,495,883	1.000	7.883.248	1.097	5,247,34	9 1.000	23,884,	582	xx
Other Med.	xx	xx	xx	2,651,245	1.000	xx	xx	3,584,51	7 1.000	6,235,	762	xx
TOTAL	xx	XX	XX	xx	xx	xx	xx	xx	xx	82,265,	502	ХХ
$\mathbf{A}.\mathbf{F}.=\mathbf{A}$	mendmer	it Factor to c	urrent la	w level.			<u> </u>					
		<u>(A</u>		1,000 \$)								
			10	15 20	25	30	40	50 75	100	150	200	250
13. Average (Incl. M	e Death C ed.)	ost 6	(A) 3,630	(B) (C)	(D)	(E)	(F)	(G) (H) (I)	(J)	(K)	(L)
14. Ratio to (A), (B),	Average (C), etc.	\div (13) .1	16	.24 .31	.39	.47	.63	.79 1.18	3 1.57	2.36	3.14	4 3.93

.453

.347

.156

.069

.027

.021

.021

15. Excess Ratio for Death

(from Tables) 16. Average P.T. Cost (Incl. Med.) .841

145,045

.761

.694

.630

.569

RETROSPECTIVE RATING

17.	Ratio to Average	07	10	14	17	21	26	74		<u> </u>	1.02	1 20	1 72
	$(A), (B), (C), etc. \div (16)$.07	.10	.14	.17	.21	.20	.54	.32	.09	1.05	1.30	1.72
18.	Excess Ratio for P.T. (from Tables)	.930	.900	.860	.831	.791	.724	.668	.510	.378	.194	.103	.059
19.	Average Major Cost (Incl. Med.)	18,891											
20.	Ratio to Average (A), (B), (C), etc. \div (19)	.53	.79	1.06	1.32	1.59	2.12	2.65	3.97	5.29	7.94	10.59	13.23
21.	Excess Ratio for Major (from Tables)	.496	.324	.200	.127	.081	.031	.007	.001	.001	.001	.001	.001
22.	Ratios to Total Cost A. Death b. P.T. c. Major	.067 .033 .292						A9					
23.	Average Excess Ratio	.232	.175	.133	.107	.088	.063	.047	.028	.017	.009	.005	.004
24.	Permissible Loss Ratio	.610			<u> </u>								
25.	(24) × 1.10	.671											
26.	(23) × (25)	.156	.117	.089	.072	.059	.042	.032	.019	.011	.006	.003	.003
27.	Flat Loadings	.005	.004	.003	.002	.002	.002	.001	.001	.001	.001	.001	.001
28.	Indicated ELPF'S (26) + (27)	.161	.121	.092	.074	.061	.044	.033	.020	.012	.007	.004	.004
29.	Proposed ELPF'S $(28) \times 1.6$.258	.194	.147	.118	.098	.070	.053	.032	.019	.011	.006	.006

APPENDIX A-1 (CONT'D)

 $*23 = [(15) \times (22a)] + [(18) \times (22b)] + [(21) \times (22c)]$

APPENDIX A-2

PRESENT PROCEDURE - BASED ON REVISED TABLES

		Policy Pe	eriod (70	-71) 2n	d		Policy	Period	(71-72) 1st				
(1) Type of	(2)	(3)	(4)	(5	5)	(6)	(7)	(8))	(9)	(10)	(11)	(12) Average
Injury	Cases	Indemnity	A.F.	Mec	lical	A.F.	Indemnity	A.F	:. М	ledical	A.F.	Tota	al ($(1) \div (2)$
Death	86	2,451,463	1.150	81	7,228	1.000	2,280,619	1.10	00	57,109	1.000	5,472	,200	63,630
P.T.	19	344,657	1.033	384	4,440	1.000	1,284,254	1.09	1 6	14.261	1.000	2,755	,853	145,045
Major	1.271	6,950,644	1.145	2,58	5,223	1.000	8,763,791	1.08	6 3,9	48,947	1,000	24,010	.134	18,891
Minor	xx	6,125,412	1.143	2,28	1,834	1.000	7,238,922	1.08	9 2.7	40,605	1.000	19,906	,971	xx
Т.Т.	xx	5,617,151	1.156	3,495	5,883	1.000	7,883,248	1.09	7 5,2	247,349	1.000	23,884	,582	xx
Other Med.	xx	XX	XX	2,65	.245	1.000	XX	XX	3.5	84.517	1.000	6,235	,762	XX
TOTAL	XX	XX	XX	х	x	ХХ	XX	XX		ХХ	λX	82,265	,502	XX
A.F. = A	mendmer	nt Factor to	current l	aw leve	I.									
		(An	nounts ir	a 1,000's	s)									
			10	15	20	25	30	40	50	75	100	150	200	250
13. Average (Incl. N	e Death C Aed.)	Cost	(A) 53,630	(B)	(C)	(D)	(E)	(F)	(G)	(H)	(1)	(J)	(K)	(L)
14. Ratio to (A), (B)	o Average , (C), etc.	$\frac{1}{2}$ (13)	16	.24	.31	.39	.47	.63	.79	1.18	1.57	2.36	3.14	3.93
15. Excess (from 7	Ratio for Fables)	Death .	918	.849	.782	.702	.626	.492	.386	.225	.143	.070	.04	1 .033

