

A Robust Bayesian Loss Development Model

Concept and Implementation in R

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**Annual Meeting
Casualty Actuarial Society
Boston, Mass.
November 15-18, 2009**

Overview

- Robust Loss Development Using MCMC
 - Main features of the model
 - Application of the model to two widely studied loss triangles
- R package *lossDev*
 - System requirements
 - License information
 - Demonstration
 - Installation
 - The *lossDev* vignette

Robust Loss Development Using MCMC

The paper of the same title is available for download at
<http://ssrn.com/author=101739>

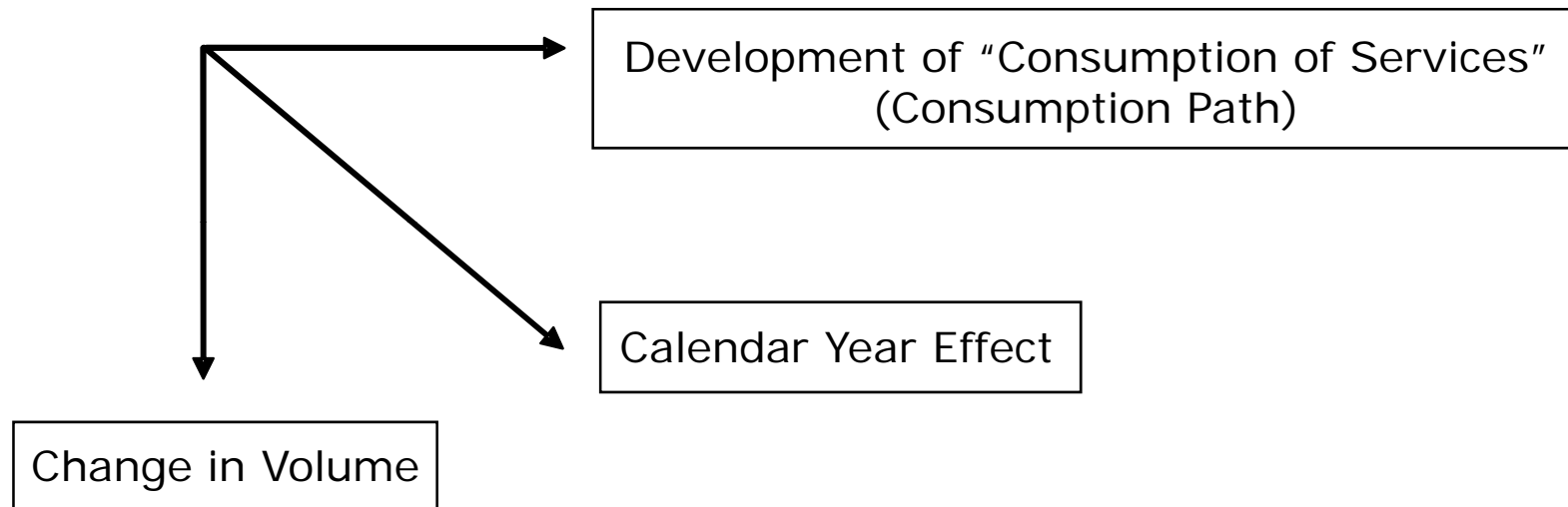
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Time Series Methodology

- Times series models of loss development have been pioneered by Kremer [3], Verrall [4, 5], Zehnwirth [6], Barnett and Zehnwirth [1], and de Jong [2]
- These times series approaches attempt to model explicitly the process that generates the data
- Unlike models that mechanistically fit to data, these time series models can not only be judged *ex post* by how well they are able to replicate the data but can also be evaluated *ex ante* by the adequacy of the equations that describe the data-generating process
 - Ex post analysis is largely confined to checking on how well the residuals agree with the distributional assumptions
- Laying out the equations for the data-generating process adds another layer of scrutiny to these models
- Estimating the equations of the data-generating process facilitates learning about the nature of loss triangles

Triangle Dynamics



For this architecture of triangle analysis, see Barnett and Zehnwirth [1]

Main Features of the Statistical Model (1/2)

- The model is Bayesian and estimated using MCMC (Markov Chain Monte Carlo simulation)
- The model fits to the (natural) logarithms of incremental payments
 - Negative payments or payments at zero amounts are coded as missing values
- The model uses a skewed Student- t likelihood with endogenous degrees of freedom
- The scale parameter of the t -distribution is allowed to vary in development time
- A Bernoulli distribution (the parameter of which varies on a Gompertz curve in development time) accounts for the variation in the probability of observing a payment at zero amount

Main Features of the Statistical Model (2/2)

- The calendar year effect is modeled as a normal distribution around an expert prior for the rate of inflation
 - For General Liability triangles, a suitable expert prior for the calendar year effect may be the CPI (Consumer Price Index) rate of inflation
 - For Auto Bodily Injury Liability triangles, the Medical Care component of the CPI (M-CPI, for short) may serve as an expert prior
- A first-order autoregressive process of the error the calendar year effect is optional and used for both triangles studied here
- There is a changepoint version of the model that allows for a structural break in the consumption path
 - An interval of exposure years has to be supplied—the model determines the changepoint endogenously within this interval

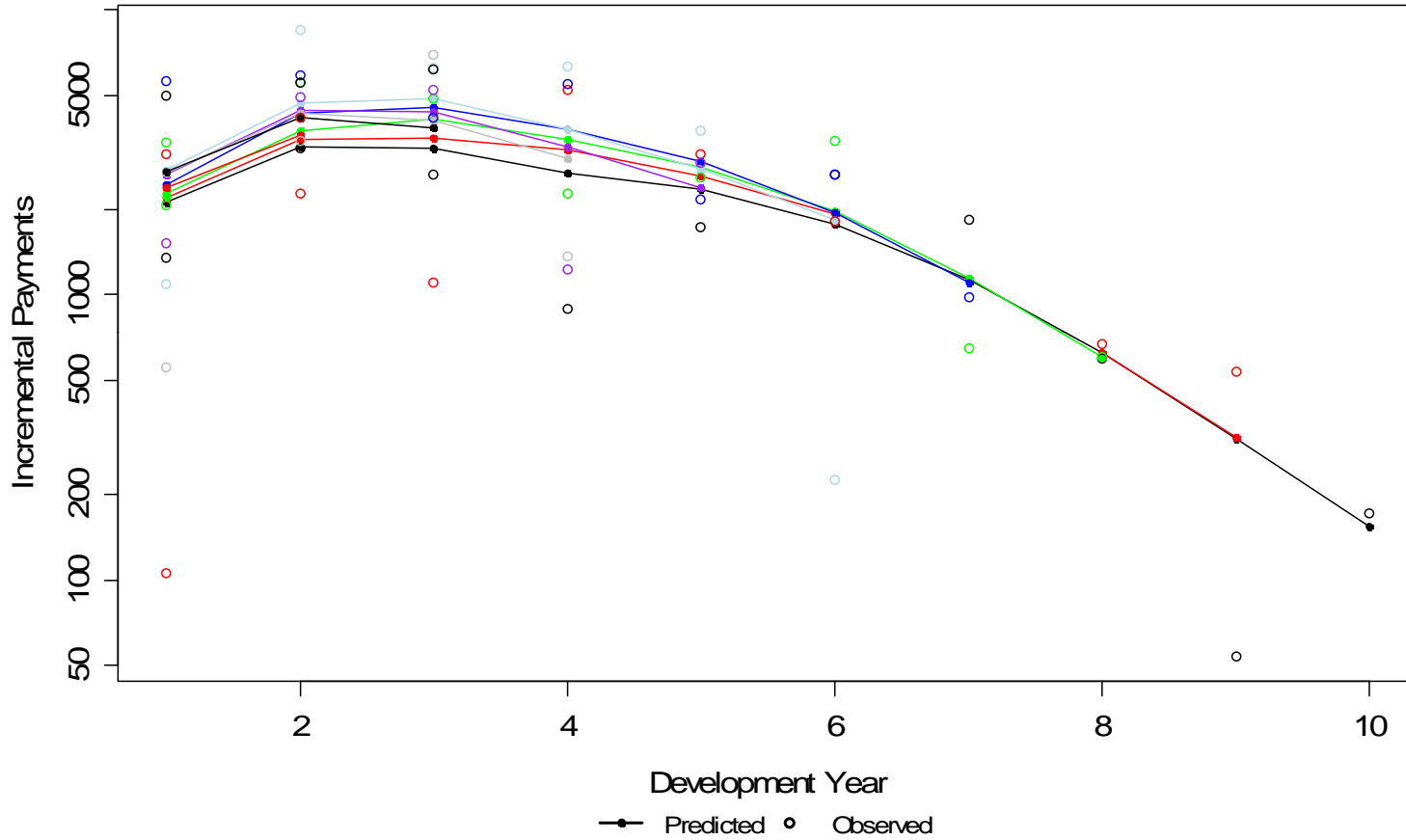
A General Liability Triangle

- Annual Incremental Incurred Loss Triangle of Automatic Facultative Business in General Liability (Excluding Asbestos & Environmental)

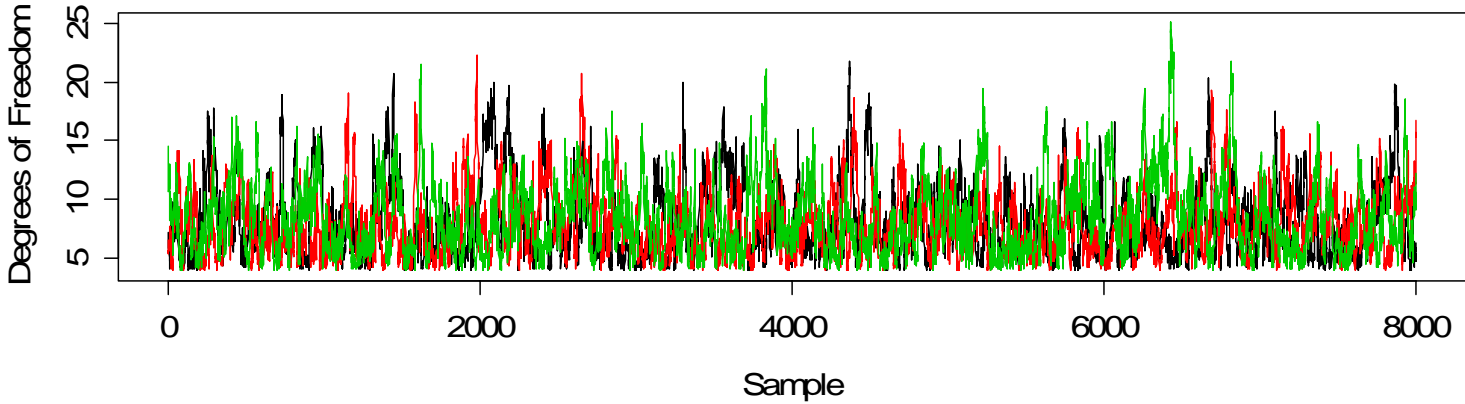
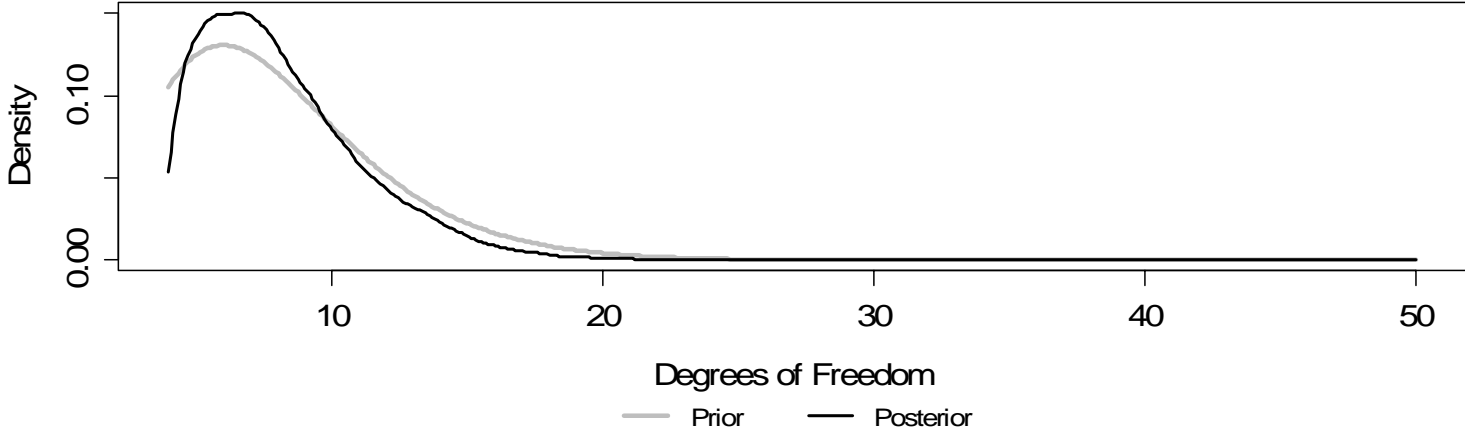
Year	1	2	3	4	5	6	7	8	9	10
1981	5,012	3,257	2,638	898	1,734	2,642	1,828	599	54	172
1982	106	4,179	1,111	5,270	3,116	1,817	-103	673	535	
1983	3,410	5,582	4,881	2,268	2,594	3,479	649	603		
1984	5,655	5,900	4,211	5,500	2,159	2,658	984			
1985	1,092	8,473	6,271	6,333	3,786	225				
1986	1,513	4,932	5,257	1,233	2,917					
1987	557	3,463	6,926	1,368						
1988	1,351	5,596	6,165							
1989	3,133	2,262								
1990	2,063									

Data source: Mack, Thomas, "Which Stochastic Model is Underlying the Chain Ladder Method," *Casualty Actuarial Society Forum*, Fall 1995, pp. 229-240, <http://www.casact.org/pubs/forum/95fforum/95ff229.pdf>

