HOSPITAL SELF-INSURANCE FUNDING: A MONTE CARLO APPROACH By Dave Bickerstaff

ABSTRACT

The common theme which appears to have evolved in the actuarial methodology for determining self-insurance funding contributions can be described in basic terms as a two-step process: (a) estimating expected retained losses for the self-insured entity and (b) estimating a safety margin or risk loading to maintain funding at a selected high level of confidence. Variations on this general theme abound. Using Hospital Professional Liability as an example, this paper sets forth a simulation technique which approximates the aggregate loss distribution and the distribution of required funding to cover losses, focusing on the interaction of several variables. Special emphasis is placed on treating the run-off of the fund's prior year losses and the prospective target year losses simultaneously in determining the required funding on a year-by-year basis.

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The establishment of self-insured trust funds has become, over the last 10-12 years, a widely accepted response by U.S. hospitals to an increasingly constricted liability and workers' compensation market. Accurate estimates relating to the total aggregate hospital funding for self-insurance may be difficult if not impossible to come by, but it seems apparent that here in the late 1980's the larger hospitals (say, 500 beds and up) who self insure a significant first layer for at least their professional liability exposure are the rule rather than the exception.

The determination of appropriate funding levels for self-insured funds calls for the careful application of a special chapter from the property-casualty actuarial repertoire. It appears from this author's perspective that, for the most part, actuarial input of one kind or another has been solicited and delivered as an integral part of the hospital self-insurance planning process. (It should be acknowledged, of course, that no small factor in the prominence and high visibility of this actuarial input was the inclusion by the HEW Department of required actuarial "certification" of self-insured funding levels in their original funding guidelines for Medicare reimbursement purposes in the mid 1970's. No attempts will be made by this author to chronicle the evolution of the Medicare guidelines. The concepts discussed in this paper are intended to be more generic, concentrating on the intrinsic risk encountered by a self-insuring entity and the funding required to retain and sustain that risk -- irrespective of government guidelines.)

Basic Principles

Any practicing actuary searching for a standard "cookbook" or "generally recognized" approach to calculating funding levels for self-insured funds will probably end up waving the white flag. It seems that there have evolved over the past decade or so several (dozens, maybe) methodologies or families of methodologies which represent variations on a general theme. Despite all the variations, it appears that the common denominator among all self-insurance funding procedures can be described in general terms as follows: An *expected* annual retained loss is estimated for the hospital, using the hospital's own loss experience to the extent deemed credible (and outside data otherwise), and, to supplement this expected level, a *safety margin* or risk loading is included in the funding, based in one way or another on some measurement of the distribution of aggregate retained losses and defining confidence intervals from that distribution. Beyond this simple theme, though, variations of all shapes and forms (which may be equally defensible) abound. In the process of walking through the development of a self-insurance procedure, or one "variation" on the common theme, this author found that the first major building block beyond the central theme is the treatment of the funding calculation for the first year of a fund contrasted with the "renewal" funding for each year thereafter. For the initial funding calculation one is concerned only with the prospective expected retained losses for the target year and with the confidence levels around that expected level. For each year thereafter, the funding level would logically be predicated on the amount required to run off the losses from prior years as well as the amount required for the prospective target year. With these dual objectives in mind, we can set forth our first general expression for determining a self-insured funding level:

Indicated funding for year N + Current Assets of fund = present value of losses from prior years paid in years N forward + Present value of losses incurred in year N.

When N=1, of course, the current assets = 0 and there is no runoff from prior years. For N > 1, however, the remaining unpaid losses from prior years and the projected losses for the next target year are treated simultaneously in determining what additional funding, when combined with the current assets which were generated from prior funding and the interest earned thereon, will be necessary to cover all future losses.

The two loss categories in the above general expression are, of course, treated as random variables and thus the value solved for -- the required year N funding level -- is also defined as a random variable. After the probability distribution of this random variable is approximated, a funding level is then determined corresponding to a desired confidence level. It is safe to assume that most of the actuarial effort expended over the past few years in the self-insurance field has been in the determination of this probability distribution, given all of the necessary parameters. It is also pretty safe to assume that it is in this phase of the actuarial exercise that most of the wide variations on the theme occur.

As the above basic formula implies, the annual funding amount is continually self-correcting, based on each new year's experience. Not unlike pension plan funding, the actuarial "gains" or "deficits" from prior years, represented in the formula by the present value of the runoff of prior years' losses less the current assets, are built into the formula to determine the indicated level of funding for the next year. Rather than treating the funding of each new year independently of the prior years and thereby stacking single year safety margins on top of prior single year safety margins, all years are treated collectively to determine the safety margin to cover all losses.

Expected Losses for Hospital

This paper will not dwell on the details of analyzing the loss and exposure data of a particular hospital and the loss experience from pertinent "global" sources to supplement the hospital-specific data. It would seem that the choice of which loss reserving techniques to use to analyze the data and project expected loss costs per exposure unit to a target year would depend largely on the size of the hospital, the availability of loss data, and the judgement of the actuary doing the analysis. Conceivably, for large hospitals with as many as 8-10 years of accessible loss data, one could construct historical loss development triangles, including paid and open claim counts and amounts, and determine historical development patterns based on the hospital's data itself. For middle-sized hospitals, the actual claim data might be used, but for purposes of loss development and trending, more global (e.g., statewide or countrywide) indications would probably be required. Finally, for the small hospitals, the loss experience of the entity itself would rarely, if ever, be used and the expected loss costs might be derived exclusively from the global sources.

Even for the larger hospitals, the final selection of the expected loss cost might be based to some extent on a credibility-weighted average of the hospital-specific data and the statewide average. Rather than being a slave to some dogmatic credibility standard (all together now, 682 claims = 100% credibility, etc.), it would seem that a great deal of actuarial judgement should be exercised in arriving at the final selections, particularly since, from a subjective standpoint, there may well be some unique risk characteristics for the hospital in question (types of procedures, etc.) which should be reflected irrespective of its sheer size and statistical credibility.

Given the projected expected loss cost for the hospital, the second task at hand in the procedure to determine funding levels is to approximate the probability distributions around the expected values from which confidence levels can be defined. To accomplish this task this author has developed a Monte Carlo simulation model to "sample" the experience of a fund, as defined by certain parameters, over a large number of trials (usually 1,000). Accordingly, no matter how the final weighted average expected loss cost is derived for the hospital, it will be necessary to break out this loss cost into a few key components, for purposes of generating the probability distribution. As a first step, an average claim cost (at some limit) and a total claim frequency would be determined, the product of which will equal the pure loss cost per exposure unit. The average claim cost can then be subdivided into: (a) average indemnity cost

and (b) average claim expense, while frequency can be subdivided into (c) percentage of claims closed with indemnity, (d) percentage of claims closed with claim expense only, and (e) percentage of claims closed with no payment.

A quick preview of the key distributions which will need to be developed in the Monte Carlo model is as follows:

- (a) Distribution of indemnity amounts
- (b) Distribution of ALAE amounts
- (c) Claim frequency distribution
- (d) Claim reporting and claim payout distributions
- (e) For renewal funding: distribution of the number of IBNR's from prior years, given the expected number of IBNR's

The key distributions used in the model will now be explored in some detail.

THE INDEMNITY SIZE OF LOSS DISTRIBUTION

The NAIC Closed Claim Studies

Perhaps the most critical component in our procedure to approximate the confidence levels of self insurance funding is the distribution of indemnity amounts (from ground up, with no limit) for one accident year. Using medical professional liability as the line of business in question, we referred to the NAIC closed claim study.¹ For this study, some 75,000 claims closed during the period 1975-78 were recorded. Among many other items of information, the accident dates, report dates, closed dates, and indemnity and ALAE amounts were included.

It has been shown by many researchers² that, in order for any calendar year closed claim distribution to accurately represent the claim-size distribution applicable to an accident year, some trending adjustments are necessary for both claim frequency and claim severity. For this author's model claim-size distribution, we first devised annual indices of claim severity and frequency (both accident year) from available national data covering a period of about 20 years

¹National Association of Insurance Commissioners, NAIC Malpractice Claims, 1980.

²See, for example, Archer McWhorter, Jr., "Drawing Inferences from Medical Malpractice Closed Claim Studies", The Journal of Risk and Insurance, XLV, no. 1 (March, 1978) and Michael R. Lamb, "Uses of Closed Claim Data for Pricing," Pricing Property and Casualty Insurance Products, 1980 C.A.S. Discussion Paper Program, p. 219.

up to calendar year 1978 (the final closing year of the study). The frequency and severity indices for each year were then expressed in terms of the 1978 index equal to 1.0. Then to each detail claim record,³ based on the accident date, we applied the reciprocal of the frequency index to the claim count (1 per record, initially) and the reciprocals of both the frequency and severity indices to the indemnity and ALAE amounts. As a result of this exercise, we produced a claim size distribution adjusted to represent the accident year 1978.

A printout of the trend-adjusted claim size distribution (indemnity) is shown in Appendix A, page 1. The brackets of indemnity size are set up on logarithmic (geometric) scale, with the end point of each bracket a constant factor (about 1.3335) times the end point of the previous bracket. A plot of the histogram for the non-zero members of this adjusted distribution is displayed on page 2 of Appendix A. The cumulative distribution ogive is then plotted on page 3. But the most revealing and useful plot of this accident-year adjusted distribution is shown on pages 4-5, on which we have plotted the cumulative distribution on lognormal probability graph paper, the grids of which are constructed so that the cumulative distribution ogive of a lognormal probability distribution is a straight line.

The lognormal model has been used extensively to represent claim size distributions in property and casualty lines.⁴ Finger, in particular, used the lognormal model to determine implied increased limit factors for medical professional liability. It would follow, then, that the lognormal would be a good candidate to investigate for modelling self-insured losses.

On the first page of our cumulative distribution graph (claims up to 100,000), the lognormal fit -- a straight line drawn though the points strictly by sight -- clearly is good enough to represent the actual data. On the continuation of the distribution on page 5, it can be noted that for values above about \$500,000 the actual data points veer out above the hand-selected lognormal line. There is a very plausible explanation for this. If the lognormal model does in fact provide a good representation of the claim size distribution with no limit, then the imposition of policy limits on the bigger claims in the data base itself would have had a dampening effect on the relative frequency of these claims in the higher, potentially excess, layers. It can be approximated from the graph, for example, that the extension of the

³In addition to referring to the hard-copy NAIC report, we also purchased the detail data tape from the association.

⁴See, for example, Charles C. Hewitt, Jr., "Credibility for Severity," PCAS, LVII (1970), p. 148; David R. Bickerstaff, "Automobile Collision Deductibles and Repair Cost Groups: the Lognormal Model," PCAS, LIX (1972), p. 68; and Robert J. Finger, "Estimating Pure Premiums by Layer -- an Approach," PCAS, LXIII (1976), p. 34.

lognormal line would indicate a frequency of claims in the \$2 million plus range about 4 to 5 times greater than the actual data points would indicate. For this reason, more than any other, this author disdained any idea of walking through a rigorous, analytical curve-fitting choreography, which would have generated a "best fitting" line that understates the potential for big claims.