16. Average P.T. Cost (Incl. Med.) 145,045

						(00.	,						
17.	Ratio to Average $(A), (B), (C), etc. \div (16)$.07	.10	.14	.17	.21	.28	.34	.52	.69	1.03	1.38	1.72
18.	Excess Ratio For P.T. (from Tables)	.976	.960	.934	.911	.877	.811	.752	.581	.449	.275	.177	.123
19.	Average Major Cost (Incl. Med.)	18,891											
20.	Ratio to Average (A), (B), (C), etc. \div (19)	.53	.79	1.06	1.32	1.59	2.12	2.65	3.97	5.29	7.94	10.59	13.23
21.	Excess Ratio for Major (from Tables)	.494	.334	.230	.166	.123	.074	.049	.021	.011	.009	.009	.009
22.	Ratios to Total Cost c. Major	.067 .033 .292											
23.	Average Excess Ratio	.238	.186	.150	.126	.107	.081	.065	.040	.028	.016	.011	.009
24.	Permissible Loss Ratio	.610											
25.	(24) × 1.10	.671	_										
26.	$(23) \times (25)$.160	.125	.101	.085	.072	.054	.044	.027	.019	.011	.007	.006
27.	Flat Loadings	.005	.004	.003	.002	.002	.002	.001	.001	.001	.001	.001	.001
28.	Indicated ELPF'S (26) + (27)	.165	.129	.104	.087	.074	.056	.045	.028	.020	.012	.008	.007
29.	Proposed ELPF'S $(28) \times 1.6$.264	.206	.166	.139	.118	.090	.072	.045	.032	.019	.013	.011

APPENDIX A-2 (CONT'D)

 $*23 = [(15) \times (22a)] + [(18) \times (22b)] + [(21) \times (22c)]$

RETROSPECTIVE RATING

APPENDIX A-3

PRESENT PROCEDURE (MODIFIED) - BASED ON REVISED TABLES

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)
Type Of Injury	No. Of Cases†	Indemnity	A.F.	Dev.	Medical	A.F.	Dev.	Indemnity	A.F .	Dev.	Medical	A.F.	Dev,	Total	(15) \div (2)
Death	110	2,451.463	1.150	1,298	87,228	1.000	1.121	2,280,619	1,100	1.482	57,109	1.000	1.207	7,543.877	68,581
P.T.	28	344.657	1.033	2.329	384.440	1.000	1.121	1,284.254	1.091	2.394	614,261	1.000	1.207	5,355,850	191,280
Major	2,082	6,950.644	1.145	1.385	2,585,223	1.000	1.121	8,763.791	1.086	1.916	3,948,947	1.000	1.207	36,922,405	17,734
Minor	xx	6,125,412	1.143	.971	2.281.834	1.000	1.121	7,238.922	1.089	1.012	2,740,605	1.000	1.207	20,641,937	xx
T .T.	xx	5,617,151	1.156	1.095	3,495,883	1.000	1.121	7.883.248	1.097	1.136	5,247,349	1.000	1.207	27,186.778	xx
Other Med.	xx	xx	XX	xx	2,651,245	1.000	1.121	xx	xx	xx	3,584,517	1.000	1.207	7,298,558	xx
TOTAL	xx	xx	xх	xx	xx	xx	XX	xx	xx	xx	xx	xx	xx	104,949,405	xx
† No. of cas	es include	e developme	nt facto	ors by ty	pe of injury	·	$\mathbf{A}.\mathbf{F}.=\mathbf{A}\mathbf{I}$	mendment F	actor to	current	law level.				
			Amou	ints in 1	,000's)										
				10	15	20	25	30	40	50	75	100	150	200	250
17. Average (Incl. M	e Death C led.)	lost	68	(A) ,581	(B)	(C)	(D)	(E)	(F)	(G)	(H)	(I)	(1)	(K)	(L)
18. Ratio to (A), (B	Average	tc. \div (17)		.15	.22	.29	.36	.44	.58	.73	1.09	1.46	2.19	2.92	3.65
19. Excess I (from T	Ratio for ables)	Death		.926	.868	.801	.732	.654	531	.423	.253	.161	.080	.047	.033
20. Average	P.T. Co	st	191.	280											