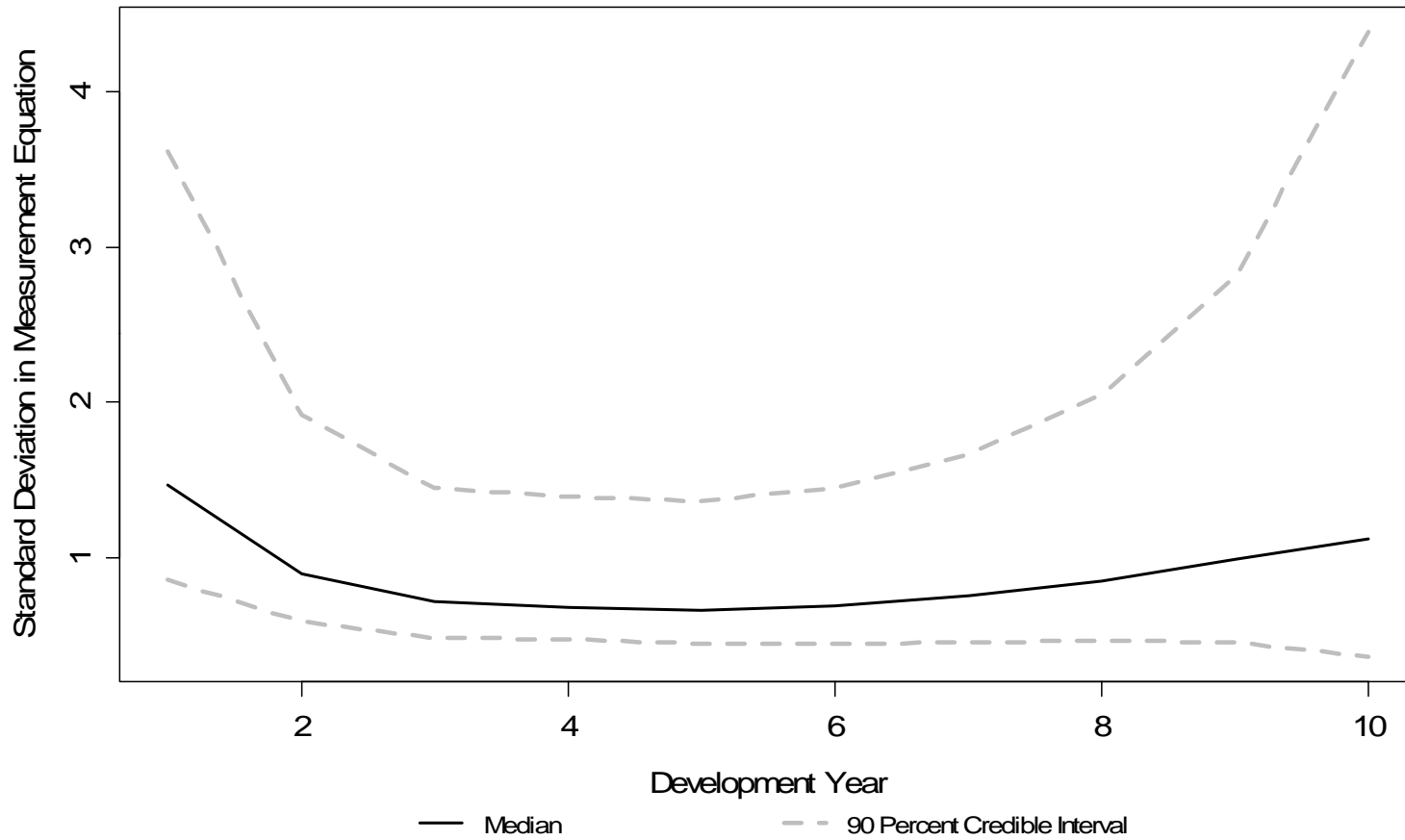
Log Incremental Payments



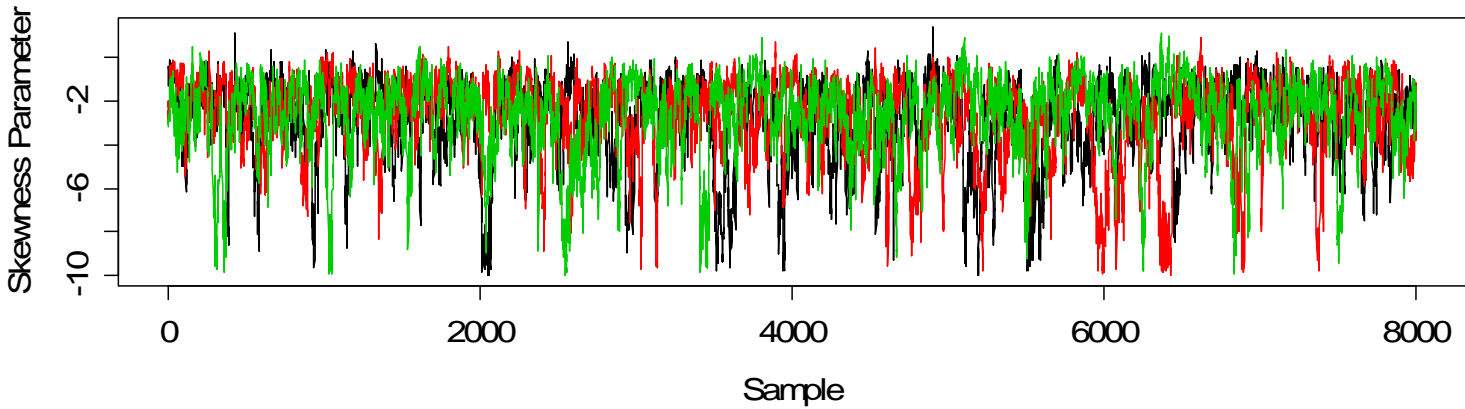
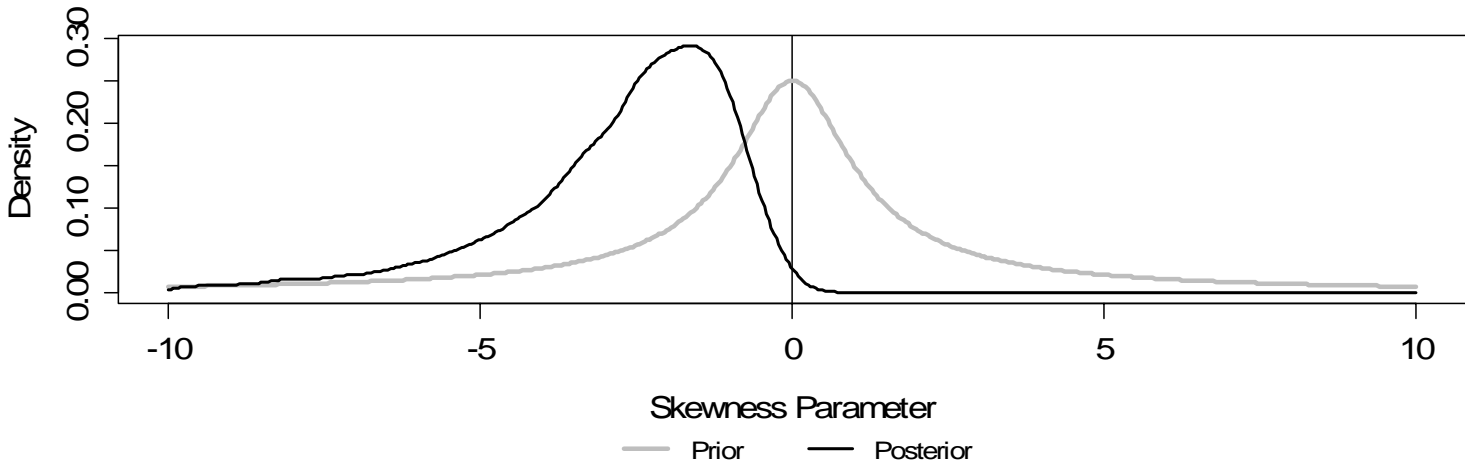
Degrees of Freedom