The selected lognormal parameters for indemnity

We estimated a mean and variance from our fitted lognormal claim size distribution by marking off the median and standard deviation directly from the graph, using the 50 percentile and +1 standard deviation marks on the vertical scale, as follows:

Observed median = e^{4} = 10650 . Observed $T = \log_{e}(68000) - \log_{e}(10650) = 1.853$

Our final selected value for the mean is, then

 $\exp(\log_{\bullet}(10650) + (1.853)^2/2) = 59300$.

The coefficient of variation (standard deviation divided by the mean) of the fitted distribution is calculated as follows:

$$(CV)^2 = e^{\sigma^2} - 1$$

= 29.988.

Thus, for future modelling purposes, we set the CV value = $\sqrt{30}$.

Working Size of Loss Model for Indemnity

The absolute values of the 1978 NAIC closed claim distribution, even after adjusting for frequency and severity trends, are not particularly important to us - especially in 1989. The shape of the adjusted, fitted distribution is the key parameter, measured by the CV. We believe that it is reasonable to assume that as the average unlimited indemnity increases over time or from one territory to another, the $(CV)^2$ should remain relatively constant. This also implies that as the *average* unlimited claim increases k percent from one point in time to another, it is reasonable to expect that the entire distribution of claims moves up about k per cent. Put another way, an \$800,000 claim has about the same relative niche in a distribution

whose unlimited mean is \$100,000 as a \$400,000 claim in a distribution with half the unlimited mean.

Our working indemnity distribution can, then, be represented by a lognormal distribution whose unlimited mean is 1.0 and whose $(CV)^2$ is 30, as shown in page 6 of Appendix A. The top line represents the basic distribution of claims by size and the bottom line depicts the *first moment* distribution.⁵ To illustrate how this graph is read, from the top line one can note that about 82.5% of all claims are less than or equal to the mean and about 96.5% of the claims are less than or equal to five times the mean. From the bottom line, one can further note that about 18% of the total *dollars* in the distribution come from claims which are less than or equal to the mean and about 47% of the dollars from claims below five times the mean.

Generation of random claim amounts from lognormal model

To tabulate sample claims from the lognormal distribution, our Monte Carlo model employs a random number generator which generates *normal* random numbers.⁶ The sample random claim size (indemnity) is determined from the following formula:

 $X = \exp(+ N\sigma)$ where = mean of the logs of the distribution = S.D. of " " " " N = normal random number (mean 0, var. 1).

From the basic relationships of the lognormal distribution,

 $M = \exp(\mu + \sigma^2/2)$ where M = mean of the distribution.

Then we have

 $= \log_{e}(M) - \sigma^{2}/2$

⁵For a discussion of moment distributions and other attributes of the lognormal distribution, see J. Aitchison and J. A. C. Brown, The Lognormal Distribution, (Cambridge University Press, 1969).

⁶A full discussion of random number generation is beyond the scope of this paper. For further reference, we recommend G. S. Fishman, **Principles of Discrete Event Simulation** (New York: John Wiley & Sons, 1978), chap. 8-9.

and then the sample claim would be generated with

$$X = \exp(\log_{e}(M) - \sigma^{2}/2 + N \sigma).$$

REPORT YEAR / CALENDAR YEAR STRATIFICATION OF ACCIDENT YEAR

In our basic funding formula, it will be recalled that we were looking for the *present value* of future losses or the distribution of the present value of losses. Furthermore, the self insured retention (SIR) limit per claim, as regards the terms with an excess carrier, may be *indexed*, i.e., the excess attachment point would be increased a specified amount (or percentage) each year based on the *calendar year* that first payment is made on the claim. Thus, we are interested not only in the distribution of claims by size but also the distribution of claims by lag time to settlement. Because of the well-recognized correlation between payment lag and payment size, we have introduced a form of stratification in the sampling of medical professional claim amounts. To accomplish this, we first set forth some basic relationships between report year and calendar year severities, within the accident year:

- Let R(i) = Frequency of claims reported in report year i of acc. year, relative to total accident year
 - C(j) = Freq. of claims of one rep. year paid in cal. year j, relative to total report year
 - S_i = Severity of claims of report year i, relative to total accident year severity
 - T_j = Severity of claims of calendar year j, relative to total severity of report year
 - n = total report years in accident year
 - m = total calendar years for each report year

Then you have

$$\sum_{i=1}^{n} R(i) = 1$$

$$\sum_{j=1}^m C(j) = 1$$

and, by definition,

$$\sum_{i=1}^{n} S_{i}R(i) = 1$$
$$\sum_{i=1}^{m} T_{j}C(j) = 1$$

The total accident year can then be stratified into n[•]m report year/calendar year cells. The cell identified by the ith report year and the jth relative calendar year in that report year would have a claim frequency of $R(i)^*C(j)$ times the total accident year frequency and a severity of $S_i^*T_j$ relative to the total accident year severity. It also holds that the mean severity over all n[•]m cells is

$$\sum_{i=1}^{n} \sum_{j=1}^{m} S_i T_j C(j) R(i) = 1$$

Since the above mean = 1, the coefficient of variation squared over all n*m cells is:

$$C^{2} = \sum_{j=1}^{n} \sum_{j=1}^{m} [S_{j}T_{j}]^{2}C(j)R(i) - 1$$

Modified CV's for stratified sampling

We earlier developed a model indemnity size-of-loss distribution for an entire accident year, with a $(CV)^2$ of 30. But instead of simply sampling indemnity amounts from the entire accident year distribution, our Monte Carlo model will first select (randomly) a report year and then a calendar year paid for each random claim and then, based on the relative severity levels discussed above, sample from an indemnity distribution the mean of which has been adjusted

to the levels corresponding to that report year and relative calendar year. Consequently, it becomes necessary to modify the CV applicable to each RY/CY stratum so that when you combine the sampled claims from the various RY/CY cells, you achieve the desired composite accident year $(CV)^2 = 30$.

To accomplish the desired approximation of the modified CV applicable to each RY/CY cell, we used a method first advanced by Hewitt.⁷ He demonstrated that, if (a) a random variable Y were stratified into groups and (b) the means of the groups were lognormally distributed and (c) the variance of the logs of the means were S², and (d) if the variance of the logs of each group were $(\sigma_{\gamma})^2$, a constant, then the variance of the logs of the combined distribution of all groups would be S² + $(\sigma_{\gamma})^2$. The "spread parameter" S² over the n*m report year/calendar cells can be determined directly from the C², calculated above:

$$C^{2} = e^{S^{2}} - 1$$

 $S^{2} = \log(C^{2} + 1)$.

Thus,

$$\log(C^2 + 1) + (f_v)^2 = Log(31)$$

and

$$(T_{\gamma})^2 = Log(31) - log(C^2 + 1)$$
.

It should be emphasized that the above expression is an "approximation" of the modified variance (of the logs) to be used in the stratified sampling, since some of Hewitt's prerequisites are not necessarily met. Therefore, it is appropriate to perform a test of the stratified sampling, using sample values of R(i), C(j), S_i , and T_j , to determine if the overall accident year CV is achieved within an acceptable tolerance.

Testing the stratified sampling parameters

To determine appropriate values for the distributions of $R(i), C(j), S_i$, and T_j , we referred again to the NAIC closed claim studies. Using the detail NAIC data base, after the frequency and severity trend adjustments, we constructed a report year/calendar year matrix as shown in

⁷Hewitt, op. cit., Appendix A, p. 167.

Appendix B. The entire claim data base, now adjusted to represent an accident year, was stratified into cells defined by ten report years and 16 calendar years (relative to the accident year). Each cell contains the (adjusted) claim counts, amounts, and averages. From the totals by report year, we derived the percentages of total claims by report year and the relative severity for each report year. On pages 5-6 of that same Appendix we determined relative severity values for calendar years, relative to report years. The values from this matrix will, then, be a starting point to determine the $R(i),C(j),S_i$, and T_j values for a specific case (it should be pointed out that the actual historical report year and calendar year patterns for a given jurisdiction and self-insured entity, to the extent that they are credible, should be given more weight than the NAIC numbers).

For this paper's case study, we have selected the report year and calendar year distributions shown in page 7 and 8 of Appendix B. We have used a total of seven report years (n = 7) and nine relative calendar years (m = 9). The relative severity factors have been selected (roughly from the NAIC matrix) and then adjusted so that the sum of the products of the frequency times the relative severities is 1.0. The $(CV)^2$ of the cell means,

$$C^{2} = \sum_{i=1}^{n} \sum_{j=1}^{m} [S_{i}T_{j}]^{2}C(j)R(i) - 1$$
$$= .2607.$$

Thus,

$$(\sigma_{\gamma}^{\prime})^2 = \text{Log}(31) - \log(1.2607)$$

= 3.20232
and ∇_{γ} = 1.7895.

Thus, while the standard deviation (of the logs) of the entire accident year is $\sqrt{\log(31)} = 1.8531$, the standard deviation applicable to each cell will be reduced to 1.7895.

The results of our test of the stratified sampling versus unstratified is summarized in Appendix C. Rather than sampling from the lognormal distribution with no limit, we sampled successively from distributions with limits of \$50,000, \$100,000, \$500,000, \$1,000,000, \$10,000,000, and \$25,000,000. In each case, the unlimited mean was \$100,000. For each limit,

we (a) calculated the mean and CV directly,⁸ (b) generated a sample mean and CV from the unstratified distribution, and (c) generated a sample mean and CV using the RY/CY strata with the adjusted means and appropriately reduced variance. To make sure we covered a full spectrum of possibilities, we used three values for $(CV)^2$: 10, 20, and 30. The report year and calendar year distributions were similar, but not identical, to those in pages 7-8 of Appendix B. For each combination, 100,000 claims were sampled.

The test samples demonstrated that the composite means and CV's derived from the stratified process were a good approximation to the direct calculation, within an acceptable tolerance.

THE ALAE COMPONENT IN THE MODEL

The ALAE-Indemnity relationship

Most excess policies written over a self-insured's SIR provide that ALAE on a claim (occurrence) is recoverable "pro rata," i.e., the percentage of the ALAE in a claim which is covered by the excess policy is the same as the percentage of the gross indemnity amount which is covered. Some contracts (relatively infrequent) set forth a retention level based on the sum of the indemnity and ALAE for one claim. In any case, the interaction between ALAE and indemnity would be an important consideration in any self-insured risk model.

It should be emphasized that in our self insured funding model the ALAE for the sampled claim is not treated as a constant factor related to the indemnity size (like tax and gratuity), but rather the *expected* ALAE (mean value of a separate ALAE distribution) is established, given the sample observed value of the indemnity. To treat ALAE otherwise would result in an understatement in the overall variability of the aggregate loss distribution.

To determine the functional relationship (if indeed a measurable relationship exists) between ALAE size and indemnity size for medical professional liability claims, we turned again to the NAIC Closed Claim Study.⁹ As shown in Appendix D, Page 1, the average ALAE was calculated for each of several brackets of indemnity size. After plotting the average ALAE in each bracket against the corresponding average indemnity for the bracket, using logarithmic X and Y axes (see Appendix D, page 2), it was observed that a reasonably good straight line

⁹NAIC, op. cit.

⁸The calculation of the moments of a lognormal distribution limited (censored) by some limit L is fairly straightforward but is not covered here.

fit was obtainable, implying that the ALAE-indemnity relationship was representable by a member of the "power" curve family, $Y=AX^{B}$.