(Incl. Med.) 21. Ratio to Average

 $(A), (B), (C), etc. \div (20)$

.05

.08

.10

.13

.16

.21

.26

.39

.52

.78

1.05

1.31

22.	Excess Ratio For P.T. (from Tables)	.985	.971	.960	.941	.918	.877	.830	.702	.581	.392	.267	.192
23.	Average Major Cost (Incl. Med.)	17,734											
24.	Ratio to Average (A), (B), (C), etc. ÷ (23)	.56	.85	1.13	1.41	1.69	2.26	2.82	4.23	5.64	8.46	11.28	14.10
25.	Excess Ratio for Major (from Tables)	.471	.306	.210	.150	.111	.066	.043	.019	.010	.009	.009	.009
26.	a. Death Ratios to Total Cost b. P.T. c. Major	.072 .051 .352											
27.	Average Excess Ratio*	.283	.220	.181	.153	.133	.106	.088	.061	.045	.029	.020	.015
28.	Permissible Loss Ratio	.610											
29	(28) × 1.10	.671											
30	. (27) × (29)	.190	.148	.121	.103	.089	.071	.059	.041	.030	.019	.013	.010
31	Flat Loadings	.005	.004	.003	.002	.002	.002	.001	.001	.001	.001	.001	.001
32	Indicated ELPF's (30) + (31)	.195	.152	.124	.105	.091	.073	.060	.042	.031	.020	.014	.011

APPENDIX A-3 (CONT'D)

* $27 = [(19) \times (26a)] + [(22) \times (26b)] + [(25) \times (26c)]$

APPENDIX B

EXHIBIT B-1

Derivation of Indicated Hazard Group Differentials (High Benefit States)†

Hazard	(1)	(2)	(3) Claim	(4) s Over 9,999	(5) Claim	(6) s over 24,999
Group	All Cases	All Losses	Cases	Losses	Cases	Losses
I	106,786	39,062,759	803	16,861,263	191	7,793,946
П	674,620	303,854,815	6,410	141,923,132	1,564	68,176,269
Ш	267,399	191,174,298	4,329	111,871,561	1,315	65,717,152
IV	39,542	33,592,782	721	21,036,472	274	14,445,293
TOTAL	1,088,347	567,684,654	12,263	291,692,428	3,344	156,132,660

Indicated Hazard Group Relativities: Losses Over 24,999

Hazard Group	(7) Average Excess Ratio [(6) - 25,000 × (5)] ÷ (2)	(8) Indicated Relativities (7) \div (7) Total
 I	.07728	.60
п	.09569	.75
ш	.17179	1.34
IV	.22610	1.77
TOTAL	.12777	

Indicated Hazard Group Relativities: Loss Over 9,999

Hazard Group	(9) Average Excess Ratio [(4) → 10,000 × (3)] ÷ (2)	(10) Indicated Relativities (9) ÷ (9) Total
	.22608	.76
II	.25612	.86
111	.35874	1.20
IV	.41159	1.38
TOTAL	.29781	

[†]Includes data from Alaska, Arizona, Connecticut, District of Columbia, Idaho, Illinois, Maine, Michigan, Minnesota, Oregon, and Rhode Island.