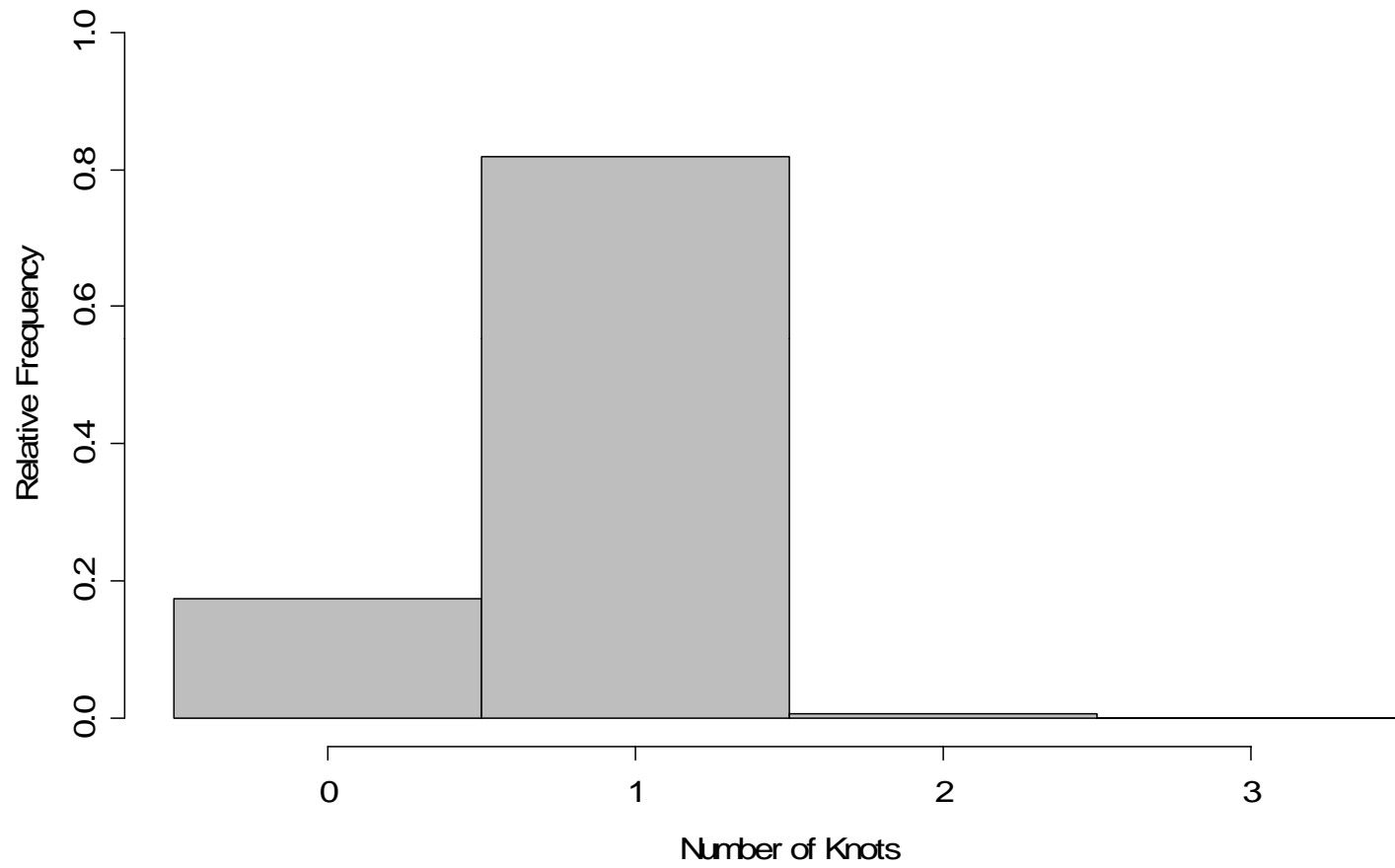
Standard Deviation



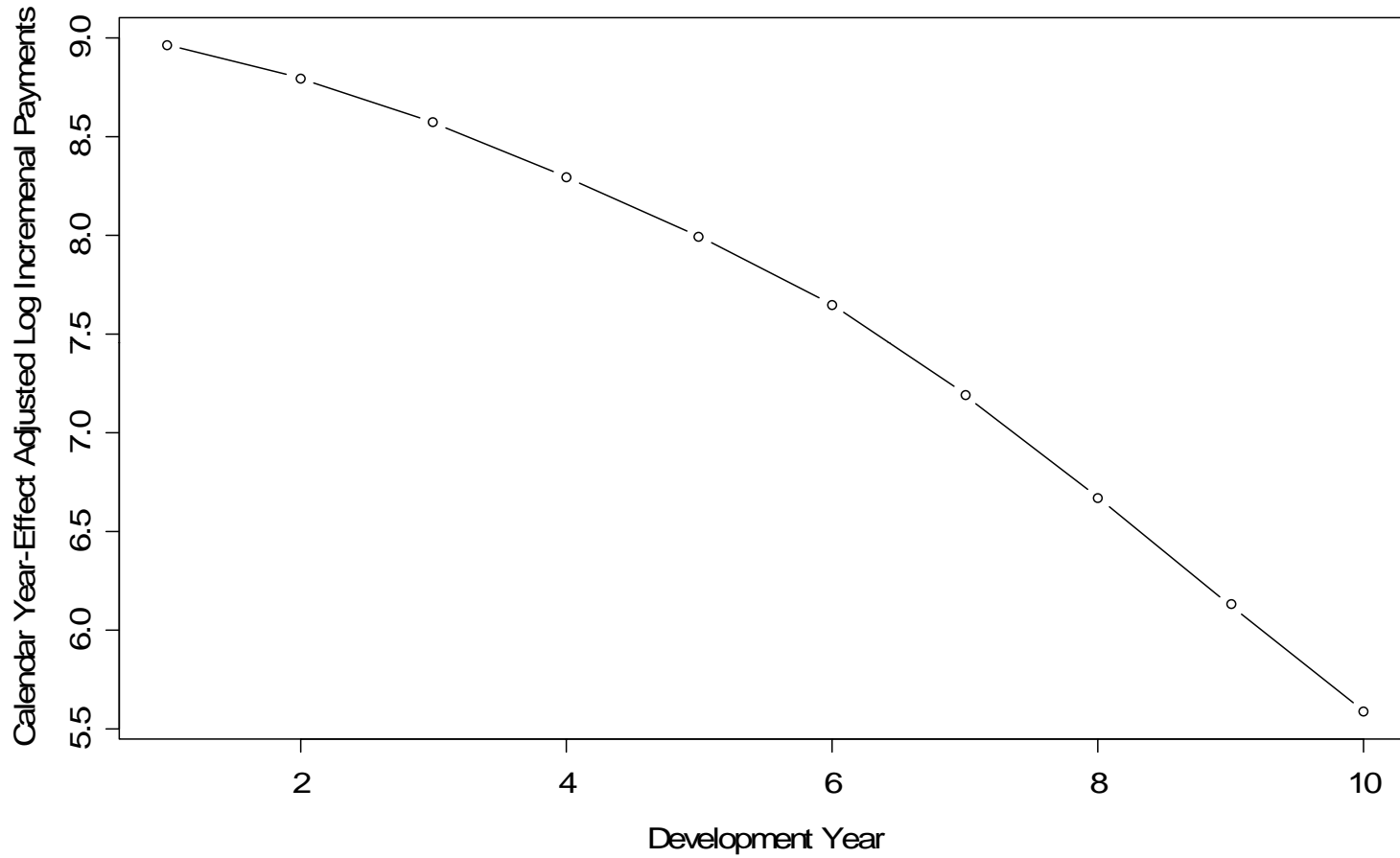
Skewness Parameter



Number of Knots

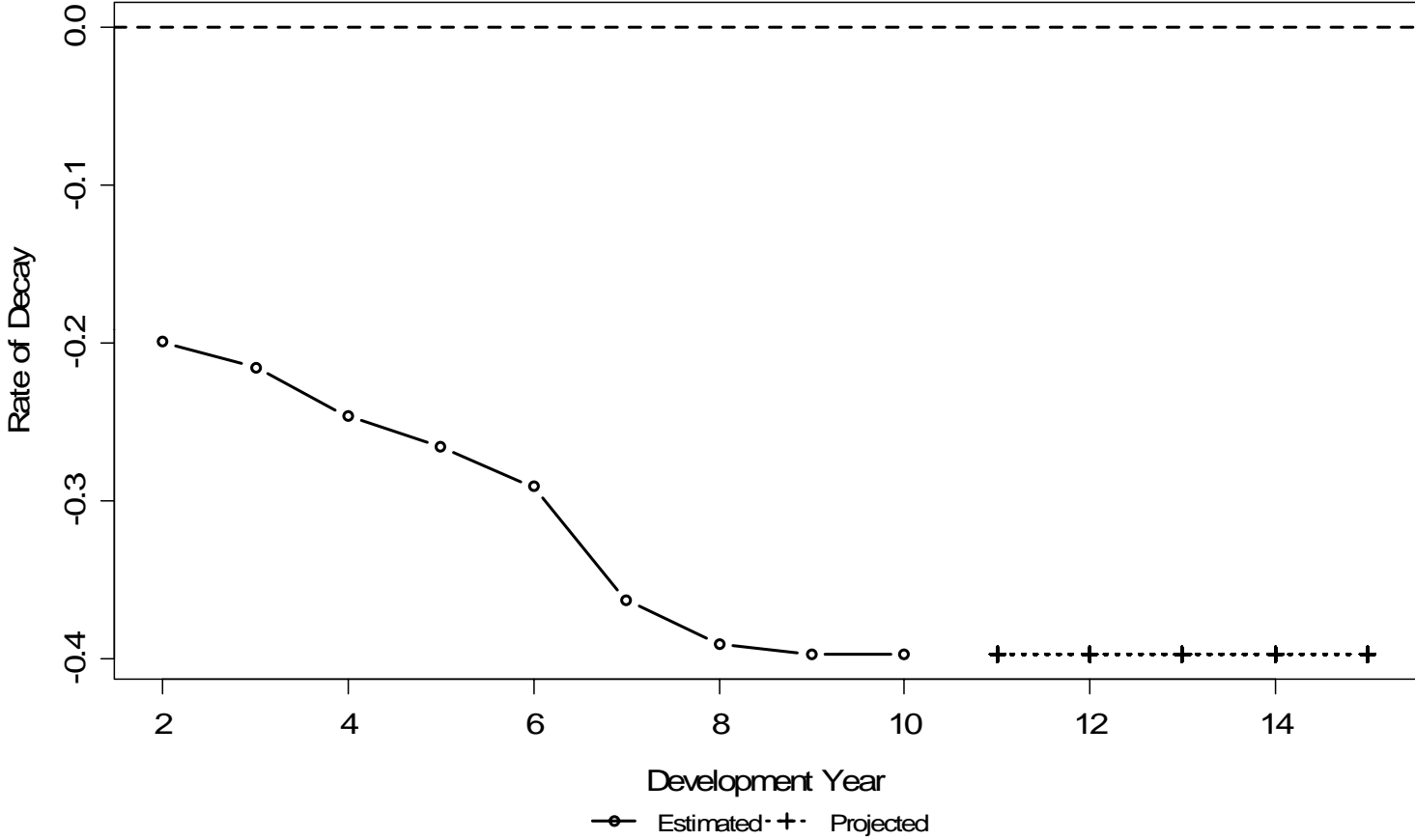


Consumption Path

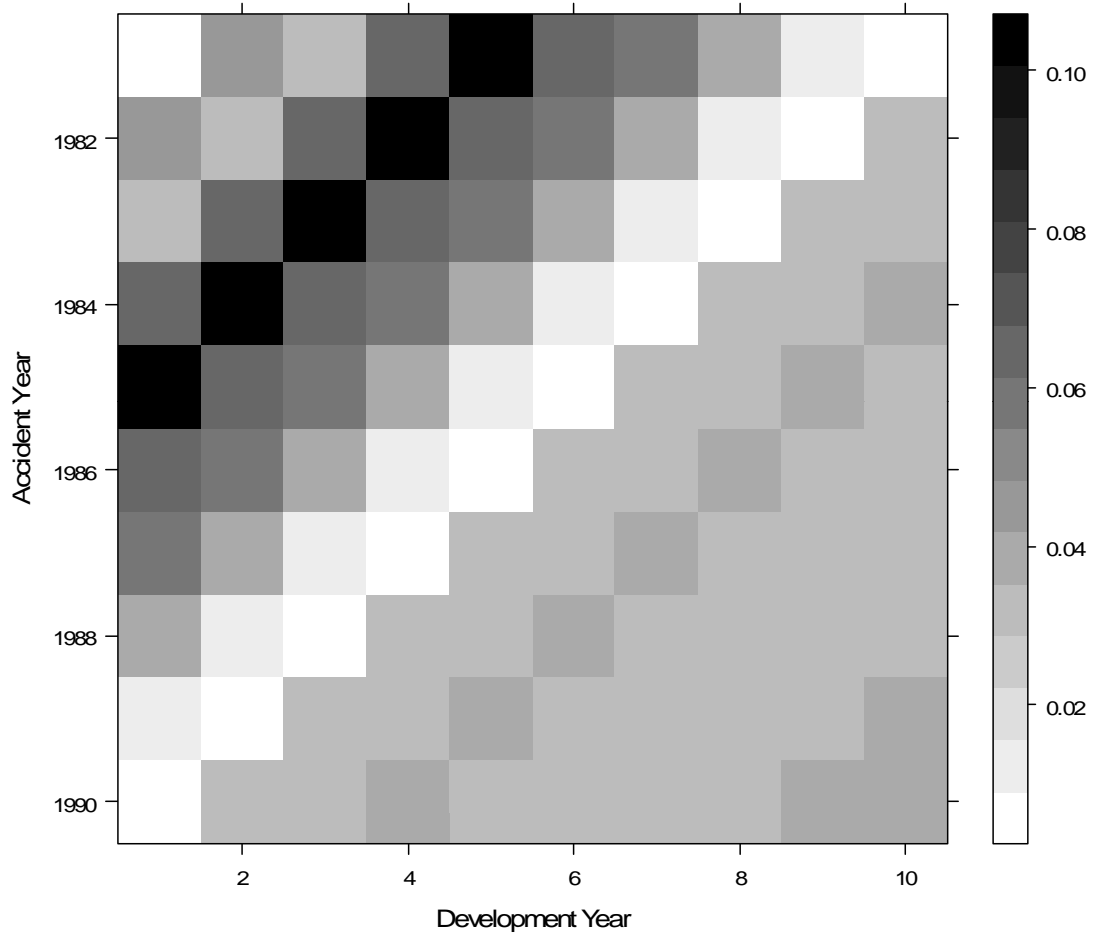


Rate of Decay

(of Calendar Year Effect Adjusted Incremental Payments)

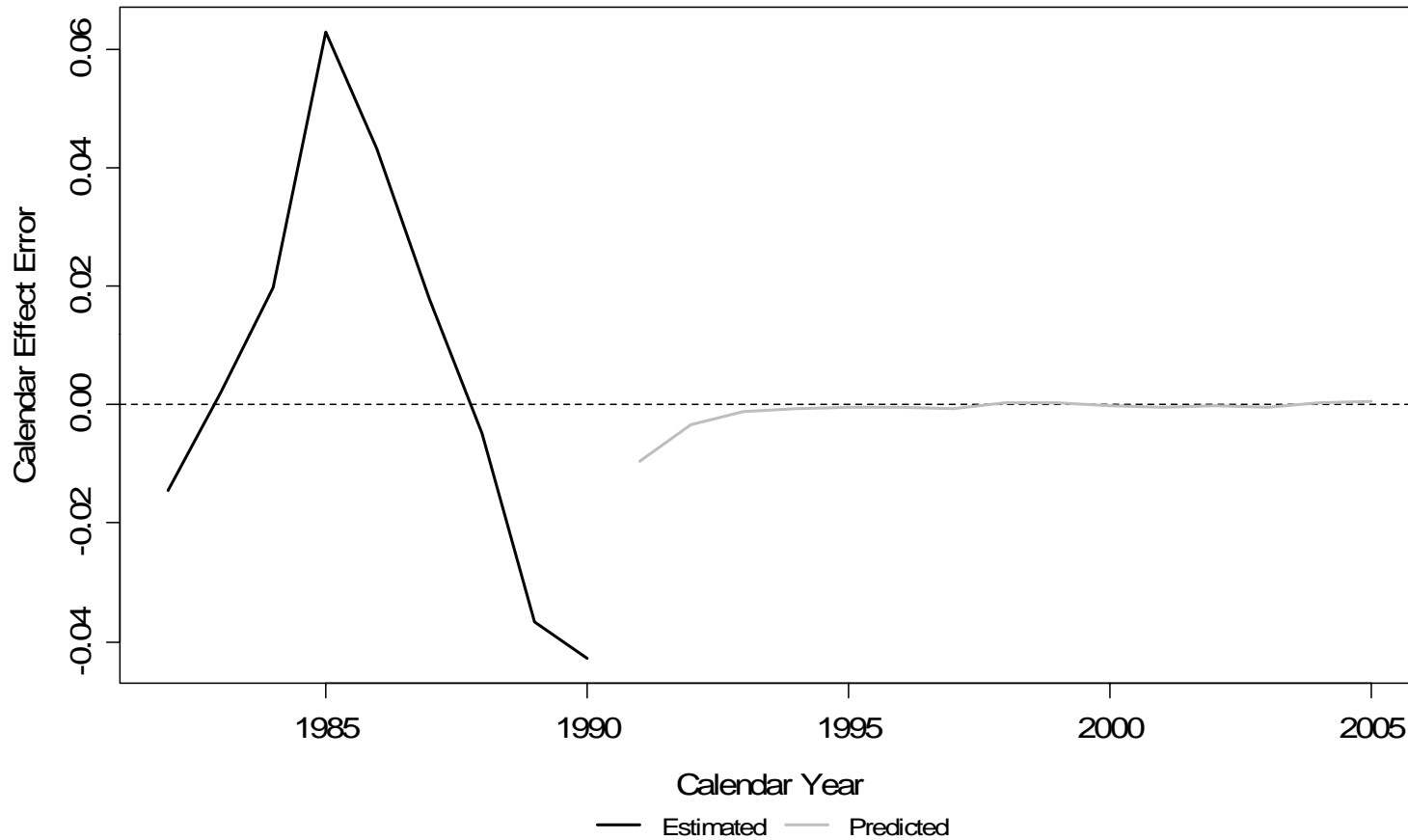


Calendar Year Effect

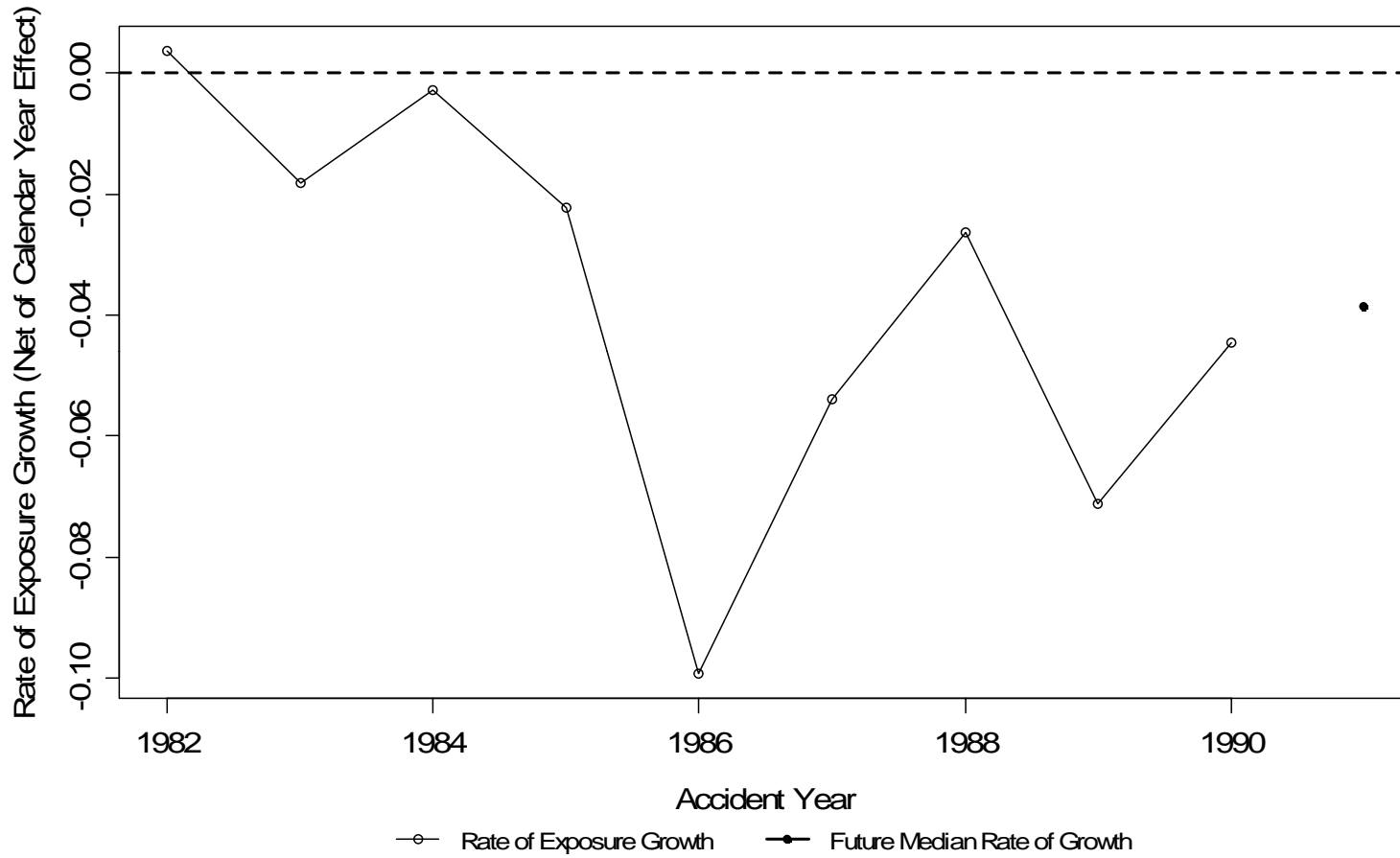


Autoregressive Error in Calendar Year Effect

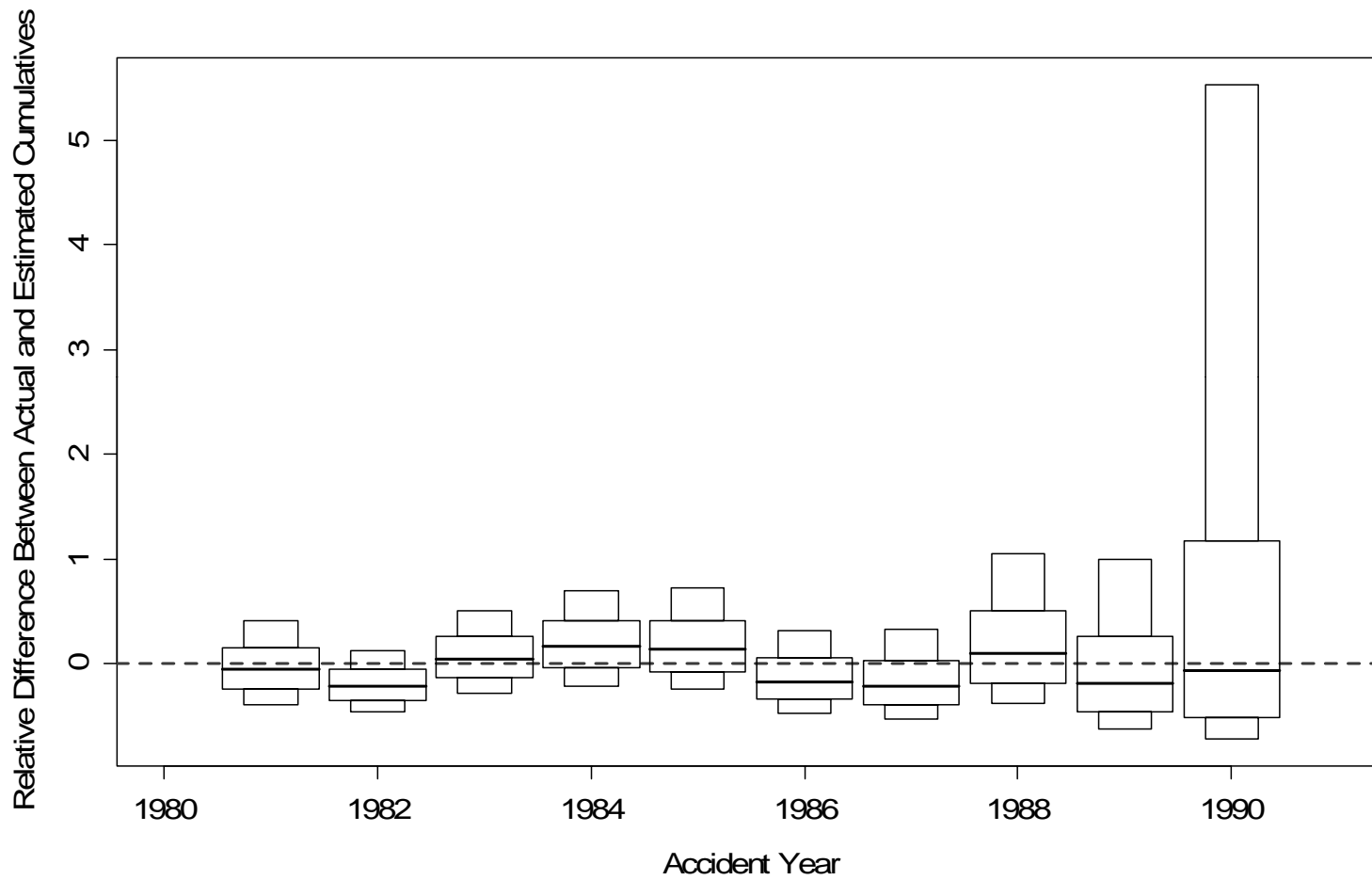
(In addition to the autoregressive process in the expert prior)