The equation used to regress the ALAE means against the indemnity values (grouped into brackets) is:

$$Log_e(Y) = A + B^*Log_e(X).$$

The weighted least squares best fit coefficients, using the number of claims in each indemnity bracket as weights, were

From the same data base which was used to develop this relationship between average ALAE and indemnity, it was also determined that the average indemnity was \$53,363. Thus,

Then restate the regression formula above by expressing both ALAE and indemnity as a ratio to the average indemnity over the entire distribution, as follows:

X'≖X/I

Then the restated expression becomes:

$$Log_e(I^*Y') = B^*Log_e(I^*X') + A .$$

Simplifying, you get

$$Log_{e}(Y') = B^{*}Log_{e}(X') + B^{*}Log_{e}(I) + A - Log_{e}(I)$$

$$= B^*Log_{e}(X') + (B-1)^*Log_{e}(I) + A.$$

Then let

$$C = (B-1)^*Log_{*}(I) + A = -1.964768$$
.

You then have

$$Log_{a}(Y') = B^{*}Log_{a}(X') + C$$

and

$$Y' = e^{C}X'^{B} = .1401884 * X'^{.482945}$$

For future reference, we call

 $D = e^{C}$.

From the above expression, it can be noted that, in approximate terms, the expected ALAE varies in proportion to the square root of the sample indemnity.

Distribution of ALAE per claim, independent of indemnity

The next step of our treatment of ALAE in the model is to examine the distribution of ALAE per claim (defendant), irrespective of indemnity amounts. To do this, we again investigated the NAIC closed claim study.¹⁰ The distribution is graphed in Appendix D, page 3. Using lognormal probability graph paper, the near straight line plot of the cumulative distribution function suggests that, just as was the case for the distribution of indemnity values by size, the ALAE amounts also can be represented quite adequately by the lognormal model.

We determined a mean and variance for the ALAE distribution two ways: first, we calculated the mean and variance directly from the data and then we followed the same procedure used for the indemnity graph. After drawing a straight line fit for the cumulative distribution function on the lognormal probability graph paper (the plotted points from the actual data were close enough to a straight line to allow us to simply draw the fitted line free-hand), we "picked off" the median and standard deviation directly from the graph, using the 50 percentile and +1

 $^{^{10}}$ For this distribution, we chose, for the sake of conservatism, the earlier 1975 version of the NAIC study, since the plotted CV was higher than that of the 1978 release.

standard deviation marks on the vertical scale, as follows:

Observed median = e^{4} = 1355. Observed $\nabla = \log_{2}(5200) - \log_{2}(1355) = 1.345$

Our final selected value for the mean is, then

 $\exp(\log_{e}(1355)+(1.345)^{2}/2) = 3348$.

Of more importance, as will become clear later, our selected value for the variance was $(1.345)^2$, or 1.809.

Parameters for conditional ALAE distribution

We established earlier that, for purposes of sampling ALAE for any Monte Carlo simulation model, the *expected* ALAE in the distribution sampled from will be dependent on the sample indemnity value, or

 $E[Y|X] = DX^{\theta}$,

where

Y = random variable ALAE, conditional on value of indemnity, X D = .1401884 B = .482945

and both Y and X are expressed relative to the unlimited mean indemnity.

Aitchison and Brown¹¹ have shown that if the random variable X is lognormally distributed with parameters $\Delta \sigma^2$, then DX⁸ is also lognormally distributed with parameters $\log(D) + B_{\alpha}$ and $B^2 \sigma^2$. The parameters are the mean and variance, respectively, of the *logs* of the random variables.

We now let S² = variance of the logs of ALAE means E[Y|X], conditional on sample indemnity values = B² π^{2}

¹¹op. cit., p. 11.

Again employing Hewitt's method of isolating the "spread parameter", ¹² we can solve for the variance applicable to each ALAE "group", $(\sigma_{\gamma})^2$, defined as the sample ALAE given the sample indemnity mean:

We earlier derived an approximation for the combined variance

then

$$(\sigma_{\gamma})^2 = 1.809 - .8009$$

= 1 (approx.)

 $S^2 + (\tau_v)^2 = 1.809$

In a word summary, then, we have established that the sample ALAE (relative to the unlimited mean indemnity) would be drawn from a lognormal distribution whose mean is .1401884 $X^{.482945}$ and the variance of whose logs is 1.0, where X represents the sample indemnity, relative to the unlimited mean indemnity.

Testing the sampled ALAE values, conditional on sample indemnity

Using the parameters estimated above, a test was set up to randomly sample 100,000 claims to make sure that the resulting overall ALAE sample moments were sufficiently close to those from direct calculations. For all ALAE combined, the coefficient of variation $(CV)_a$ is determined:

$$(CV_a)^2 = e^{S^2 + \sigma^2} - 1$$

= 5.104
 $CV_a = 2.259$.

From our sample of 100,000 claims, the sample CV for ALAE was 2.24363.

THE MONTE CARLO MODEL

Having highlighted the key actuarial considerations in approximating the probability

¹²Hewitt, loc. cit.

distribution of self insured losses, we are now ready to describe the Monte Carlo model in some detail. The use of Monte Carlo models shows up with increasing regularity in the actuarial literature.¹³ But despite the general agreement, in risk theory circles, that Monte Carlo models are an acceptable technique for approximating these distributions, this author perceives that any number of the direct approximation methods¹⁴ are considered superior, assuming that the mean and variance of the distribution can be calculated directly and precisely.

Given all of the interactions between the many variables discussed above -- e.g., the calendar year payout and the present value calculation and the indexed retention and the ALAE-indemnity relationship -- plus the necessity of treating the runoff of prior years' losses and the target prospective year simultaneously, this author is hard pressed to identify any direct approximation formula from any risk theory text which will yield adequate results for the defined problem. The use of a Monte Carlo model, in which all of the interactions can be adequately defined and programmed into one composite risk process, would appear to be the only satisfactory approach.

A full description of our self-insurance Monte Carlo risk model is included in Appendix E. In the first section, we have listed the miscellaneous assumptions, the input parameters, and the various distributions from which samples are made. For our selected case study (which we will call "XYZ Hospital"), the initial target year is accident year 1989. A second run, made one year later, considers the run off from the 1989 year and the 1990 prospective losses. In the second section of the outline the actual simulation process for one trial (normally, at least 1,000 trials are run for a given case study) is outlined in pseudo code. Tracking the program flow through this pseudo code will reveal how the many variables interact with each other.

Parameter variance

Over the past few years there have been welcome additions to the body of actuarial literature dealing with *parameter variance*, as it relates to simulation models to approximate aggregate loss distributions. We will not attempt in this paper to supply another textbook treatment of *parameter variance* and *process variance*. Suffice it to say that it would be hard to imagine deriving any valid results from a Monte Carlo risk model which did not incorporate some kind of parameter variance -- particularly for a line with as much uncertainty surrounding the

¹³See, for example, P. E. Heckman and G. G. Meyers, "The Calculation of Aggregate Loss Distributions from Claim Severity and Claim Count Distributions," PCAS, LXX (1983), p. 22.

¹⁴No attempt will be made to provide a list of these methods here.

"universe" means (frequency and severity) as medical professional liability.

The key point is that the parameter variance is the same over all size of hospital risks. The vagaries of the business -- the social, economic, and legal dynamics which dictate that we do not deal from the same 52-card deck from one year to the next -- apply equally to all sizes of risks. Thus, while the process variance may play the lead role in driving the overall aggregate loss distribution for small hospitals, the parameter variance is predominate in models of larger risks, for which the process variance, or the pure statistical sampling error, has been reduced simply by virtue of the larger volume.

Rather than mathematically rolling the parameter and process variances into one combined variance for simulation purposes, this author chose to incorporate the two variances into the model as separate routines, in step-wise fashion. For a given trial, the first step is to randomly select the "universe" frequency and severity (average unlimited indemnity) from distributions the means of which represent our best estimate of these two parameters, based on the data which is available (statewide, countrywide, the hospital itself). The standard deviations of these distributions of the frequency and severity universe means are judgmentally selected to represent the "uncertainty" surrounding these means, resulting from many forces. This author is not aware of any successful attempts to quantify these factors, if, indeed, all of them have identified.

After the universe mean frequency and severity have been selected, the second step is to select the sample frequency (or total claim count) and then, for each claim, the sample claim amount. For sampling the frequency distribution, we use a Poisson process, unless the "universe" mean, selected in the first step, is greater than 15, in which case the model uses the normal approximation. As developed earlier in some detail, the lognormal distribution is used in the sampling of the individual claim amounts.

IBNR Distribution

Treating the runoff from prior years as a random process in our model requires not only simulating the payoff of reported and unpaid claims but also determining the *expected* IBNR from those years and the distribution around that expected value. As was shown in the description of the model and the "pseudo-code", the open cases are treated separately from the IBNR's. For our model, the expected number of IBNR's is determined by selecting an *a priori* total ultimate claim count for each of the prior years, and multiplying times the reporting percentages taken from our assumed reporting distribution. The actual *sample* number of

IBNR's for a particular trial is then determined by randomly selecting an ultimate number of claims for the prior year in question and then for each of these claims randomly selecting the report year (again from the report year distribution). If the report year thus selected is prior to the current year (thus indicating the claim would have already been reported) the claim is not counted as an IBNR and the loop continues to the next claim.

DERIVATION OF THE PROBABILITY DISTRIBUTION OF REQUIRED CONTRIBUTIONS

The Simulated Loss Distribution

With the Monte Carlo model loaded up with the appropriate input parameters and distributions, we can now make the run for our selected case study. For case 1, the initial year of the fund, the resulting printout of the distribution, generated from 1,000 trials of the model, is shown in Appendix F, page 2. A printout of the input parameters is on page 1 of that appendix. The results of the 1,000 trials have been tabulated and summarized into 31 intervals of retained losses (at present value), including the number of "hits" in each bracket and also the total retained losses in each bracket.

For case 2, performed on the same hospital at the beginning of the second year of the fund, the input parameters are shown on page 3 of Appendix F. For this case, the current assets become part of the input variables, as well as the assumed expected average indemnity on unpaid claims from the prior year. The resulting distribution of required *additional* funding for year 2 is shown on page 4. It can be noted that in over half of the trials no additional funds would have been required. In other words, the assets of the fund after one year (the first year's contribution plus earned interest less the losses paid) would have carried forward sufficient safety margin to cover not only the run-off from year one but also a second year's incurred losses. However, in order to continue to maintain funding at a high level of confidence for year 2, additional funding is required.

The histogram of the simulated distribution and the cumulative distribution ogive for cases 1 and 2 are shown on pages 5 and 6, for the first and second year funding. These plots display a fairly smooth and regular contour -- so much so that, with enough effort and with an appropriate set of parameters, someone could undoubtedly uncover some exotic probability density function which would supply an acceptable "fit" to this curve. But what purpose would this serve? It would be unlikely that such a curve, or even a member of its immediate family, would adequately fit another case defined by an entirely different set of initial variables (retentions, unlimited means, report-year/calendar-year payouts, etc.). Thus, the final estimated loss and required contribution distributions in Appendix F, generated solely for this one particular situation, initial funding and second year renewal funding, are simply what they are. They need no name.

