

The Return of the Bell Double-Croctic

by John P. Robertson

Allan Bell has produced another fine double-croctic for *The Actuarial Re-*

view. On this page, the first column of the solutions to the clues gives the

name of the author and the title of the work.

A. CAS President and actuarial philosopher who wrote the classic paper "Experience Rating Plan Credibilities"	122	30	150	101	6	51	89	188	
B. City famed for the Temple of Artemis, one of the Seven Wonders of the Ancient World	178	61	153	19	131	93	47		
C. Grooved, furrowed	90	75	121	148	104	53			
D. Chief Actuary of the Social Security Administration (1975-1978) and author of <i>The Coming Revolution in Social Security</i>	172	109	70	128	44	21	151	87	5
E. 1923 Nobel Prize recipient who devoted his career to the development of Irish national literature	141	52	28	72	107				
F. Accounting term for premium, receipts, and investment income less payments for underwriting expenses, loss adjustment expenses, and losses (two words)	157	137	7	59	112	27	173	81	
G. Cassowaries, emus, kiwis, and ostriches	23	45	177	130	66	91	152		
H. Only survivor of the <i>Pequod</i>	82	179	36	3	147	60	123		
I. The product of x, y, and z, given $x=y+z+1$, $3y=x+z+1$, and $4z=x+y+1$	43	63	187	103	26	2	138	161	120
J. Villain who manipulates Desdemona's husband into murdering her	106	169	144	22					84
K. Perennial composite herb with hoof-shaped leaves used at one time in cough medicine	125	57	146	33	185	168	100	17	78
L. One of two or more forms of an element that has the same atomic number but a different atomic weight	1	38	149	96	62	181	126		
M. Fire and casualty company that has the second largest premium volume among stock insurers (two words)	184	58	164	13	80	99	37	142	116
N. "The _____ and Destiny of the CAS," 1991 Presidential Address of Charles Bryan	86	124	29	145	182	9	102	163	67
O. Side of a coin that bears the main design	97	140	170	40	118	12	64		
P. Class of property for which theft losses are limited to \$2,000 under standard homeowners forms	88	54	127	183	160	20	110	35	
Q. Pitcher who earned 234 of his 286 wins while playing for Philadelphia (ME.)	98	133	162	41	175	8	71		
R. River (or strait) whose features include Flushing Bay, Hell Gate, and Roosevelt Island	34	117	165	56					
S. Broadway role played by Julie Andrews opposite Richard Burton and Robert Goulet	92	180	115	55	11	129	77	31	159
T. "_____ Loss Development Factors," 1994 Woodward-Fondiller Prize paper by Daniel M. Murphy	69	134	39	186	156	83	15	108	
U. Adjective describing the point of the nadir on the celestial sphere	158	49	105	24	135	76			
V. A procedure for solving a mathematical problem in a finite number of steps that frequently involves repetition of an operation	176	94	25	154	50	73	10	114	136
W. The amount of vertical displacement produced by a geological fault; a light coverlet	113	79	65	171	155				
X. Eighth century B.C. Hebrew prophet whose theology emphasizes Yahweh's kingship and His holiness	166	68	95	132	32	14			
Y. Period when charges are less expensive because usage is lower	85	48	174	16	143	4	119		
Z. English mathematician (1642-1727) who discovered integral calculus	167	139	18	74	111	42			

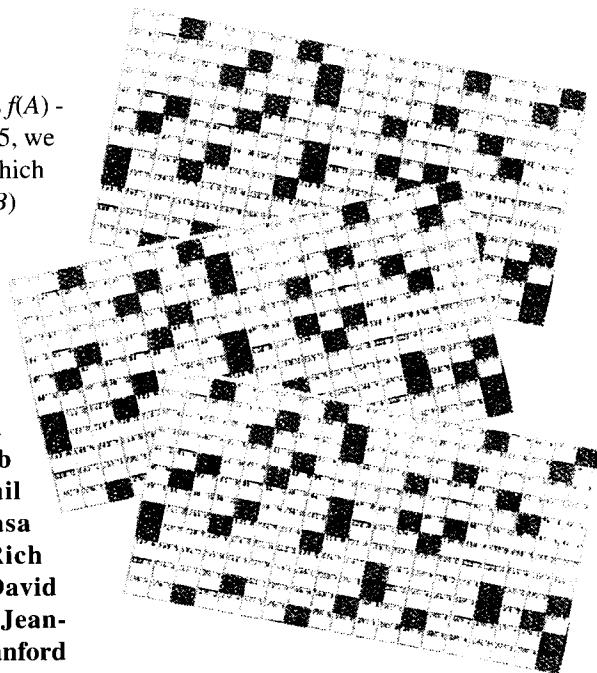
Once solved, the diagram below will contain a quotation relevant to the insurance business. The quotation is used with permission (we'll divulge whose permission in the next issue).