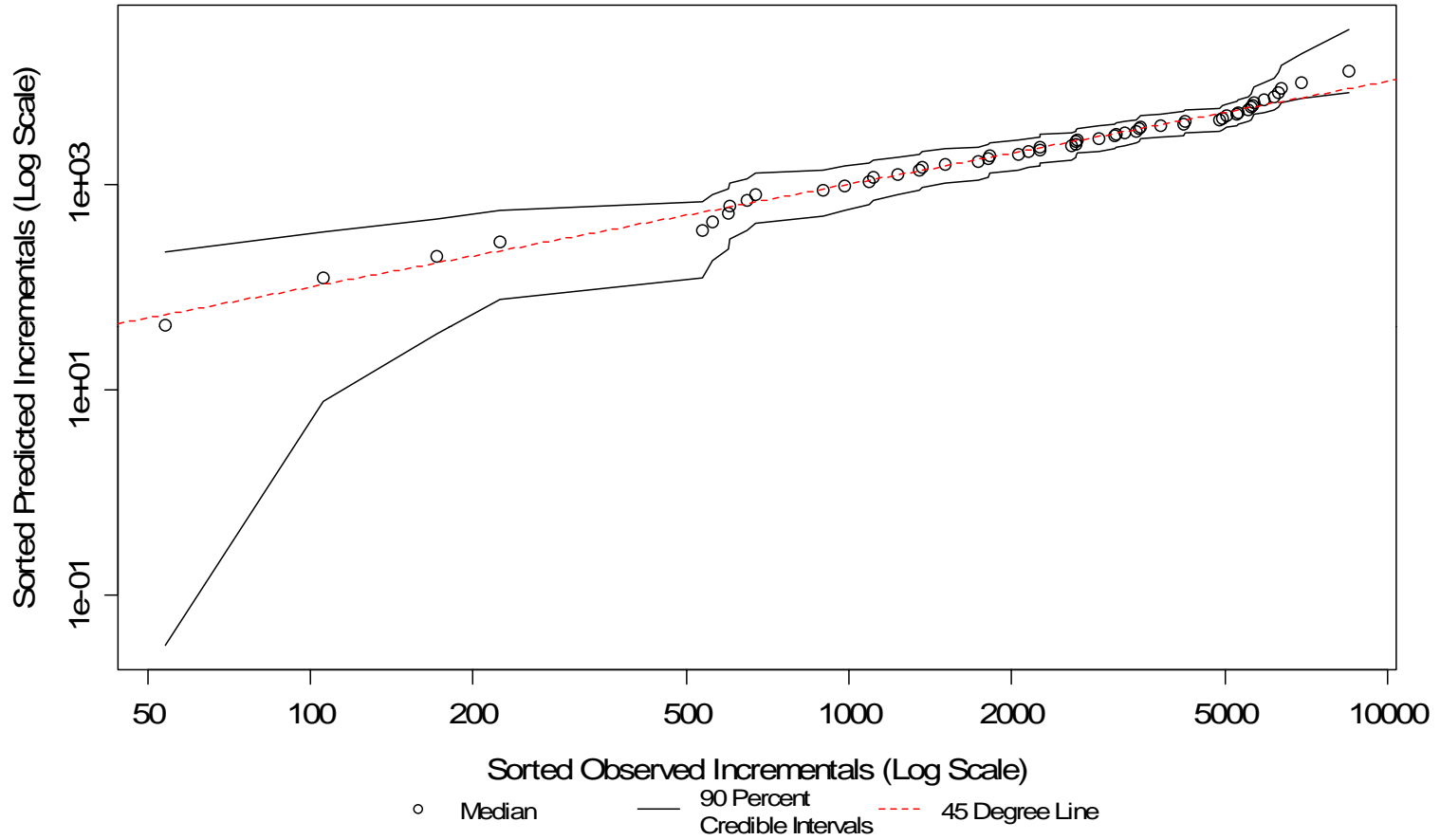
Exposure Growth



Cumulative Diagnostic Chart



A Generic QQ-Plot



An Auto Bodily Injury Liability Triangle (1/2)

- Annual Cumulative Paid Loss Triangle of Private Passenger Auto Bodily Injury Liability

Year	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1974	267	1,975	4,587	7,375	10,661	15,232	17,888	18,541	18,937	19,130	19,189	19,209	19,234	19,234	19,246	19,246	19,246	19,246
1975	310	2,809	5,686	9,386	14,884	20,654	22,017	22,529	22,772	22,821	23,042	23,060	23,127	23,127	23,127	23,127	23,159	
1976	370	2,744	7,281	13,287	19,773	23,888	25,174	25,819	26,049	26,180	26,268	26,364	26,371	26,379	26,397	26,397		
1977	577	3,877	9,612	16,962	23,764	26,712	28,393	29,656	29,839	29,944	29,997	29,999	29,999	30,049	30,049			
1978	509	4,518	12,067	21,218	27,194	29,617	30,854	31,240	31,598	31,889	32,002	31,947	31,965	31,986				
1979	630	5,763	16,372	24,105	29,091	32,531	33,878	34,185	34,290	34,420	34,479	34,498	34,524					
1980	1,078	8,066	17,518	26,091	31,807	33,883	34,820	35,482	35,607	35,937	35,957	35,962						
1981	1,646	9,378	18,034	26,652	31,253	33,376	34,287	34,985	35,122	35,161	35,172							
1982	1,754	11,256	20,624	27,857	31,360	33,331	34,061	34,227	34,317	34,378								
1983	1,997	10,628	21,015	29,014	33,788	36,329	37,446	37,571	37,681									
1984	2,164	11,538	21,549	29,167	34,440	36,528	36,950	37,099										
1985	1,922	10,939	21,357	28,488	32,982	35,330	36,059											
1986	1,962	13,053	27,869	38,560	44,461	45,988												
1987	2,329	18,086	38,099	51,953	58,029													
1988	3,343	24,806	52,054	66,203														
1989	3,847	34,171	59,232															
1990	6,090	33,392																
1991	5,451																	

Data source: Hayne, Roger M., "Measurement of Reserve Variability," *Casualty Actuarial Society Forum*, Fall 2003, pp. 141-172, <http://www.casact.org/pubs/forum/03fforum/03ff141.pdf>

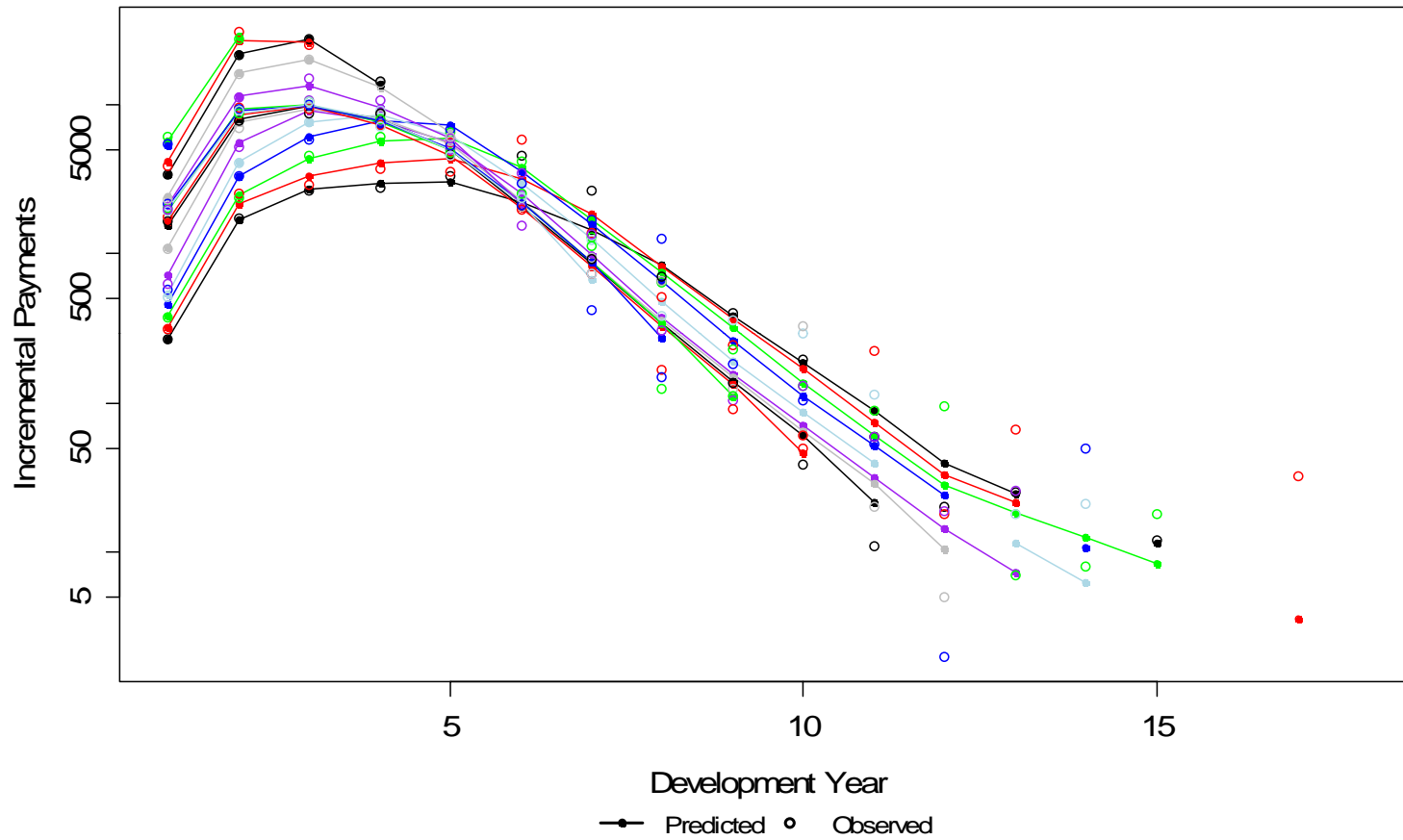
An Auto Bodily Injury Liability Triangle (2/2)

- The triangle exhibits payments at zero amounts in high development years
- Potentially, there is a structural break in the consumption path
 - Roger Hayne provided the following background information to the triangle:

In late December 1986 there was a judicial decision limiting a judge's power to dismiss a case as a matter of law in certain non-trivial circumstances (thus not requiring a trial of fact). For quite some time prior to this a judge could review a case and determine if injuries were threshold-piercing as a matter of law and not as a matter of fact to be decided by the trier of fact (jury or judge).

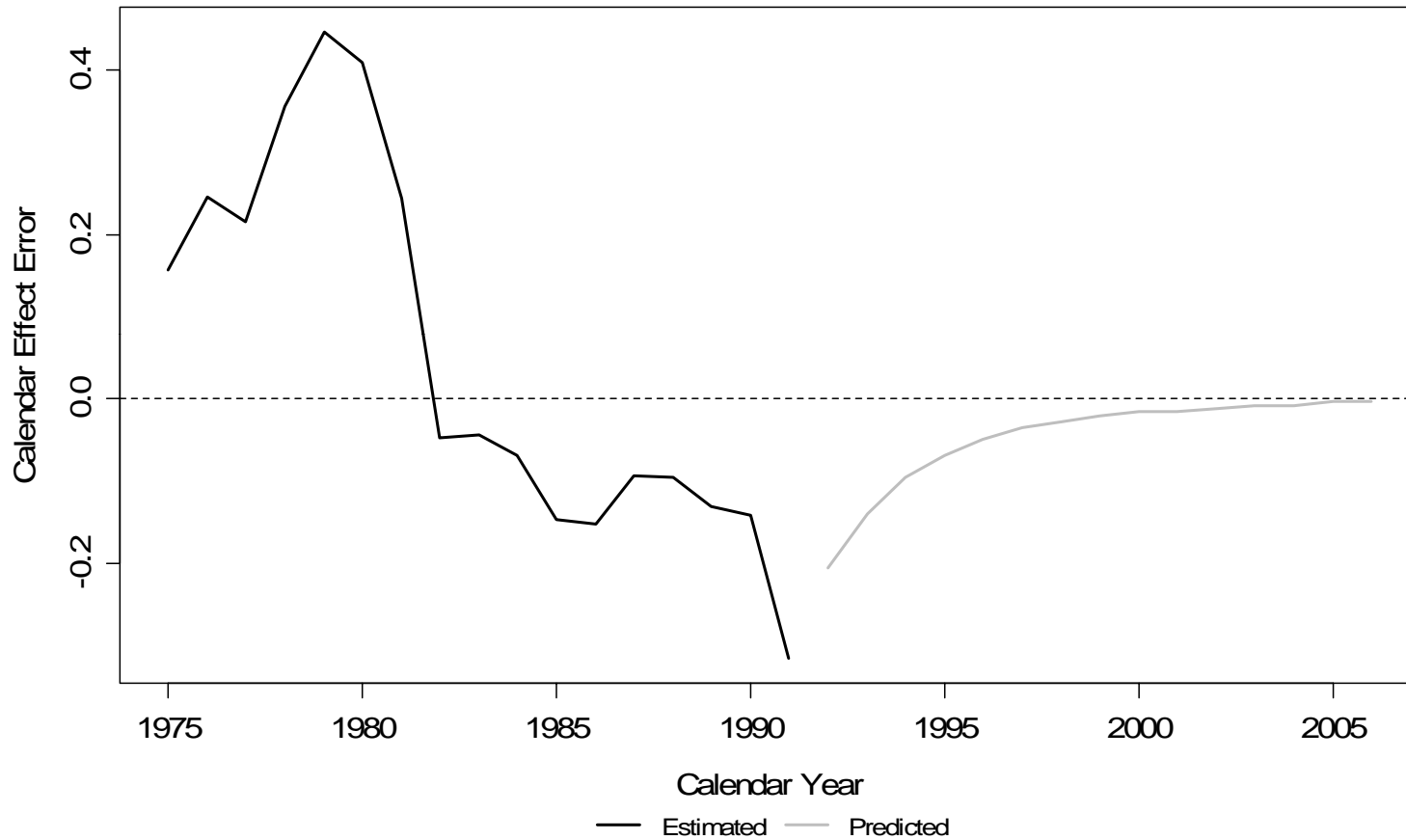
Data source: Hayne, Roger M., "Measurement of Reserve Variability," *Casualty Actuarial Society Forum*, Fall 2003, pp. 141-172, <http://www.casact.org/pubs/forum/03fforum/03ff141.pdf>