From the final simulated distributions of required funding, one needs only to make a few simple interpolations to approximate the indicated funding levels at selected confidence levels. For this example we chose to display the 90%, 95%, and 99% confidence levels. These interpolations are shown at the end of the printouts on pages 2 and 4. Thus, the indicated funding levels for the two years would be as follows:

| | | Confidence Level | | |
|--------|-------------|------------------|-------------|--|
| | 90% | 95% | 99% | |
| Year 1 | \$2,340,000 | \$2,734,000 | \$3,594,000 | |
| Year 2 | 1,457,000 | 1,968,000 | 2,980,000 | |

The second year funding indication depends, of course, on which funding level was selected for year one (corresponding to a selected level of confidence) and what the assets were at the beginning of year 2. For our case study, we assumed that the assets, after the first year's contribution, one year's interest earnings on the funds, less the disbursements (paid losses) were \$2,950,000. We further assumed that there were seven claims reported and unpaid from year 1 at the beginning of year 2, with an average reserve of \$130,000.

SUMMARY AND CONCLUSIONS

In this paper we have developed a procedure to determine the required funding for hospitals which self insure some layer of their professional liability exposure. The method would apply equally to workers' compensation. To derive indicated funding at various confidence levels, a probability distribution is approximated which combines the runoff of losses from prior years with the prospective losses of the target year. This distribution is approximated with a Monte Carlo simulation model, incorporating the interaction of many variables. The model is designed to be run on an annual basis, and at each renewal it calculates the distribution of additional contributions required which, when combined with the current assets, will cover the present value of all losses.

NAIC CLOSED CLAIM DATA BASE - ADJUSTED FOR FREQUENCY/SEVERITY INDICES

Distribution by Size of Loss

All Claims Combined

| Bracket# | # Claims | Cum. # Claims | Indem. Amount | Avg. Indem. | Exp.Amount | Avg. Expense |
|-----------|------------|-----------------|---------------|-------------|------------|--------------|
| 0 | 51607.8 | 51607.8 | 0 | 0 | 133432000 | 2586 |
| 100 | 358.3 | 51966.1 | 18105 | 51 | 82011 | 229 |
| 133 | 103.2 | 52069.3 | 11821 | 115 | 28022 | 272 |
| 178 | 145.3 | 52214.6 | 22401 | 154 | 24138 | 166 |
| 237 | 167.7 | 52382.3 | 34386 | 205 | 65789 | 392 |
| 316 | 242.8 | 52625.1 | 67813 | 279 | 127607 | 526 |
| 422 | 292.9 | 52918.0 | 108852 | 372 | 120612 | 412 |
| 562 | 411.8 | 53329.8 | 201463 | 489 | 306647 | 745 |
| 750 | 581.2 | 53911.0 | 379945 | 654 | 409760 | 705 |
| 1000 | 828.3 | 54739.3 | 720464 | 870 | 767031 | 926 |
| 1334 | 1015.0 | 55754.3 | 1167310 | 1150 | 1408230 | 1387 |
| 1778 | 1170.2 | 56924. 5 | 1831020 | 1565 | 1483850 | 1268 |
| 2371 | 1477.1 | 58401.6 | 3059210 | 2071 | 2794090 | 1892 |
| 3162 | 1499.5 | 59901.1 | 4177710 | 2786 | 2815350 | 1878 |
| 4217 | 1640.8 | 61541.9 | 6069360 | 3699 | 3594630 | 2191 |
| 5623 | 2180.2 | 63722.1 | 10755100 | 4933 | 5663140 | 2598 |
| 7499 | 2071.1 | 65793.2 | 13590200 | 6562 | 6580210 | 3177 |
| 10000 | 1884.5 | 67677.7 | 16401600 | 8703 | 5619610 | 2982 |
| 13335 | 2029.0 | 69706.7 | 23358300 | 11512 | 7190910 | 3544 |
| 17783 | 1906.4 | 71613.1 | 29460500 | 15453 | 9797740 | 5139 |
| 23714 | 1848.9 | 73462.0 | 37950200 | 20526 | 8096010 | 4379 |
| 31623 | 1564.3 | 75026.3 | 42906200 | 27428 | 8307880 | 5311 |
| 42170 | 1448.2 | 76474.5 | 53156900 | 36705 | 8734200 | 6031 |
| 56234 | 1340.3 | 77814.8 | 65590800 | 48937 | 9357350 | 6982 |
| 74989 | 1171.7 | 78986.5 | 76561700 | 65342 | 9231510 | 7879 |
| 100000 | 926.5 | 79913.0 | 79771100 | 86099 | 7090310 | 7653 |
| 133352 | 917.8 | 80830.8 | 105277000 | 114706 | 8637350 | 9411 |
| 177828 | 746.2 | 81577.0 | 114798000 | 153843 | 10081600 | 13511 |
| 237137 | 722.3 | 82299.3 | 148033000 | 204947 | 10681500 | 14788 |
| 316228 | 456.1 | 82755.4 | 124647000 | 273289 | 6077140 | 13324 |
| 421697 | 402.6 | 83158.0 | 145920000 | 362444 | 7202570 | 17890 |
| 562341 | 247.9 | 83405.9 | 120768000 | 487164 | 4983840 | 20104 |
| 749894 | 199.7 | 83605.6 | 129525000 | 648598 | 7204110 | 36075 |
| 1000000 | 112.6 | 83718.2 | 97909200 | 869531 | 2094480 | 18601 |
| 1333520 | 93.3 | 83811.5 | 106538000 | 1141890 | 2284480 | 24485 |
| 1778280 | 34.0 | 83845.5 | 50086600 | 1473140 | 1177000 | 34618 |
| 2371370 | 15.1 | 83860.6 | 30357800 | 2010450 | 434327 | 28763 |
| 3162280 | 22.4 | 83883.0 | 62135900 | 2773920 | 978374 | 43677 |
| 4216970 | 4.9 | 83887.9 | 19205700 | 3919530 | 206093 | 42060 |
| 5623410 | 0.0 | 83887.9 | 0 | 0 | 0 | 0 |
| 7498940 | 0.0 | 83887 9 | ň | ŏ | ŏ | Ő |
| 10000000 | 0.0 | 83887.9 | ŏ | ŏ | ŏ | ŏ |
| | | | · | | | |
| TOTALS | | 83887.9 | 1722570000 | 20534 | 295171000 | 3519 |
| TOTAL, EX | KCL. CNP*s | 32280.1 | 1722570000 | 53363 | 161739000 | 5011 |

#End point of interval of indemnity amount



Appendix A

112



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Appendix A



CUMULATIVE DISTRIBUTION BY SIZE OF LOSS





Appendix A





MAIC CLOSED MEDICAL LIABILITY CLAIMS - ADJUSTED FOR FREQUENCY/SEVERITY TRENDS

REPORT YEAR/CALENDAR YEAR MATRIX FOR LOSSES OF ONE ACCIDENT YEAR

page 1 of 4

| | Report Year | | | | | | | | | _ | |
|-------------|-------------|----------|----------|----------|---------|-----|-----|-----|-----|-----|-----------|
| Cal.Year | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10+ | Total CY |
| 1: | | | | | | | | | | | |
| 1939 | 4218.5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4218.5 |
| INDEM | 32999300 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 32999300 |
| OCW1/CWE | 2822.5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 2822.5 |
| ALAE | 1985220 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1985220 |
| \$CNP | 11648.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 11648.7 |
| AV6.INCEN | 7823 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 7823 |
| HVD.ALAE | 703 | v | v | U | U | 0 | U | U | U | U | 705 |
| 2: | | | | | | | | | | | |
| ACHI | 3400.8 | 998.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4399.5 |
| INDEM | 97259700 | 15718500 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 112478000 |
| #C#1/C#E | 4685.5 | 1305.3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5990.8 |
| ALAE | 11119700 | 2209980 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 13329700 |
| #CNP | 6591.1 | 2076.2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 8667.3 |
| AV6.INDEM | 28599 | 15238 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 25566 |
| AV6. ALAE | 2373 | 1693 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2225 |
| ٠. | | | | | | | | | | | |
| 5. 50 HT | 2771 4 | 2013 0 | 450 A | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5447 8 |
| THOFM | 114001000 | ATR47100 | 11473500 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 189182000 |
| #CWL/CWE | 4473.3 | 4075.9 | 1418.5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 9967.7 |
| ALAE | 18193800 | 10811900 | 2336750 | 0 | 0 | 0 | 0 | 0 | 0.0 | 0 | 31242400 |
| OCNP | 1754.2 | 2141.0 | 956.9 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4862.1 |
| AVG. INDEM | 41135 | 31717 | 17339 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 34770 |
| AV6.ALAE | 4067 | 2653 | 1647 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3144 |
| 4. | | | | | | | | | | | |
| NCN1 | 2059.9 | 2065.8 | 1183.4 | 196.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5505.8 |
| INDEM | 119169000 | 97840500 | 37162100 | 5590990 | 0 | 0 | 0 | 0 | 0 | 0 | 259752000 |
| ACHI/CHE | 3439.6 | 3982.1 | 2687.5 | 425.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 10434.3 |
| ALAE | 22287000 | 22019200 | 9143340 | 750406 | 0 | 0 | 0 | 0 | 0 | C | 54200000 |
| UCNP | 512.5 | 700.7 | 745.5 | 367.6 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 2526.3 |
| AV6. INDEM | 57852 | 47362 | 31403 | 28424 | 0 | 0 | 0 | 0 | 0 | 0 | 47180 |
| AV6. ALAE | 6480 | 5672 | 3402 | 1766 | 0 | 0 | 0 | 0 | 0 | C | 5194 |
| 5: | | | | | | | | | | | |
| 101 | 1287.5 | 1494 5 | 1353.5 | 365.7 | 100.4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4601.R |
| INDER | 90294500 | 99669400 | 60844300 | 19196000 | 4768230 | 0 | 0 | 0 | 0 | | 274992000 |
| SCHI/CHE | 2012.5 | 2716.1 | 2502.3 | 852.4 | 165.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 8248.4 |
| ALAE | 15079500 | 18122900 | 12210800 | 2898220 | 360409 | 0 | 0 | 0 | 0 | (| 48671900 |
| \$CNP | 221.8 | 359.9 | 411.7 | 357.0 | 175.5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |) 1525.9 |
| AV6. INDEP | 70132 | 55691 | 44953 | 52491 | 49585 | 0 | 0 | 0 | 0 | | 59758 |
| AV6.ALAE | 7493 | 6672 | 4880 | 3400 | 2183 | 0 | 0 | 0 | 0 | (| D 5901 |