Four Degrees of Matthew Rodermund

The puzzle was to find a fourth degree polynomial, $f(x) = ax^4 + bx^3 + cx^2 + dx + e$, with integer coefficients, so that $f(25) = 13$ and $f(1974) = 1999$, or show that no such polynomial exists. **Tom Struppeck's** solution is essentially as follows. Suppose there were such a polynomial. For any two values of x , say A and B , we can write $f(A) - f(B) = a(A^4 - B^4) + b(A^3 - B^3) + c(A^2 - B^2) + d(A - B)$. The factor $A - B$ divides each of $A^4 - B^4$, $A^3 - B^3$, $A^2 - B^2$,

and $A - B$, so $A - B$ evenly divides $f(A) - f(B)$. Taking $A = 1974$ and $B = 25$, we have $A - B = 1974 - 25 = 1949$, which does not evenly divide $f(A) - f(B) = 1999 - 13 = 1986$. So there can be no such polynomial. This proof clearly can be extended to polynomials of any degree.

Solutions were also sent in by Nilgun Akgul, **David Atkinson, Walter Fransen, Bob Hallstrom, Eric Halpern, Phil Heckman, Mike Hobart, Rasa McKean, Claude Nadeau, Rich Newell, Randy Nordquist, David Oakden, Stephen Riihimaki, Jean-Denis Roy, Matthew Schutz, Sanford R. Squires, and David Uhland.** ■



1 L	2 I		3 H	4 Y	5 D	6 A		7 F	8 Q	9 N	10 V	11 S	12 O		13 M	14 X	15 T	
16 Y	17 K	18 Z	19 B	20 P		21 D	22 J		23 G	24 U	25 V	26 I	27 F	28 E	29 N	30 A		31 S
32 X	33 K	34 R	35 P		36 H	37 M	38 L		39 T	40 O	41 Q	42 Z		43 I	44 D	45 G	46 N	47 B
48 Y	49 U	50 V	51 A	52 E	53 C		54 P	55 S	56 R	57 K		58 M	59 F	60 H		61 B	62 L	63 I
64 O	65 W		66 G	67 N		68 X	69 T	70 D	71 Q	72 E	73 V	74 Z	75 C	76 U	77 S		78 K	79 W
80 M		81 F	82 H	83 T	84 I	85 Y	86 N		87 D	88 P		89 A		90 C	91 G	92 S	93 B	94 V
95 X	96 L	97 O	98 Q		99 M	100 K	101 A		102 N	103 I	104 C		105 U	106 J	107 E	108 T	109 D	110 P
	111 Z	112 F		113 W	114 V	115 S		116 M	117 R	118 O	119 Y	120 I	121 C	122 A	123 H	124 N	125 K	126 L
	127 P	128 D	129 S	130 G	131 B	132 X	133 Q	134 T	135 U		136 V	137 F	138 I	139 Z		140 O	141 E	
142 M	143 Y	144 J	145 N	146 K	147 H	148 C	149 L	150 A	151 D		152 G	153 B	154 V	155 W		156 T		157 F
158 U	159 S	160 P	161 I		162 Q	163 N	164 M	165 R		166 X	167 Z		168 K	169 J	170 O	171 W	172 D	
173 F	174 Y		175 Q	176 V	177 G	178 B		179 H	180 S	181 L	182 N	183 P	184 M	185 K	186 T	187 I	188 A	