Log Incremental Payments

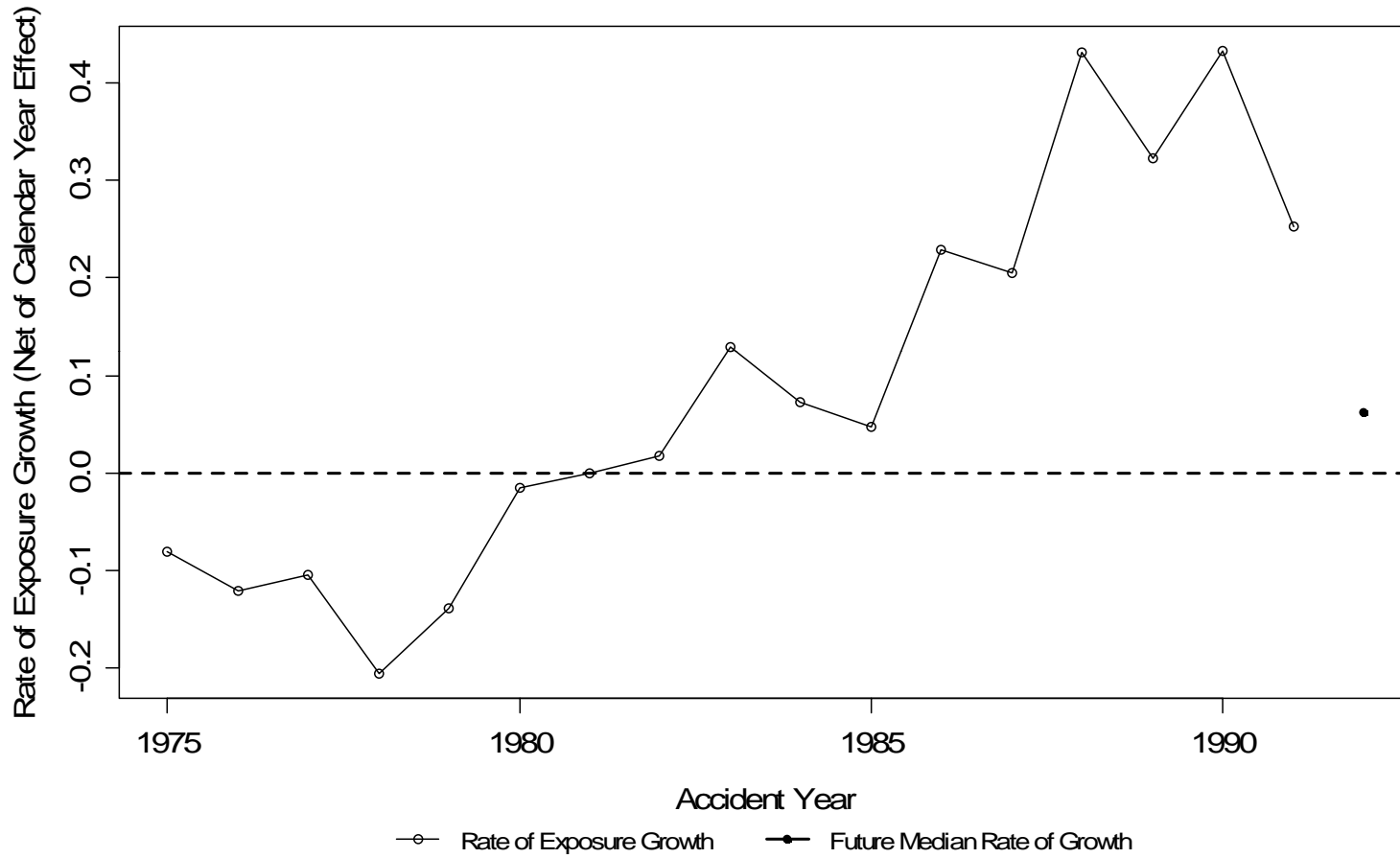


Autoregressive Error in Calendar Year Effect

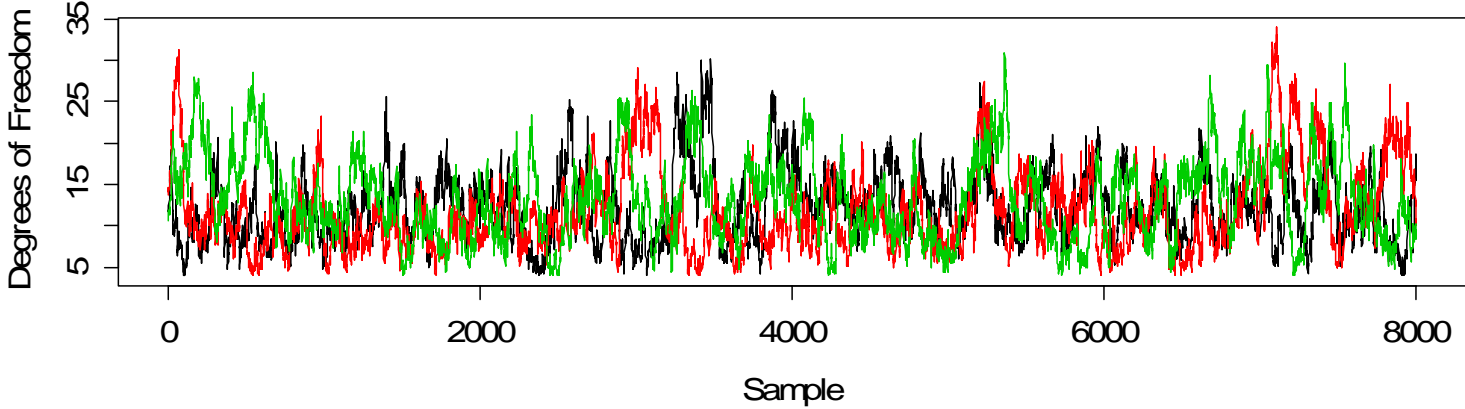
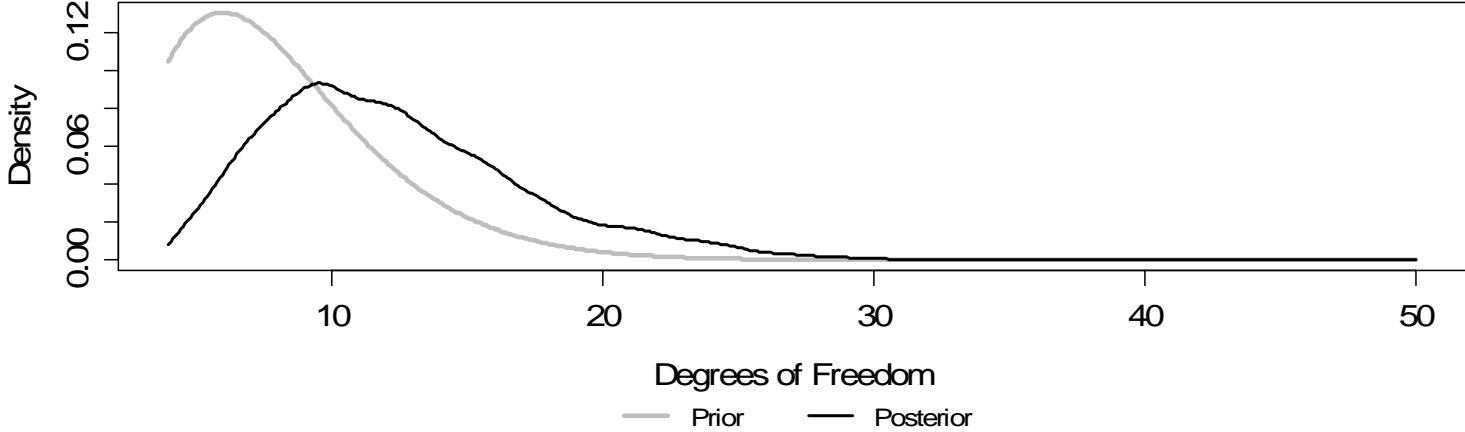
(In addition to the autoregressive process in the expert prior)



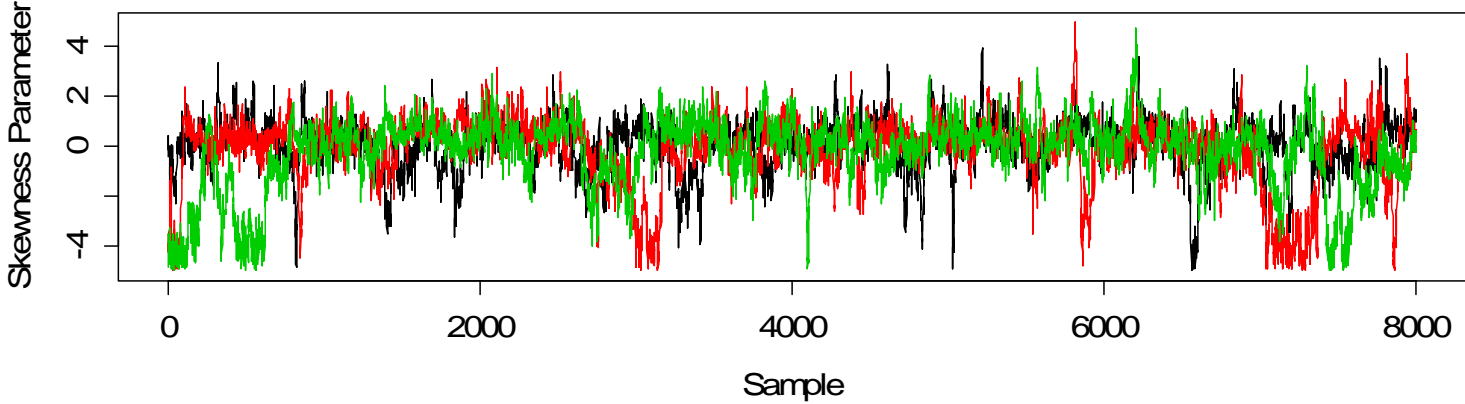
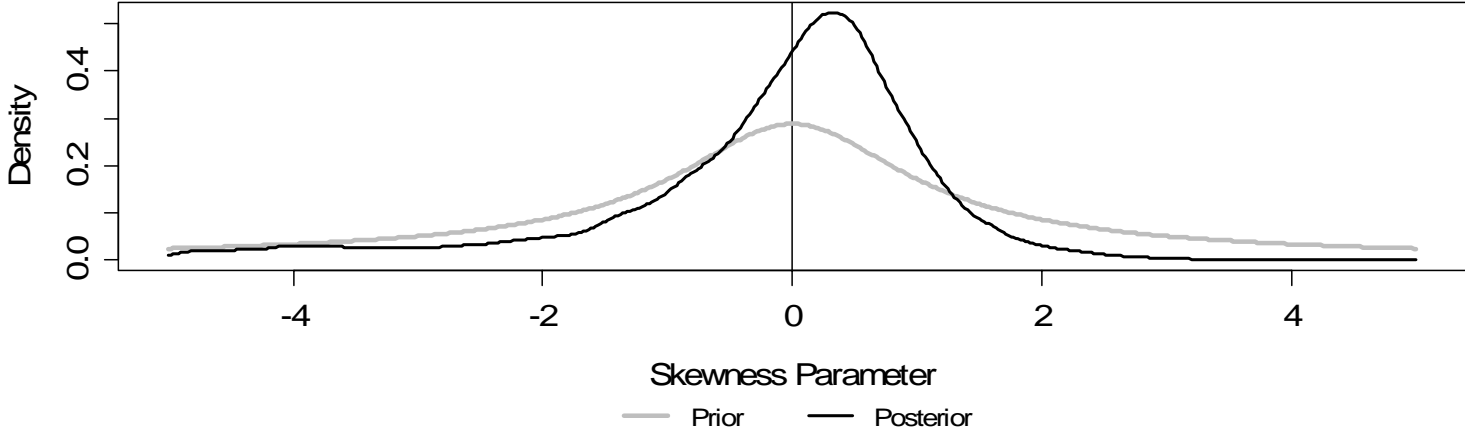
Exposure Growth