NAIC CLOSED WEDICAL LIABILITY CLAINS - ADJUSTED FOR FREQUENCY/SEVERITY TRENDS

REPORT YEAR/CALENDAR YEAR NATRIX FOR LOSSES OF ONE ACCIDENT YEAR

page 2 of 4

Report Year

| Cal.Year | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10+ | Total CY |
|-------------|----------|----------|-------------------|----------|----------|----------|--------------|---------|---------|------------|-----------|
| 6: | | | | | | | | | | | |
| OCNI | 637.0 | 954.0 | 936.5 | 448.5 | 175.6 | 40.5 | 0.0 | 0.0 | 0.0 | 0.0 | 3192.1 |
| INDER | 62810500 | 68Z29600 | 51776400 | 29412800 | 7451200 | 2176270 | 0 | 0 | 0 | 0 | 221857000 |
| OCW1/CWE | 1047.0 | 1611.6 | 1645.2 | 822.7 | 354.8 | 72.2 | 0.0 | 0.0 | 0.0 | 0.0 | 3333.3 |
| ALAL | 8419780 | 13/49100 | 11532300 | 5062490 | 13948/0 | 124000 | v | | 0 | 0 | 42/81100 |
| AUC THREE | 119.7 | 239.3 | 237.7 | 199./ | 100.3 | 87778 | 0.0 | 0.0 | 0.0 | 0.0 | 1027.2 |
| AUC ALAT | 70004 | /1320 | 3328/ | 63300 | 42933 | 33/33 | Ň | v | | 0 | 7707 |
| NAD' NE NE | 0010 | 1116 | 7010 | 0134 | 2721 | 1/1/ | v | v | U | v | //05 |
| 7: | | | | | | | | | | | |
| ACM1 | 312.0 | 457.1 | 501.4 | 288.3 | 159.3 | 91.9 | 35.5 | 0.0 | 0.0 | 0.0 | 1845.5 |
| INDEN | 25695300 | 43347500 | 36378300 | 28472600 | 7354830 | 7186140 | 1840770 | 0 | 0 | 0 | 150276000 |
| SCH1/CHE | 519.9 | 842.0 | 850.2 | 588.1 | 311.2 | 186.9 | 64.2 | 0.0 | 0.0 | 0.0 | 3362.5 |
| ALAE | 5202720 | 7814970 | 7501700 | 5747590 | 1468480 | 847159 | 119039 | 0 | 0 | 0 | 28701700 |
| #CHP | 63.4 | 118.7 | 161.5 | 64.2 | 72.1 | 119.8 | 76.6 | 0.0 | 0.0 | 0.0 | 675.3 |
| AV6.INDEM | 82357 | 94832 | 72553 | 98760 | 46170 | 78195 | 51853 | 0 | 0 | 0 | 81428 |
| AVG. ALAE | 10007 | 9281 | 8823 | 9773 | 4719 | 4533 | 1854 | 0 | 0 | ¢ | 8576 |
| ۰. | | | | | | | | | | | |
| 0: | | 1/0.0 | | | 107.7 | | | 40 1 | | | 1040 4 |
| THUEN | 22553100 | 20194800 | 24585500 | 137.7 | 14556600 | 8577540 | 15314400 | 10.0 | 0.0 | V.V 0 | 177158000 |
| ACKS/CHE | 741 4 | 747 5 | 14303300 508 7 | 19 7 | 17330000 | 178 9 | 13314800 | 52 4 | 0.0 | 0 n | 1917 4 |
| | 1390770 | 1491480 | 5584570 | 2777160 | 1476690 | 1047770 | 561138 | 104096 | 0.0 | 0.0 | 17615900 |
| ACNP | 57 4 | 57 0 | 40.5 | 74 4 | 11000,0 | 32.2 | 78 4 | 54 9 | 0 0 | 0.0 | 394 7 |
| AUS. THOSE | 175777 | 118875 | 99900 | 149674 | 135789 | 71099 | 220354 | 48351 | 0.0 | v.v 0 | 126057 |
| AV6.ALAE | P146 | 10747 | 10978 | 8687 | 8224 | 7687 | 4066 | 2017 | ò | Ō | 9092 |
| в. | | | | | | | | | | | |
| T1 BCHT | Q1 0 | 125 1 | 178 1 | 87 3 | | 76.6 | 4 L L | 45 1 | 17 6 | ^ • | 499 B |
| INDER | 14072400 | 14704000 | 20059500 | 10419100 | 4722270 | 14750000 | 7.0L | 4101200 | 557704 | 0.0 | 000.0 |
| AURITICAE | 10032800 | 208.2 | 744 1 | 197 0 | 108 4 | 104 0 | 222200V | 0000300 | 17 0 | 0.0 | 10103000 |
| AL AF | 2408700 | 2345090 | 4452540 | 2499220 | 1299700 | 799795 | 574145 | 559948 | 17809 | 0.0 | 15126000 |
| #CNP | 17.6 | 27.6 | 46.9 | 22.8 | 16.0 | 21.9 | 50.8 | 61.2 | 31.2 | 0.0 | 296.0 |
| AV6. INDEN | 174457 | 130136 | 203182 | 213277 | 77878 | 212141 | 59107 | 148261 | 43945 | | 159935 |
| AVG.ALAE | 13502 | 11332 | 17617 | 12686 | 11990 | 7615 | 5483 | 5633 | 1001 | 0 | 11870 |
| | | | | | | | | | | | |
| 10: | | | | | | _ | | | | | |
| OCMI | 38.2 | 59.6 | 102.1 | 64.4 | 30.8 | 33.5 | 33.0 | 46.3 | 40.9 | 9.4 | 458.2 |
| INDEM | 6153010 | 10470000 | 25091200 | 11632900 | 7919250 | 9263940 | 6371450 | 7106910 | 6234870 | 550632 | 90794100 |
| UCHI/EWE | 77.4 | 99.1 | 153.7 | 100.6 | 70.3 | 59.8 | 61.3 | 70,1 | 72.5 | 21.1 | 785.9 |
| ALAL | 181007 | 1575940 | 2390640 | 1606360 | 1013300 | 495524 | 477845 | 302084 | 354016 | 791528 | 9792240 |
| SUNP | 7.0 | 12.2 | 30.3 | 17.0 | 2.2 | 0.0 | 9,8 | 7.4 | 30,5 | 7.1 | 125.5 |
| HYD.INUER | 1610/4 | 1/36/1 | 243/51 | 180635 | 25/119 | 276536 | 193074 | 155497 | 152442 | 58578 | 198154 |
| HYD.ALAL | 9910 | 15084 | 10004 | 15968 | 14414 | 8286 | 7795 | 4307 | 4883 | 37513 | 12460 |

NAIC CLOSED MEDICAL LIABILITY CLAINS - ADJUSTED FOR FREQUENCY/SEVERITY TRENDS

REPORT YEAR/CALENDAR YEAR MATRIX FOR LOSSES OF ONE ACCIDENT YEAR

page 3 of 4

| Report Year | | | | | | | | | | | |
|---------------|---------|---------------|-----------------|---------|---------|---------|---------|----------|---------------|----------|----------|
| Cal.Year | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10+ | Total CY |
| 11: | | | | | | | | | | | |
| 40¥1 19550 | 32.4 | 28.4 | 5974420 | 27.5 | 10.6 | 12.8 | 40.6 | 20.3 | 30.8 | 47.0 | 307.9 |
| ACMI/CHE | 47.1 | 55.4 | 3634620 80.9 | 50.7 | 23.5 | 14.9 | 47.9 | 54.2 | 59.2 | 54.5 | 510.3 |
| ALAE | 747815 | 842896 | 1031990 | 859194 | 329762 | 109646 | 626445 | 510024 | 462201 | 185338 | 5705310 |
| ECNP | 10.5 | 12.1 | 10.4 | 4.8 | 0.0 | 7.6 | 5.3 | 2.6 | 17.6 | 46.0 | 116.9 |
| AVG. INDEM | 135384 | 149067 | 115537 | 202396 | 126393 | 59774 | 78518 | 188029 | 48077 | 100982 | 117398 |
| AV6. ALAE | 15877 | 15215 | 12756 | 16947 | 14032 | 7359 | 9226 | 9075 | 7807 | 3401 | 11180 |
| 121 | | | | | | | | | | | |
| ECHI | 8.3 | 24.1 | 24.2 | 15.0 | 12.8 | 16.5 | 13.4 | 28.0 | 28.1 | 57.6 | 227.0 |
| INDER | 1117480 | 6275840 | 4763150 | 2770500 | 2870580 | 403B150 | 1583540 | 2216640 | 5530560 | 6412130 | 37578600 |
| CHI/CHE | 32.7 | 51.7 | 37.0 | 17.0 | 18.1 | 19.3 | 29.8 | 28.3 | 44.1 | 109.9 | 389.9 |
| ALAE | 545520 | 764081 | 426788 | 214047 | 146696 | 109696 | 443067 | 434754 | 1042200 | 13770900 | 17897800 |
| #CNP | 8.0 | 0.0 | 10.8 | 10.7 | 5.2 | 0.0 | 0.0 | 2.7 | 0.0 | 47.1 | 84.5 |
| AVE. INDEM | 134636 | 260408 | 196824 | 173156 | 224264 | 244736 | 118175 | 85255 | 196817 | 111322 | 165544 |
| NVD. HL HL | 10097 | 14//9 | 11222 | 11266 | 8100 | 2984 | 14898 | 10362 | 23633 | 123504 | 43704 |
| 13: | | | | | | | | | | | |
| ICNI | 5.4 | 5.3 | 22.4 | 2.8 | 5.3 | 2.B | 5.2 | 8.9 | 24.B | 57.5 | 140.4 |
| INDEM | 1103330 | 1078500 | 6978730 | 137336 | 560984 | 610383 | 1687220 | 10049400 | 5933220 | 6842250 | 34981300 |
| OCWI/CWE | 8.2 | 16.5 | 30.6 | 5.4 | 13.9 | 2.7 | 13.6 | 8.9 | 24.8 | 98.2 | 222.8 |
| ALAL | 11/986 | 232890 | 551016 | 97325 | 50023 | 29515 | 212639 | 367939 | 349327 | 5/1351 | 2583010 |
| AUC THICH | 2.5 | 2.0 | 711550 | 0.0 | 105044 | 2.3 | 776464 | 8.3 | 13.0 | 110001 | 240155 |
| AVS. ALAE | 14389 | 14296 | 18007 | 18023 | 3599 | 10931 | 15635 | 41341 | 14086 | 5818 | 11593 |
| | | | | | | | | | | | |
| 14: | | | | | | | | | | | |
| THREN | 0.0 | J.8 810084 | 14.4 | 0.0 | 0.0 | 0.0 | 0.0 | 2.8 | 3./ 705700 | 14017800 | 107./ |
| ACHI/CHC | 101201 | 317034 | 1370470 | < 7 | ~ ~ ~ | 513732 | 0.0 | 2130340 | 004L04 | 14012200 | 19423190 |
| ALAE | 27520 | 178291 | 246741 | 26013 | 0.0 | 60947 | 0.0 | 1896 | \$25605 | 805173 | 1872190 |
| ICKP | 5.8 | 0,0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 17.8 | 23.6 |
| AV6. INDEM | 18452 | 87492 | 110451 | 0 | 0 | 111988 | 0 | 762979 | 67612 | 210098 | 177056 |
| AV6. ALAE | 3058 | 20260 | 10728 | 4564 | 0 | 11081 | 0 | 677 | 36756 | 8986 | 11797 |
| 15; | | | | | | | | | | | |
| #C#1 | 5.7 | 3.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 3.1 | 0.0 | 14.B | 26.7 |
| INDEM | 1076180 | 274815 | 0 | 0 | 0 | 0 | 0 | 1544170 | 0 | 1588750 | 4483920 |
| OCWI/CWE | 14.5 | 3.1 | 0.0 | 3.0 | 0.0 | 0.0 | 0.0 | 3.1 | 3.0 | 43.9 | 70.6 |
| ALAE | 221683 | 99595 | 0 | 80071 | 0 | 0 | 0 | 609400 | 29850 | 473084 | 1513680 |
| BUNP | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 3.0 | 0.0 | 0.0 | 5.8 | 8.8 |
| AVE ALAS | 188804 | 88650 | 0 | 0 | 0 | 0 | 0 | 498121 | 0 | 107348 | 167937 |
| HYD.HLHE | 10788 | 52127 | Q | 26690 | 0 | 0 | 0 | 140281 | 4420 | 10776 | 21440 |