APPENDIX B

EXHIBIT B-2

Derivation of Indicated	Hazard Groun	Differentials	(Medium	Benefit	States) †
Berradion of maleutea	riuzura Oroup	· Longerending ·	(meculum	Denent	orares / 1

Hazard	(1)	(2)	(3) Claims	(4) s Over 9,999	(5) Claims	(6) s over 24,999
Group	All Cases	All Losses	Cases	Losses	Cases	Losses
1	94,238	22,064,844	362	6,133,760	46	1,595,904
11	657,109	187,377,649	3,367	64,327,682	563	23,329,029
Ш	257,383	123,407,829	2,629	58,061,238	606	26,863,892
IV	41,777	25,527,288	596	14,455,738	177	7,812,199
TOTAL	1,050,507	358,377,610	6,954	142,978,418	1,392	59,601,024

Indicated Hazard Group Relativities: Losses Over 24,999

	(7)	(8)
Hazard	Average Excess Ratio	Indicated Relativities
Group	$[(6) - 25,000 \times (5)] \div (2)$	$(7) \div (7)$ Total
I	.02021	.29
II	.04939	.71
III	.09492	1.37
IV	.13269	1.92
TOTAL	.06920	

Indicated Hazard Group Relativities: Loss Over 9,999

Hazard Group	(9) Average Excess Ratio $[(4) - 10,000 \times (3)] \div (2)$	(10) Indicated Relativities (9) ÷ (9) Total
<u> </u>	.11393	.56
II	.16361	.80
III	.25745	1.26
IV	.33281	1.62
TOTAL	.20492	

⁺Includes data from Arkansas, Colorado, Hawaii, Indiana, Iowa, Kentucky, Maryland, Missouri, Nebraska, New Hampshire, South Dakota, Tennessee, Vermont and Wisconsin.

APPENDIX B EXHIBIT B-3

Derivation of Indicated Hazard Group Differentials (Low Benefit States) †

Hazard	(1)	(2)	(3) Claim	(4) s Over 9,999	(5) Claims	(6) 5 over 24,999
Group	All Cases	All Losses	Cases	Losses	Cases	Losses
1	106,736	28,424,675	486	8,633,223	58	2,396,027
П	693,890	193,922,765	3,853	71,691,448	519	21,896,794
Ш	334,485	158,990,080	3,750	74,442,781	654	27,209,740
IV	53,826	31,652,377	783	18,042,199	182	8,726,708
TOTAL	1,188,937	412,989,897	8,872	172,809,651	1,413	60,229,269

Indicated Hazard Group Relativities: Losses Over 24,999

Hazard Group	(7) Average Excess Ratio $[(6) - 25,000 \times (5)] \div (2)$	(8) Indicated Relativities (7) ÷ (7) Total
 I	.03328	.55
II	.04601	.76
III	.06830	1.13
IV	.13196	2.19
TOTAL	.06030	

Indicated Hazard Group Relativities: Loss Over 9,999

Hazard Group	(9) Average Excess Ratio [(4) – 10,000 × (3)] ↔ (2)	(10) Indicated Relativities (9) \div (9) Total
I	.13274	.65
II	.17100	.84
III	.23236	1.14
IV	.32264	1,58
TOTAL	.20361	

[†]Includes data from Alabama, Florida, Georgia, Kansas, Louisiana, Mississippi, Montana, New Mexico, North Carolina, Oklahoma, South Carolina, Utah, and Virginia.

APPENDIX B EXHIBIT B-4

Derivation of Indicated Hazard Group Differentials (All States) †

Hazard	(1)	(2)	(3) Claim	(4) s Over 9,999	(5) Claim	(6) is over 24,999
Group	All Cases	All Losses	Cases	Losses	Cases	Losses
I	307,760	89,552,278	1,651	31,628,246	295	11,785,877
П	2,025,619	685,155,229	13,630	277,942,262	2,646	113,402,092
ш	859,267	473,572,207	10,708	244,375,580	2,575	119,790,784
IV	135,145	90,772,447	2,100	53,534,409	633	30,984,200
TOTAL	3,327,791	1,339,052,161	28,089	607,480,497	6,149	275,962,953

Indicated Hazard Group Relativities: Losses Over 24,999

Hazard Group	(7) Average Excess Ratio [(6) - 25,000 × (5)] ÷ (2)	(8) Indicated Relativities $(7) \div (7)$ Total
<u> </u>	.04925	.54
II	.06897	.76
III	.11702	1.28
IV	.16700	1.83
TOTAL	.09129	

Indicated Hazard Group Relativities: Loss Over 9,999

Hazard Group	(9) Average Excess Ratio $[(4) - 10,000 \times (3)] \div (2)$	(10) Indicated Relativities (9) ÷ (9) Total
	.16882	.69
II	.20673	.85
III	.28991	1.19
IV	.35842	1.47
TOTAL	.24390	

†Includes data from the states listed in exhibits I, II, and III.