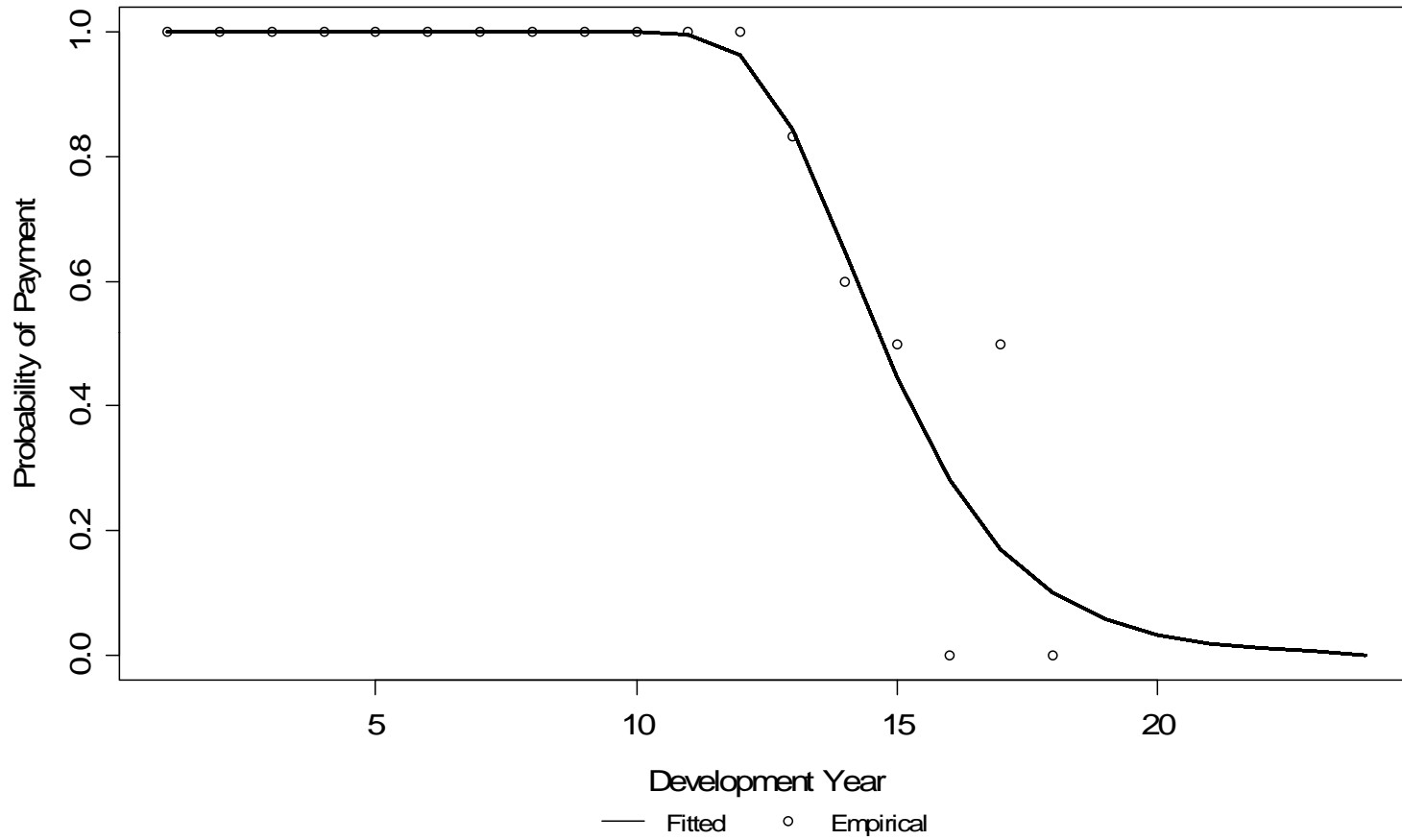
Degrees of Freedom



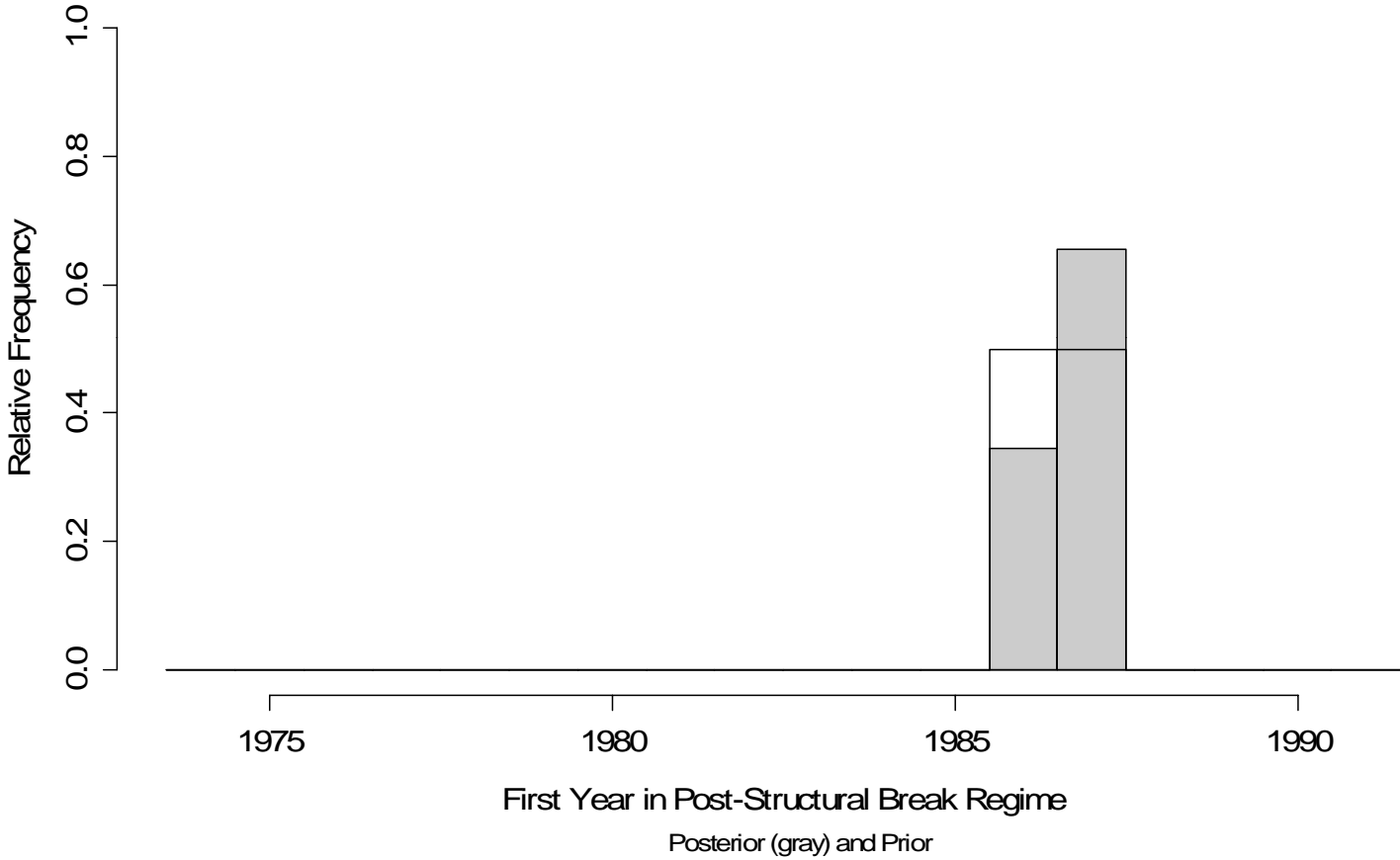
Skewness Parameter



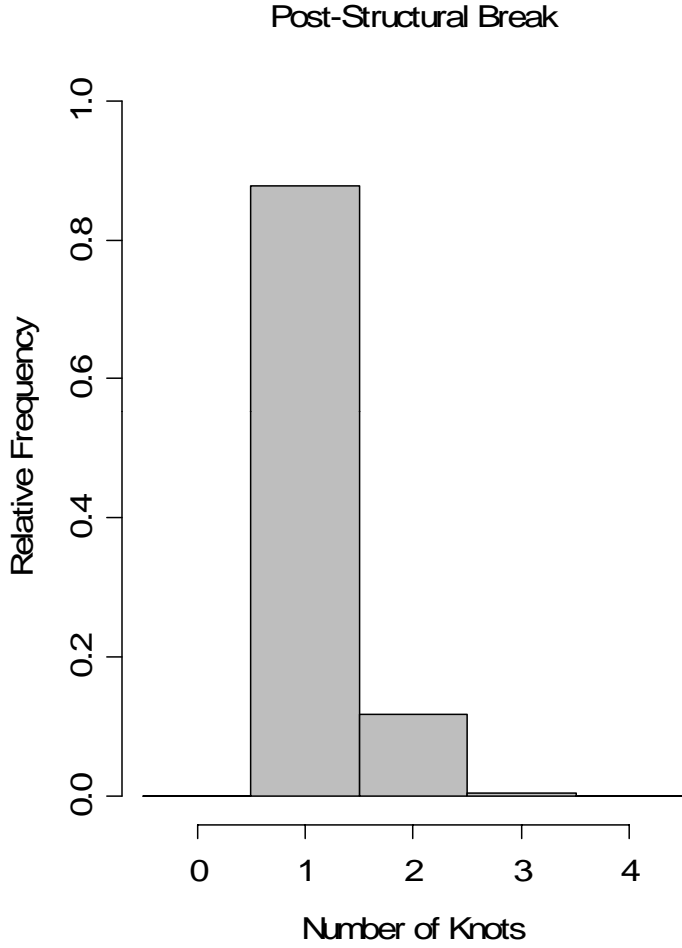
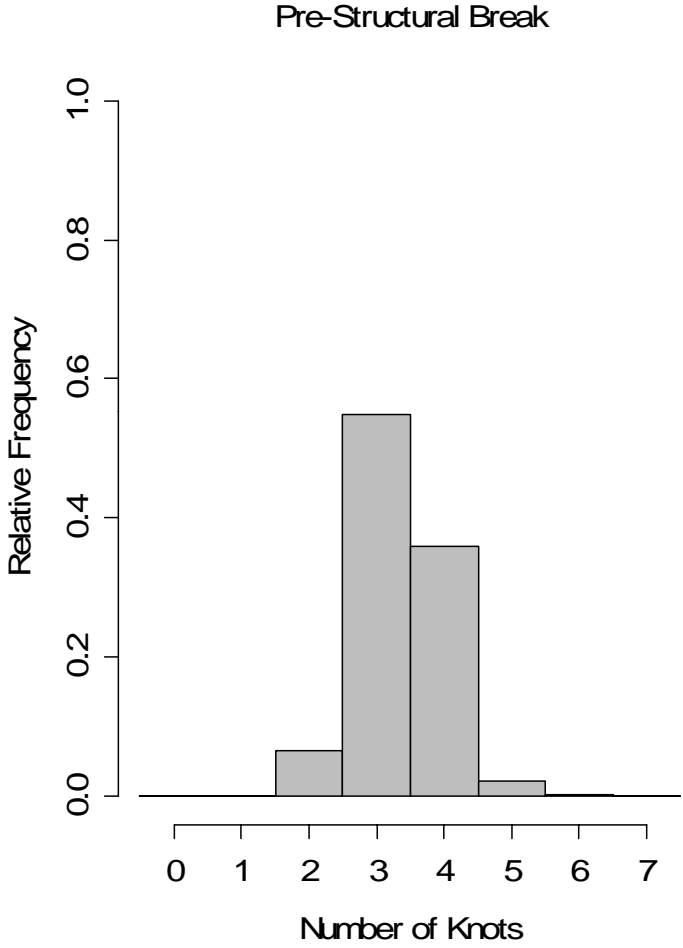
Probability of Not Observing a Payment at the Zero Amount