NAIC CLOSED MEDICAL LIABILITY CLAIMS - ADJUSTED FOR FREQUENCY/SEVERITY TRENDS

REPORT YEAR/CALENDAR YEAR MATRIX FOR LOSSES OF ONE ACCIDENT YEAR

page 4 of 4

| Report | Year |
|--------|------|
| REDUTL | 1241 |

| Cal.Year | 1 | 2 | 2 | 4 | 5 | 6 | 7 | 8 | 9 | 10+ | Total CY |
|-------------------------------------|--------------------------|-----------|-----------|-----------|----------|----------|----------|----------|----------|----------|------------|
| 16: | | | | | | | | | | | |
| BCWI | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 70.4 | 70.4 |
| INDEM | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 15784300 | 15784300 |
| SCW1/CWE | 0.0 | 0.0 | 0.0 | 3.1 | 0.0 | 3.1 | 0.0 | 0.0 | 0.0 | 80.3 | 86.5 |
| ALAE | 0 | 0 | 0 | 16284 | 0 | 65949 | 0 | 0 | 0 | 1951080 | 2033320 |
| #CHP | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 21.4 | 21.4 |
| AV6. INDEM | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 224209 | 224209 |
| AVG. ALAE | 0 | 0 | 0 | 5253 | 0 | 21274 | 0 | 0 | 0 | 24297 | 23507 |
| Total Reg Year | | | | | | | | | | | |
| 1414 | 15044 4 | 9404 A | 5232.0 | 1451 4 | 657.7 | 366.2 | 253 6 | 201 1 | 147.9 | 325 4 | 30079 5 |
| INDEM | 594814000 | 447507000 | 294498000 | 144500000 | 51343700 | 49433500 | 33319100 | 36878800 | 20119200 | 50139700 | 1722570000 |
| ACHI/CHE | 19679.0 | 15219.8 | 10201.8 | 3392.4 | 1240.0 | 608.2 | 470.4 | 321.4 | 235.7 | 497.5 | 51816.2 |
| ALAE | 90013400 | 86499500 | 57609200 | 22634400 | 7499930 | 3709000 | 2964320 | 2892160 | 2781010 | 18548500 | 295151000 |
| #CHP | 21011.7 | 5742.5 | 2904.9 | 1015.2 | 491.0 | 272.6 | 226.5 | 139.3 | 97.9 | 170.0 | 32066.8 |
| AV5. THDEN | 39537 | 53246 | 56288 | 87491 | 78096 | 134990 | 131384 | 183386 | 140792 | 154086 | 53364 |
| AVG. ALAE | 4586 | 5683 | 5647 | 6672 | 6048 | 6098 | 6302 | 8999 | 11799 | 37283 | 5096 |
| Ratio, av indemnitv total acc | g. to .vr74 | 1.00 | 1.05 | 1.64 | 1.46 | 2.53 | 2.46 | 3.44 | 2.64 | 2.89 | |
| "Secothed avg. inde ratio | • 8. .74 | 1.00 |) 1.20 | 1.40 | 1.60 | 2.00 | 2.35 | 2.70 | 2.845 | i 3.00 | I |
| Ratio, to # claims total acc | stal to :.vr. ,484 | . 250 |) .156 | . 053 | . 021 | .011 | . 008 | . 005 | .004 | . 008 | I |

Source: NAIC Malpractice Claims: Medical Malpractice Closed Claims. 1975-78, Mational Association of Insurance Commissioners. 1980. Adjustments for frequency/severity trends performed by the author on the detail data tape purchased from MAIC. Accordingly, the conclusions drawn from the adjusted data are those of the author and not necessarily those of the MAIC.

MAIC CLOSED MEDICAL LIABILITY CLAINS - ADJUSTED FOR FREQUENCY/SEVERITY TRENDS

REPORT YEAR/CALENDAR YEAR MATRII FOR LOSSES OF ONE ACCIDENT YEAR

Average Indepnity by Calendar Year Components of Report Year Page 1 of 2

| | Report Year | | | | | | | | | | |
|----------------|------------------|-----------------|-----------------|-------------------------|----------------------|-----------------|-----------------|-----------------|------------|-------------------------|-----------|
| Cal. Year | 1 | 2 | 3 | 4 | 5 | 6 | 7 | B | 9 | 10+ | |
| 1: | 7823 | (| / | iverage in Natio, av | ndeenity g. indee | nity to | avg.ind. | ,total r | eport ye | ur | |
| 2: | 28599 | 15238 |) | | | | - | | | | |
| 3: | 41135 | 31717 | 17339 |) | | | | | | | |
| 4. | 1.040 | 47367 | 31403 | 28474 | | | | | | | |
| | 1,463 | 0.890 | 0.558 | 0.325 | | | | | | | |
| 5: | 70132 1.774 | 66691 1.253 | 44953 0.799 | 52491 0,600 | 49585 | Ì | | | | | |
| 6: | 98604 2.494 | 71520 1.343 | 55287 0.982 | 65580 0.750 | 42433 0.543 | 53735 | 2 | | | | |
| 7: | 82357 2.083 | 94832 1.781 | 72553 1.289 | 98760 1.129 | 46170 0.591 | 78195 | 51853 |) | | | |
| 8: | 135373 3.424 | 118875 2.233 | 99900 1.775 | 149624 | 135789 | 99043 0.734 | 220354 | 68351 0.373 |) | | |
| 9: | 174457 | 130136 | 203182 3.610 | 213277 2.438 | 77878 0.997 | 212141 | 59107 0.450 | 148261 | 43945 |) | |
| 10: | 161074 | 175671 3.299 | 245751 4.366 | 180635 | 257119 3.292 | 276536 | 193074 1.470 | 153497 0.837 | 152442 | 58578 | Rel. CY 1 |
| 11: | 135384 | 149067 | 115537 | 202396 | 126392 | 59774 0, 443 | 78518 0.598 | 188029 1.025 | 48099 | 100982 | Rel. CY 2 |
| 12: | 134636 | 260408 | 196824 | 173156 | 224264 | 244736 | 118175 | 85255 | 196817 | 111322 | |
| 13: | 204320 | 203491 | 311550 | 49049 | 105846 | 217994 | 324465 | 1129150 | 239243 | 118996 | |
| 14. | 5.168 | 3.822 | 5.535 | 0.561 | 1.355 | 1.615 | 2.470 | 6.157 | 1.699 | 0.772 | etc. |
| 141 | 0.467 | 1.681 | 1.962 | 0.000 | 0.000 | 0.830 | 0.000 | 4.161 | 0.480 | 1.364 | |
| 15: | 188804 4.775 | 88650 1.665 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 498119 2.716 | 0 0.000 | 1073 48 0.697 | |
| 16: | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 0 0.000 | 224209 1.455 | |
| Total rep.v | 39537 r 1.000 | 53246 1.000 | 56288 1.000 | 87491 1.000 | 78096 1.000 | 134990 | 131384 | 182386 | 140792 | 154086 | |

Appendix B

MAIC CLOSED MEDICAL LIABILITY CLAIMS - ADJUSTED FOR FREQUENCY/SEVERITY TRENDS

REPORT YEAR/CALENDAR YEAR MATRIX FOR LOSSES OF DRE ACCIDENT YEAR

Average Indeamity by Calendar Year Commonents of Report Year Page 2 of 2

Composite Average Indeanity by Relative Calendar Year Cells

Secothed

| relative cal. | year 1 avg. = | 0.233 | .25 |
|---------------|---------------|-------|------|
| relative cal. | year 2 avg. = | 0.669 | .67 |
| relative cal. | vear 3 avg. = | 0.891 | .89 |
| relative cal. | vear 4 avg. = | 1.295 | 1.30 |
| relative cal. | year 5 avg. = | 1.531 | 1.53 |
| relative cal. | year 6 avg. = | 2.125 | 2.13 |
| relative cal. | year 7 avg. * | 2.623 | 2.60 |
| relative cal. | year 8 avg. = | 3.173 | 2.80 |
| relative cal. | vear 9 avg. = | 2.972 | 3.00 |

XYZ HOSPITAL

Assumed Distribution of Claims by Report Year

For Claims Incurred in One Accident Year

| Report Year | (1) Ratio, Number of Claims Reported to Total Accident Year Claims | (2) Ratio, Average Indemnity to Average for Entire Accident Year | (3) Ratio, Amount of Indemnity to Total Accident Year = (1) x (2) |
|----------------|--|--|---|
| 1 | .387 | .73873 | .28589 |
| 2 | .300 | .98498 | .29549 |
| 3 | .201 | 1.18197 | .23758 |
| 4 | .066 | 1.37897 | .09101 |
| 5 | .025 | 1.67446 | .04186 |
| 6 | .012 | 2.16695 | .02600 |
| 7 | .009 | 2.46245 | .02216 |
| | 1.0000 | | 1.000 |

Total

Appendix B

XYZ HOSPITAL

Assumed Distribution of Claims by Calendar Year of Payment

For Claims Incurred in One Report Year

| | (1) | (2) | (3)* |
|------------------|--|---|--|
| Calendar Year | Ratio, Number of Claims Paid to Total Report Year | Ratio, Average Indemnity to Average for Entire Report Year | Ratio, Amount of Indemnity to Total Report Year = (1) x (2) |
| 1 | .25742 | .26416 | .068 |
| 2 | .18505 | .70794 | .131 |
| 3 | .25840 | .94040 | .243 |
| 4 | .13104 | 1.37362 | .180 |
| 5 | .07175 | 1.61664 | .116 |
| 6 | .03110 | 2.25062 | .070 |
| 7 | .02403 | 2.74724 | .066 |
| 8 | .02197 | 2.95857 | .065 |
| 9 | .01924 | 3.16989 | .061 |
| Total | 1.0000 | | 1.000 |
| Total | 1.0000 | | 1.000 |

* Column (1) x Column (2)

Note: Distribution includes all claims from ground up

MEDICAL PROFESSIONAL LIABILITY CLAIM SIZE DISTRIBUTION

TEST OF SAMPLED MEANS AND CV'S, STRATIFIED AND UNSTRATIFIED COMPARED TO DIRECT CALCULATIONS, WITH VARIOUS POLICY LIMITS

Lognormal distribution with Unlimited mean = 100,000

Each sample = 100,000 random trials

| | Unlim. | CV ² =10 | Unlim. | CV ² =20 | Unlim. CV ² =30 | | |
|------------------|-----------------|---------------------|-----------------|---------------------|----------------------------|---------------|--|
| | Limited Mean | Limited CV | Limited Mean | Limited CV | Limited Mean | Limited CV | |
| Limit=50.000 | **** | | | | | | |
| Direct Calc. | 29686 | 0.6361 | 26076 | 0.7511 | 24185 | 0.8173 | |
| Sample, unstrat | 29716 | 0.6352 | 26119 | 0.7502 | 24231 | 0.8164 | |
| Sample, strat. | 29242 | 0.6525 | 25717 | 0.7655 | 23861 | 0.8309 | |
| Limit=100,000 | | | | | | | |
| Direct Calc. | 43878 | 0.8464 | 38297 | 0.9696 | 35416 | 1.0413 | |
| Sample, unstrat. | 43960 | 0.8453 | 38370 | 0.9681 | 35476 | 1.0395 | |
| Sample, strat. | 43245 | 0.8614 | 37723 | 0.9831 | 34868 | 1.0544 | |
| Limit=500.000 | | | | | | | |
| Direct Calc. | 77888 | 1.4981 | 70163 | 1.6635 | 65847 | 1.7595 | |
| Sample, unstrat. | 77742 | 1.4948 | 69996 | 1.6605 | 65667 | 1.7566 | |
| Sample, strat. | 77020 | 1.5166 | 69251 | 1.6829 | 64935 | 1.7796 | |
| Limit=1,000,000 | | | | | | | |
| Direct Calc. | 88071 | 1.8412 | 81451 | 2.0531 | 77437 | 2.1725 | |
| Sample, unstrat. | 87797 | 1.8374 | 81158 | 2.0508 | 77136 | 2.1711 | |
| Sample, strat. | 87386 | 1.8657 | 80648 | 2.0786 | 76594 | 2.1988 | |
| Limit=10,000,000 | | | | | | | |
| Direct Calc. | 99499 | 2.8548 | 98364 | 3.5134 | 97273 | 3.8728 | |
| Sample, unstrat. | 98367 | 2.7628 | 96964 | 3.4215 | 95784 | 3.7946 | |
| Sample, strat. | 99335 | 2.9231 | 98250 | 3.5966 | 97164 | 3.9585 | |
| Limit=25,000,000 | | | | | | | |
| Direct Calc. | 99916 | 3.0473 | 99582 | 3.9620 | 99169 | 4,4987 | |
| Sample, unstrat | 98575 | 2.8535 | 97794 | 3.7435 | 97141 | 4.2810 | |
| Sample, strat | 99619 | 3.0336 | 99436 | 3,9946 | 99192 | 4.5895 | |
| | | | | | | | |

Notes:

The objective of this test is to establish the reliability of the Monte Carlo simulation process in sampling indemnity amounts, both stratified and unstratified. The stratified process samples from distributions for assigned report year/calendar year subsets of an accident year. Prior to each RY/CY sampling, the report year and calendar year are selected randomly from RY/CY distributions. For the selected subset, the mean has been adjusted by report year and calendar year severity relativity factors and the variance has been adjusted downward from the variance for the entire accident year, so that the total sample variance for all subsets combined will approximate that of the overall accident year. The unstratified sampling bypasses the partitioning of the accident year into report year/calendar cells and simply samples from the total accident year distribution, using the accident year wear and overall variance.

NAIC CLOSED CLAIM STUDY Regression of Avg. Expense Versus Avg. Indemnity

| Average | Y = | | |
|-----------|--------------|--------------------|----------------|
| Indemnity | Average ALAE | Weight | |
| Bracket | In Bracket | (Number of Claims) | Computed Y |
| 51 | 220 | 359.3 | 259.2 |
| 115 | 243 | 103.2 | 384.0 |
| 154 | 166 | 105.2 | J07.3 AAA 3 |
| 205 | 392 | 145.5 | 509.9 |
| 279 | 526 | 242.8 | 591.9 |
| 372 | 412 | 292.0 | 679.5 |
| 489 | 745 | 411.8 | 776.0 |
| 654 | 705 | 581.2 | 892.6 |
| 870 | 926 | 828 3 | 1024.6 |
| 1150 | 1387 | 1015.0 | 1172.5 |
| 1565 | 1268 | 1170.2 | 1360.5 |
| 2071 | 1892 | 1477.1 | 1557.7 |
| 2786 | 1878 | 1499.5 | 1797.6 |
| 3699 | 2191 | 1640.8 | 2061.3 |
| 4933 | 2598 | 2180.2 | 2368.8 |
| 6562 | 3177 | 2071.1 | 2718.7 |
| 8703 | 2982 | 1884.5 | 3116.1 |
| 11512 | 3544 | 2029.0 | 3566.7 |
| 15453 | 5139 | 1906.4 | 4111.7 |
| 20526 | 4379 | 1848.9 | 4715.8 |
| 27428 | 5311 | 1564.3 | 5424.5 |
| 36706 | 6031 | 1448.2 | 6244.1 |
| 48937 | 6982 | 1340.3 | 7174.5 |
| 65342 | 7879 | 1171.7 | 8249.5 |
| 86099 | 7653 | 926.5 | 9425.2 |
| 114706 | 9411 | 917.8 | 10825.7 |
| 153844 | 13511 | 746.2 | 12474.7 |
| 204947 | 14788 | 722.3 | 14328.0 |
| 273289 | 13324 | 456.1 | 16464.3 |
| 362444 | 17890 | 402.6 | 18869.6 |
| 487164 | 20104 | 247.9 | 21766.5 |
| 648598 | 36075 | 199.7 | 24993.1 |
| 869532 | 18601 | 112.6 | 28794.1 |
| 1141890 | 24485 | 93.3 | 32843.9 |
| 1473140 | 34618 | 34.0 | 37143.0 |
| 2010450 | 28763 | 15.1 | 43161.8 |
| 2773930 | 43677 | 22.4 | 50421.5 |
| 3919530 | 42060 | 4.9 | 59583.4 |

B = 0.48294500 A= 3.66331000

X =

EQUATION: $Log(Y) = A+B^*LOG(X)$





Appendix E

DESCRIPTION OF MONTE CARLO MODEL TO GENERATE PROBABILITY DISTRIBUTION OF REQUIRED SELF INSURANCE CONTRIBUTION

I. Miscellaneous Assumptions, Input parameters, and Distributions

(a) Report year distribution of accident year losses, with relative severity factors by report year - see Appendix B, page 7.

(b) Calendar year distribution of report year losses, with relative severity factors by calendar year - see Appendix B, page 8.

(c) Distribution of claims (indemnity) by size - see Appendix A, page 6.

Note: the basic distribution applies to all claims of one accident year, using the overall mean value for the entire year. The model stratifies the claims first in 63 report year/calendar year cells, each with a modified mean value from (a) and (b) above. Accordingly the variance applicable to each cell has been reduced from the overall variance for random selection purposes, such that the combined sample variance over all 63 cells will approximate the entire accident year distribution.

(d) Average unlimited indemnity by year - used as the parameter in the size of loss distribution for each accident year:

year 1: \$200,000 year 2: \$225,000

(e) Average claim expense by year. Based on the functional relationship derived between expected average ALAE and the sample indemnity value (see Appendix D), the sample ALAE is SELECTED from a distribution the *mean* of which is determined as a function of the sample indemnity. The starting values for the average ALAE for the entire accident year, over all indemnity values, are:

year 1: \$12,000 year 2: \$13,000

(f) Total *expected* number of claims by accident year, including claims closed with indemnity (CWI) and claims closed with expense only (CWE):

year I: 20

Appendix E

year 2: 21 (claims closed with no payment are excluded)

(g) Percentages for claims disposed, all years: CWI: 60% CWE: 40%

(h) Self insured retention, all years: per claim: \$1,000,000 annual aggregate: \$5,000,000

(i) Parameter variance (uncertainty factor). These values are expressed in relation to the expected population frequency and severity, which are input. In this case study we are assuming a "standard error" of .15 for frequency and .18 for severity, both expressed relative to the expected values.

II. The Monte Carlo Simulation Process (in Pseudo Code)

Accumulators set up:

(1) Aggregate retained loss brackets (31) for all trials combined (probability distribution), less current assets. One accumulator for counts (number of trials falling into bracket) and another for total loss dollars.

(2) Total retained by policy year. To be compared with aggregate SIR. Reinitialized for each trial.

Input:

(1) Uncertainty factors for population mean frequency and severity (parameter variance).

(2) Retentions by policy year and index amount (if applicable). Per claim and aggregate

(3) Current assets

(4) Number of claims open for all prior years and assumed average indemnity for these open claims by year.

(5) Assumed average unlimited indemnity, claim frequency, and average ALAE for next (target) year.

(6) Assumed rate of return for present value discounting

(7) Number of trials to sample

(8) Present (target) year of coverage [Y1]. For initial funding Y1=1.

(9) Percentage of claims closed with expense only (CWE). Note: claims closed with no payment ignored.

** Main trial loop

For each trial

If Y1= 1 then skip to Routine for current year

For each prior year 1 to Y1-1

If Number of claims open for year = 0 then skip to [next year]

For each open claim for year

(1) Determine year reported (from actual, if available, else by randomizing from report year distr.)

(2) Establish mean indemnity for year from input values for open claims for that year.

(3) SELECT calendar year paid, relative to report year, and modify mean indemnity by calendar year severity factor

(4) Establish retention per claim applicable to calendar year, including index, if applicable.

(5) SELECT mode of closure (CWI or CWE). If CWE, SELECT ALAE amount only and then skip to next claim.

(6) SELECT gross (unlimited) indemnity from size of loss distribution, the mean of which was adjusted by calendar year severity factors from (3).

(7) Limit indemnity to per-claim retention for that year, as necessary.

(8) If claim burns through remaining annual aggregate SIR, then limit claim accordingly.

(9) Based on indemnity amount, adjust *expected* ALAE, and SELECT sample gross ALAE from distribution.

(10) Add retained indemnity and pro-rata retained ALAE to retained accumulator for calendar year of payment selected in (3).

(11) Add retained indemnity to the aggregate losses for that year.

Next claim

Next year

** Now do loop for prior year's IBNR's and/or current year's losses

For each year 1 to Y1

SELECT "universe" mean frequency and severity, drawing from expected and using the parameter variances (input).

SELECT sample number of claims for year, drawing from "universe". If expected

number < 15, use Poisson, else use normal distribution.

For each claim

(1) Determine year reported (from report year distr.). If claim already reported (report year < Y1), then branch to next claim. Thus, IBNR claims from prior years are included.

(2) Establish mean indemnity from input value for that year and modify with report year severity factor.

(3) SELECT calendar year paid, relative to report year, and further modify mean indemnity by calendar year severity factor.

(4) Establish retention per claim applicable to calendar year, including index, if applicable.

(5) SELECT mode of closure (CWI or CWE). If CWE, SELECT ALAE amount only and then skip to next claim.

(6) SELECT gross (unlimited) indemnity from size of loss distribution, the mean of which was adjusted by report year and calendar year severity factors from (2) and (3).

(7) Limit indemnity to per-claim retention for that year, as necessary.

(8) If claim burns through remaining annual aggregate SIR, then limit claim accordingly.

(9) Based on indemnity amount, adjust *expected* ALAE, and SELECT sample gross ALAE from distribution.

(10) Add retained indemnity and pro-rata retained ALAE to retained accumulator for the calendar year of payment from (3).