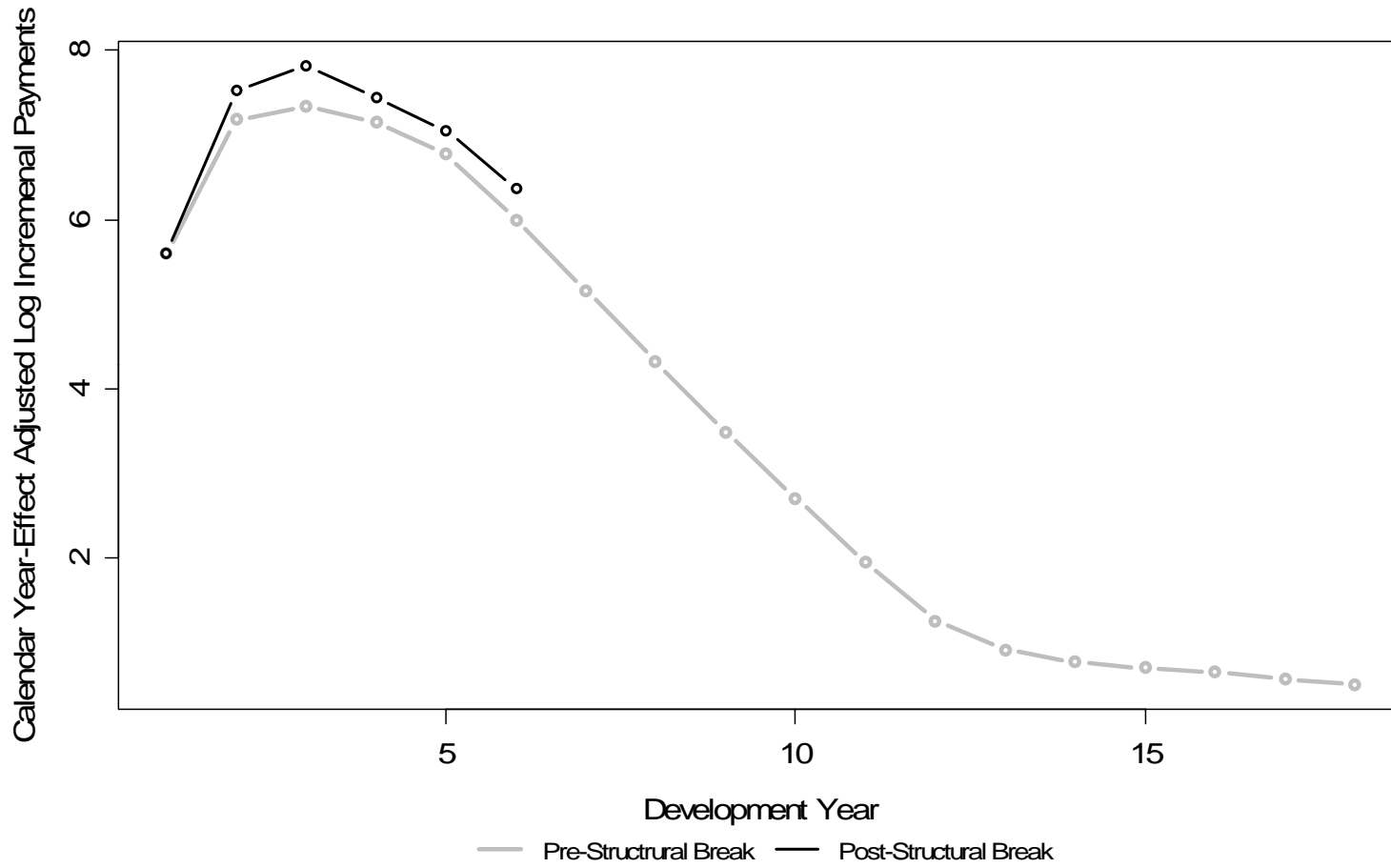
Distribution of Changepoint



Number of Knots

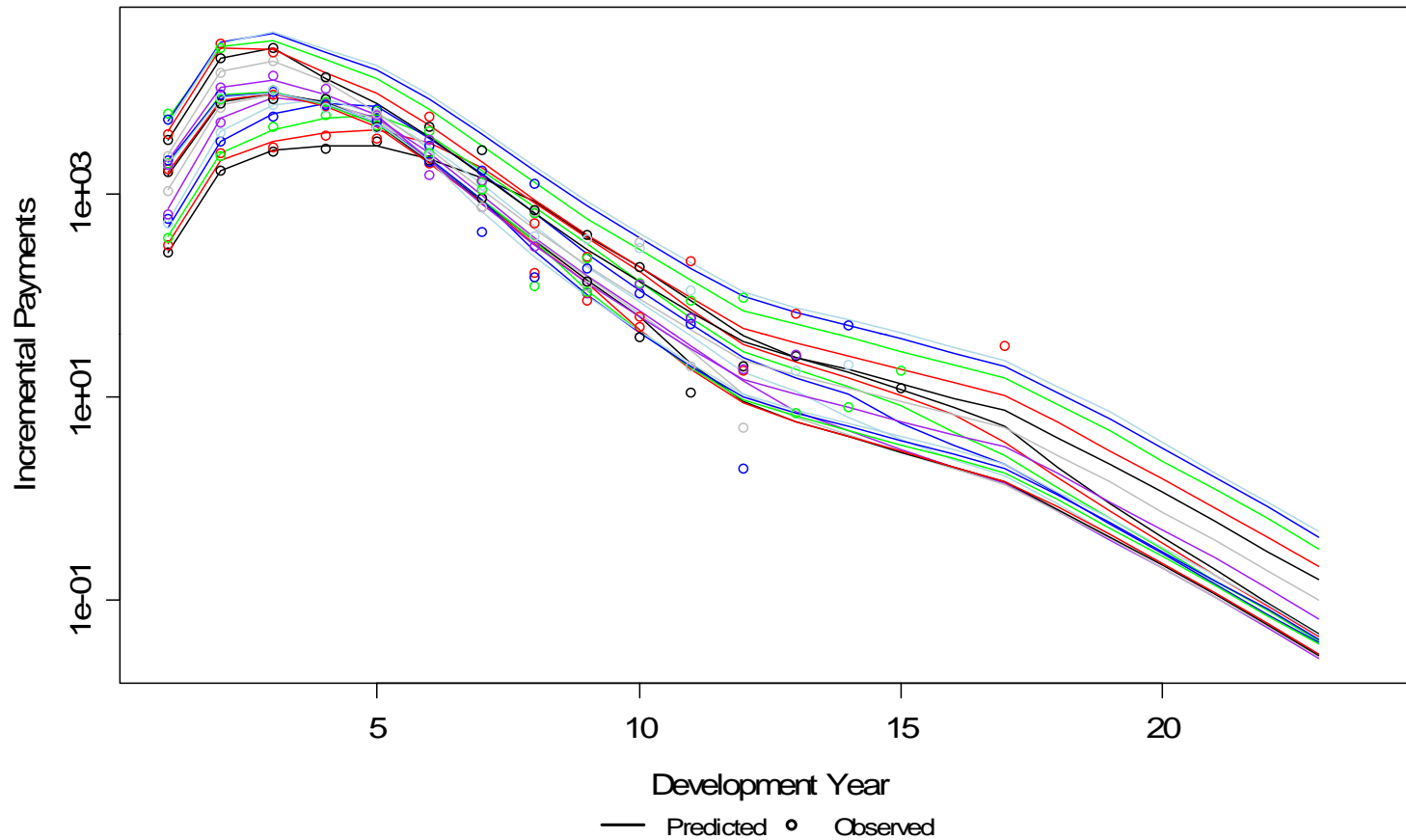


Consumption Path

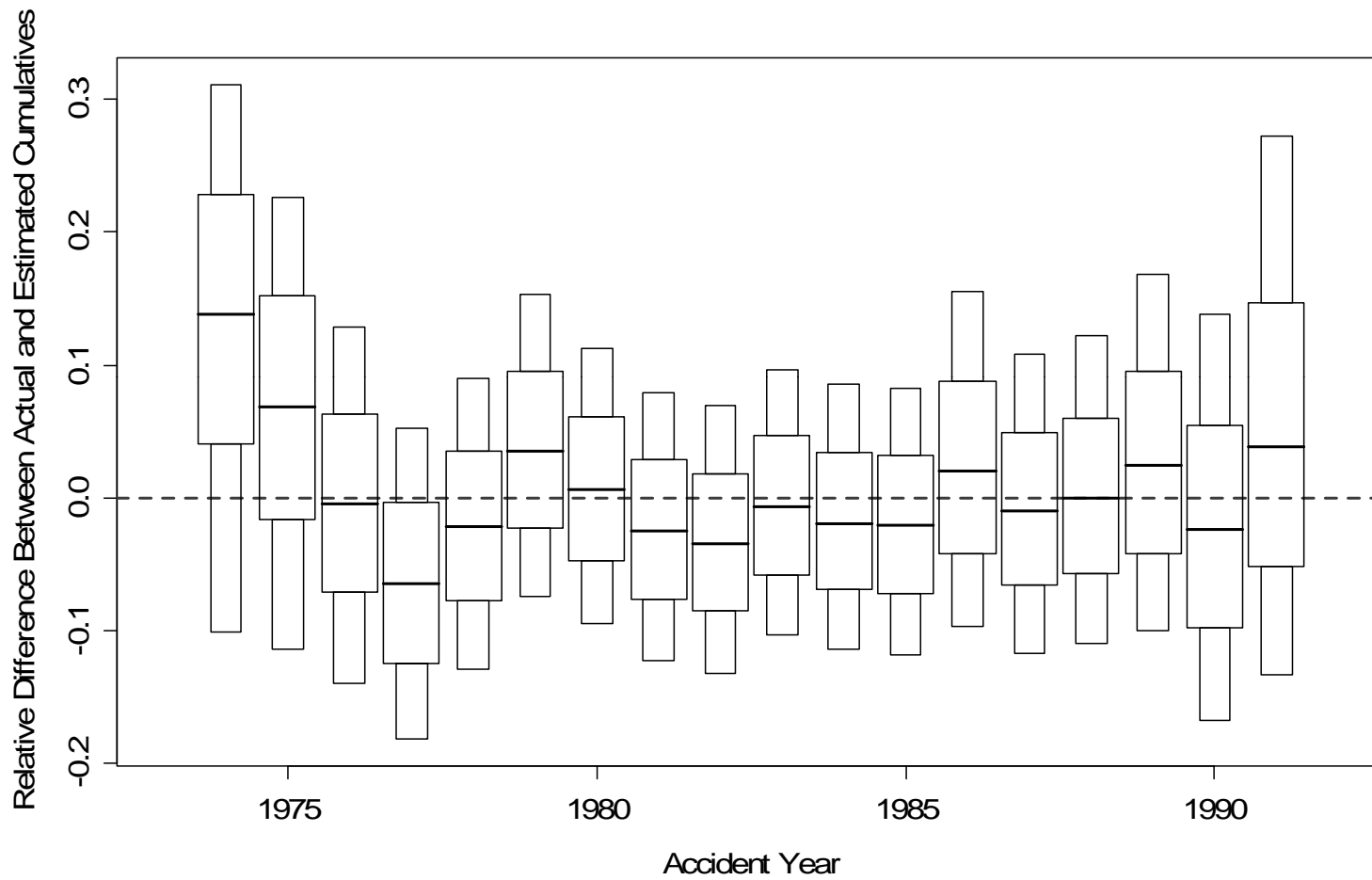


Log Incremental Payments

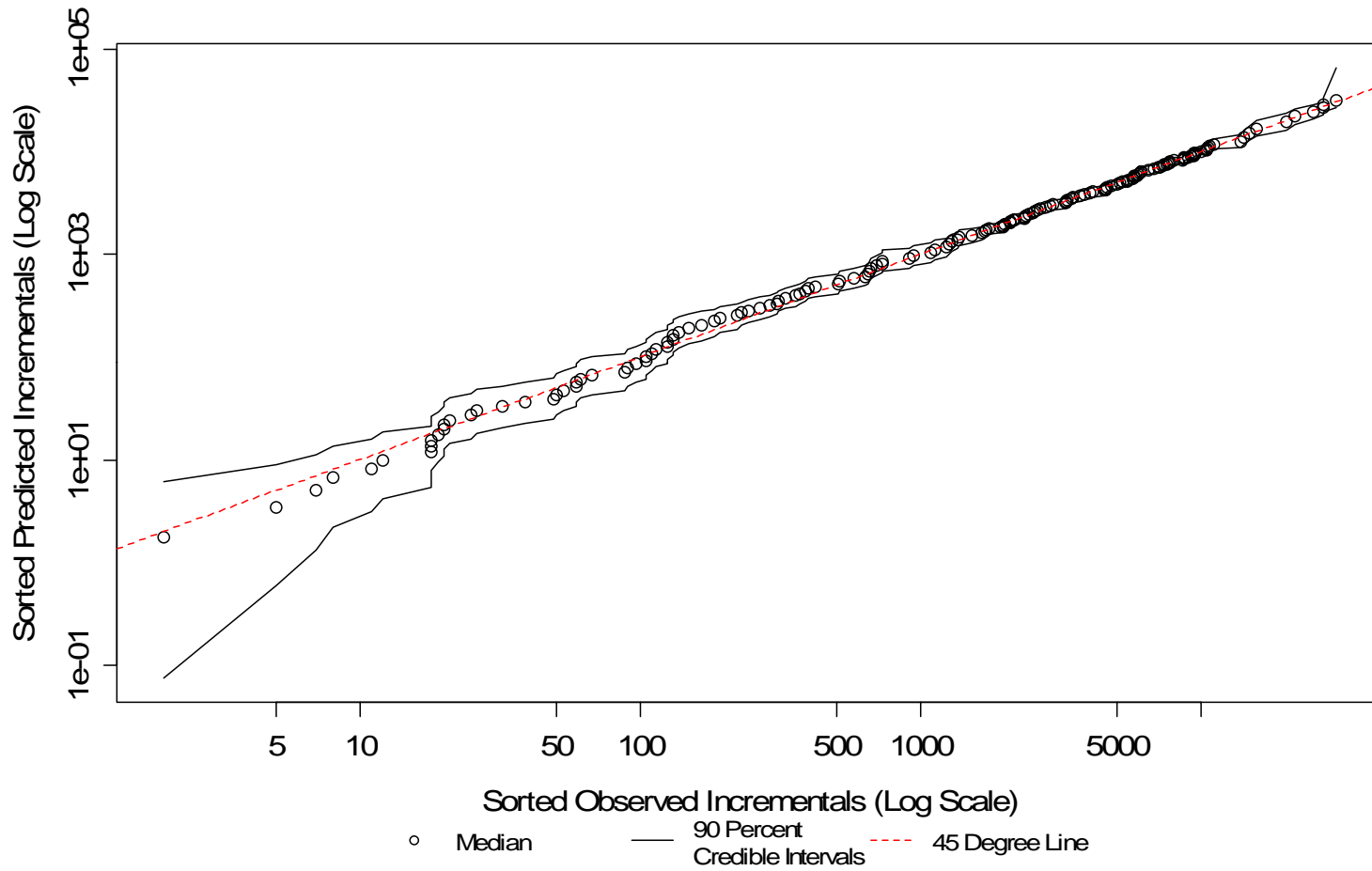
Adjusted for "Probability of Payment"



Cumulative Diagnostic Chart

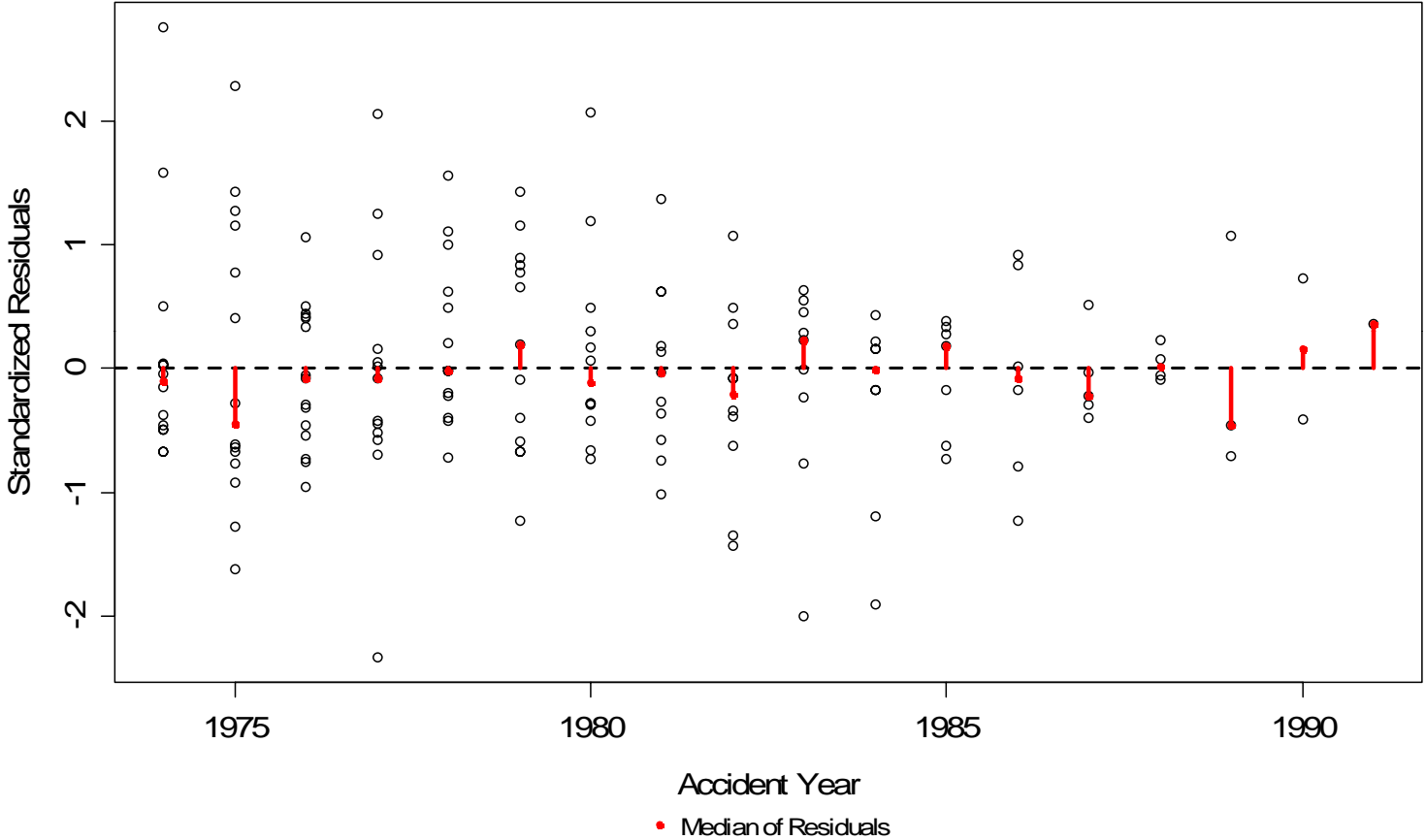


A Generic QQ-Plot



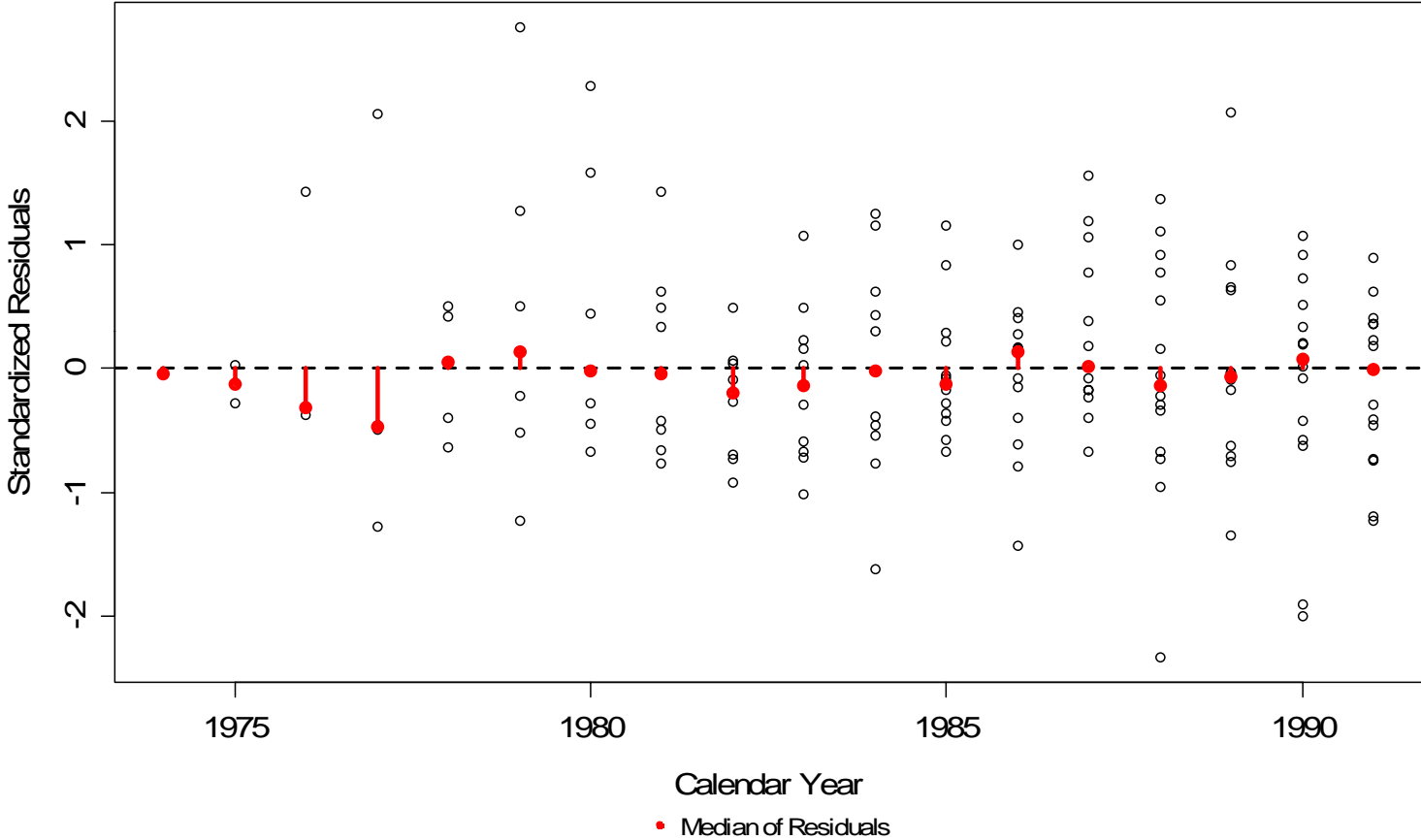
Standardized (Skewed) Residuals

Accident Year



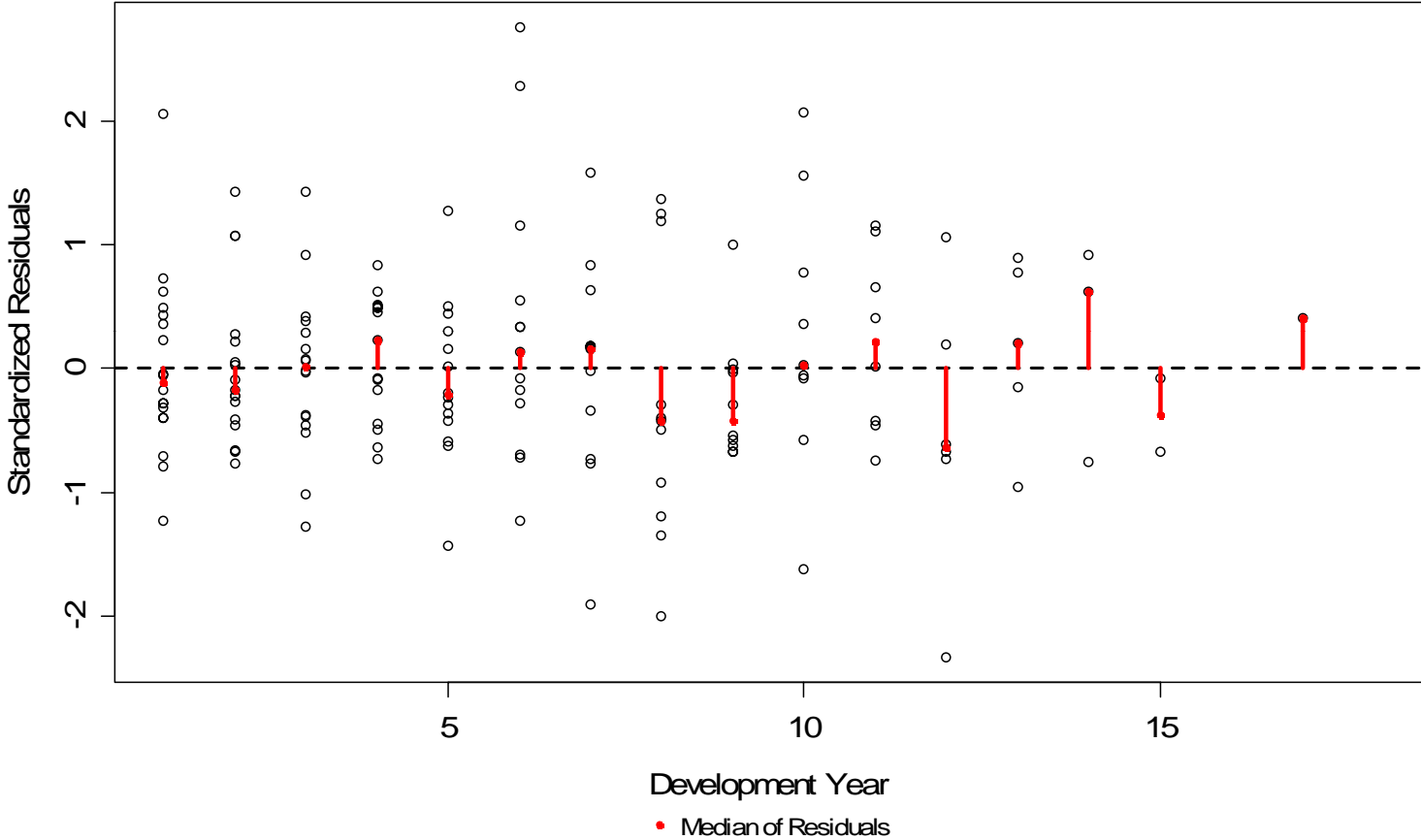
Standardized (Skewed) Residuals

Calendar Year



Standardized (Skewed) Residuals

Development Year



Conclusion

- The presented model of loss development is robust to heavy tails, skewness, and heteroskedasticity
- The model employs RJMCMC to determine the optimal trajectory of the calendar year effect adjusted and exposure adjusted incremental payments
- Further, in its changepoint version, the model is capable of accounting for a structural break, the location of which does not have to be exactly known but is determined by the model within a supplied time interval
- Taken together, the model offers a high degree of responsiveness to data, given the specified data-generating process and the chosen prior distributions

References

- [1] Barnett, Glen, and Ben Zehnwirth, "Best Estimates for Reserves," *Casualty Actuarial Society Proceedings*, Vol. 37, No. 167, 2000, pp. 245-321, <http://www.casact.org/pubs/proceed/proceed00/00245.pdf>.
- [2] De Jong, Piet, "Forecasting Runoff Triangles," *North American Actuarial Journal*, Vol. 10, pp. 28-38, http://www.soa.org/library/journals/north-american-actuarial-journal/2006/april/naaj0602_2.pdf.
- [3] Kremer, Erhard, "A Class of Autoregressive Models for Predicting the Final Claim Amount," *Insurance Mathematics and Economics*, Vol. 3, 1984, pp. 111-119.
- [4] Verrall, Richard, "Modelling Claims Run-Off Triangles with Two-Dimensional Time Series," *Scandinavian Actuarial Journal*, 1989, pp. 129-138.
- [5] Verrall, Richard, "A State Space Representation of the Chain Ladder Linear Model," *Journal of the Institute of Actuaries*, Vol. 116, 1989, pp. 589-610.
- [6] Zehnwirth, Ben, "Probabilistic Development Factor Models with Applications to Loss Reserve Variability, Prediction Intervals and Risk Based Capital," *Casualty Actuarial Society Forum*, Vol. 2, Spring 1994, pp. 447-605, <http://www.casact.org/pubs/forum/94spforum/94spf447.pdf>.