(11) Add retained indemnity to the aggregate losses for that year.

Next claim

Next year

** Tally section for this trial

Determine present value of all retained losses from accumulator by calendar year and deduct current assets to get required funding for this trial (if < 0 then make it 0).

Determine which one of the 31 brackets of aggregate retained losses this trial falls in and bump the corresponding accumulators for counts (1) and total retained dollars.

Reinitialize all accumulators, except aggregate loss brackets.

Next trial

Print out probability distribution

NOTE: Each time the word "SELECT" is used in the above process, the program randomly samples from the appropriate distribution described in Part I, using a random number generator.

```
SELERISE
            SUN, FEB 26 1989
                                     13:23:56
Report year distribution:
RY Cum.
           Re).
   counts Sev.
-- ----- -----
1 .38700 .73873
2 .58700
           .98498
3 .88800 1.18197
4 .95400 1.37897
5 .97900 1.67446
6 .99100 2.16595
7 1.00000 2.46245
Cal. Year distribution:
CY Cum.
            Rel.
   Counts
             Sev.
-- ---- -----
1 .25742 .26415
          .70794
2 .44247
3 .70087
           .94040
4 .83191 1.37362
5 .90366 1.81664
6 .93476 2.25062
1 .95879 2.74724
8 .98075 2.95857
9 1.00000 3.16989
INPUT RATE OF RETURN (X.XX) 71.07
51=.99999999999999
                           [mean of ry*cy severities]
S2=1.632776340059
                            [second moment of ry*cy severities]
NET S2=.4902818419985
                            [log(S2)]
ADJUSTED S=1.715722985358 [ sqrt[log(31) - log(S2)] ]
INPUT NO. TRIALS ? 10000
INPUT PERCENT CLAIMS CLOSED EXPENSE ONLY 2.4
INPUT UNLIMITED SEVERITY TREND (X.XX) ?1.12
INPUT ALAE TREND (x.xx) ?1.08
INPUT FREQUENCY TREND (X.XX) 21.04
INPUT CLIENT NAME
2XYZ HOSPITAL
INPUT PRESENT YEAR OF COVERAGE
21
INPUT LIMIT PER CLAIM FOR THIS YEAR FORWARD
21000000
INPUT AGGREGATE LIMIT FOR THIS YEAR FORWARD
25000000
INPUT AVERAGE INDEMNITY WITH NO LIMIT FOR THIS YEAR
2200000
AVERAGE ALLOCATED CLAIMS EXPENSE FIRST YEAR 12000
ALAE ADJ. FACTOR = .65711657248
INPUT EXPECTED TOTAL CLAIM COUNT FOR THIS YEAR
220
INPUT NET EXPECTED RETAINED LOSSES FOR THIS YEAR
21000000
UNCERTAINTY FACTORS FOR POPULATION MEAN FREQUENCY AND SEVERITY (.XX, .XX)7.15,.18
STARTING
```

RUN

XYZ HOSPITAL

ANNUAL BREAKEVEN CONTRIBUTION FOR SELF-INSURANCE TRUST

| INTERVAL | NUMBER OF | CUMULATIVE | | CUMULATIVE |
|-----------|-----------|---------------|--------------|--------------|
| END POINT | TRIALS | NUMBER TRIALS | TOTAL AMOUNT | TOTAL AMOUNT |
| | | | | |
| 0 | 0 | 0 | 0 | 0 |
| 100000 | 20 | 20 | 1567150 | 1567150 |
| 117210 | 9 | 29 | 988079 | 2555229 |
| 137382 | 23 | 52 | 2979852 | 5535081 |
| 161026 | 31 | 83 | 4660393 | 10195474 |
| 188739 | 39 | 122 | 5842149 | 17037623 |
| 221222 | 71 | 193 | 14544679 | 31582303 |
| 259294 | 98 | 291 | 23550079 | 55132382 |
| 303920 | 128 | 419 | 36079809 | 91212191 |
| 356225 | 202 | 621 | 66547061 | 157759252 |
| 417532 | 237 | 858 | 91816354 | 249575605 |
| 489390 | 324 | 1182 | 146497576 | 396073181 |
| 573615 | 384 | 1566 | 204715603 | 600788784 |
| 672336 | 512 | 2078 | 318352411 | 919141195 |
| 788045 | 547 | 2725 | 473392789 | 1392533984 |
| 923671 | 770 | 3495 | 659660990 | 2052194975 |
| 1082637 | 941 | 4436 | 943185973 | 2995380948 |
| 1268961 | 965 | 5401 | 1131134839 | 4126515787 |
| 1487352 | 1048 | 5449 | 1441512233 | 5568128020 |
| 1743329 | 1004 | 7453 | 1614047558 | 7182175578 |
| 2043360 | 957 | 8410 | 1806550499 | 8988726077 |
| 2395027 | 591 | 9101 | 1529247998 | 10517974074 |
| 2807216 | 479 | 9580 | 1238595136 | 11756569210 |
| 3290345 | 248 | 9826 | 737560999 | 12494130209 |
| 3856621 | 133 | 9959 | 465756993 | 12959887202 |
| 4520354 | 40 | \$999 | 152542492 | 13122529594 |
| 5298317 | 1 | 10000 | 4539766 | 13127069460 |
| 5210170 | 0 | 10000 | 0 | 13127069460 |
| 7278954 | C | 10000 | 0 | 13127069460 |
| 8531679 | 0 | 10000 | 0 | 13127069460 |
| 10000000 | 0 | 10000 | 0 | 13127069460 |

Interpolated values for selected confidence levels: (geometric interpolation)

| 2340077 | 9000 |
|---------|------|
| 2733743 | 9500 |
| 3594291 | 9900 |

Appendix F > RLIN 15:28:11 SUN, FE8 26 1989 SELFRIS8 Report year distribution: Re). RY Cum. counts Sev. -- ----- -----1 .38700 .73873 2 .68700 .98498 3 .88800 1.18197 4 .95400 1.37897 5 .97900 1.67445 6 .99100 2.16695 7 1.00000 2.46245 Cal. Year distribution: CY Cua. Rel. Counts Sev. -- -----1 .25742 .25418 2 .44247 .70794 3 .70087 .94040 4 .83191 1.37382 5 .90365 1.51564 8 .93476 2.25082 7 .95879 2.74724 8 .98076 2.95857 9 1.00000 3,15989 INPUT RATE OF RETURN (X.XX) 21.07 51#.9999999999999 (mean of ry*cy severities) [second moment of ry*cy severities] 52=1.532778340059 NET S2=.4902818419985 [log(\$2)] ADJUSTED S=1.715722985358 [sqrt[log(31) - log(S2)]] INPUT NO. TRIALS ? 10000 INPUT PERCENT CLAIMS CLOSED EXPENSE ONLY ?.4 INPUT UNLIMITED SEVERITY TREND (X.XX) 71.12 INPUT ALAE TREND (x.xx) ?1.08 INPUT FREQUENCY TREND (X.XX) 21.04 INPUT CLIENT NAME 2XYZ HOSPITAL INPUT PRESENT YEAR OF COVERAGE 22 INPUT PRESENT FUND ASSETS 22950000 INPUT NUMBER CLAIMS OUTSTANDING FOR EACH OF THE FIRST 1 YEARS OF COVERAGE YEAR 1 27 INPUT ULTIMATE AVERAGE (UNLIMITED) INDEWNITY RESERVE FOR OPEN CLAIM FOR EACH OF THE FIRST 1 YEARS OF COVERAGE YEAR 1 2130000 INPUT LIMIT PER CLAIM FOR EACH OF THE FIRST 1 YEARS OF COVERAGE YEAR 1 71000000 INPUT TARGET AGGREGATE EACH OF THE FIRST IYEARS OF COVERAGE YEAR 1 24960000 INPUT LIMIT PER CLAIM FOR THIS YEAR FORWARD 71000000 INPUT AGGREGATE LINIT FOR THIS YEAR FORWARD 25000000 INPUT AVERAGE INDERNITY WITH NO LIMIT FOR THIS YEAR 2225000 AVERAGE ALLOCATED CLAINS EXPENSE FIRST YEAR 13000 ALAE ADJ. FACTOR =.6327789216474 INPUT EXPECTED TOTAL CLAIM COUNT FOR THIS YEAR 221 INPUT NET EXPECTED RETAINED LOSSES FOR THIS YEAR 21200000 UNCERTAINTY FACTORS FOR POPULATION MEAN FREQUENCY AND SEVERITY (.XX, .XX)?. 15...18 STARTING

XYZ HOSPITAL

ANNUAL BREAKEVEN CONTRIBUTION FOR SELF-INSURANCE TRUST

| INTERVAL END POINT | NUMBER OF TRIALS | CUMULATIVE NUMBER TRIALS | TOTAL AMOUNT | CUMULATIVE TOTAL AMOUNT |
|-----------------------|---------------------|-----------------------------|--------------|----------------------------|
| ****** | | | | |
| 0 | 5583 | 5583 | 0 | 0 |
| 120000 | 414 | 5997 | 24648222 | 24548222 |
| 140652 | 91 | 5088 | 11830798 | 36479020 |
| 164859 | 81 | \$169 | 12307073 | 48786092 |
| 193231 | 76 | 6245 | 13571310 | 62357402 |
| 225487 | 118 | \$353 | 24705475 | 87053878 |
| 255466 | 133 | 6496 | 32901574 | 119965452 |
| 311153 | 138 | 5634 | 39861548 | 159827100 |
| 364703 | 151 | 6785 | 50702085 | 210529184 |
| 427470 | 158 | 5943 | 62734582 | 273253867 |
| 501038 | 189 | 7132 | 88302392 | 361566259 |
| 587268 | 235 | 7357 | 127689223 | 489255482 |
| 688338 | 251 | 7618 | 159438597 | 648694178 |
| 805803 | 281 | 7899 | 209627405 | 858321584 |
| 945656 | 293 | 8192 | 257166219 | 1115487803 |
| 1108405 | 289 | 8481 | 296198263 | 1411586055 |
| 1299164 | 321 | 8802 | 386577962 | 1798264028 |
| 1522753 | 274 | 9075 | 384974193 | 2183238221 |
| 1784823 | 281 | 9357 | 462473361 | 2645711581 |
| 2091995 | 233 | 9590 | 449359285 | 3095070867 |
| 2452032 | 185 | 9775 | 418087511 | 3513158478 |
| 2874032 | 109 | 9884 | 286821719 | 3799980197 |
| 3368660 | 70 | 9954 | 215857101 | 4015837298 |
| 3948414 | 30 | 9984 | 107482515 | 4123319913 |
| 4627945 | 16 | 10000 | 68141591 | 4191461605 |
| 5424425 | 0 | 10000 | 0 | 4191461605 |
| 6357980 | 0 | 10000 | 0 | 4191461605 |
| 7452203 | 0 | 10000 | 0 | 4191461605 |
| 8734745 | 0 | 10000 | 0 | 4191461605 |
| 10238015 | 0 | 10000 | 0 | 4191461605 |
| 12000000 | 0 | 10000 | 0 | 4191451605 |

Interpolated values for selected confidence levels: (geometric interpolation)

| 1457137 | 9000 |
|---------|------|
| 1987531 | 9500 |
| 2980257 | 9900 |