Technical Appendix: The Skewed Student- t Likelihood (1/3)

$$y_{i,j} \sim \mathbf{N}\left(\mu_{i,j} + \frac{\alpha}{\tau_{i,j}}, \tau_{i,j}\right)$$

$$\alpha \sim \text{Student}(0, 0.5, 2.1) \mathbf{I}(-l, l), \quad l > 0$$

- The Student- t distribution is implemented as a mean-variance mixture of normal distributions
- The mean of the conditionally Gaussian random variable moves in proportion to its stochastic latent variance $1/\tau_{i,j}$
- For a skewness parameter α of zero, the skewed Student- t collapses into a symmetric (conventional) Student- t
- The prior for the skewness parameter is a truncated central Student- t distribution with low degrees of freedom (2.1)

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix: The Skewed Student-*t* Likelihood (2/3)

$$\tau_{i,j} = \frac{\omega_{i,j}}{\nu \cdot \sigma_j^2}$$

$$\omega_{i,j} \sim \chi_{(\nu)}^2$$

$$\nu \sim \chi_{(8)}^2 \text{I}(4, 50)$$

- The mixing distribution for the latent variance is an inverse Chi-squared distribution
- The degrees of freedom are drawn from a truncated Chi-squared distribution—the truncation at 4 (2) ensures a finite variance (when the skewness parameter is set to zero)
- The model is heteroskedastic by allowing the scale parameter σ_j to vary on the development time axis

Indexes: *i* represents rows (exposure years); *j* represents columns (development years)

Technical Appendix: The Skewed Student-*t* Likelihood (3/3)

$$\log(\sigma_j^2) \sim N\left(2 \cdot \log(\sigma_{j-1}^2) - \log(\sigma_{j-2}^2), \nu\right), j \geq 3$$

$$\nu \sim \text{Ga}(10, 0.5)$$

$$\sigma_j \sim U(0, 10), j = 1, 2$$

- The log of the squared scale parameter is smoothed using a second-order random walk
- The innovation variance of the random walk is an inverse gamma distribution
- The scale parameters of the first two development years have highly uninformed uniform priors

Indexes: *i* represents rows (exposure years); *j* represents columns (development years)

Technical Appendix: The Log Incremental Payments

$$\mu_{i,j} = S_j + \sum_{k=2}^{i+j} \kappa_k + \sum_{k=1}^i \eta_k$$

$$\delta_j = S_j - S_{j-1}, \quad j \geq 2$$

$$\mu_{i,j} = S_1 + \sum_{k=2}^{i+j} \kappa_k + \sum_{k=1}^i \eta_k + \sum_{k=1}^j \delta_k$$

- The log incremental payments (net of the shift due to skewness) is the sum of (1) the calendar-year effect adjusted log incremental payments in the first exposure year S_1, \dots, S_K , (2) the cumulative calendar year effect, and (3) the cumulative exposure growth
- The rate of decay (on the logarithmic scale) is backed out of the log consumption path S_1, \dots, S_K
- The third equation re-states the log incremental payments in (log) growth rates

Indexes: i represents rows (exposure years); j represents columns (development years)
 K is the dimension of the triangle (number of rows, equal to number of columns)

Technical Appendix: The Calendar Year Effect (1/4)

$$\kappa_{i+j} \sim N\left(\mu_{\kappa,i+j}, \tau_{\kappa}\right), \quad i+j \geq 3$$

$$\tau_{\kappa} = 1/\sigma_{\kappa}^2$$

$$\sigma_{\kappa} \sim U(0,10)$$

- The calendar year effect is normally distributed around an expert prior
- The standard deviation of this normal has a highly uninformed uniform prior
- $\mu_{\kappa,i+j}$ may be a weighted average of a constant nonzero rate of inflation, a zero rate of inflation, and a stochastic rate of inflation
- For instance, different types of workers' compensation indemnity claims may escalate at different rates (e.g., Fatals at 4 percent, Permanent Totals at the CPI, and all others at zero)

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix: The Calendar Year Effect (2/4)

- It may be argued that the expert rate of inflation systematically falls short of the true (yet unobserved) rate of inflation in the pertinent line of insurance
 - For instance, it may be argued that the rate of inflation in Auto Bodily Injury Liability triangles differs from the rate M-CPI inflation (by a negative or positive) constant c (on the logarithmic scale)
- If this is indeed the case, then the constant c factors into the rate of exposure growth and the rate of decay, thus leaving the estimated ultimate loss unaffected:

$$\mu_{i,j} = S_1 + \sum_{k=2}^{i+j} (\kappa_k - c) + \sum_{k=1}^i (\eta_k + c) + \sum_{k=1}^j (\delta_k + c)$$

- When simulating future calendar year effects, however, the mean to which the stochastic rate of inflation approaches asymptotically needs to be adjusted by this constant

Indexes: i represents rows (exposure years); j represents columns (development years)

Technical Appendix: The Calendar Year Effect (3/4)

$$\mu_{\kappa,i+1} = \text{N}\left(a \cdot \mu_{\kappa,i} + b, \tau_{\varepsilon}\right), \quad 0 < a < 1$$

$$a \sim \text{Beta}(1,1)$$

$$b \sim \text{N}\left(0, 10^{-6}\right)$$

$$\tau_{\varepsilon} \sim \text{Ga}(0.001, 0.001)$$

- When a stochastic rate of inflation is used as an expert prior (such as the CPI or M-CPI), then future values of this rate of inflation are simulated using an Ornstein-Uhlenbeck (O-U) process
- The simulation of future rates of inflation using the Ornstein-Uhlenbeck process implies a return of the inflation rate to its historic mean
- The discrete Ornstein-Uhlenbeck process can be calibrated by estimating an autoregressive process

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix: The Calendar Year Effect (4/4)

$$\tilde{\lambda}_{i+j} \sim \text{N}\left(0, \tau_{\lambda} \cdot \left(1 - \rho_{\lambda}^2\right)\right), \quad i+j=3$$

$$\tilde{\lambda}_{i+j} \sim \text{N}\left(\rho_{\lambda} \cdot \tilde{\lambda}_{i+j-1}, \tau_{\lambda}\right), \quad i+j \geq 4$$

$$\lambda_{i+j} = \tilde{\lambda}_{i+j} - \frac{1}{K-1} \sum_{i+j=3}^{i+j=K+2} \tilde{\lambda}_{i+j}, \quad i+j=3, \dots, K+2$$

$$\tau_{\lambda} \sim \text{Ga}(2, 0.01)$$

$$\rho_{\lambda} \sim \text{Beta}(2, 4)$$

$$\mu_{i,j} = \sum_{k=2}^{i+j} \lambda_k + \sum_{k=2}^{i+j} \kappa_k + \sum_{k=1}^i \eta_k + S_j$$

- The specification of the calendar year effect can be expanded to account for an autoregressive error (beyond the autoregressive nature of the Ornstein-Uhlenbeck process)
- The autoregressive process is centered on zero for identification
- The beta prior for the autoregressive parameter is right-skewed, thus favoring small values
- The last equation shows the log incremental payments (net of shift due to skewness) when the autoregressive process is added

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix: Exposure Growth

$$\eta_i \sim \text{N}(\mu_\eta, \tau_\eta)$$

$$\mu_\eta \sim \text{N}(0, 1)$$

$$\tau_\eta = 1 / \sigma_\eta^2$$

$$\sigma_\eta \sim \text{U}(0, 10)$$

- The rate of exposure growth is the growth in the volume of payments in a given exposure year, net of the calendar year effect
- The rate of exposure growth is modeled with shrinkage, which means that the smaller the number of observations that contribute to the estimation of the rate of exposure growth for a given exposure year, the more this rate is shrunk toward the common mean

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix: The Consumption Path (Without Break)

$$S_j = \beta_0 + \sum_{g=1}^{\xi} \beta_g \cdot (j - \theta_g) \cdot I(j - \theta_g > 0)$$

$$\beta_g \sim N(0, 0.0001), \quad g = 0 \dots \xi$$

$$\mathcal{G}_1 = 1$$

$$\frac{\mathcal{G}_g - 1}{(b-1)} \sim \text{Beta}(\gamma_1, \gamma_2), \quad g = 2 \dots \xi$$

$$\theta_{1 \dots \xi} = \text{Sort}(\mathcal{G}_{1 \dots \xi})$$

$$\xi \sim \text{Cat}(p_1 \dots p_\lambda), \quad p_i = 1/\lambda, \quad i = 1 \dots \lambda$$

- The consumption path is modeled as a linear spline
- The location of the knots are endogenous, and so is their number
- The linear spline is estimated using RJMCMC (Reversible Jump MCMC), which facilitates Gibbs sampling when the dimension of the parameter space (e.g., locations of knots) changes
- It is recommended to use parameters for the beta distribution (which governs the location of the knots) that generate right skew, such as Beta(1,2) or, if the data are very noisy in the highest development years, Beta(1,3)

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix: The Changepoint

- As an option, the model allows for a structural break in the consumption path (a changepoint)
- The model estimates the probability distribution of the changepoint within a provided interval of exposure years
- Such an interval may be set at one year, but in general may comprise several years
- The changepoint C has a beta prior that is “inverse u-shaped”

$$C \sim \text{Beta}(2,2)$$

- During the years of the changepoint interval, the consumption path is a mixture between the pre- and post-break regimes:

$$\mu_{i,j} = S_1 + \sum_{k=2}^{i+j} \kappa_k + \sum_{k=1}^i \eta_k + V_{i,j}$$

$$V_{i,j} = \begin{cases} R_{1,j} & \text{for } i < M \\ R_{1,j} \cdot \mathbf{I}(C + M - 1 > i) + R_{2,j} \cdot \mathbf{I}(C + M - 1 \leq i) & \text{for } M \leq i \leq L \\ R_{2,j} & \text{for } L < i \leq K \end{cases}$$

Indexes: i represents rows (exposure years); j represents columns (development years)

Technical Appendix: The Consumption Path (With Break)

$$R_{i,j} = \beta_{i,0} + \sum_{g=1}^{\xi} \beta_{i,g} \cdot (j - \theta_{i,g}) \cdot \mathbf{I}(j - \theta_{i,g} > 0), i = 1, 2$$

$$\beta_{i,g} \sim \mathbf{N}(0, 0.0001), g = 0 \dots \xi, i = 1, 2$$

$$\mathcal{G}_{i,1} = 1, i = 1, 2$$

$$\frac{\mathcal{G}_{i,g} - 1}{(b_i - 1)} \sim \text{Beta}(\gamma_{i,1}, \gamma_{i,2}), g = 2 \dots \xi_i, i = 1, 2$$

$$\mathcal{G}_{i,1 \dots \xi_i} = \text{Sort}(\theta_{i,1 \dots \xi_i}), i = 1, 2$$

$$\xi_i \sim \text{Cat}(p_1 \dots p_{\lambda_i}), p_j = 1/\lambda_i, j = 1 \dots \lambda_i, i = 1, 2$$

- There are two consumption paths, one that applies to the pre-structural break regime, and one that applies to the post-structural break regime
- Thus, there are two beta distributions governing the locations of the knots for the two regimes
- It is recommended to use parameters for the beta distribution of the pre-structural break regime that similar to the ones in the version without a break: Beta(1,2) or, if the data are very noisy in the highest development years, Beta(1,3)
- For the post-structural break regime, if the consumption path is short, a uniform distribution, that is Beta(1,1), is recommended; otherwise, Beta(1,2)

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

Technical Appendix:

Probability of Payment (1/2)

- The model fits to logarithmic incremental payments—because the logarithm of zero (or less) is undefined, incremental payments at amounts of zero (or at negative amounts) are treated as missing values
- In order to account for payments at zero amounts, a Bernoulli process is estimated alongside the model to determine the probability that there occurs a payment at a zero amount
- The estimated incremental payments of the model are multiplied by the one minus the parameter of this Bernoulli process, iteration by iteration
- Observations of payments at zero amounts may be sparse (if not non-existent). Further, although the proportions by column of payments at zero amounts may increase as development time progresses, the total number of observations by column invariably approaches unity before the triangle runs out of reported development years
- For this reason, when estimating the Bernoulli process, the prior of the parameter of this Bernoulli distribution (which varies by development year) is determined using a parametric specification

Technical Appendix: Probability of Payment (2/2)

$$u_{i,j} \sim \text{Bern}(p_j)$$

$$p_j = 1 - \exp(-\varphi_1 \cdot \exp(-\varphi_2 \cdot j))$$

$$\log(\varphi_1) \sim \text{N}\left(\log(\mu_{\varphi,1}) - \frac{1}{2 \cdot \tau_{\varphi_1}}, \tau_{\varphi_1}\right)$$

$$\log(\varphi_2) \sim \text{N}\left(\log(\mu_{\varphi,2}) - \frac{1}{2 \cdot \tau_{\varphi_2}}, \tau_{\varphi_2}\right)$$

$$\tau_{\varphi_i} \sim \text{Ga}(10, 0.1), \quad i = 1, 2$$

- The chosen functional form is a Gompertz curve, which affords the trajectory of the Bernoulli parameter a fair amount of flexibility
- The expected values $\mu_{\varphi, i+j}$ of the prior distributions of the Gompertz parameters are determined by means of nonlinear optimization prior to estimating the model
- $u_{i,j}$ is equal to 0 if there was a payment at a zero amount, equal to 1 if there was a payment at a positive amount, and a missing value otherwise

Indexes: i represents rows (exposure years); j represents columns (development years)

Note: The second parameter of the normal distribution indicates the precision, which is defined as the reciprocal value of the variance.

R Package *lossDev*

The R package is available for download at
<http://lossDev.r-forge.r-project.org>

Chris Laws
NCCI, Inc.
Boca Raton, Florida

Annual Meeting
Casualty Actuarial Society
Boston, Mass.
November 15-18, 2009

lossDev

- Robust Bayesian loss development
 - MCMC estimation performed in JAGS
 - Custom-written JAGS module adds lacking functionality
 - R package *rjags* provides link to JAGS from within R
 - Object oriented
 - Uses S4 objects and methods

System Requirements



- Version 2.9.2 or higher
- Supported operating systems
 - Windows (currently supported)
 - Linux\Unix (*forthcoming*)
- JAGS – Just Another Gibbs Sampler
 - Version 1.0.3

License

- *lossDev*
 - GNU General Public License Version 3 (GPLv3)
- JAGS (and *rjags*)
 - GNU General Public License Version 2 (GPLv2)



- GNU General Public License Version 2 (GPLv2)

Demonstration

- Download and installation
 - Microsoft Windows
- Walk through vignette, available at <http://lossdev.r-forge.r-project.org/>
 - Standard model
 - Change point model

Links



- <http://www.r-project.org/>
- *lossDev*
 - <http://lossDev.r-forge.r-project.org/>
 - <http://r-forge.r-project.org/projects/lossdev/>
- JAGS
 - <http://calvin.iarc.fr/~martyn/software/jags/>
- GNU General Public License
 - <http://www.gnu.org/licenses/gpl.html>